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Implementing an Integer Linear Approach to Multi-Objective Phasor Measurement Unit Placement

Amir Baharvandi¹, Miadreza Shafie-khah¹, Saber Talari¹, and João P.S. Catalão^{1,2,3}

C-MAST, University of Beira Interior, Covilhã 6201-001, Portugal
 INESC TEC and the Faculty of Engineering of the University of Porto, Porto 4200-465
 INESC-ID, Instituto Superior Técnico, University of Lisbon, Lisbon 1049-001, Portugal amir.baharvandi@gmail.com; miadreza@ubi.pt; saber.talari@ubi.pt; catalao@fe.up.pt

Abstract. In this paper, an Integer Linear Programming (ILP) problem for a model of Multi-Objective Optimal PMU Placement (MOPP) is proposed. The proposed approach concurrently deals with two objectives. The first objective is the number of phasor measurement units (PMUs) which should be minimized. The second objective function is measurement redundancy which is the number of observable buses in the case of PMU outage. In fact, whatever the amount of second objective increases, the system would be more reliable. Furthermore, some linearized formulations are defined for each nonlinear formula. In fact, the nonlinear nature of formulation related to redundancy is substituted by linear inequality and so there is no nonlinear formula such that the calculation of the problem would be simplified. Finally, a modified 9-bus test system is implemented to show how the proposed method is effective.

Keywords: Phasor Measurement Unit (PMU), Multi-objective Mathematical Programming, Integer Linear Programming, Optimal PMU Placement.

1 Introduction

The key element of the wide-area monitoring system and application of smart systems is to attain a instantaneous measurement of state variables which Phasor Measurement Units (PMUs) are able to deliver it [1-3]. To increase the security of the system, the future state of the entire network should be estimated [4]. Accordingly, devices known as PMU are used to measure the system's phasors (voltage and current) [5], [6].

In this paper, two previously mentioned objective functions will be described as a Multi-Objective problem in the optimum PMU placement area. Also, to prove the usefulness of the method a case study is tested.

2 Relationship to Smart Systems

Since the metering of the smart systems is of paramount importance to the operator. There are several devices equipping smart cities. These devices are in the kind of electronic devices base of Internet of Things (IoT) [7]. Additionally, the internet facilitates interconnection between people and objects and it is known as the main revolution of the internet infrastructure.

One of these devices using Global Positioning System (GPS) to increase the reliability of the system is Phasor Measurement Unit. It is absolutely certain that implementation of the technological devices has increased drastically in smart cities. In this condition, Phasor Measurement Units can be very applicable in the power electrical systems of smart cities.

To make a clear relationship between the proposed research area and smart system, it should be noted that in the basis of IoT, there is a huge communication between devices using the internet. Likewise, in the smart systems, consumers can manage their consumption in order to decrease their cost of electricity [8].

First relationship between PMU and smart systems is about using the internet. PMUs implement GPS to calculate the voltage phasor of buses and in this process gathers data from buses and uses an internet interconnection with satellite subsequently sends data to a central server. This process is shown in Fig. 1. Another relationship between PMU device and smart system is about managing consumption in smart grids [9].

The calculation of phasors by PMU is utilized to estimate the future states of the power systems and this help to anticipate several parameters such as future consumption in order to supply future loads [10]. State estimating helps the generators and consumers to manage their supply and consumption.

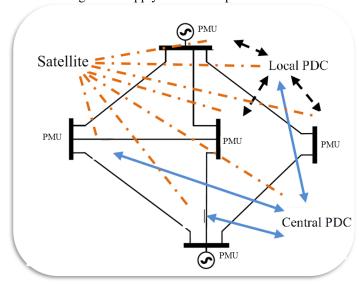


Fig. 1. PMU process

3 Problem Formulation

In the MOPP problem the best condition is making the entire network observable while the redundancy of the system is in a suitable range. It goes without saying that this observability is better to achieve using the minimum PMUs and at the same time all the system constraints would be satisfied.

In the following objective functions and constraints are introduced.

3.1 Objective Function

F₁: First Objective Function

As mentioned before we want to increase the observability of the system (all buses) by minimum cost. Thus, minimum number of PMU which is equivalent the minimum cost is the first objective function:

$$\min F_1 = \sum_{\forall i \in I} x_i. \tag{1}$$

where F_I is the first objective function, x_i is a binary variable (which equals to 0 if the bus has not PMU and 1 otherwise) and I is a set for all buses from 1 to N_b (N_b is the number of buses).

F₂: Second Objective Function

The second objective is redundancy which is associated with contingency occurrence in the system. This contingency may be PMU. It means when a contingency occurs how many buses lose their observability. The desire condition is that we will have the minimum number of unobservable bus. In other word it is absolutely certain that whatever the PMUs increases the number of unobservable buses decreases as well as the redundancy increases. On the contrary, whatever the number of PMUs would be more the cost of installation related to the first objective function increases. So, we have the limitation of PMU and cost and should be aware about it.

Redundancy parameter (r) is equal to the number of observable buses while a contingency occurs. In this study we suppose that this contingency could be PMU loss. The second objective function is introduced as the number of set of buses which are observable when all the contingencies occur separately. This set is defined as R and the member of this set (r) should be maximized. Furthermore, maximizing of r is equivalent to the following formulation:

$$\min F_2 = N_b - r. \tag{2}$$

If a PMU is placed on especial bus, that bus and buses connected to that bus are observable. For Example, in Fig. 2, assume that 3 PMUs are located at buses 1, 2, and 7 and all buses are observable. To explain the redundancy criterion, we should disregard PMUs one by one and after each contingency the observability of buses should be analyzed. Now suppose that PMU installed at bus 1 is failed. In this state,

all the buses are observable too. Accordingly, the PMU located at bus 7 would be failed. In this contingency bus 7 would be unobservable. Similarly, in the case of PMU outage at bus 2, buses 3, 4 and 5 are unobservable. Thus, the number of entire unobservable buses in all PMU outages is 4 and this is the value of second objective function.

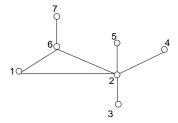


Fig. 2. Example for illustration

3.2 Constraints

As mentioned before, an installed PMU results in observability for he installed bus and its adjacent buses. A function (f_i) is introduced as sum of u_i for bus i and its neighbors.

$$f_i = GX = \sum_{j \in I} g_{ij} \times u_j, \quad \forall i \in I.$$
 (3) where,

$$G = \left[g_{ij}\right]_{N_b \times N_b}$$

$$g_{ij} = \begin{cases} 1, & \text{if bus } i \text{ and } j \text{ are connected or } i = j \\ 0, & \text{otherwise} \end{cases}$$
(5)

$$U = \left[u_1 \, u_2 \, ... u_{Nb} \, \right]^T \tag{6}$$

To avoid any unobservable bus, all the functions of f_i should be nonzero:

$$f_i \ge 1, \quad \forall i \in I. \tag{7}$$

There is another issue related to zero injection buses. These buses may reduce the PMU number using KCL. In fact, when all buses associated with a zero injection bus are observable but one of them is unobservable, the KCL law leads to observability of that unobservable bus. Therefore, f_i in (3) would be as follows [11]:

$$f_i = \sum_{j \in I} g_{ij} \times u_j + \sum_{j \in I} g_{ij} \times t_j \times q_{ij}, \quad \forall i \in I.$$
 (8)

$$t_{j} = \sum_{i \in I} u_{ij} \times q_{ij}, \quad \forall j \in I.$$
(9)

where, t_i is another binary variable (1 for zero injection bus and zero otherwise) and q_{ij} represents an auxiliary binary variable. Suppose a zero injection bus j with t_i =1. In this state in (9) just one of the q_{ij} equals to 1 which means zero injection bus jresults in bus i to be observable and the equality (9) would be correct. Hence, the impact of zero injection buses is taken into account as the second part of (8) that is increased if a zero injection bus causes that another bus is observable. The zero injection buses, t_i and q_{ij} are explained completely in [11]. Similarly, when a power flow is placed on one line, if one of the sending-end or receiving-end buses of that line is observable, there is no need for other end-bus to have PMU for observability and it can be observable due to other bus. Thus, constraint (7) for line ij which is a power flow line is substituted by:

$$f_i + f_j \ge 1 \tag{10}$$

To formulate redundancy mathematically the following formula is presented using another binary variable i.e. β_i :

$$\frac{1}{2 \times N_b} + \frac{f_i - 3}{N_b} \le \beta_i \le 1 + \frac{f_i - 3}{N_b}.$$
 (11)

In inequality (11), when f_i is higher than 2 the left hand side of (11) will be between zero and one, and the other side would be greater than one so β_i will be 1. Also, it is be equal to 0 if $f_i < 2$, then $\beta_i = 0$. Thus, sum of β_i denotes the redundant buses with $f_i > 2$.

$$F_2 = N_b - \sum_{\forall i \in I} \beta_i. \tag{12}$$

This is the constraint of redundancy which should be greater than a specific value according to necessity of system operator.

$$r \ge p_{\min}. \tag{13}$$

where the required minimum value of redundancy is p_{min} .

3.3 Multi-Objective Solution Methodology

The MOPP problem is as follows: $\min \{F_1(x), F_2(x)\}$

$$st.: g(x) \le 0, \quad h(x) = 0.$$
 (14)

4 Simulation Results

A nine-bus test system has been implemented to simulate the proposed multiobjective optimization problem. The proposed approach has been employed through a Pentium IV, 1-GHz Core i5 with 8 GB RAM using mixed integer linear programming solver CPLEX 9.0 in the GAMS [14]. Fig. 3 shows the 9-bus test system. Except buses 1, 2 and 4 all the buses have load and also there are 2 generation units located at buses 1 and 2. Thus, bus 4 has no load and generator and is considered as a zero injection bus.

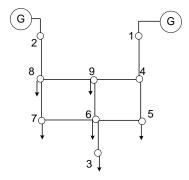


Fig. 3. Modified 9-bus test system

If the first objective function is considered as the main objective, we can have an observable system using lowest number of PMUs that is 3 PMUs at buses 4, 6 and 8. Subsequently, the amount of second objective stays in the worst state and there is no redundant bus with $f \ge 2$.

$$F_2 = N_b - \sum_{\forall i \in I} \beta_i = 9 - 0 = 9.$$

In the flip side, if we solve the single objective problem so that the second objective function is the main objective, there would be 6 PMU at buses 4-9. In this condition the second objective is equal to 3. The amount of F_2 cannot be less than 3, because there are 3 buses in the system which cannot have $f \ge 2$.

The Pareto points of the proposed Multi-objective method are shown in Fig. 4 and Table I. As we can see from these Figure and Table, two objective functions have conflict manner and they cannot be optimum simultaneously. Whatever the first objective function would be minimized the second one would be worse and conversely.

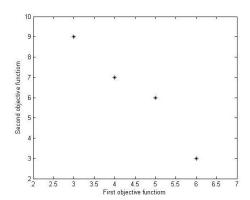


Fig. 4. Pareto set related to test system

Table.1 Pareto points for 9-Bus	Test System	According to MOPP

Pareto #	F_1	F_2	Number of PMU buses	Number of Redundancy buses
1	3	9	4,6,8	-
2	4	7	6,7,8,9	7,8
3	5	6	2,5,6,7,8	6,7,8
4	6	3	4,5,6,7,8,9	4,5,6,7,8,9

Also, constraint (13) can decrease the number of points. For example in the case of $p_{\min} = 1$ (the system needs 1 redundant bus) the first row of Pareto set in Table I should be disregarded. It is noteworthy that, the proposed approach can be implemented on larger case studies such as 118-bus or more because the formulation is linear and not complex.

5 Conclusion

This paper proposed a multi-objective PMU placement taking into account the redundancy as an extra objective. The redundancy criterion was introduced when a PMU was not in a suitable operation mode. Moreover, the formulation is linear for redundancy which decreases the complexity of the calculation. Two conflict objective functions are minimized simultaneously and the system operator can make a trade-off between points in the Pareto set and choose the best solution point according to the system requirements.

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