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A Three Revolute-Revolute-Spherical wearable fingertip cutaneous device for stiffness rendering

Francesco Chinello, Claudio Pacchierotti, Monica Malvezzi, and Domenico Prattichizzo

Abstract—We present a novel three Revolute-Revolute-Spherical (3RRS) wearable fingertip device for the rendering of stiffness information. It is composed of a static upper body and a mobile end-effector. The upper body is located on the nail side of the finger, supporting three small servo motors, and the mobile end-effector is in contact with the finger pulp. The two parts are connected by three articulated legs, actuated by the motors. The end-effector can move toward the user’s fingertip and rotate it to simulate contacts with arbitrarily-oriented surfaces. Moreover, a vibrotactile motor placed below the end-effector conveys vibrations to the fingertip. The proposed device weights 25 g for 35×50×48 mm dimensions. To test the effectiveness of our wearable haptic device and its level of wearability, we carried out two experiments, enrolling thirty human subjects in total. The first experiment tested the capability of our device in differentiating stiffness information, while the second one focused on evaluating its applicability in an immersive virtual reality scenario. Results showed the effectiveness of the proposed wearable solution, with a JND for stiffness of 208.5 ± 17.2 N/m. Moreover, all subjects preferred the virtual interaction experience when provided with wearable cutaneous feedback, even if results also showed that subjects found our device still a bit difficult to use.

Index Terms—Haptic interfaces, wearable haptics, cutaneous devices, fingertip devices, softness rendering

1 INTRODUCTION

Wearable haptics is recently gaining great attention in the haptics and robotics fields. The demand for lightweight, compact, and unobtrusive wearable interfaces challenges researchers to pursue innovative solutions to make existing technologies more portable and wearable. Commercially-available wearable devices, such as the Apple Watch, the Motorola Moto 360, and the Microsoft Band, already provide simple vibrotactile haptic feedback to the wearer. For example, the Apple Watch embeds a linear actuator that can make the watch vibrate. It is used whenever the wearer receives an alert or notification, or to communicate with other Apple Watch owners. There are also applications being specifically developed to exploit the haptic capabilities of these devices. For example, the application “Feel The Wear”, available in the Google PlayStore, enables the user to create custom vibration patterns by simply tapping the screen; and the application “Touch Room”, available in the Apple’s AppStore, enables two users that are far away to feel each other’s touch through the screen of the device.

However, although quite interesting and promising, the haptic stimuli provided by these devices are still limited to vibrations, reducing the possibility of simulating rich contact sensations. Toward more compelling interactions, researchers have recently focused on wearable fingertip devices providing tactile stimuli through moving tactors, which are able to translate, rotate, and orient to simulate haptic interaction with different surfaces. Frisoli et al. [1] presented already in 2008 a fingertip haptic display for improving curvature discrimination using a moving platform. The device is designed to bring a plate into contact with the fingertip at different orientations, defined by the normal to the virtual surface at the point of contact. The system is composed of a parallel platform, actuating a translation stage for positioning the plate relatively to the fingerpad, and of a serial wrist, in charge of adjusting its orientation. The device is actuated via sheathed tendons. A more portable and improved design solution of the same concept has been later developed in [2], [3]. A voice-coil actuator was introduced for simulating fast contact transition, and the overall system mobility was reduced to 3-degrees-of-freedom (3-DoF): two degrees of freedom for the orientation and one linear degree of freedom to control the contact force at the fingertip. Gabardi et al. [4] further improved the above design by replacing sheathed tendons actuation with DC motors mounted directly on the joints. Moreover, they increased the portability and wearability of the system by reducing the overall weight and dimensions. The total weight of this device is now only 30 g for 66×35×38 mm dimensions.

Similarly, Prattichizzo et al. [5] presented a wearable 3-degrees-of-freedom (3-DoF) cutaneous device for the fingertip. It consists of two platforms: one is located on the back of the finger, supporting three small DC motors, and the other one is in contact with the volar surface of the fingertip. The motors shorten and lengthen three cables to move the platform toward the user’s fingertip and re-angled to it to simulate contacts with arbitrarily oriented surfaces. Tsetterukou et al. [6] developed a 2-DoF wearable fingertip cutaneous device. It is composed of two DC motors driving a five-bar linkage mechanism mounted at the sides of the fingertip. Similarly to [7], when motors rotate in the same direction the linkage slides tangentially on the finger pad. On the other hand, when motors rotate in the same direction, the linkage moves towards or away from the fingertip. More recently, Leonardis et al. [8] presented a 3RSR wearable skin stretch cutaneous device.
for the fingertip. An asymmetrical 3RSR configuration allowed compact dimensions with minimum encumbrance of the hand workspace and minimum inter-finger interference. Girard et al. [9] developed a wearable haptic device able to simulate 2-DoF shear forces at the fingertip. It is composed of a parallelogram structure actuated by two DC motors able to move a peg responsible for the shear feedback. It weights only 22 g for a total dimension of 20×34×35 mm.

The above mentioned devices have been used for the rendering of shapes, forces, and compliance. In the last couple of years, the rendering of softness/compliance have became a popular topic in haptics research. Softness represents indeed one of the most fundamental haptic properties [10], and it plays a crucial role for task accomplishment in many scenarios and applications. For example, De Rossi [11] integrated electroactive polymeric materials into wearable garments to endow them with sensing and actuation properties, for applications in post-stroke rehabilitation. Mueller [12] proposed an air-inflatable vest that can be remotely triggered to create a sensation of being hugged. Bau et al. [13] developed a matrix of electromagnetic actuators enclosed in fabric, able to expand and shrink. Sahoo et al. [14] presented a tabletop display providing controlled self-actuated deformation to an elastic fabric surface. The surface is composed of a highly-stretchable pure spandex fabric, which is electrostatically actuated by nine electrodes. More recently, Bianchi et al. [15], [16] proposed a wearable softness display for the fingertip. It controls the stretching state of a fabric to reproduce different stiffness levels, and it can convey, at the same time, softness information, tangential cues, and enable both passive and active haptic exploration. It weights 100 g for 100×60×36 mm dimensions. The same group also applied a similar fabric-based rendering principle at the forearm [17] and arm [18].

A more extensive review of the literature on wearable cutaneous devices for the fingertip can be found in [19], [20].

This paper presents a the application of a 3RRS wearable fingertip device (see Fig. 1) to render the softness of a surface. It is composed of a static upper body and a mobile end-effector: the upper body is located on the nail side of the finger, supporting three small servo motors, and the mobile end-effector is in contact with the finger pulp. The two parts are connected by two articulated legs, actuated by the motors. The end-effector can move toward the user’s fingertip and rotate it to simulate contacts with arbitrarily-oriented surfaces. Moreover, a vibrotactile motor placed below the end-effector conveys vibrations to the fingertip. The device was preliminarily introduced in [21], [22]. However, these two works mainly focused on its mechatronic design, mechanical analysis and design, and position control system. In this paper, we will show how the device can be used to render the softness of a surface and, in particular, we will focus on its stiffness control system.

The paper is organized as follows. Section 2 introduces the device and summarizes its main features, and in particular some details on the device mechanical model and on the evaluation of the Jacobian matrix, necessary to evaluate the equivalent stiffness matrix in the actuated joint space. Section 4 describes the main outcomes of device kinematics model and proposes a position control system in which the stiffness can be regulated to render the compliance of a virtual surface. Section 5 shows some experiments in which the proposed control scheme is exploited. Finally, Sec. 6 discusses the obtained results.

2 DEVICE DESCRIPTION

As previously introduced, the wearable fingertip device proposed in this paper has a 3-DoF parallel structure, in which each leg connecting the end-effector to the upper body is composed of two rigid links constrained to each other, the body, and the end-effector, according to a RRS (Revolute-Revolute-Spherical) kinematic chain (see Fig. 2a and 2b). Specifically, three spherical (S) joints connect the distal links of the legs to the end-effector, one revolute (R) joint connects the distal and proximal links of each leg, and another revolute (R) joint connects the proximal link of each leg to the body. The three revolute joints between the proximal links and the body are actuated by the servo motors. In each leg, the axes of the two revolute joints are parallel, so that it constitutes a 2-DoF planar articulated mechanism, constraining the motion of the center of each spherical joint on a plane fixed w.r.t. the body. The mobile end-effector has therefore 3-DoF w.r.t.
the body. The proposed device weights 25 g for 35×50×48 mm dimensions.

With respect to the cable-driven fingertip devices presented in [5], [23], [24], this device solves the indeterminacy due to the underactuation of the platform. In fact, the platform is moved through three articulated legs, constraining its motion in a three-dimensional subspace [25]. This mechanical structure decouples position and force control problems, simplifying the control structure with respect to the solution proposed in [5]. The fingertip device is wired to an arm band on the upper arm, that hosts a Raspberry Pi Model B, an Arduino Nano, and two 2 Ah batteries. The arm band is in charge of providing the required power to the device and to manage the wireless communication between the device and an external computer.

For our prototype, shown in Fig. 2a and 1b, we used three HS-5035HD servomotors by Hi-Tech Motors and one 304-101 vibration motor by Precision Microdrives. The stall torques provided by each servomotor allow us to reach a maximum force of 4.7 N at the end-effector. The overall performance and operative parameters of our device are summarized in Table 1.

### 3 Device Analysis

In this section, we summarise some details on the device mechanical model, in particular on the evaluation of the Jacobian matrix and of the equivalent stiffness matrix, necessary to simulate the contact with surfaces of different compliance values. Further details on the device mechanical analysis, including some numerical simulations, and manipulability evaluation, are available in [21].

In this section, we summarise the main elements of the device mechanical model, necessary to develop the stiffness control system we adopted in the remaining of the paper. A complete analysis of the device kinematics and dynamics is out of the scope of this work; however, we have reported some necessary details in the following, regarding, in particular, the evaluation of the complete Jacobian matrix.

The meaning of the main symbols adopted in this section, representing device geometrical properties, are shown in Fig. 2b. Coherently with the model presented in [21], let us indicate with $B_i$, $i = \{1, 2, 3\}$ the centers of the spherical joints on the mobile platform. They define a plane on which we fix the origin $O_1$ of the frame $S_1 = (O_1, x_1, y_1, z_1)$. Let us then indicate with $u_i$ the unit vectors identifying, for each leg, the direction of the revolute joint axes, and with $A_i$ and $D_i$, the points indicating the joints connecting each leg to the upper body, and to the middle joint, respectively. On the upper body, we also define a reference frame $S_0 = (O_0, x, y, z)$.

The mobile platform will move w.r.t. the upper body according to the rotations imposed by the actuators to the joints passing through $A_i$ and according to the kinematic constraints imposed by the mechanical structure. In particular, since the axes of the revolute joints of each leg are parallel, each $B_i$ and $D_i$ points move on the respective plane, that we indicate with $\pi_i$. The overall six dimensional motion of the platform is the composition of a translational and rotational motion, that can be represented by a three dimensional vector $p = [p_x, p_y, p_z]^T$, containing the coordinates of $O_1$ w.r.t. $S_0$, and another three dimensional vector $\varphi = [\psi, \theta, \phi]^T$, containing the roll ($\psi$), pitch ($\theta$) and yaw ($\phi$) angles that describe the relative orientation between frames $S_1$ and $S_0$. From this, we can define a vector $\zeta = [p^T, \varphi^T]^T$ collecting all the six parameters necessary to define position and orientation of the mobile platform with respect to the upper body.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Control System</td>
<td>Atmega328</td>
</tr>
<tr>
<td>Operating Voltage range</td>
<td>4.8 to 6.0 V</td>
</tr>
<tr>
<td>Operating Joints Speed</td>
<td>0.2 s/60° to 0.1 s/60°</td>
</tr>
<tr>
<td>Maximum Normal Force</td>
<td>4.7 N</td>
</tr>
<tr>
<td>Maximum Roll Angle</td>
<td>$\frac{\pi}{2}$ rad</td>
</tr>
<tr>
<td>Maximum Pitch Angle</td>
<td>$\frac{\pi}{2}$ rad</td>
</tr>
<tr>
<td>Maximum Vertical Displacement</td>
<td>15 mm</td>
</tr>
<tr>
<td>Frequency vibration range</td>
<td>50 – 240 Hz</td>
</tr>
<tr>
<td>Amplitude vibration range</td>
<td>0.05 – 1 g</td>
</tr>
</tbody>
</table>

| TABLE 1: Specifications for the proposed 3-DoF cutaneous device. |
3.1 Inverse kinematics

As previously introduced, each leg connecting the mobile part of the device with the part fixed on the finger, is composed of two links connected to form a RRS (revolute-revolute-spherical) kinematic chain. The mechanism that constitutes the device is therefore 3-DoF, and we can choose three variables to describe its configuration. Since the device has been designed to render the shape and stiffness of virtual and remote objects, a convenient choice for the independent variables includes the displacement in the z direction, \( p_z \), and the roll (\( \psi \)) and pitch (\( \theta \)) angles. Let us collect those variables in the vector \( \xi = [p_z, \psi, \theta]^T \).

Recalling the rotation matrix expression as a function of the \( \xi \) variables, i.e., yaw angle \( \phi \), and \( p_x \) and \( p_y \) components of \( O_1 \) coordinates, as

\[
\begin{align*}
\phi &= \arctan \left( \frac{(b - b_h) \sin \theta \sin \psi}{b_h (\cos \theta + \cos \psi)} \right), \\
p_x &= b_h (\cos \phi \cos \theta - \sin \phi \sin \theta \sin \psi - \cos \phi \cos \psi), \\
p_y &= -b_h \sin \phi \cos \theta,
\end{align*}
\]

where \( b \) and \( b_h \) are the geometrical parameters of the mobile platform, as shown in Fig. 2a.

When controlling the platform, according to the interaction between the fingertip and the environment, we set a reference value for the device platform configuration, \( \xi_d \). Using the relationships in eqs. (1), (2) and (3), we can then evaluate the overall platform configuration corresponding to the desired values of the independent parameters, i.e., \( \xi_d = [\psi^d, \theta^d]_i^T \). Through the inverse kinematics, we can then evaluate the corresponding reference values for the actuator rotation angles, collected in the vector \( q_d = [q_{1,d}, q_{2,d}, q_{3,d}]^T \). For this type of parallel manipulator, the solution of the inverse kinematics problem is straightforward, differently from the direct kinematics one, that, in general, admits multiple solutions.

The coordinates of each \( B_i \) point, \( i = \{1, 2, 3\} \), w.r.t. \( S_0 \), collected in the three dimensional vectors \( b_i = [b_{1,i}, b_{2,i}, b_{3,i}]^T \), can be evaluated as

\[
b_i = p + R b_i^l,
\]

where \( b_i^l \) represents the vectors containing the coordinates of \( B_i \) points w.r.t. the reference frame \( S_1 \), defined on the mobile platform. Since \( B_i \) points move on three fixed planes \( \pi_i \) (see Fig. 2b), the following constraint equations hold

\[
\begin{align*}
b_{1,i} &= 0, \\
b_{2,i} &= \frac{2b_h}{b_d} b_{2,y}, \\
b_{3,i} &= -\frac{2b_h}{b_d} b_{3,y}.
\end{align*}
\]

Eq. (5) introduces three constraints that limit the generic six-dimensional motion of the mobile platform. In particular, since three independent constraints have been introduced, the mobile platform will have three degrees of freedom.

Let us assume that the independent variables \( \xi = [p_z, \psi, \theta]^T \) are defined, and that we need to evaluate the corresponding rotations \( q = [q_1, q_2, q_3]^T \) of the actuated revolute joints in \( A_i \). For a given \( \xi \), it is possible to evaluate, through the constraint equations eq. (1), (2), and (3), the vector \( p \) and the rotation matrix \( R \), completing the representation of the mobile platform configuration. Then, from eq. (4), it is possible to evaluate the coordinates of \( B_i \) w.r.t. \( S_0 \). Finally, angles \( q_i \) can be evaluated by solving the triangles \( A_i B_i D_i \), in which three edges are known. In particular, the actuator rotation angles \( q_i \) can be evaluated as

\[
q_i = \alpha_i + \delta_i,
\]

where angles \( \alpha_i \) and \( \delta_i \) are as follows

\[
\alpha_i = \arctan \left( \frac{s_{ic}}{\sqrt{s_{ic}^2 + s_{ic}^2}} \right), \quad \delta_i = \arccos \left( \frac{l_1^2 + s_{ic}^2 - l_2^2}{2l_1 s_{ic}} \right),
\]

where \( l_1 \) and \( l_2 \) are the lengths of the proximal and distal link of each leg, respectively, i.e., \( l_1 = |D_i A_i| \), and \( l_2 = |B_i D_i| \), and \( s_i = b_i - a_i \).

3.2 Velocity analysis

We can express the velocities of the \( B_i \) points, \( i = \{1, 2, 3\} \), as

\[
v_{B_i} = v + \omega \times (b_i - p),
\]

where \( v \) is the velocity of \( O_1 \) and \( \omega \) is the angular velocity of the mobile platform, expressed w.r.t. the \( S_0 \) reference frame. Since the \( B_i \) points move on planes perpendicular to the respective \( u_i \) directions, which identify the direction of revolute joint axes, the following relationship holds

\[
\dot{u}_i \cdot v_{B_i} = 0,
\]

which leads to

\[
\dot{u}_i^T v - \omega_i^T S(b_i - p) \omega = 0,
\]

where the operator \( S(\cdot) \), applied to a generic three dimensional vector, gives the corresponding skew matrix. Eq. (9) constitutes an homogeneous linear system with three equations and six unknowns,

\[
U v = 0,
\]

where \( v = [v^T, \omega]^T \) represents the twist of the device mobile platform, and matrix \( U \in \mathbb{R}^{3 \times 6} \) is defined as

\[
U = \begin{bmatrix}
\dot{u}_1^T & -\omega_1^T S(b_1 - p) \\
\dot{u}_2^T & -\omega_2^T S(b_2 - p) \\
\dot{u}_3^T & -\omega_3^T S(b_3 - p)
\end{bmatrix}.
\]

The solutions of this homogeneous system represent, at a given configuration, all the possible twists that can be imposed to the platform.

Since the system has three degrees of freedom, we can express the twist of the platform as a function of three independent velocity components. Similarly to the position analysis described in Sec. 3.1, in our device we want to control the components \( v_z \) (component of the velocity in the direction perpendicular to the platform), \( \omega_z \) (roll velocity), and \( \omega_x \) (pitch velocity), collected in the vector \( \chi = [v_z, \omega_z, \omega_x]^T \). We collect the remaining components in the vector \( \tilde{\chi} = [v_x, v_y, \omega_x]^T \). It is now clear that

\[
v = T \begin{bmatrix} \chi \\ \tilde{\chi} \end{bmatrix},
\]
where \( T \in \mathbb{R}^{6 \times 6} \) is a matrix that changes vector component order, specifically
\[
T = \begin{bmatrix}
0 & 0 & 0 & 1 & 0 & 0 \\
0 & 0 & 0 & 0 & 1 & 0 \\
1 & 0 & 0 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 & 0 & 0 \\
0 & 0 & 1 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 1
\end{bmatrix}.
\] (13)

It is worth to observe that, in general, \( \chi \neq \dot{\xi} \), and \( \nu \neq \dot{\xi} \). The approximation \( \dot{\chi} \approx \dot{\xi} \) is possible only if rotation angles \( \psi \) and \( \theta \) are small.

We can then rearrange the system in eq. (10) as
\[
U_X \dot{\chi} + U_X \ddot{X} = 0,
\] (14)

with \( U_X, U_X \in \mathbb{R}^{3 \times 3} \). Assuming that \( U_X \) is non-singular, we can then express
\[
\ddot{X} = -U_X^{-1} U_X \dot{\chi},
\] (15)

and, therefore, we can express the device platform twist as a function of the controlled components of the velocity,
\[
\nu = H \dot{\chi},
\] (16)

where \( H \in \mathbb{R}^{6 \times 3} \) is a matrix whose components depend on platform configuration, specifically
\[
H = T \begin{bmatrix}
I \\
-U_X^{-1} U_X
\end{bmatrix}.
\] (17)

The velocities of \( B_i \) points can also be evaluated considering the articulated mechanism of each leg, as follow
\[
\nu_B = \omega_t \times (d_i - a_i) + \omega_t' \times (b_i - d_i),
\] (18)

where \( \omega_t = \dot{q}_t u_t \) are the angular velocities of the links connected to the upper body, actuated by the motors, and \( \omega_t' \) are the angular velocities of the links connected to the mobile platform, that are not actuated (passive joints). The directions of both \( \omega_t \) and \( \omega_t' \) are parallel to \( u_i \) (see Fig. 2). From eq. (8) and (18), dot multiplying both sides by \( (b_i - d_i) \), we get
\[
(b_i - d_i)^T \nu = (b_i - d_i)^T S(b_i - p) \omega = (b_i - d_i)^T S(d_i - a_i) \omega_t. \] (19)

Collecting the actuator angular velocity magnitudes in a vector \( \dot{q} = [\dot{q}_1, \dot{q}_2, \dot{q}_3]^T \), eq. (19) can be written in matrix form as
\[
E \dot{\nu} = F \dot{q},
\] (20)

where \( E \in \mathbb{R}^{3 \times 6} \) and \( F \in \mathbb{R}^{3 \times 3} \) are defined as
\[
E = \begin{bmatrix}
(b_i - d_i)^T & (b_i - d_i)^T S(b_i - p)
\end{bmatrix},
\]
\[
F = \begin{bmatrix}
(b_i - d_i)^T S(d_i - a_i) u_i
\end{bmatrix}, \quad i = 1, 2, 3.
\]

If \( F \) is invertible, recalling eq. (16), it is possible to evaluate the actuator velocities \( \dot{q} \) as a function of the platform twist \( \dot{\nu} \), i.e.,
\[
\dot{q} = J \dot{\nu},
\] (21)

where \( J = F^{-1} E \in \mathbb{R}^{3 \times 6} \) is the complete Jacobian matrix.

If we consider also the constraint in eq. (9), we can define the constrained Jacobian matrix \( J = \tilde{J} H = F^{-1} E H \in \mathbb{R}^{3 \times 3} \), relating the actuator angular velocities to the independent twist components, i.e.,
\[
\dot{q} = J \chi.
\] (22)

If the mechanism is not in a singular configuration, i.e., if \( J \) is full-rank, eq. (22) can be inverted to solve the direct differential kinematic problem, i.e. \( \chi = J^{-1} \dot{q} \).

### 3.3 Statics
Let us consider now the static equilibrium of the device. We indicate with \( w = [f, m]^T \in \mathbb{R}^6 \) the wrench applied to the mobile platform, where \( f \) is the resulting force applied to the mobile platform and \( m \) is the resulting moment evaluated w.r.t. \( O_1 \). This wrench represents the resultant of the interaction between the platform and the fingertip, dependent on the fingertip skin deformation. The skin deformation and the stress distribution are related by an impedance relationship that is non-linear and dependent on several parameters \([26, 27, 28, 29]\).

Let us indicate with \( \tau = [\tau_1, \tau_2, \tau_3]^T \) the torques applied by the actuators to the links connected to the upper body.

Considering a virtual displacement of the mobile platform, \( \delta \zeta \), generated by a small variation of actuator joint angles, \( \delta q \), according to the Principle of Virtual Works, the following relationship can be written
\[
\delta \zeta^T \nu = \delta q^T \tau.
\] (23)

The components of \( \delta \zeta \) are not independent, since the device has 3-DoF. Recalling the constraint relationships in eq. (16) and eq. (22), we get
\[
\delta \chi^T H^T \nu = \delta \chi^T J^T \tau.
\] (24)

Since \( \delta \chi \) components are independent, this relationship holds for any \( \delta \chi \) only if
\[
H^T \nu = J^T \tau,
\] (25)

and, consequently, if the Jacobian matrix \( J \) is invertible, i.e., if the device is in a nonsingular configuration,
\[
\tau = J^{-T} H^T \nu.
\] (26)

### 4 DEVICE CONTROL

#### 4.1 Equivalent stiffness evaluation

The objective of our stiffness control system is to simulate contact with a surface of given stiffness, represented by the matrix \( K_d \).

Indicating with
\[
K_p = \text{diag}(k_x, k_y, k_z), \quad K_q = \text{diag}(k_p, k_g, k_h),
\] (27)

the desired translational stiffness and the desired rotational stiffness, respectively, the desired stiffness matrix is defined as
\[
K_d = \text{diag}(K_p, K_q).
\] (28)

When the platform is in a generic configuration \( \zeta \), the corresponding wrench that has to be applied to the fingertip is given by
\[
w = K_d \Delta \zeta,
\] (29)

where \( \Delta \zeta = \zeta - \zeta_0 \) and \( \zeta_0 \) is an initial configuration corresponding to \( w = 0 \). \( \Delta \zeta \) is related to a variation of the independent variables \( \Delta \chi \) through the relationships in eq. (1), (2), and (3). For small values of \( \Delta \zeta \), we can use the approximation
\[
\Delta \chi = H \Delta \zeta,
\] (30)
Device and finger interaction

where $H$ is defined in eq. (16). Assuming for the device actuator an impedance (stiffness) control system, the torque applied by device actuators, necessary to balance the wrench $-\mathbf{w}$ that the fingertip exerts on the platform, can be expressed as

$$\mathbf{\tau} = K_d \Delta \mathbf{q},$$

where $\Delta \mathbf{q} = \mathbf{q} - \mathbf{q}_0$ and $\mathbf{q}_0$ represents the joint configuration corresponding to $\xi_0$. For small values of $\Delta \mathbf{q}$ we can use the approximation

$$\Delta \mathbf{q} = \mathbf{J} \Delta \xi,$$

where $\mathbf{J}$ is defined in eq. (21). By substituting eq. (29), (30), (31), and (32) in eq. (25), we get

$$K_d \mathbf{J} \Delta \xi = \mathbf{J}^{-T} \mathbf{H}^T K_d \mathbf{H} \Delta \xi.$$

Since this relationship holds for any $\Delta \xi$, whose components can be set independently, the following matrix equality can be set

$$K_d \mathbf{J} = \mathbf{J}^{-T} \mathbf{H}^T K_d \mathbf{H}.$$

Finally, assuming again a non-singular configuration and that the Jacobian matrix $\mathbf{J}$ is invertible, we can right-multiply both sides of eq. (34) by $\mathbf{J}^{-1}$. We then obtain the expression that allows to evaluate the stiffness matrix in the joint space, $K_d$, corresponding to a given stiffness matrix in the operative space of the device platform, $K_d$:

$$K_d = \mathbf{J}^{-T} \mathbf{H}^T K_d \mathbf{H} \mathbf{J}^{-1}.$$

It is worth to observe that $K_d$ components depend on the stiffness $K_d$ that has to be rendered, but also on the platform configuration, that affects the values of matrices $\mathbf{J}$ and $\mathbf{H}$.

4.2 Control system description

Let us consider a Virtual Reality (VR) scenario, in which we haptically render the stiffness of different virtual surfaces, e.g., grasping and interacting with surfaces that have different mechanical properties. For the sake of clarity, let us consider only one cutaneous device. However, thanks to the wearability of our system, this framework can be easily extended to multi-contact interactions (see the multi-contact experience of Sec. 5.2). Let us also assume the availability of a hand motion capture system, able to measure the configuration (position and orientation) of the $\{S_0\}$ frame, introduced at the beginning of Sec. 3. This measure is adopted to render the position and orientation of the user’s fingertip avatar in the VR environment. A contact detection algorithm is then used to recognize the interactions between the haptic-equipped fingertip and the virtual objects, i.e., the desired configuration of the device’s platform $\xi_d$ with respect to $\{S_0\}$. Let us assume $K_d$ to be the stiffness matrix of the simulated contact surface. The complete position and orientation vector $\xi_d$ is evaluated by means of eqs. (1), (2), and (3). Reference values for the device actuators angular positions $\mathbf{q}_d$ can be evaluated by applying the inverse kinematic procedure detailed in Sec. 3. These reference values $\mathbf{q}_d$ are then compared with the angles measured by the actuator encoders, $\mathbf{q} = [q_1, q_2, q_3]^T$, and their difference is sent to a position controller with a proportional-derivative (PD) scheme. The proportional term $K_p$ is dynamically evaluated to simulate the stiffness of the virtual surface, as a function of the desired stiffness $K_d$ and of the platform configuration, i.e., matrices $\mathbf{H}$ and $\mathbf{J}$, according to eq. (35).

Moreover, the derivative term $D_d \in \mathbb{R}^{3 \times 3}$ is set to have a suitable damping in system dynamical behavior. In future developments of this work, also $D_d \in \mathbb{R}^{3 \times 3}$ will be dynamically regulated to simulate a viscous behaviour in the interaction with the virtual environment. Finally, the torque $\mathbf{\tau}$ generated by actuators is evaluated as

$$\mathbf{\tau} = K_d (\mathbf{q}_d - \mathbf{q}) + D_d (\mathbf{q}_d - \dot{\mathbf{q}}).$$

A simplified block diagram of the proposed stiffness control algorithm is shown in Fig. 3.

5 Experimental evaluation

We carried two experiments to test the effectiveness of our wearable haptic device and its level of wearability. In the first experiment we aimed at evaluating the effectiveness of our wearable haptic device in rendering stiffness information, while in the second experiment we focused on the evaluation of its immersiveness and wearability.

5.1 Experiment #1: stiffness discrimination experiment

In order to test the effectiveness of our wearable haptic device in rendering stiffness information, we carried out a stiffness discrimination experiment using the same-different procedure of TSD (theory of signal detection) [30]. This technique enables us to evaluate the differential stiffness threshold for our device. The differential threshold can be defined as “the smallest amount of stimulus change necessary to achieve some criterion level of performance in a discrimination task” [30]. It gives us information about how different two displacements provided with our device need to be in order to be perceived as different by a human user. This threshold is often referred to as just-noticeable difference or JND. The differential threshold of a perceptual stimulus reflects also the fact that people are usually more sensitive to changes in weak stimuli than they are to similar changes in stronger or more intense stimuli. The German physician Ernst Heinrich Weber proposed the simple proportional law $JND = kI$, suggesting that the differential threshold increases with increasing the stimulus intensity $I$. Constant $k$ is thus referred to as “Weber’s fraction”.

5.1.1 Setup

The experimental setup is composed of two wearable fingertip devices attached to the end-effectors of two 3-DoF Falcon haptic interfaces (Novint Technologies, USA), as shown in Fig. 4. The Falcon interfaces are placed so that the centers of their end-effectors are at a distance of 13 cm in the nominal position,
and the wearable devices are mounted to have the end-effectors of the devices facing each other. Each Falcon has a workspace of $11 \times 12.5 \times 13$ cm and a tracking accuracy of 0.06 mm [31]. Subjects were blindfolded and asked to wear the two wearable fingertip devices on the thumb and index finger of their right hand.

### 5.1.2 Methods

Eighteen participants (15 males, 3 females, age range 22 – 37) took part to the experiment, all of whom were right-handed. Nine of them had previous experience with haptic interfaces. None of the participants reported any deficiencies in their perception abilities and they were all naive as to the purpose of the study.

We evaluated the differential threshold for stiffness discrimination using the same different procedure [30]. Each trial involved interacting, in succession, with two virtual spheres rendered between the two wearable devices (see Fig. 4). Subjects were asked to judge, on each trial, if the stiffness of the two virtual spheres was different or the same. The hit rate $p_h$ corresponded to the percentage of correct responses given by a subject (“yes, the spheres are different”) when the two objects had different stiffness, while the false alarm rate $p_f$ corresponded to the percentage of incorrect responses (“yes, the spheres are different”) when the stiffness of the two objects were the same [30]. No visual feedback on the virtual sphere was provided.

The two Falcon haptic interfaces were only used to track the position of the fingers and did not provide any external force to the user, i.e., they were programmed to provide only gravity compensation. We decided to use these grounded interfaces, instead of, e.g., a wireless motion tracking system, to enable a more precise tracking of our devices. We will focus on the evaluation of the wearability and portability of our system in the experiment of Sec. 5.2.

We evaluated the differential threshold for stiffness discrimination when employing

- (S) cutaneous feedback provided only by the servo motors of the wearable device (no vibrations),
- (V) cutaneous feedback provided only by the vibrotactile motor of the wearable device (platform not moving),
- (SV) cutaneous feedback provided both by the servo motors and the vibrotactile motor of the wearable device.

In condition S, the servo motors move the end-effector to render the contact with the virtual sphere, and the vibrotactile motor is not active. The interaction is designed according to the god-object model [32], and the magnitude of the force applied at the fingertip is evaluated as

$$f_S = k_S \Delta x,$$

where $\Delta x$ is the penetration of the finger inside the virtual object and $k_S$ is the simulated stiffness constant. More in detail, in this experiment the desired translational stiffness matrix $K_p$ introduced in eq. (27) is defined as $K_p = k_S I_{3 \times 3}$, where $I_{3 \times 3}$ identifies the three dimensional identity matrix. The same numerical values were assumed for the sake of simplicity also for the $K_g$ matrix introduced in eq. (27), even if its values are represented with different units. Once the desired stiffness $K_d$ matrix is set as in eq. (28), the equivalent $K_d$ matrix can be evaluated according to eq. (35).

In condition V, the vibrotactile motor provides a 100-ms vibration burst when the finger contacts the virtual sphere. The amplitude $A_V$ of the vibration is proportional to the stiffness of the virtual sphere [33], i.e.,

$$A_V = \left( \frac{k_S}{1500} + 0.4 \right) G,$$

where $G$ is the acceleration from gravity. In this case, the servo motors are not active, and the mobile platform always contacts the fingertip. Providing a vibration burst of fixed duration on making/breaking contact events has been proved to improve the performance of several (tele)manipulation tasks [34], [35], [36], [37]. Moreover, amplitude (and frequency) of the contact vibration has been proved to generally increase with increasing stiffness of the touched object [38].

Finally, in condition SV, cutaneous feedback is provided both by the servo motors and the vibrotactile motor, as indicated in eqs. (37) and (38).

Each subject carried out three series of trials, in which the virtual sphere stiffness $k_S$ assumed two different values, $k_S = k_{a,*}$. 

Fig. 4: Experimental setup. Two wearable devices are attached to the end-effectors of two Falcon interfaces, with the end-effectors facing each other. The Falcon interfaces are only used to track the position of the fingers and do not provide any external force to the user.

Fig. 5: Differential threshold for stiffness discrimination. Mean and 95% confidence interval are plotted for condition providing cutaneous feedback only by the servo motors (S), only by the vibrotactile motor (V), and both by the servo motors and the vibrotactile motor (SV).
and $k_5 = k_b$, where $k_{a,s}$ and $k_b$ assumed the following numerical values:

(i) $k_{a,1} = 500 \text{ N/m}$ and $k_b = 900 \text{ N/m}$ ($k_{a,1} - k_b = 400 \text{ N/m}$) for Series 1,
(ii) $k_{a,2} = 600 \text{ N/m}$ and $k_b = 900 \text{ N/m}$ ($k_{a,2} - k_b = 300 \text{ N/m}$) for Series 2,
(iii) $k_{a,3} = 700 \text{ N/m}$ and $k_b = 900 \text{ N/m}$ ($k_{a,3} - k_b = 200 \text{ N/m}$) for Series 3.

Each series consisted of 36 repetitions of the stiffness discrimination task, with 12 trials for each feedback condition. The entire experiment lasted approximately 35 minutes.

On each repetition of each series, two virtual spheres with random stiffness ($k_{a,s}$ or $k_b$) were rendered, i.e., the probability of interacting with a pair of objects with same (different) stiffness was 0.5. The order of presentation of the sequence of series and conditions was different for each subject, in order to minimize learning and fatigue effects.

5.1.3 Results
False alarm and hit rate were converted to z scores of the normal distribution [30], [39]. The sensitivity index $d'$ was then calculated as the difference

$$d' = z_h - z_f.$$  

According to the criterion commonly adopted [1], [5], [30], the discrimination threshold can be defined as the difference between the stiffness for which $d' = 1$. The threshold was computed for each subject for each condition S, V, and SV, assuming a linear proportionality between the values of $d'$.

The overall JND was then computed as the mean of the values obtained for all the subjects. Fig. 5 shows the average JND and 95% confidence interval for each condition. The collected data of each condition passed the Shapiro-Wilk normality test and the Mauchly’s test of sphericity. A repeated-measures ANOVA was then performed, with 12 trials for each feedback condition. The entire experiment lasted approximately 35 minutes.

5.2 Experiment #2: Interaction with a virtual immersive environment
In order to test the level of wearability of our cutaneous device, we carried out a second experiment, where subjects are requested to interact with a virtual immersive environment. This experiment has been inspired by the experiments carried out in [40], [41]. Since here we focus on the wearability aspect of our system, we substituted the two Falcon interfaces with the unobtrusive Leap Motion tracking system. The interaction forces are still computed according to the stiffness rendering algorithm of Sec. 4.

5.2.1 Setup and Methods
The experimental setup is composed of a Leap Motion controller, one wearable fingertip device, and a virtual environment. The Leap Motion controller is a small USB peripheral device that uses two monochromatic IR cameras and three infrared LEDs to track the position of the fingertip in 3-D space. It observes a hemispherical area up to a distance of 1 m with an average accuracy of 0.7 mm [42]. Subjects are required to wear two fingertip devices on the thumb and index finger of their right hand, and interact with the virtual environment (see Fig. 6). The subjects hand pose is tracked using the Leap Motion controller and a virtual hand mimicked the subjects hand pose in the virtual environment. Every time the index finger comes in contact with a virtual object, the cutaneous device applies a suitable amount of force to the fingertip. Interaction forces in the virtual environment are computed using a virtual proxy approach [43] and were provided by the cutaneous device as indicated in Sec. 4. The virtual environment is composed of a baseball and a teddy bear, as shown in Fig. 6.

Twelve participants (10 males, 2 females, age range 21 – 35) took part to the experiment, all of whom were right-handed. Eight of them had previous experience with haptic interfaces. None of the participants reported any deficiencies in their perception abilities and they were all naïve as to the purpose of the study.

The task consisted of interacting with the two virtual objects for 5 minutes, either wearing two wearable cutaneous devices (condition C, as in Fig. 6) or barehanded (condition N).

5.2.2 Results
We evaluated the immersiveness of the haptic-enabled virtual reality scenario through the Usefulness, Satisfaction, and Ease of use (USE) questionnaire [44], asking subjects to compare the experience while wearing the wearable devices vs. bare hand. Our
The assertion. Questions and results are reported in Table 2.

The other three sets of questions contained a set of assertions, where a score of 9 was described as “completely agree” and a score of 1 as “completely disagree” with having any force feedback (N). The analysis revealed significant statistical difference between answers QB5 (p = 0.050), QB6 (p = 0.013), QB7 (p = 0.012), QC1 (p = 0.003), QC2 (p = 0.016), QD1 (p = 0.010), QD2 (p = 0.015), and QD4 (p = 0.005). Answers that resulted statistically significantly different are reported in red in Table 2.

We also asked which condition the subjects preferred. All subjects preferred the condition where they were wearing the wearable cutaneous devices. However, four subjects out of twelve complained that, while wearing the wearable devices, the tracking of the fingertip seemed less accurate with respect to interacting with the environment barehanded.

6 Discussion and Conclusions

This work presented the application of a 3RRS wearable fingertip device for stiffness discrimination. Three servo motors move a mobile end-effector toward the user’s fingertip and re-angled it to simulate contacts with arbitrarily oriented surfaces. Moreover, a vibrotactile motor conveys vibrations to the fingertip. The device was preliminary introduced in [21], [22]. In this paper, we have extended the analysis and evaluation of the device with a novel stiffness control system and an in-depth kinematics analysis. Moreover, in order to test the effectiveness and wearability of our wearable haptic device, we carried out two experiments.

Stiffness discrimination experiment. The first experiment tested the capability of our device in differentiating stiffness information. We considered three feedback conditions: cutaneous feedback provided only by the servo motors (S), only by the vibrotactile motor (V), and both by the servo motors and the vibrotactile motor (SV). In the best condition, SV, subjects were able to differentiate

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**Table 2: Experiment #2. Usefulness, Satisfaction, and Ease of use (USE) questionnaire results.**

<table>
<thead>
<tr>
<th>QA. Usefulness (condition C with respect to condition N)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. It helps me be more effective. 8.3 ± 0.9</td>
</tr>
<tr>
<td>2. It helps me be more productive. 7.9 ± 1.2</td>
</tr>
<tr>
<td>3. It is useful. 6.8 ± 1.3</td>
</tr>
<tr>
<td>4. It makes the things I want to accomplish easier to get done. 8.1 ± 0.7</td>
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</tbody>
</table>

**Experiment in condition C (statistically different values in red)**

<table>
<thead>
<tr>
<th>QB. Ease of use</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. It is easy to use. 3.4 ± 1.9</td>
</tr>
<tr>
<td>2. It is simple to use. 7.2 ± 1.5</td>
</tr>
<tr>
<td>3. It is user friendly. 6.3 ± 1.4</td>
</tr>
<tr>
<td>4. Using it is effortless. 5.5 ± 1.2</td>
</tr>
<tr>
<td>5. I can use it without written instructions. 2.6 ± 1.4</td>
</tr>
<tr>
<td>6. I don’t notice any inconsistencies as I use it. 6.7 ± 7.6</td>
</tr>
<tr>
<td>7. Both occasional and regular users would like it. 7.3 ± 0.6</td>
</tr>
<tr>
<td>8. I can recover from mistakes quickly and easily. 7.3 ± 1.2</td>
</tr>
<tr>
<td>9. I can use it successfully every time. 4.1 ± 1.6</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>QC. Ease of learning</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. I learned to use it quickly. 4.3 ± 1.4</td>
</tr>
<tr>
<td>2. It is easy to learn to use it. 5.9 ± 1.4</td>
</tr>
<tr>
<td>3. I quickly became skillful with it. 6.4 ± 0.9</td>
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<table>
<thead>
<tr>
<th>QD. Satisfaction</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. I am satisfied with it. 7.1 ± 1.4</td>
</tr>
<tr>
<td>2. It is fun to use. 8.7 ± 0.5</td>
</tr>
<tr>
<td>3. It works the way I want it to work. 7.3 ± 1.4</td>
</tr>
<tr>
<td>4. It is wonderful. 7.6 ± 1.6</td>
</tr>
<tr>
<td>5. It is pleasant to use. 7.2 ± 1.3</td>
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</tbody>
</table>

<table>
<thead>
<tr>
<th>Experiment in condition N (statistically different values in red)</th>
</tr>
</thead>
<tbody>
<tr>
<td>QB. Ease of use</td>
</tr>
<tr>
<td>1. It is easy to use. 4.2 ± 2.2</td>
</tr>
<tr>
<td>2. It is simple to use. 6.7 ± 2.0</td>
</tr>
<tr>
<td>3. It is user friendly. 7.1 ± 1.9</td>
</tr>
<tr>
<td>4. Using it is effortless. 5.8 ± 0.7</td>
</tr>
<tr>
<td>5. I can use it without written instructions. 5.4 ± 1.4</td>
</tr>
<tr>
<td>6. I don’t notice any inconsistencies as I use it. 7.6 ± 0.8</td>
</tr>
<tr>
<td>7. Both occasional and regular users would like it. 5.2 ± 1.7</td>
</tr>
<tr>
<td>8. I can recover from mistakes quickly and easily. 7.5 ± 1.2</td>
</tr>
<tr>
<td>9. I can use it successfully every time. 4.4 ± 1.6</td>
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<table>
<thead>
<tr>
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</tr>
</thead>
<tbody>
<tr>
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</tr>
<tr>
<td>2. It is easy to learn to use it. 7.7 ± 1.3</td>
</tr>
<tr>
<td>3. I quickly became skillful with it. 6.8 ± 0.6</td>
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</tr>
<tr>
<td>5. It is pleasant to use. 7.1 ± 0.7</td>
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values of stiffness different by 208.5 ± 17.2 N/m (mean ± 95% confidence interval). Surprisingly, adding vibrotactile feedback did not significantly improved the performance of the stiffness discrimination task. However, subjects appreciated the capability of the vibrations to effectively notify the making contact with the virtual surface. The Weber fraction (JND/\text{v} \text{S}) for conditions S, V, and SV is 31.5%, 39.0%, and 23.2%, respectively, which is in agreement with previous results in the literature. For example, Lécuyer et al. [45] used a passive isometric input device, together with visual feedback, to provide the operator with pseudo-haptic feedback. The Weber Fraction for stiffness between a real spring and a spring rendered using the isometric input device was 16%. Genevoc et al. [46] presented a tactile display capable of simultaneously and independently controlling its stiffness and geometry via particle jamming and pneumatic actuation. The Weber Fraction for stiffness was also 16%. Gurari et al. [47] compared the Weber fraction for human perception of stiffness among three conditions: vision, proprioceptive motion feedback, and their combination. Results gave average Weber fractions of 5.6% for vision, 3.6% for proprioception, and 3.9% for their combination. As expected, our performance is slightly worse with respect to [45], [46] and significantly worse than [47]. This can be justified by the fact that we are using wearable tactile interfaces with limited actuation and sensing capabilities, and no visual feedback was provided.

In this experiment, to precisely track the position of the fingers, we used two Falcon interfaces (see Fig. 4), able to guarantee a high tracking accuracy (i.e., more than 10 times higher than the Leap Motion used in the second experiment). However, of course, this choice severely reduced the workspace of the system and did not enable us to evaluate the portability and wearability of our system, which is one of the main points of our work. Moreover, the Falcon interfaces, even when commanded to provide no external force, shows an internal stiffness and friction that is unwittingly displayed to the user. However, since this effect was present in all the considered comparisons, we expect it to have negligible effect in the final computation of the differential thresholds.

**Immersive environment experiment.** The second experiment tested the effectiveness of our device in an immersive virtual reality scenario, focusing on its wearability and portability. All subjects preferred the experience while being provided with cutaneous feedback. Moreover, cutaneous feedback made the interaction more satisfactory (question QD1), more fun to use (QD2), and more “wonderful” (QD4). On the other hand, as expected, wearing the two devices made the task more difficult to learn (QB5, QC1, QC2). Indeed, most of the subjects had no previous experience with wearable interfaces, and they had to get used to wearing them before starting to truly appreciate the additional information provided. In fact, as mentioned above, after this initial setback, all subjects preferred using the system with the cutaneous devices. Finally, subjects complained that the fingertip tracking worked better when using the system barehanded (QB6). These results show that the proposed wearable solution is definitely well-received and well-appreciated. However, there is still some work to be done to improve the wearability of these systems and the quality of the tracking.

**Future Work.** In the next future, we are planning to integrate our fingertip device with a compact and lightweight finger exoskeleton, able to provide kinesthetic feedback to the PIP and DIP joints. In order to improve the tracking of fingers wearing cutaneous devices, we will also consider using more sophisticated tracking systems, such as the V:120 Trio by OptiTrack, or placing the devices on other parts of the hand. A promising solution is moving the device from the fingertip to the proximal phalanx, similarly to what has been done in [48], [49], [50]. Moreover, we are also considering the possibility of including an Inertial Measurement Unit (IMU) unit directly on the cutaneous device, in order to combine the information coming from the external tracker (e.g., a Leap Motion) together with the information captured by the IMU. A similar approach is currently being used by the company GoTouchVR for their wearable fingertip device [20]. Finally, to improve the immersiveness of the virtual environment, we will consider using a Virtual Reality headset, such as an Oculus Rift Head-Mounted Display (HMD). We are also interested in studying how amplitude and duration of vibration bursts affect the sensation of making and breaking contact with virtual objects in wearable haptics.

**References**


Francesco Chinello received the M.S. degree in Computer Engineering (focus on Robotics and Industrial automation) in 2010 from the University of Siena with a thesis entitled “System software for rapid prototyping of anthropomorphic manipulators.” On February 2014, he received his Ph.D. on Information Engineering. After that, he has been Post-Doc at the SIRSLab (University of Siena) and a guest researcher at the Department of Advanced Robotics (Italian Institute of Technology). Since January 2017, he is an Assistant Professor of the Department of Business Development and Technology, Aarhus School of Business and Social Science, at Herning (Denmark).
Claudio Pacchierotti (S’12, M'15) received the Ph.D. degree from the University of Siena, Italy, in 2014. He has been a postdoctoral researcher at the Dept. of Advanced Robotics of the Italian Institute of Technology, Genova, Italy in 2015 and 2016. He visited the University of Padua, University of Pennsylvania, and University of Twente in 2013, 2014, and 2015, respectively. He received the 2014 EuroHaptics Best PhD Thesis Award for the best doctoral thesis in the field of haptics, and the 2015 Meritorious Service Award for his work as a Reviewer for the IEEE Transactions on Haptics. He has also been Associate Editor for the 2017 IEEE World Haptics conference as well as the Publicity Chair for the 2017 IEEE World Haptics and 2018 Asia Haptics conferences. He is currently a CR2 researcher of the CNRS at Irisa and Inria Rennes Bretagne Atlantique, France, in the Lagadic group. His research deals with robotics and haptics, focusing on cutaneous feedback techniques, wearable devices, shared control, and haptics for robotic surgery.

Monica Malvezzi (M’12) has been Assistant Professor of Mechanics and Mechanism Theory at the Dept. of Information Engineering and Mathematics of the University of Siena since 2009. She has been visiting scientist at Istituto Italiano di Tecnologia, IIT, in Genova, Italy, since 2015. She received the Laurea degree in Mechanical Engineering from the University of Florence in 1999 and the Ph.D. degree in Applied Mechanics from the University of Bologna in 2003. From 2002 to 2008 she was researcher at the University of Florence, Energy Department. Her main research interests are in control of mechanical and mechatronic systems, robotics, haptics, vehicle localization, multibody dynamics, grasping and dexterous manipulation.

Domenico Prattichizzo (F’15) received the Ph.D. degree in Robotics and Automation from the University of Pisa in 1995. Since 2002 he is an Associate Professor of Robotics at the University of Siena and since 2009 he is a Scientific Consultant at Istituto Italiano di Tecnologia. In 1994, he was a Visiting Scientist at the MIT AI Lab. Since 2014, he is Associate Editor of Frontiers of Biomedical Robotics. From 2007 to 2013 he has been Associate Editor in Chief of the IEEE Transactions on Haptics. From 2003 to 2007, he has been Associate Editor of the IEEE Transactions on Robotics and IEEE Transactions on Control Systems Technologies. He has been Chair of the Italian Chapter of the IEEE RAS (2006-2010), awarded with the IEEE 2009 Chapter of the Year Award. Research interests are in haptics, grasping, visual servoing, mobile robotics and geometric control. He is currently the Coordinator of the IP collaborative project “WEARable HAPtics for Humans and Robots” (WEARHAP).