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Multifractal Desynchronization of the **Cardiac Excitable Cell Network During Atrial Fibrillation. I.** Multifractal Analysis of Clinical Data

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Atrial fibrillation (AF) is a cardiac arrhythmia characterized by rapid and irregular atrial electrical activity with a high clinical impact on stroke incidence. Best available therapeutic strategies combine pharmacological and surgical means. But when successful, they do not always prevent long-term relapses. Initial success becomes all the more tricky to achieve as the arrhythmia maintains itself and the pathology evolves into sustained or chronic AF. This raises the open crucial issue of deciphering the mechanisms that govern the onset of AF as well as its perpetuation. In this study, we develop a wavelet-based multi-scale strategy to analyze the electrical activity of human hearts recorded by catheter electrodes, positioned in the coronary sinus (CS), during episodes of AF. We compute the so-called multifractal spectra using two variants of the wavelet transform modulus maxima method, the moment (partition function) method and the magnitude cumulant method. Application of these methods to long time series recorded in a patient with chronic AF provides quantitative evidence of the multifractal intermittent nature of the electric energy of passing cardiac impulses at low frequencies, i.e., for times $(\geq 0.5 \text{ s})$ longer than the mean interbeat ($\simeq 10^{-1} \text{ s}$). We also report the results of a two-point magnitude correlation analysis which infers the absence of a multiplicative time-scale structure underlying multifractal scaling. The electric energy dynamics looks like a "multifractal white noise" with quadratic (log-normal) multifractal spectra. These observations challenge concepts of functional reentrant circuits in mechanistic theories of AF, still leaving open the role of the autonomic nervous system (ANS). A transition is indeed observed in the computed multifractal spectra which group according to two distinct areas, consistently with the anatomical substrate binding to the CS, namely the left atrial posterior wall, and the ligament of Marshall which is innervated by the ANS. In a companion paper (II. Modeling), we propose a mathematical model of a denervated heart where the kinetics of gap junction conductance alone induces a desynchronization of the myocardial excitable cells, accounting for the multifractal spectra found experimentally in the left atrial posterior wall area.

Keywords: mechanisms of atrial fibrillation, heart electrical activity, multifractal analysis, wavelet transform modulus maxima method, two-point magnitude correlation analysis, multifractal noise

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1. INTRODUCTION

116 AF is an arrhythmia originating in the rapid and irregular 117 electrical activity of the atria (the heart's two upper chambers) 118 that causes their pump function to fail, increasing up to fivefold 119 the risk of embolic stroke (Wolf et al., 1978, 1991; Attuel 120 et al., 1986; Lip and Lane, 2015). Isolated short episodes of 121 tachy-arrhythmias may be normal, but if they become more 122 frequent and last longer than 1 min then paroxysmal AF is 123 declared. This condition alone requires treatment of the atrial 124 electrophysiological substrate, all the more so as AF often coexists 125 with and predisposes to heart failure, with increased morbidity 126 and mortality (Middlekauff et al., 1991; Stevenson and Stevenson, 127 1999; Wang et al., 2003). Management of AF by drug therapy 128 aims at controlling either the ventricular rate, for instance by use 129 of negative chronotropes such as beta-adrenergic blockers, or the 130 rhythm, by use of anti-arrhythmic drugs interfering with ionic 131 membrane currents of the excitable cells to prolong the action 132 potential duration (APD), in combination with anticoagulants, 133 but it does not lead to a cure (Roy et al., 2008; Al-Khatib 134 et al., 2014). Since the work of Haïssaguerre et al. (1998), 135 radio-frequency ablation of the pulmonary veins in the left 136 atria has been developed for patients with paroxysmal AF as 137 drug efficacy was found to be poor or even to become pro-138 arrhythmic (Echt et al., 1991; The CAST II investigators, 1992). 139 This type of intervention seeks to punctually destroy sources 140 of abnormal focal electrical activity susceptible to trigger the 141 arrhythmia. Alternative strategies that have been developed lately 142 include compartmenting the atrium in order to block possible 143 reentrant circuits, or even directly targeting areas of abnormally 144 fractionated activity (Nademanee et al., 2004; Camm et al., 2010). 145 Despite the association of various strategies, clinical efficiency 146 remains disappointing (Ganesan et al., 2013; Takigawa et al., 147 2014). The rate of AF recurrences after an initial ablation 148 procedure treating paroxysmal AF increases with time (Bertaglia 149 et al., 2010), necessitating multiple redos, and most patients 150 suffering persistent AF are resistant to treatment (Camm et al., 151 2010; Verma et al., 2015; Wynn et al., 2016). 152

The prevailing electrophysiological concepts describing tachy-153 arrhythmias are more than a century old. They involve abnormal 154 automaticity and conduction (Janse, 1997). Initiation and 155 maintenance are thought to arise from a vulnerable substrate 156 prone to the emergence of multiple self-perpetuating reentry 157 circuits, also called "multiple wavelets" (Moe and Abildskov, 158 1959; Moe et al., 1964). Reentries may be driven structurally, 159 for instance because of locally high fibrous tissue content which 160 badly conducts, or functionally because of high spatial dispersion 161 of decreased refractoriness and APD (Misier et al., 1992). The 162 latter is coined the leading circle concept with the clinically 163 more relevant notion of a critical "wavelength" (in fact the 164 length) of the cardiac impulse (Allessie et al., 1977; Smeets 165 et al., 1986; Rensma et al., 1988; Attuel et al., 1989). The related 166 concept of vulnerability was originally introduced to uncover a 167 physiological substrate evolving from normality to pathology. 168 It was found in vulnerable patients that high rate frequency 169 would invariably lead to functional disorder as cardiac cells 170 would no longer properly adapt their refractoriness (Attuel et al., 171

1982). Mathematical models have managed to exhibit likewise 172 phenomena, with the generation of breaking spiral waves in 173 various conditions (Ito and Glass, 1991; Karma, 1993). The 174 triggering role of abnormal ectopic activity of the pulmonary 175 veins has been demonstrated on patients with paroxysmal AF 176 resistant to drug therapy (Haïssaguerre et al., 1998), but its 177 origin still remains poorly understood. This region is highly 178 innervated with sympathetic and parasympathetic stimulation 179 from the ANS (Tan et al., 2007; Ulphani et al., 2007; Arora, 180 2012). In particular, Coumel et al. (Coumel et al., 1978; Coumel, 181 1994) have revealed the pathophysiological role of the vagal 182 tone on a vulnerable substrate. It is frequently observed that 183 rapid tachycardia of ectopic origin transits to AF. This is known 184 to result from electrical remodeling. As described for the first 185 time by Allessie et al. (Allessie, 1998), remodeling is a transient 186 and reversible process by which the impulse properties such 187 as its refractory period are altered during the course of the 188 arrhythmia, promoting its perpetuation: "AF begets AF" (Wijffels 189 et al., 1995). Under substantial beating rate increase, cells may 190 undergo remodeling to overcome the toxicity of their excessive 191 intercellular calcium loading, by a rapid down regulation (a few 192 minutes) of their L-type calcium membrane current (Yue et al., 193 1997; Nattel et al., 2008). Moreover, other ionic channel functions 194 are also modified such as the potassium channel function, 195 inducing a change in the conduction properties including the 196 conduction velocity (Iwasaki et al., 2011; Nattel and Harada, 197 2014). The intercellular coupling at the gap junction level shows 198 also alterations of their connexin expression and dispersion 199 (Severs et al., 2008). For more details, one may consult van 200 Marion et al. (2015) and Zipes et al. (2017). 201

In this study, we delve into the complexity of voltage signals 202 recovered with bipolar electrodes in the CS during chronic AF. 203 Attempts to assess visually the spatio-temporal complexity of 204 voltage signals using maps of unipolar electrodes revealed various 205 complex patterns of activity not all compatible with reentries 206 (Konings et al., 1994, 1997). We use here two declinations 207 of a wavelet-based multi-scale method, the moment (partition 208 function) method and the magnitude cumulant method (Muzy 209 et al., 1994; Arneodo et al., 2008), as originally introduced in 210 the field of fully developed turbulence (Muzy et al., 1991). This 211 methodology has been extensively applied in different domains 212 of fundamental and applied sciences, including geophysics 213 (Venugopal et al., 2006), econophysics (Muzy et al., 2001), 214 biology (Arneodo et al., 2011) and medicine (Gerasimova et al., 215 2014; Gerasimova-Chechkina et al., 2016). In the context of 216 cardiac physiology, this methodology was shown to be valuable 217 in assessing congestive heart failure from the monitoring of sinus 218 heart rate variability (Ivanov et al., 1999, 2001; Goldberger et al., 219 2002). The wavelet-based multifractal analysis of the electric 220 energy of passing cardiac impulses during AF reported in the 221 paper provides unprecedented experimental estimates of the 2.2.2 multifractal spectra in different heart areas. The reported results 223 show that the electric energy dynamics looks like a log-normal 224 "multifractal white noise" with no underlying multiplicative 225 time-scale structure. Long time series recordings, at various 226 locations throughout the whole atria of many patients, are 227 mandatory to obtain and analyze with the aim at identifying 228

how many multifractal scalings exist. For instance, what is the 229 effect on multifractal scaling of altered cell network topologies, 230 especially when fibrosis is present? Or how is such scaling 231 correlated to the disease temporal evolution, with or without 232 drug therapy or surgical intervention, when the substrate is 233 remodeled? In a companion paper (Attuel et al., submitted), 234 we start tackling the problem at source, in the simplest (1D) 235 cell network topology, by exploring the possibility that the 236 substrate function is modulated by the kinetics of conduction. 237 A simple reversible mechanism of short term remodeling under 238 rapid pacing is demonstrated, by which ionic overload acts 239 locally (dynamical feedback) on the kinetics of gap junction 240 241 conductance. The whole process may propagate and pervade the myocardium via electronic currents. No influence of the 242 ANS is included and no structural inhomogeneities are taken 243 into account. Then the complete network of excitable cells 244 becomes desynchronized, with induced dispersion of remodeled 245 refractoriness and APD, and abnormal automaticity. Contrary to 246 existing mathematical models based on circuit reentries, a spatio-247 temporal multifractal intermittent dynamics emerges similar to 248 the one found in the CS next to the left atrial posterior wall 249 area, opening a new avenue toward the understanding of AF 250 mechanisms of perpetuation. 251

2. METHODS OF ANALYSIS

The wavelet transform (WT) is a mathematical microscope (Arneodo et al., 1988, 1995b, 2008; Muzy et al., 1991, 1994) that is well suited for the analysis of complex non-stationary time-series such as those found in genomics (Nicolay et al., 2007; Arneodo et al., 2011; Audit et al., 2013) and physiological systems (Ivanov et al., 1999, 2001; Goldberger et al., 2002; Ciuciu et al., 2012; Chudácek et al., 2014; Gerasimova et al., 2014; Richard et al., 2015). Thanks to its ability to be blind to non-stationary lowfrequency (polynomial) trends in the analyzed signal E(t) (or E(x)), it has been early recognized as well adapted to reveal the hierarchy that governs the temporal (or spatial) distribution of singularities of multifractal signals including singular measures and functions (Arneodo et al., 1988; Holschneider, 1988; Jaffard, 1989; Muzy et al., 1991, 1994; Mallat and Hwang, 1992). It is therefore implemented in robust methods capturing the selfsimilar intricate fractal structures hidden in signals that exhibit a typical "1/f noise" scaling as seen in the Fourier spectral density (Mandelbrot, 1982, 1998; West and Shlesinger, 1988).

2.1. The Wavelet Transform Microscope: A 2.7. Singularity Scanner

The WT is a time-scale decomposition method which consists in expanding signals in terms of wavelets constructed from a single function, the "analyzing wavelet" ψ , by means of translations and dilations (Grossmann and Morlet, 1984; Daubechies, 1992; Meyer, 1992; Mallat, 1998). The WT of a real-valued function *E* is defined as:

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$$T_{\psi}[E](t_0, a) = \frac{1}{a} \int_{-\infty}^{+\infty} E(t)\psi(\frac{t - t_0}{a})dt,$$
 (1)

where t_0 is a time parameter and a (> 0) a scale parameter (inverse of frequency). By choosing a wavelet ψ which has its first n_{ψ} moments null [$\int t^m \psi(t) dt = 0, 0 \le m < n_{\psi}$], it can be proven that the behavior of $T_{\psi}[E](t_0, a)$ as a function of the scale a, as $a \to 0^+$, characterizes the local behavior of E(t) (Arneodo et al., 1988, 1995b, 2008; Jaffard, 1989; Muzy et al., 1991, 1994; 291 Mallat and Hwang, 1992): 292

$$\Gamma_{\psi}[E](t_0, a) \sim a^{h(t_0)}, \ a \to 0^+,$$
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provided $n_{\psi} > h(t_0)$, where $h(t_0)$ is the point-wise Hölder 296 297 exponent that characterizes the maximum regularity of the signal 298 E at point t_0 . If $n < h(t_0) \le n + 1$, the (n - 1)th derivative of E(t) is regular and its *n*th derivative is singular at t_0 . Thus 299 the larger $h(t_0)$, the smoother the function, the faster the power-300 301 law decrease of $T_{\psi}[E]$ when $a \to 0^+$. For $h(t_0) = 0$, E(t) is discontinuous and bounded at t_0 and the wavelet transform no 302 longer depends on *a*. For discontinuous "noise" signals, $h(t_0) < 0$ 303 and $T_{\psi}[E](t_0, a)$ increases when $a \to 0^+$. For instance, $h(t_0) =$ 304 -1 corresponds to a delta distribution at $t = t_0$, while if 305 almost everywhere $h(t) = -\frac{1}{2}$, the single exponent $H = \frac{1}{2}$ is 306 characteristic of a "white" noise (Muzy et al., 1994). To resolve all 307 308 the cusp singularities present in a function, the analyzing wavelet must be chosen to have enough vanishing moments to resolve 309 the singularities with Hölder exponent h_{max} , namely $n_{\psi} \ge h_{\text{max}}$. 310 Since h_{max} is not known a priori, the most appropriate way to 311 correctly estimate all singularities is to analyze the given function 312 313 with analyzing wavelets of increasing order n_{ψ} until a robust estimate of the so-called spectrum of singularities is obtained 314 315 (Bacry et al., 1993; Muzy et al., 1994; Arneodo et al., 1995b) (see section 2.2). In the present study, we use the successive 316 derivatives of a Gaussian function $g^{(N)}(t) = \frac{d^N}{dt^N} \left(e^{-t^2/2} \right)$ as 317 318 analyzing wavelets with $n_{\psi} = N$ (Muzy et al., 1994; Arneodo 319 et al., 1995b) (Figure S1). 320

2.2. A Wavelet-Based Canonical Multifractal Formalism: The Wavelet Transform Modulus Maxima Method

The wavelet transform modulus maxima (WTMM) method 325 (Muzy et al., 1991, 1994; Bacry et al., 1993; Arneodo et al., 326 1995b, 2008) was originally developed to generalize box-counting 327 techniques (Arneodo et al., 1987) and to remedy the limitations 328 of structure functions method (Muzy et al., 1993) in performing 329 multifractal analysis of one-dimensional (1D) velocity signals 330 in fully-developed turbulence. It has proved very efficient to 331 estimate scaling exponents and multifractal spectra (Muzy et al., 332 1994; Audit et al., 2002; Arneodo et al., 2008). From the deep 333 analogy that links the multifractal formalism to thermodynamics 334 (Bohr and Tél, 1988; Arneodo et al., 1995b), the WTMM method 335 provides a canonical description (Arneodo et al., 1995b) of the 336 distribution of point-wise Hölder exponents for finite a. The 337 WTMM method allows therefore some control and mastering 338 of finite-size effects and statistical convergence issues. As $a \rightarrow$ 339 0^+ , the thermodynamic limit is reached formally guaranteeing 340 an equivalence with micro-canonical approaches such as found 341 in Turiel et al. (2008). To account for the possible presence of 342

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oscillating (chirps) (Arneodo et al., 1995a), a grand-canonical 343 multifractal formalism has also been developed for signals 344 involving cusp and oscillating singularities (Arneodo et al., 345 1997b). The canonical 1D WTMM method has been generalized 346 in 2D for the multifractal analysis of rough surfaces (Arneodo 347 et al., 2000, 2003; Decoster et al., 2000; Roux et al., 2000) and for 348 the analysis of 3D scalar and vector fields (Kestener and Arneodo, 349 2003, 2004; Arneodo et al., 2008) with successful applications in 350 astrophysics (Khalil et al., 2006; Kestener et al., 2010; McAteer 351 et al., 2010), geophysics (Venugopal et al., 2006; Roux et al., 352 2009), surface science (Roland et al., 2009), image processing 353 (Mallat, 1998; Arneodo et al., 2003, 2008; Antoine et al., 2008), 354 355 cellular biology (Khalil et al., 2007; Snow et al., 2008; Goody et al., 2010; Grant et al., 2010; Martinez-Torres et al., 2014, 2015) 356 and medicine (Kestener et al., 2001; Arneodo et al., 2003; Khalil 357 et al., 2009; Batchelder et al., 2014; Gerasimova-Chechkina et al., 358 2016; Marin et al., 2017). Note that alternative approaches to 359 the WTMM method have been developed using discrete wavelet 360 bases, including the recent use of wavelet leaders (Jaffard et al., 361 2007; Wendt et al., 2007). 362

2.2.1. The Method of Moments

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364 In 1D, the WTMM method (Muzy et al., 1991, 1993, 1994; 365 Bacry et al., 1993; Arneodo et al., 1995b) consists in computing 366 the WT skeleton defined, at each fixed scale a, by the local 367 maxima $\mathcal{L}(a)$ of the WT modulus $|T_{\psi}[E](t,a)|$. These WTMM 368 are disposed on curves connected across scales called maxima 369 lines (see Figure 2C). Along these maxima lines l, Mallat and 370 Hwang (1992) have shown that Equation (2) also applies for 371 the WTMM that behave as $|T_{\psi}[E](t,a)| \sim a^{h(t)}$, where h(t)372 is the Hölder exponent characterizing the singularity of the 373 signal E at time t. The canonical multifractal formalism (Muzy 374 et al., 1994; Arneodo et al., 1995b) characterizes the relative 375 contributions of each Hölder exponent value via the estimate of 376 the singularity spectrum D(h) defined as the fractal (Hausdorff) 377 dimension of the set of points t where h(t) = h. This spectrum 378 can be obtained by investigating the scaling behavior of partition 379 functions defined in terms of WTMM (and which correspond to 380 the moments of the WTMM probability distribution function): 381

$$Z(q,a) = \sum_{l \in \mathcal{L}(a)} |T_{\psi}[E](t,a)|^{q} \sim a^{\tau(q)}, \ a \to 0^{+},$$
(3)

where $q \in \mathbb{R}$, and $\mathcal{L}(a)$ is the set of all maxima lines *l* that 386 satisfy: $l \in \mathcal{L}(a)$, if $\forall a' \leq a, \exists (t, a') \in l$. In the framework of 387 the analogy with thermodynamics (Bohr and Tél, 1988; Arneodo 388 et al., 1995b), q and $\tau(q)$ play respectively the role of an inverse 389 temperature and a free energy. The main result of the canonical 390 wavelet-based multifractal formalism is that in place of energy 391 and entropy (i.e., the variables conjugated to q and τ), we have 392 h, the Hölder exponent, and D(h), the singularity spectrum. 393 This means that the singularity spectrum of E(t) is a convex 394 function that can be calculated from the Legendre transform of 395 the partition function scaling exponents $\tau(q)$ (Bacry et al., 1993; 396 Muzy et al., 1993, 1994; Arneodo et al., 1995b): 397

$$D(h) = \min_{q} [qh - \tau(q)]. \tag{4}$$

In practice, to avoid instabilities in performing the Legendre transform, we instead compute the following expectation values (Muzy et al., 1994; Arneodo et al., 1995b), analogous to the fundamental thermodynamic relations, by inversion of Equation (4):

$$h(q,a) = \frac{\partial}{\partial q} \ln(Z(q,a)) = \sum_{l \in \mathcal{L}(a)} \ln\left(|T_{\psi}[E](t,a)|\right) \cdot W_{\psi}[E](q,l,a),$$

and

$$D(q,a) = q \frac{\partial}{\partial q} \ln(Z(q,a)) - \ln(Z(q,a))$$
$$= \sum_{l \in \mathcal{L}(a)} W_{\psi}[E](q,l,a) \cdot \ln\left(W_{\psi}[E](q,l,a)\right), \quad (6)$$

where $W_{\psi}[E](q, l, a) = |T_{\psi}[E](t, a)|^q/Z(q, a)$ corresponds to the Bolzmann weight in the analogy that connects the multifractal formalism to thermodynamics (Arneodo et al., 1995b). Then, from the slopes of h(q, a) and D(q, a) vs. ln a, we get h(q) and D(q), and therefore the D(h) singularity spectrum as a curve parametrized by q. For further mathematical developments on the 1D WTMM method, we refer the reader to Bacry et al. (1993) and Jaffard (1997a,b).

2.2.2. The Method of Magnitude Cumulants

With the previous method of moments, to compute the entire 429 $\tau(q)$ curve, we need to perform linear regression fits of $\ln Z(q, a)$ 430 vs. $\ln a$ (Equation 3) for a wide range of q values and then to 431 proceed to a polynomial fit of the $\tau(q)$ data prior to the Legendre 432 transform (Equation 4) to get the D(h) singularity spectrum. 433 An alternative method based on magnitude cumulants has been 434 introduced by Delour et al. (2001) to minimize the number of 435 linear regression fits (as few as 3) while still adequately inferring 436 and accurately estimating the nonlinear behavior of the $\tau(q)$ 437 spectrum. This method is based on the following reasoning. 438 The computation of the partition function Z(q, a) amounts to 439 computing the following arithmetic mean of the WTMM to the 440 power q: 441

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$$\langle |T_a|^q \rangle = \frac{1}{N_a} Z(q, a), \tag{7} \quad {}^4_4$$

where we simplified notations $T_a \equiv T_{\psi}[E](\cdot, a)$, and where N_a is the number of maxima lines at scale *a*, which scales as $\sim a^{-D_f}$, where $D_f = -\tau(0)$ is the fractal dimension of the support set of the singularities in the signal E(t). From Equations (3) and (7), we get the expansion

$$[\tau(q) + D_f] \ln a \sim \ln\{\langle e^{q \ln |T_a|} \rangle\},\$$

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where $C_n(a)$ are the cumulants of the magnitude $\ln |T_a|$. Then from the behavior of these cumulants:

$$C_{1}(a) \equiv \langle \ln |T_{a}| \rangle \sim c_{1} \ln(a),$$

$$C_{2}(a) \equiv \langle \ln^{2} |T_{a}| \rangle - \langle \ln |T_{a}| \rangle^{2} \sim -c_{2} \ln a,$$

$$C_{3}(a) \equiv \langle \ln^{3} |T_{a}| \rangle - 3 \langle \ln^{2} |T_{a}| \rangle + 2 \langle \ln |T_{a}| \rangle^{3} \sim c_{3} \ln a,$$

$$\dots$$
(9)

we get the following expansion formula for $\tau(q)$:

$$\tau(q) = -D_f \frac{q^0}{0!} + \sum_{n=1}^{\infty} \left[\frac{C_n(a)}{\ln a} \right] \frac{q^n}{n!},$$

$$= -c_0 + c_1 q - c_2 q^2 / 2! + c_3 q^3 / 3! \cdots$$
(10)

where the coefficients $c_n > 0$ are estimated as the slope of $C_n(a)$ vs. $\ln(n = 1, 2, 3, \dots)$, and $c_0 = D_f$.

The implication of the above developments is that we can estimate $\tau(q)$ from the polynomial expansion of Equation (10), where the coefficients are obtained from the log-log linear regressions of the cumulants of the magnitude $C_n(a)$ vs. $\ln(a)$ 477 (Equation 9) (Delour et al., 2001). A quadratic log-normal $\tau(q)$ approximation would need only three such linear regressions, $c_n = 0, \forall n > 2.$

2.3. Monofractal vs. Multifractal Functions

Homogeneous monofractal signals (distributions) are signals 483 with singularities of unique Hölder exponent H. Their $\tau(q)$ 484 spectrum is a linear function of q with slope $c_1 = H$ 485 (Equation 9). Monofractal scaling indeed means that the shape 486 of the probability distribution function (pdf) of rescaled wavelet 487 coefficients does not change across scales as expressed by the 488 following relationship between the WTMM pdfs $P_a(T)$ and 489 $P_{a'}(T)$ at scale a and a' > a respectively (Arneodo et al., 2002, 490 2011): 491

$$P_a(T) = \left(\frac{a'}{a}\right)^{-H} P_{a'}\left(\left(\frac{a'}{a}\right)^{-H}T\right).$$
(11)

A nonlinear $\tau(q)$ is the signature of multifractal signals with Hölder exponent h(t) fluctuating over time t (Muzy et al., 1991, 1994; Bacry et al., 1993; Arneodo et al., 1995b, 2002, 2008). In this study, we fit the $\tau(q)$ data by the so-called log-normal quadratic approximation $\tau(q) = -c_0 + c_1 q - c_2 q^2/2$. The corresponding singularity spectrum has a quadratic single humped shape:

$$D(h) = c_0 - (h - c_1)^2 / 2c_2,$$
(12)

where $c_0 = -\tau(0) = D_f$ is the fractal dimension of the 504 support of singularities of E(t), c_1 is the value of h that maximizes 505 D(h), and the intermittency coefficient c_2 (Delour et al., 2001) 506 characterizes the width of the D(h) spectrum as an indication 507 of a change in WTMM coefficient statistics across scales. If h(t)508 fluctuates according to a pdf $\rho(h)$, then (Castaing et al., 1990, 509 1993; Arneodo et al., 1997a, 1998c, 1999): 510

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$$P_a(T) = \int \rho(h) \left(\frac{a'}{a}\right)^{-h} P_{a'}\left(\left(\frac{a'}{a}\right)^{-h}T\right) dh, \quad (13)$$

meaning that the pdf at scale *a* can be expressed as a weighted 514 sum of dilated pdfs at larger scales a' > a. Let us point out that the 515 monofractal situation (Equation 11) is recovered when assuming 516 that $\rho(h) = \delta(h - H)$ in Equation (13). 517

Note that $\tau(2) = c_0 + 2c_1 - 2c_2$, also called the correlation dimension, is related to the "1/f" scaling exponent of the Fourier spectral density (Muzy et al., 1994; Mandelbrot, 1998):

$$|\widehat{E}(f)|^2 \sim f^{-\beta}$$
, with $\tau(2) = \beta - 2$. (14)

2.4. In Quest of an Underlying Time-Scale Multiplicative Structure: The Two-Points Magnitude Correlation Method

527 Multiplicative cascade processes (Arneodo et al., 1998b) are 528 paradigmatic mechanisms generating multifractal distributions, 529 with as historical examples the Kolmogorov-Obukhov log-530 normal energy cascade model of fully developed turbulence 531 (Kolmogorov, 1962; Oboukhov, 1962; Mandelbrot, 1974), 532 and the Multifractal Random Walk (MRW) model recently 533 introduced to account for the intermittency observed in financial 534 time series (Muzy et al., 2000; Bacry et al., 2001). But, if 535 multifractal scaling implies some evolution of the WTMM 536 statistics across scales, it does however not require any correlation 537 of the wavelet coefficients across scales. In addition to the above 538 one-point WTMM statistics, it is thus useful to study the two-539 point correlation function of the logs of the WTMM coefficients 540 $\ln |T_a(t)|$, which determines the way the correlation structure 541 of the Hölder exponents h (or singularities) changes with scale 542 (Arneodo et al., 1998a,b). Defining the two-point magnitude correlation function $C(a, \Delta t)$ as:

$$C(a, \Delta t) = \langle \left(\ln |T_a(t)| - \langle \ln |T_a(t)| \rangle \right) \cdot \left(\ln |T_a(t + \Delta t)| - \langle \ln |T_a(t)| \rangle \right) \rangle,$$
(15)

and seeing how this correlation changes as a function of Δt at scale a, provides information about the time-scale structure that underlies the multifractal properties of the considered signal. As demonstrated by Arneodo et al. (1998a,b) for random multiplicative cascades on wavelet dyadic trees (see also Meneveau and Sreenivasan, 1991):

$$C(a, \Delta t) \sim -c_2 \ln \Delta t, \qquad \Delta t > a,$$
 (16) 555

where the proportionality coefficient c_2 is the intermittency 557 coefficient defined in Equation(9) (Note that $C(a, \Delta t = 0) \equiv$ 558 $C_2(a) \sim -c_2 \ln a$. Thus, by computing $C(a, \Delta t)$ from Equation 559 (15) and plotting it as a function of $\ln \Delta t$, inferences can 560 be made about long-range dependence and consistency with 561 a multiplicative cascading process (Arneodo et al., 1998a,b). 562 Applications of the two-point magnitude correlation method 563 have already provided insight into a wide variety of problems, 564 e.g., the validation of the log-normal cascade phenomenology of 565 fully developed turbulence (Arneodo et al., 1998a,c, 1999) and of 566 high resolution temporal rainfall (Venugopal et al., 2006; Roux 567 et al., 2009), and the demonstration of the existence of a causal 568 cascade of information from large to small scales in financial time 569 series (Arneodo et al., 1998d; Muzy et al., 2001). 570

3. DESCRIPTION OF DATA

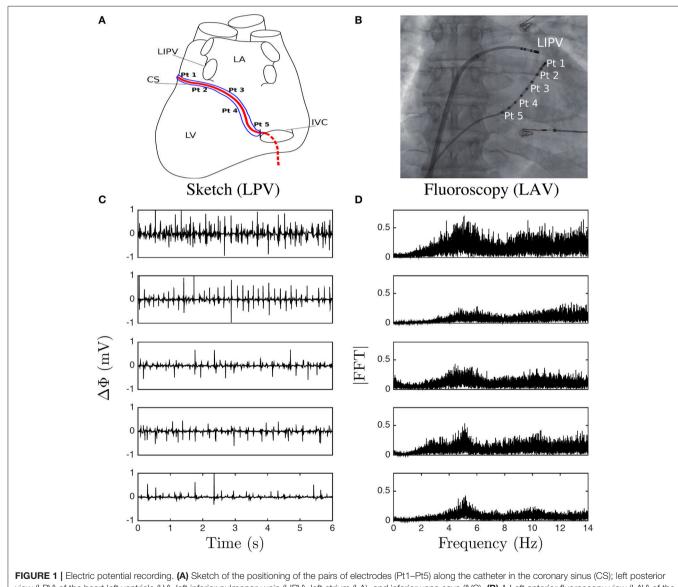
3.1. Study Design and Population

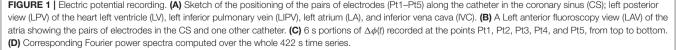
The experimental data are hospital-based. We have analyzed data recorded in the atria of 8 patients with persistent or chronic AF, chosen without any prior explicit exclusion criteria. These patients were enrolled to undergo radio frequency ablation between 2010 and 2012, in the international cardiac electrophysiology service of public hospital CHU Haut-Lévêque in Pessac, France. All patients gave written informed consent to the investigation of data from the intervention. A protocol for clinic research was approved by the institutional Clinical Research and Ethics Committee. For this specific investigation of the data, the authors accessed fully anonymized and de-identified

data. As representative of the results obtained with our set of patients, we report in this manuscript the results of a detailed wavelet-based multifractal analysis of five long time series specially recorded in one of the 8 patients with chronic AF.

3.2. Electric Potential Recording

A steerable decapolar catheter, equipped with five 1 mm distant pairs of electrodes, each pair separated by 5 mm (Xtrem, Sorin Medical ©), was positioned in the CS as recommended in (Figures 1A,B). The distal leads of the catheter tip are positioned in a region near the left pulmonary veins, while the proximal leads lie closer to the right atrium orifice of the CS. This catheter was immobile and probed the electrical activity of those





Multiracial Desynchronisation of the Atria

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areas in the left atrium. Monitoring typically lasted the whole 685 intervention which could take hours. Our file consists of 5 686 simultaneous recordings at points Pt1 to Pt5, from distal to 687 proximal positioning along the vein (Figure 1A), each lasting 688 422 s with sampling time 10^{-3} s, a few minutes before the 689 first ablation procedure started. The potential difference $\Delta \phi(t)$ 690 between each of the two electrodes in each pair was recorded, 691 with the convention of distal minus proximal (Figure 1C). The 692 normal to rapid frequency in sinus rhythm varies in the range 693 $1 \,\mathrm{Hz} \, \lesssim \, f \, \lesssim \, 3 \,\mathrm{Hz}$, whereas during AF it is typically in the 694 range $3 \text{ Hz} \lesssim f \lesssim 10 \text{ Hz}$ (Figure 1D). But the most obvious 695 observation is that on-site recordings during AF contrast with 696 697 the ones during sinus rhythm as the former seem to fluctuate randomly at even higher frequencies. Physiologically, a natural 698 high frequency cut-off is somewhere in between 100 Hz $\leq f_c \leq$ 699 1,000 Hz, which corresponds to the shortest characteristic time 700 scale in a cardiac cell cycle, that is depolarization. Furthermore, 701 AF is considered as the most irregular cardiac arrhythmia 702 (Konings et al., 1994, 1997). 703

3.3. Local Impulse Energy 705

Each electrode averages the electric potential over its surface. 706 During depolarization, ions flow through the cell membrane 707 channels and the gap junction channels, inducing a rapid change 708 of the electric potential (~ 10^{-2} s). Then, repolarization is a 709 much smoother event. Bipolar electrodes are separated by a few 710 millimeters which is typically the length scale of a depolarizing 711 front in the atria with a conduction velocity $c \sim 10^{-1}$ m/s 712 and a refractory period $RP \sim 10^{-1}$ s (Figures S2A,B), thus 713 defining the so-called "wavelength" scale $c \times RP$ (Smeets et al., 714 1986; Rensma et al., 1988). Any spatio-temporal variation of the 715 vulnerable substrate function happens over larger time scales. 716 717 Thus the conduction velocity can be considered constant over such small scales and the bipolar electric potential difference is 718 therefore "frozen." It follows that the bipolar electric potential 719 difference is locally advected with velocity c: 720

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$$\frac{\partial \Delta \phi(t)}{\partial t} = -c \overrightarrow{\nabla} \Delta \phi(t). \tag{17}$$

Under this assumption, the evaluation of the local electric energy 725 of a cardiac impulse is straight-forward: 726

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$$\frac{\varepsilon}{2}\mathcal{E}^{2}(t) = \frac{\varepsilon}{2c^{2}}\left(\frac{\partial}{\partial t}\Delta\phi(t)\right)^{2},$$
(18)

731 where \mathcal{E} is the electric field magnitude and ε is the dielectric 732 bulk permitivity of the (inter-) cellular medium. Energy will thus 733 peak when the impulse travels between the two electrodes. It 734 fully incorporates ionic flux through membrane channels and 735 electrotonic currents, specifically those taking place at the gap 736 junctions. Because we have no means to assess the conduction 737 velocity c, we will use in this study the following definition of the energy: 738

$$E(t) = \left(\frac{\partial \Delta \phi(t)}{\partial t}\right)^2,$$
(19)

after dropping the term in front of the r.h.s. of Equation (18), 742 i.e., $\varepsilon/2c^2$ which remains constant at first order as long as the 743 conduction velocity c does not fluctuate too much. To practically 744 derive E(t) from the recorded $\Delta \phi(t)$, we used an order 4 finite 745 difference scheme on a oversampled ($\Delta t_0 = 10^{-4}$ s) cubic-spline 746 fitting of the data (Figures S2C,D). This is needed to estimate 747 peaks in the energy within temporal windows as narrow as 748 $\sim 10^{-3}$ s (Figures S2E,F). We have checked that the scaling 749 properties displayed by E(t) in the low frequency range of interest 750 here (0.08 Hz $\leq f \leq$ 2 Hz) are not affected by this discretization 751 scheme. 752

Let us note that Equation (19) is not without reminding the 1D 753 surrogate dissipation approximation $E_{\rm dis}(t) \sim (\partial \upsilon / \partial t)^2$, where 754 v is the longitudial velocity, in fully developed (homogeneous 755 and isotropic) turbulence under the Taylor hypothesis of "frozen" 756 turbulence (Meneveau and Sreenivasan, 1991; Frisch, 1995). 757

3.4. Software and Documentation

The numerical procedure to perform the WTMM analysis of 1D signals can be downloaded at

http://perso.ens-lyon.fr/benjamin.audit/LastWave

LastWave is open source software written in C. We recommend interested users to read the LastWave C-Application Programming Interface documentation and to contact the corresponding author to be directed to the part of the code of most relevance to them.

4. RESULTS

4.1. One-Point Multifractal Analysis of Local Impulse Energy Data

774 We first present an exhaustive step-by-step analysis of one of the impulse energy time-series recorded at the electrode Pt2 as an 775 776 illustration of the intricacies involved in the methodology and as a demonstration that without a priori knowledge about the 777 signal, a reliable multifractal analysis requires an iterative process 778 779 between diagnosis and estimation until robustness is achieved. In Figure S3 is illustrated how the WT microscope is able to filter out 780 the nonstationarities (polynomial trends) in E(t) (Figure S3A) 781 when using analyzing wavelets $g^{(N)}$ (Figure S1) of increasing 782 order (Figures S3B–D). 783

4.1.1. Multifractal Analysis of the Impulse Energy Data With the WTMM Method of Moments

When applying the WTMM method to the impulse energy 787 time-series recorded at Pt2 (Figure 2A), we revealed that the 788 partition functions Z(q, a) (Equation 3) obtained from the 789 WT computed with the analyzing wavelet $g^{(3)}$ (Figure 2B) and 790 its skeleton (Figure 2C), display nice scaling properties for 791 q = -1 to 5 over a range of time-scales larger than the 792 mean interbeat ~ 0.5 s (Figure 1D). We strictly limited this 793 range to (0.6, 10 s) for linear regression fit estimates in a 794 logarithmic representation (Figure 3A). The $\tau(q)$ so-obtained 795 is well approximated by a quadratic spectrum with parameters 796 $[c_0, c_1, c_2] = [1.01, -0.34, 0.053]$ and $c_n = 0$ for n > 2797 (Equation 10) (Figure 4A). This signature of multifractality with 798

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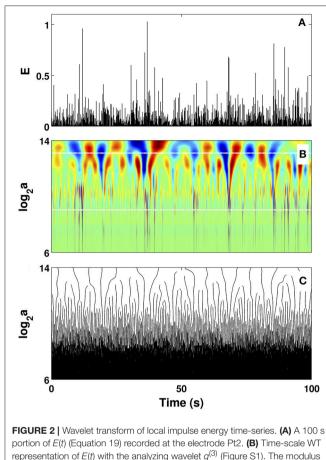
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portion of E(t) (Equation 19) recorded at the electrode Pt2. (B) Time-scale WT representation of E(t) with the analyzing wavelet $g^{(3)}$ (Figure S1). The modulus of the WT is coded, independently at each scale a, using 256 colors from black ($|T_{q^{(3)}}(t, a)| = 0$) to red (max_t $|T_{q^{(3)}}(t, a)|$). (C) WT skeleton defined by the maxima lines. The scale $a = \Delta t / \Delta t_0$, where $\Delta t_0 = 10^{-4}$ s. In **(B)** the white horizontal dotted lines delimit the range of time scales ($2^9 \le a \le 2^{13}$) used to perform linear regression fit estimates of the $\tau(q)$ and D(h) multifractal spectra.

a support of singularities of fractal dimension $D_f \approx 1$, and 836 an intermittency coefficient $c_2 = 0.053 \pm 0.010$ (Table 1) is 837 confirmed when respectively plotting $h(q, a) / \ln 2$ (Equation 5) 838 and $D(q, a) / \ln 2$ (Equation 6) vs. $\log_2 a$ Figures 3B,C. From the 839 estimate of the slopes h(q) and D(q), we get the single humped 840 D(h) spectrum shown in **Figure 4B** which is well approximated 841 by the quadratic spectrum defined in Equation (12) with the 842 above parameter values obtained from a polynomial fitting of 843 the $\tau(q)$ data. Interestingly, when comparing the results obtained 844 with the analyzing wavelet $g^{(3)}$ with those obtained with $g^{(1)}$ 845 and $g^{(2)}$ in **Figures 3**, **4**, we notice that except some slight 846 differences observed when using the first-order analyzing wavelet 847 $g^{(1)}$, the multifractal spectra obtained with the second-order 848 wavelet $g^{(2)}$ and the third-order wavelet $g^{(3)}$ almost superimpose 849 (**Figure 4**, **Table 1**) with singularities of Hölder exponent $h \leq 0$, 850 characteristic of a multifractal "noise" signal. 851

This multifractal diagnosis is confirmed in Figure 5 where the 852 WTMM pdfs obtained at different scales with $g^{(3)}$ (Figure 5A) 853 are shown to collapse on each other when using the propagative 854 equation of the statistics across scales (Equation 13) with 855

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the quadratic $\tau(q)$ spectrum estimated just above (Figure 5B) 856 (Castaing et al., 1990, 1993; Arneodo et al., 1997a, 1998c, 1999; 857 Venugopal et al., 2006). 858

4.1.2. Multifractal Analysis of the Impulse Energy Data With the Method of Magnitude Cumulants

After the WTMM partition function approach, we turn 862 our attention to the alternate magnitude cumulant analysis 863 methodology. The first-, second- and third-order cumulants were 864 computed using Equation (9) and are plotted vs. the logarithm 865 of the scale in **Figure 6**. As expected $C_1(a)$, $C_2(a)$ and $C_3(a)$ 866 display consistent scaling behavior over the same range of scales 867 $2^9 \leq a \leq 2^{13}$ ($a = \Delta t / \Delta t_0$, where the oversampling time 868 is $\Delta t_0 = 10^{-4}$ s) and this for the three analyzing wavelets 869 $g^{(1)}$, $g^{(2)}$ and $g^{(3)}$. The results obtained for $C_3(a)$ (Figure 6C) 870 confirm that with the limited statistical sample at our disposal 871 (422 s long time series), there is no way to conclude about the 872 possible departure from a log-normal quadratic $\tau(q)$ spectrum 873 $(c_3 \equiv 0)$. Nicely, the quadratic $\tau(q)$ spectrum obtained with $g^{(3)}$ 874 with parameters $c_1^* = -0.33 \pm 0.01$ and $c_2^* = 0.047 \pm 0.028$ is 875 found in good agreement with the one previously estimated with 876 the method of moments, confirming the multifractal diagnosis 877 of the local impulse energy at low frequencies. Let us point out 878 that, as reported in **Table 1**, the $\tau(q)$ spectrum obtained with $g^{(1)}$ 879 is again slightly different from the ones obtained with $g^{(2)}$ and 880 $g^{(3)}$ which turn out to be indistinguishable. This is the numerical 881 demonstration that a robust estimate of the multifractal 882 spectra is achieved when using the third-order analyzing 883 wavelet $g^{(3)}$. 884

4.1.3. Summary of One-Point Multifractal Analysis of the Impulse Energy Data

Similar analysis was performed on the four other local impulse 888 energy time-series recorded at electrodes Pt1 (Figures S4, 889 S8, S11), Pt3 (Figures S5, S9, S12), Pt4 (Figures S6, S13), and 890 Pt5 (Figures S7, S10, S14). As already noticeable on the power 891 spectrum in **Figure 1D**, the electric potential $\Delta \phi(t)$ recorded at 892 electrode Pt4 presents some subharmonic oscillatory component 893 at frequency ~2.5 Hz that dramatically spoils the scaling behavior 894 previously obtained at Pt2 over the range of time-scales (0.6, 895 10 s) (Figures S6, S13). We can speculate on the signature of 896 the nearby mitral valve influence. This explains that Pt4 will be 897 singled out in the rest of our study. Figure 7 displays the $\tau(q)$ 898 (Figure 7A) and D(h) (Figure 7B) spectra of the local impulse 899 energy E(t) obtained with the WTMM method of moments 900 when using the analyzing wavelet $g^{(3)}$ (the corresponding spectra 901 obtained with analyzing wavelets $g^{(1)}$ and $g^{(2)}$ are shown in 902 Figures S15, S16 respectively). The spectra obtained for the 903 time-series recorded at electrode Pt1 situated, as Pt2, in the 904 ligament of Marshall anatomic area innervated by the ANS 905 (Figure 1A), are very similar to the ones observed at Pt2. 906 Both $\tau(q)$ and D(h) spectra are well approximated by quadratic 907 spectra (Equations 9 and 10, respectively) with parameters 908 $[c_0, c_1, c_2] = [1.01, -0.28, 0.064]$ (Figure 7) with a definitely 909 positive finite intermittency coefficient $c_2 = 0.064 \pm 0.014$ 910 (Table 1). Interestingly, time series recorded at electrodes Pt3 911 and Pt5 in a different anatomical area next to the left atrial 912

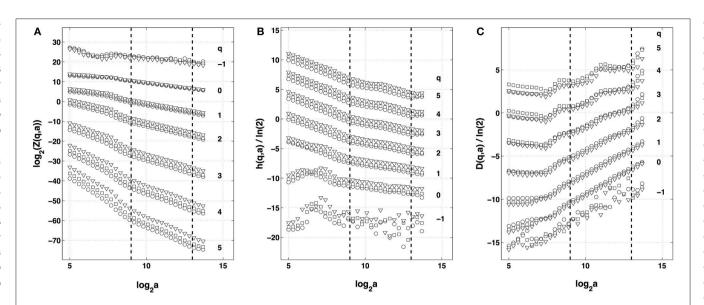
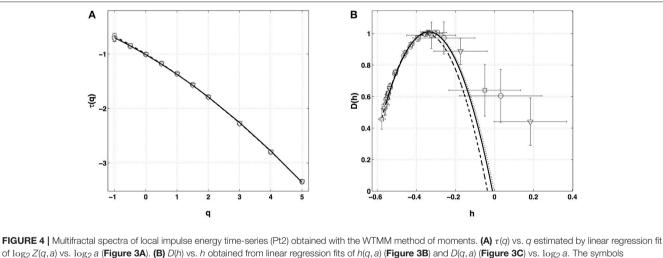


FIGURE 3 Multifractal analysis of local impulse energy time-series recorded at the electrode Pt2 with the WTMM method. (A) $\log_2 Z(q, a)$ vs. $\log_2 a$ (Equation 3). (B) $h(q, a)/\ln 2$ vs. $\log_2 a$ (Equation 5). (C) $D(q, a)/\ln 2$ vs. $\log_2 a$ (Equation 6). The computation were performed for different values from q = -1 to 5 with the analyzing wavelet $g^{(1)}(\nabla)$, $g^{(2)}(\Box)$ and $g^{(3)}(\circ)$ (Figure S1). The vertical dashed lines delimit the range of scales ($2^9 \le a \le 2^{13}$) used for the linear regression estimate of $\tau(q)$, h(q) and D(q) in **Figure 4**.



of $\log_2 Z(q, a)$ vs. $\log_2 a$ (Figure 3A). (B) D(h) vs. h obtained from linear regression fits of h(q, a) (Figure 3B) and D(q, a) (Figure 3C) vs. $\log_2 a$. The symbols correspond to the analyzing wavelets $g^{(1)}(\nabla)$, $g^{(2)}(\Box)$ and $g^{(3)}(\circ)$ (Figure S1). The curves correspond to quadratic spectra (Equations 10 and 12) with parameters $[c_0, c_1, c_2] = [1.01, -0.33, 0.055](\cdots, g^{(1)}), [1.00, -0.35, 0.049](- - -, g^{(2)}), [1.01, -0.34, 0.053](-, g^{(3)})$ (see Table 1).

posterior wall (Figure 1A) both show rather similar $\tau(q)$ and D(h) multifractal spectra but significantly different from the ones obtained at electrodes Pt1 and Pt2 (Figure 7). Again these spectra are found nearly quadratic with parameters $[c_0, c_1, c_2] =$ [1.02, -0.48, 0.098] for Pt3, and [1.03, -0.38, 0.152] for Pt5 (Table 1). Local impulse Local impulse energy time series at Pt3 and Pt5 show higher intermittency with larger c2 values whereas they display weaker long-range correlations $c_1 = \langle h \rangle \sim$ -0.45 (i.e., closer to $c_1 = -0.5$ a value characteristic of uncorrelated white noise), instead of the value $c_1 \sim -0.3$ for Pt1 and Pt2 characteristic of positive long-range correlations. As reported in Table 1, this regionalization of the multifractal

properties of the local impulse energy is quantitatively confirmed when using the magnitude cumulant method. It is further corroborated when reproducing this multifractal analysis for other patients with paroxysmal, persistent or chronic AF (**Figure 8A**) and for a patient at different periods of time preceding ablation procedure (**Figure 8B**) as an indication of stationarity.

4.2. Two-Point Magnitude Analysis of Local Impulse Energy Data

The results of the two-point magnitude correlation analysis of 1025 the local impulse energy time series recorded at the positions 1026

Pt1, Pt2, Pt3, and Pt5 along the CS vein are shown in Figure 9. $C(a, \Delta t)$ (Equation 15) computed with the analyzing wavelet $g^{(3)}$ is represented vs. Δt for two scales $a = 2^9$ and 2^{10}

TABLE 1 | Results of the WTMM multifractal analysis of the local impulse energy time-series recorded along the CS vein at electrodes Pt1, Pt2, Pt3, and Pt5.

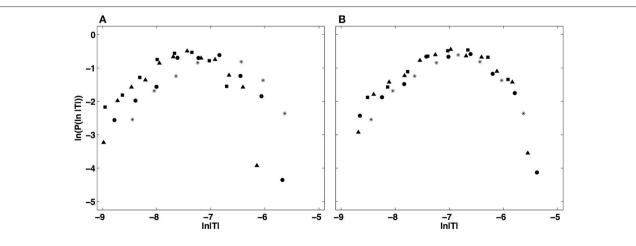
	g ⁽¹⁾	g ⁽²⁾	g ⁽³⁾
Point1			
c ₀	0.961 ± 0.001	0.995 ± 0.001	1.009 ± 0.002
C1	-0.351 ± 0.003	-0.298 ± 0.005	-0.281 ± 0.007
c*1	-0.353 ± 0.017	-0.297 ± 0.011	-0.274 ± 0.011
C2	0.048 ± 0.006	0.063 ± 0.011	0.064 ± 0.014
c [*] 2	0.050 ± 0.032	0.082 ± 0.018	0.096 ± 0.020
Point2	2		
C0	1.011 ± 0.002	0.998 ± 0.001	1.011 ± 0.00^{-1}
C1	-0.333 ± 0.007	-0.348 ± 0.003	-0.337 ± 0.005
c*	-0.307 ± 0.012	-0.335 ± 0.011	-0.331 ± 0.01
C2	0.055 ± 0.013	0.049 ± 0.007	0.053 ± 0.010
C2*	0.076 ± 0.030	0.031 ± 0.027	0.047 ± 0.028
Point3	}		
c ₀	1.023 ± 0.003	1.005 ± 0.002	1.021 ± 0.003
C1	-0.472 ± 0.014	-0.496 ± 0.008	-0.481 ± 0.01
C [*] 1	-0.445 ± 0.011	-0.480 ± 0.008	-0.464 ± 0.00^{-1}
C2	0.082 ± 0.028	0.091 ± 0.015	0.098 ± 0.022
c [*] 2	0.164 ± 0.031	0.103 ± 0.023	0.164 ± 0.020
Point5	;		
c ₀	1.044 ± 0.003	1.017 ± 0.003	1.029 ± 0.002
C1	-0.320 ± 0.014	-0.365 ± 0.011	-0.383 ± 0.009
c*1	-0.256 ± 0.015	-0.335 ± 0.018	-0.365 ± 0.023
C2	0.176 ± 0.028	0.167 ± 0.022	0.152 ± 0.01
c*2	0.175 ± 0.043	0.106 ± 0.029	0.114 ± 0.03

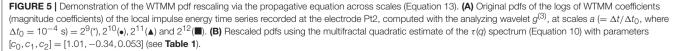
 c_0 , c_1 , c_2 are the coefficients of the polynomial expansion of $\tau(q)$ (Equation 10) obtained with the WTMM method of moments when using the analyzing wavelets $g^{(1)}$, $g^{(2)}$, and $g^{(3)}$ respectively (Figure S1). c_1^* and c_2^* are the corresponding coefficients obtained with the magnitude cumulant method.

in the scaling range. Strikingly for all four time series, for $\Delta t \gtrsim a, C(a, \Delta t)$ drops to zero as a clear indication that the magnitudes are uncorrelated. As a reference, we put in each panel of Figure 9, a dashed straight line of slope $-c_2$ as predicted by Equation (16) for multifractal signals exhibiting a cascading multiplicative structure along a time-scale tree (Arneodo et al., 1998b). The slow decay predicted by the "multiplicative" log-normal model with intermittency coefficient c₂ is definitely not observed. Thus, local impulse energy time-series look much more like what has been called log-normal "mutlifractal white noise" in pioneering works to distinguish "uncorrelated" and "multiplicative" log-normal models (Arneodo et al., 1998a). A similar absence of magnitude correlation is observed when reproducing this two-point magnitude analysis with the analyzing wavelets $g^{(1)}$ (Figure S17) and $g^{(2)}$ (Figure S18).

5. DISCUSSION

To summarize, we showed that the wavelet-based multifractal analysis of long time series of the local impulse energy recorded in the CS of a patient with chronic AF was able to reveal and quantify the intermittent nature of these signals at low frequency $(f \lesssim 2 \text{ Hz})$. To our knowledge, our study is the first to report on the observation and quantification of such multifractal dynamics of the endocavitary electrical activity during chronic AF which is found more complex than previously suspected. On the basis of the analysis of the time-series recorded at 4 catheter electrodes out of 5 positioned in the CS, two main observations can be made: (i) the local impulse energy displays different multifractal properties in the left atrial wall area than in the ligament of Marshall area consistently with different anatomical substrate conditions, and (ii) while recorded along the CS vein, the local impulse energy does not exhibit long-range dependence associated with an underlying multiplicative cascade, or in other words the multifractal distribution of the





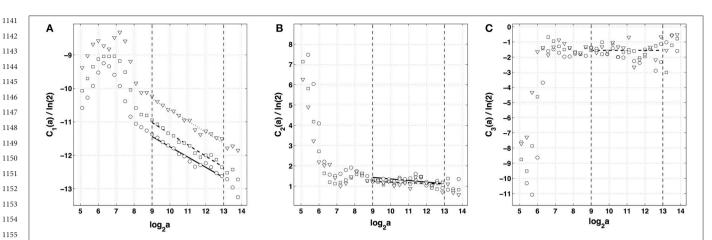


FIGURE 6 | Magnitude cumulant analysis of local impulse energy time-series (Pt2). (A) $C_1(a)/\ln 2$ vs. $\log_2 a$. (B) $C_2(a)/\ln 2$ vs. $\log_2 a$. (C) $C_3(a)/\ln 2$ vs. $\log_2 a$. The computation of the $C_n(a)$ (Equation 9) was performed with the analyzing wavelets $g^{(1)}(\nabla)$, $g^{(2)}(\Box)$ and $g^{(3)}(c)$ (Figure S1). The vertical dashed lines delimit the range of scales ($2^9 \le a \le 2^{13}$) used for the linear regression estimate of coefficients c_1^* , c_2^* and c_3^* of $\tau(q)$ (Equation 10) reported in **Table 1**.

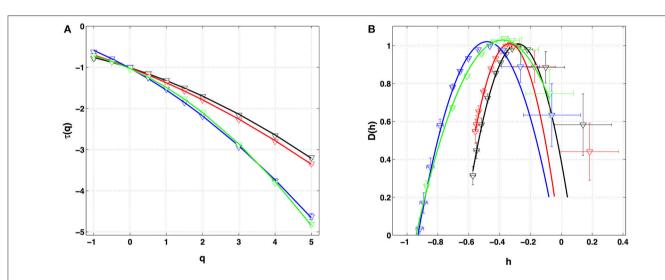


FIGURE 7 | Multifractal spectra of local impulse energy time-series recorded along the CS vein. (A) $\tau(q)$ vs. *q* estimated by linear regression fit of $\log_2 Z(q, a)$ vs. $\log_2 a$. (B) D(h) vs. *h* obtained from linear regression fits of h(q, a) and D(q, a) vs. $\ln_2 a$. The analyzing wavelets is $g^{(3)}$. The colored symbols correspond to the electrodes Pt1 (black), Pt2 (red), Pt3 (blue) and Pt5 (green). The curves correspond to quadratic spectra (Equations 10 and 12) with parameters $[c_0, c_1, c_2] = [1.01, -0.28, 0.064]$ (black, Pt1), [1.01, -0.34, 0.053] (red, Pt2), [1.02, -0.48, 0.098] (blue, Pt3), and [1.03, -0.38, 0.152] (green, Pt5) (see **Table 1**).

singularities inferred by the two-point magnitude analysis does not display any correlation across scales just like a log-normal "multifractal white noise" (Arneodo et al., 1998a). The nature of this study was exploratory, with a data set limited to a few patients, and with a few time series rather long for clinical practice (422 s) but not so long regarding the range of time scales [0.6, 10 s] where scaling was observed. This is the reason for the different complementary analyses employed in this paper including the WTMM method of moments, the WTMM method of magnitude cumulants, and the two-points magnitude cumulant method, using analyzing wavelets of different orders, until reliable estimates were obtained. Of course our results deserve to be confirmed over a large set of patients at different stages of AF development and to be explored in different areas

of the atria. The goal would be to exhibit precise determinants of the diseased substrate using multifractal scaling analysis. But this preliminary analysis definitely challenges current knowledge in physical, physiological and clinical fundamentals of AF arrhythmia. Specifically, it challenges the mechanistic approach of AF based on circuit reentries.

The absence of an underlying cascading process is not such a surprise since underlying the multifractal properties displayed by the local impulse energy at low frequencies ($f \leq 2$ Hz), there is no clear 3D "fragmentation" (Mandelbrot, 1982) process inducing some cascading of energy from large to small time scales and also no obvious 2D "aggregation, coalescence or growth" (Vicsek, 1989) process bringing energy from small to large time scales. What are the physical and physiological mechanisms that drive

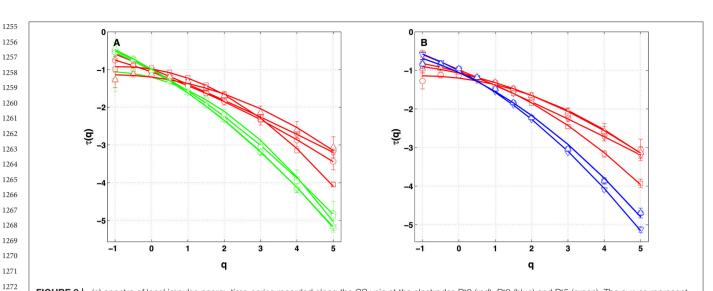


FIGURE 8 | $\tau(q)$ spectra of local impulse energy time-series recorded along the CS vein at the electrodes Pt2 (red), Pt3 (blue) and Pt5 (green). The curves represent quadratic polynomial fit of the data (Equation 10). (A) The symbols correspond to the reference Patient 1 (chronic AF, ∇) and to Patients 2 (chronic AF, \circ), 3 (paroxysmal AF, \Box) and 4 (persistent AF, \triangle). (B) The symbols correspond to the reference Patient 1 (∇) and to three different time-series for Patient 4 (\circ , \Box , \triangle) recorded at different periods of time preceding ablation procedure.

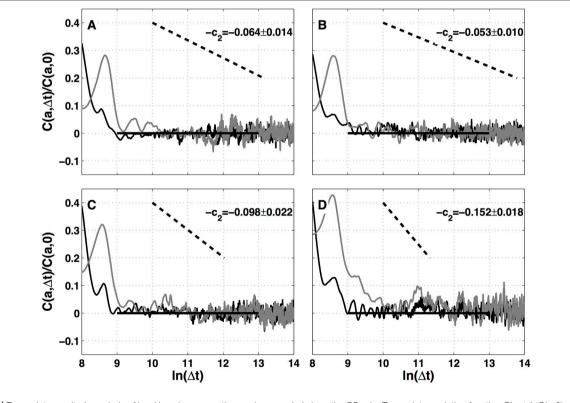


FIGURE 9 | Two-point magnitude analysis of local impulse energy time-series recorded along the CS vein. Two-point correlation function $C(a, \Delta t)/C(a, 0)$ vs. $\ln(\Delta t)$ (Equation 15) for local impulse energy E(t) computed with the analyzing wavelet $g^{(3)}$. The two curves correspond to scales $a = 2^9$ (black) and 2^{10} (gray) within the scaling range. (A) Pt1, (B) Pt2, (C) Pt3, and (D) Pt5.

the multifractal nature of local impulse energy and give rise to the observed differences according to area is still an open question. Nonetheless, these results already undermine the commonly accepted concepts revolving around circuit reentries, and a fortiori spiral waves, as being basic mechanisms for the onset and perpetuation of AF. The mechanistic "wavelength" criterion 1367

indeed conveys the idea that random spatio-temporal dispersion 1369 of refractoriness, or more generally of functional properties, leads 1370 to random mixing of circuit reentries. The "wavelength" scale 1371 adjusts naturally to the typical scale λ of dispersion when it exists 1372 $c \times RP \lesssim \lambda$, as would be the case for Gaussian statistics of 1373 dispersion. In that case, the statistics of the local impulse energy 1374 remains Gaussian throughout scales. On the contrary, to fit our 1375 new observations we have seen that the statistics is not Gaussian 1376 and evolves across scales through a log-normal propagation 1377 law which accounts for the intermittency observed over the 1378 range of a few beat cycles (~ 0.6 s) to several tens (~ 10 s) (and 1379 possibly more), therefore spanning the whole atria. Although 1380 the ligament of Marshall area is highly innervated (Tan et al., 1381 2007; Ulphani et al., 2007; Arora, 2012), it is guite unlikely that 1382 modulations by the ANS, that affects heart rate, play a significant 1383 role in the intermittent dynamics since the documented three 1384 peak frequencies at ~ 0.4 , ~ 0.15 , and ~ 0.04 Hz (Akselrod et al., 1385 1981) do not show up in our analysis. Furthermore, we have 1386 found at least two areas with different multifractal regimes. 1387 Thus, our findings raise new challenging questions calling for 1388 ongoing efforts to develop physiological heart tissue models 1389 that account for the low frequency intermittent nature of local 1390 impulse energy. Recent studies in animal models suggest the 1391 protective role of connexin gene transfer to prevent sustained 1392 AF (Bikou et al., 2011; Igarashi et al., 2012). In this spirit, in a 1393 companion modeling paper (Attuel et al., submitted), we propose 1394 a model of gap junction conduction remodeling in a denervated 1395 heart that accounts for the observed intermittent dynamics over 1396 large time scales, as resulting from incoherent random back 1397 scatterings leading to the desynchronization of the network of 1398 cardiac excitable cells. 1390

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AUTHOR CONTRIBUTIONS

Conception and design: GA, HY, AA. Development and methodology: EG-C, FA, AA. Analysis and interpretation of data: GA, EG-C, FA, HY, AA. Acquisition of data (provided animals, acquired and managed patients, provided facilities, etc.): GA, HY. Writing, review, and/or revision of the manuscript: GA, EG-C, FA, HY, AA. Administrative, technical or material support (i.e., requiring and organizing data, constructing databases): GA, EG-C.

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SUPPLEMENTARY MATERIAL

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Conflict of Interest Statement: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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