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Combining Free choice and Time in Petri Nets

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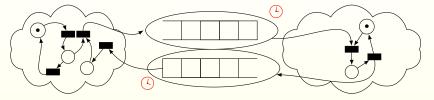
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TRENDS Sept. 9th 2017

[TIME'16]

Motivation 1 : Modeling issues

Model Time constrained unbounded concurrent systems



Desired features

- Latency : messages take at least 10 ms to reach their destination
- Timeout/urgency : a message not consumed after 200ms is lost
- Rates : a message is received every γ t.u,...

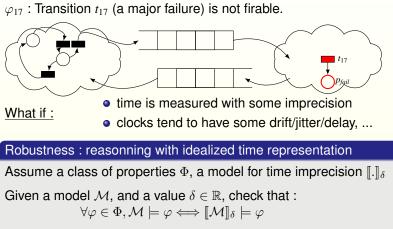
Standard questions

- Reachability : is marking M reachable from initial marking M₀?
- Coverability : Given a marking *M*, is there a marking *M'* reachable from *M*₀ such that *M'*(*p*) > *M*(*p*) for every place *p*?
- Boundedness : is there a bound K such that for every reachable marking, every place p, M(p) ≤ K?
- Firability : is there an execution in which transition *t* is fired?

Objectives

- Decidability for these questions
- Efficient algorithms

Motivation 3 : Robustness

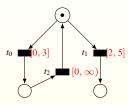


Given a model \mathcal{M} , check if :

 $\exists \Delta, \forall \delta \leq \Delta, \forall \varphi \in \Phi, \mathcal{M} \models \varphi \Longleftrightarrow \llbracket \mathcal{M} \rrbracket_{\delta} \models \varphi$

Time vs Timed Petri nets

Time Petri nets [Merlin74]

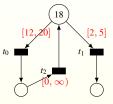


Pros :

- time
- Urgency
- unbounded places
- Expressive power

Cons : Undecidability

Timed Petri nets [Walter83]



Pros :

- time
- unbounded places
- Ages
- WSTS ≡ decidability of coverability, boundedness,...

Cons : no urgency

Free-choice Multiserver Time Petri nets

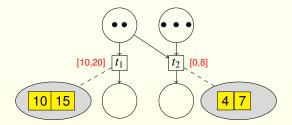
- Processes and their relation to untimed nets
- Firability
- Robustness

TPN Multiserver Semantics : Configuration

Configuration (Threshold Semantics)

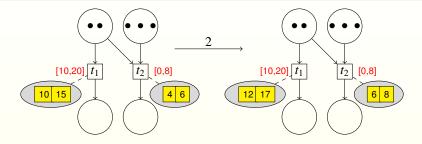
C = (M, mem)

- M : marking, enables transitions several times
- *mem* : remembers for each enabling instance of a transition for how long it has been enabled



 $M(p_0) = 2; M(p_1) = 3; M(p_3) = 0; M(p_4) = 0$ $mem(t_1) = \{10; 15\} mem(t_2) = \{4; 7\}$

TPN Multiserver Semantics : timed move



Timed Move : $C \xrightarrow{\delta} C'$

Let a duration δ elapse = update memorized durations

Urgency of a transition t in C = (M, mem)

Let t be a transition such that :

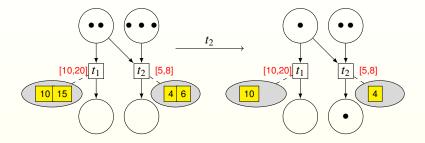
• I(t) = [l, u]

• t has been enabled for u t.u, i.e., max mem(t) = u

then, t is urgent.

Time cannot progress, a discrete move must occur.

TPN Multiserver Semantics : discrete move



Discrete firing : $C \stackrel{t_i}{\longrightarrow} C'$

- $I(t_i) = [l, u], \max(mem(t_i)) > l$ (t_i need not be urgent)
- modification of memory for transitions in competition with t_i
- Other enabling instances remain untouched

Behaviors of a net

• Labeled Transition System : $(\mathcal{C}, \longrightarrow, C_0)$

Restrictions (to obtain decidable classes)

Forbid nets that can force zero-delay behaviors.

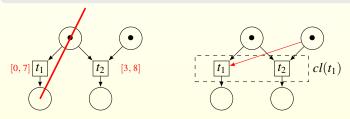




Free choice PN and free choice TPN

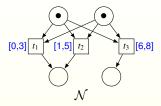
(FC-PN) $\mathcal{U} = (P, T, F)$ is free choice if $\forall t, t' \in T, \bullet t \cap \bullet t' \neq \emptyset \implies \bullet t = \bullet t'$. (FC-TPN) $\mathcal{N} = (\mathcal{U}, M_0, I)$ is a free choice TPN if $Untime(\mathcal{N}) = \mathcal{U}$ is free choice.

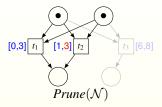
The cluster of transition *t* is $Cl(t) = \{t' \in T \mid \bullet t \cap \bullet t' \neq \emptyset\}$



Pruning FC-TPN (a.k.a normalization [Chatain13]),

Some transitions in FC-TPNs will obviously never fire !





To obtain a Pruned FC-TPN

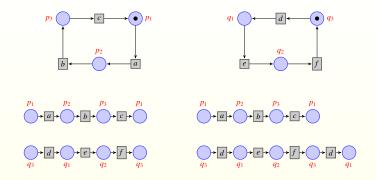
- remove unfirable transitions :
 - $t: I(t) = [a, b] \land \exists t', I(t') = [c, d]$ with d < a

• Associate to remaining transition possible values for intervals $I(t) = [a, b] \Rightarrow I'(t) = [a, \max_{t \in Cl(t)} (lft(t'))]$

Pruning Lemma : Let ${\mathcal N}$ be a FC-TPN, then

the transition systems associated with N and Prune(N)) are isomorphic. (not true outside FC-TPNs)

Causal processes



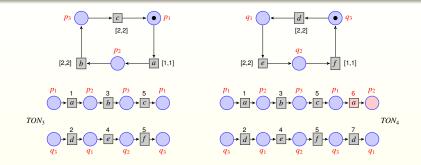
Untimed causal processes ON1 and ON2

Causal processes

- A partial order representation of executions
- **Principle :** Unfold the net by glueing transitions/places occurrences one after another starting from the initially marked places

Still an untimed setting!

Timed causal processes



Advantages of Timed Causal processes

- Partial order timed representation of timed executions
- URGENCY is considered : if *d* occurs at date 7 in *TON*, all urgent transitions before *d* also occur in *TON*.

Relation between Timed causal Processes and timed languages

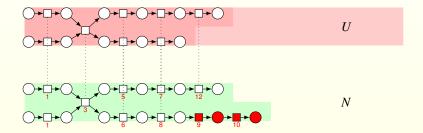
Let $\mathcal P$ be the set of timed causal processes of $\mathcal N.$ Then,

$$Lang(\mathcal{N}) = \bigcup_{N \in \mathcal{P}} Lang(N)$$

Theorem 1 : Inclusion of untimed prefixes

Let $\mathcal{N} = (\mathcal{U}, M_0, I)$ be a pruned FC-TPN (w.o. forced 0-delay sequences). U be an (untimed) causal process of $\mathcal{U} = Untime(\mathcal{N})$.

Then there exists a timed causal process *N* of \mathcal{N} such that $U \leq Untime(N)$.

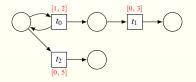


Decidability

Theorem 2 : Fireability

Let $\mathcal{N} = (\mathcal{U}, M_0, I)$ be an FC-TPN (w.o. forced 0-delay). Checking fireability of a transition $t \in T$ in \mathcal{N} is decidable.

<u>Proof idea</u> :Firability \sim coverability in untimed nets [Rack78]



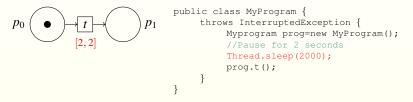
Theorem 3 : Termination

Let $\mathcal{N} = (\mathcal{U}, M_0, I)$ be an FC-TPN (w.o. forced 0-delay). It is decidable if \mathcal{N} terminates.

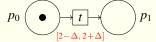
Proof Idea :

an infinite run of $U = Untime(Prune(\mathcal{N}))$ has a timed counterpart in \mathcal{N} and conversely. (and termination is decidable in untimed Petri nets)

A major drawback of timed models :



What the implementation might really do :



 $p_0 \underbrace{\bullet}_{[1+\Delta,2-\Delta]} p_1$

Guard Shrinking

Guard enlargement

Form now : $\mathcal{N}_{\delta} = \mathcal{N}$ with enlarged guards

Definition (robustness problems for TPNs)

Given a TPN $\mathcal{N},$ does there exist $\Delta \in \mathbb{Q}_{>0}$ such that $\forall \delta \leq \Delta$

- $Fireable(\mathcal{N}) = Fireable(\mathcal{N}_{\delta})$?
- \mathcal{N} terminates iff \mathcal{N}_{δ} terminates
- \mathcal{N} is bounded iff \mathcal{N}_{δ} is bounded...

<u>Note</u> : Firability, termination, boundedness are not a priori robust/non robust properties of the whole class of FC-TPNs.

Theorem 4

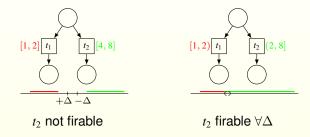
Let \mathcal{N} be a FC-TPN without forced 0-delay time firing sequences. Then robustness of fireability is decidable. If \mathcal{N} has robust fireability, bound Δ can Be effectively computed.

Theorem 5

Let \mathcal{N} be a FC-TPN without forced 0-delay time firing sequences. Then it is decidable whether temination is a robust property of \mathcal{N} .

Proof idea

If $Prune(\mathcal{N})$ and $Prune(\mathcal{N}_{\Delta})$ have the same clusters, then Δ -enlargement of \mathcal{N} does not modify firable transitions.



Check for each accessible cluster *C* whether intervals can be enlarged by some Δ_C without changing firable transitions

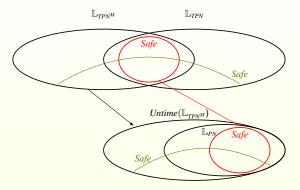
Contributions so far :

- A FC-Multiserver PN variant with its process semantics
- Decidable firability, termination
- Decidability of robustness of firability, termination, wrt enlargement (and shrinking)

Open questions :

- decidability of Coverabillity, reachability and boundedness for FC-TPNs?
- Robustness of more properties?
- same issues without multi-enabledness?
- Expressiveness of FC-TPNs?

 \mathbb{L}_{TPN^M} : Timed languages expressible with Time Petri nets (Multiserver) \mathbb{L}_{TPN} : Timed languages expressible with Time Petri nets \mathbb{L}_{PN} : Untimed languages expressible with Petri nets



(Thm. 1) In free choice nets, timed / untimed processes tightly related What about Languages?

 $\mathbb{L}_{PN} \subseteq Untime(\mathbb{L}_{TPN^{M}}) \quad \mathbb{L}_{PN \cap Safe} = Untime(\mathbb{L}_{TPN^{M} \cap Safe}) \quad \mathbb{L}_{PN} \neq Untime(\mathbb{L}_{TPN^{M}}??)$

Time & PN related Publis (SUMO group, INRIA Rennes) :

[AHP16]S. Akshay, L. Hélouët, R. Phawade, *Combining free choice and time in petri nets*, IEEE Proc. of TIME 2016, pp. 120–129, 2016.

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