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Tumor cell load and heterogeneity estimation from diffusion-weighted MRI calibrated with histological data: an example from lung cancer

Yi Yin, Oliver Sedlaczek, Benedikt Müller, Arne Warth, Margarita Gonzalez-Vallinas, Bernd Lahrmann, Niels Grabe, Hans-Ulrich Kauczor, Kai Breuhahn, Irene E. Vignon-Clementel, Dirk Drasdo*

Abstract—Diffusion-weighted magnetic resonance imaging (DWI) is a key non-invasive imaging technique for cancer diagnosis and tumor treatment assessment, reflecting Brownian movement of water molecules in tissues. Since densely packed cells restrict molecule mobility, tumor tissues produce usually higher signal (a.k.a. less attenuated signal) on isotropic maps compared to normal tissues. However, no general quantitative relation between DWI data and the cell density has been established.

In order to link low-resolution clinical cross-sectional data with high-resolution histological information, we developed an image processing and analysis chain, which was used to study the correlation between the diffusion coefficient (D value) estimated from DWI and tumor cellularity from serial histological slides of a resected non-small cell lung cancer (NSCLC) tumor. Color deconvolution followed by cell nuclei segmentation was performed on digitized histological images to determine local and cell-type specific 2d (two-dimensional) densities. From these the 3d (three-dimensional) cell density was inferred by a model-based sampling technique, which is necessary for the calculation of local and global 3d tumor cell count. Next, DWI sequence information was overlaid with high-resolution CT data and the resected histology using prominent anatomical hallmarks for co-registration of histology tissue blocks and non-invasive imaging modalities’ data. The integration of cell numbers information and DWI data derived from different tumor areas revealed a clear negative correlation between cell density and D value. Importantly, spatial tumor cell density can be calculated based on DWI data.

In summary, our results demonstrate that tumor cell count and heterogeneity can be predicted from DWI data, which may open new opportunities for personalized diagnosis and therapy optimization.

Index Terms—DWI, heterogeneity, histology data, histopathology, image analysis, tumor cellularity.

I. INTRODUCTION

Cancer is one of the leading causes of mortality worldwide. In the medical treatment of cancer, the histopathology of tumor specimens provides the basis for diagnosis and therapy-planning. However, biopsies reflect only very restricted tumor areas, which might be of impaired significance with regard to the majority of systemic tumor load and respective therapeutic approaches [1]. The second pillar of tumor characterization is non-invasive imaging, which yields a relatively low-resolution picture of the local tissue, mapping information from different components (such as water content, radiation attenuation, cell density, extracellular matrix density etc.) on voxel intensity values [2]. This reduction of information impedes interpretation of the images. An example for non-invasive imaging of ultrastructural information available in almost every clinical magnetic resonance imaging (MRI) is diffusion-weighted imaging (DWI). The potential of DWI on non-invasive prediction of cell density has become a research focus. DWI has been shown to be effective in assessing cancer treatment response [3]–[7]. DWI reflects the motion of water molecules in tissue. For example, higher packing of the cells is associated by a restricted random (Brownian) movement of water, which is associated by a higher (i.e., less attenuated) signal in DWI. Its voxel resolution is typically in the range of mm [8]. The water molecule diffusion-driven displacement levels probe the tissue structure at different scales, including intracellular, intercellular, and supra-cellular scales, the latter by sensing water molecule...
movement in vascular networks [8]. Most often cell density is higher in the solid portion of the vital part of a tumor than in normal tissue, and thus diffusion is expected to be restricted due to densely packed tumor cells [9]. However, tissue microarchitecture and composition may to some extent influence the voxel intensity value. The relation between DWI intensity and cell density is not unique for all tissues.

The intravoxel incoherent motion (IVIM) model is an advanced method to separate diffusion and perfusion in DWI, in which the signal decay in each voxel can be described by: 

$$\frac{S(b)}{S_0} = (1 - f) \cdot \exp(-b \cdot D) + f \cdot \exp(-b \cdot (D + D^*)). \tag{1}$$

Here, $S(b)/S_0$ is the ratio of echo signal amplitude of diffusion-weighted to non diffusion-weighted intensity [10]. Parameter $b$ defines the degree of diffusion sensitization, depending on magnitude, duration of the gradient pulse and the time interval between two successive pulses. The precise mathematical relation depends on the shape of the pulses [11].

D is the diffusion coefficient, characterizing the restricted mobility of water molecules, for example in intercellular spaces. $D^*$ is pseudo-diffusion coefficient related to blood flow in the capillary network, that in a voxel often has a pseudorandom orientation. $f$ is proportional to the blood vessel volume fraction.

Different attempts have been undertaken to relate $S/S_0$ to tissue characteristics. A common approach uses instead of the bi-exponential function a fit to only one exponential, $S(b)/S_0 = \exp(-b \cdot ADC)$. ADC lumps together contributions from water movement by diffusion and perfusion within the voxel (and is thus called apparent diffusion coefficient) [8], [10], hence it is inherently less accurate in probing true diffusion. Changing $b$ changes the weight of the terms; at large $b$ true diffusion is probed to a greater extend.

So far, a few studies comparing DWI and histological information have been performed [12]–[17]. In [12], Kono et al. computed the average ADC vs. the expectation value of the nuclear area fraction in patients with brain tumors, representing each patients by one single point in the graph. Histological evaluation was performed on selected sample images. The same quantity was computed by Hayashida et al. [13] for metastases of different primary tumors in brain. Lyng et al. [14] considered human melanoma xenografts in mice, calculating ADC vs. manually detected cell density for different tumors and different regions within the same tumor. Anderson et al. [15] computed the ADC vs. cell volume fraction in cell suspensions and packed arrays of human glial and red blood cells. Ginat et al. [16] correlated the manual estimated cell densities with ADC values measured in different patient tumors to differentiate benign from malignant skull lesions. Schmandt [17] investigated the utility of ADC in diagnosis and treatment in glioma based on the inverse correlation between ADC and tumor and tissue cell density. In each case, a negative correlation between the ADC value and the measure characterizing cell density in the histological or in-vitro samples was found [12]–[17]. Among these studies, the histology analysis was performed either manually or by simple image processing tool that used global thresholding, which is sensitive to errors [12]. Besides, the quantitative analysis was limited to only a small number of histological slices.

Some investigators compared simulated cell density differences to relative ADC values, to estimate tumor cell numbers. The studies were based on the negative correlation and tumor growth mathematical models [18]–[21]. For example, Atuegwu et al. [18] estimated the growth rate for brain cancer in rat based upon a logistic growth model in each voxel in combination with the ADC. Weis et al. [19] estimated the cellularity in human breast cancer from a Fisher-KPP equation with the local ADC coupled to the mechanical stress modified by the growing tumor, using the maximal number of cells fitting within a voxel as fit parameter. Further applications based on [19] were proposed in [20] for response of breast cancer to neoadjuvant therapy and in [21] for glioma growth in rat brain.

Most studies address animal tumors or xenograft [14], [15], [18], [21], [22] and consider mean values for the individual tumors without statistical quantification of variation. Moreover, the ADC value lumping perfusion and diffusion was used [23].

The ADC is usually computed as the mean measurement of different regions of interest (ROIs) [12], [13], [16] or on each voxel of one large (tumor-size scale) ROI [18]–[21] on one MRI slice without further consideration of the local tumor micro-structure.

In this study we investigate both, the diffusion value $D$ vs. 3d (‘d’=dimension) cell density relation, and the $D$ vs. area fraction relation for a single patient non-small cell lung cancer (NSCLC) tumor. By using $D$ instead of ADC we inherently address diffusion only, hence avoid lumping diffusion and perfusion together. ADC is formally equivalent to $D$ when $f$ is zero. In our study given the ranges of $b$ and $f$, ADC is not equal to $D$. Besides, ADC is approximately equal to $D$ at very large $b$ values by eliminating the effects of perfusion. However, the increase of $b$ leads to a higher probability of lower SNR.

For our analysis we developed an automated image segmentation pipeline as this facilitates analysis of large histological samples necessary to reduce statistical errors. A large variety of methods have been proposed for cell nuclei segmentation on cancer histological images [24]. Popular approaches to segment cell nuclei include the Hough transform [25], voting along the direction of the image gradient to infer the center of the object [26]–[28] separating clustered nuclei along points of high concavity [29], [30], unsupervised Bayesian classification [31] and supervised methods [32]. Our algorithm combines the image local intensity minimum and gradient information to detect the cell nucleus with low staining quality, such as irregular nucleus contour, small fragments inside individual nucleus, which can be detected as multiple nuclei by the previous mentioned algorithms. We use KL1 staining as cancer cell marker to ensure identification accuracy between cancer and non-cancer cells within the tumor. The code can be downloaded at msysbio.com/cellssegmquant (integration into software TiQuant [33] is envisaged).

The automated segmentation is in-line with the aims of digital pathology. The routine analysis of tissue samples performed by pathologists is tedious, subjective, and time consuming. Tissue slides are digitized for quantitative analysis.
based on image processing techniques and automated analysis. The later increase speed and reproducibility of cancer evaluation and staging. By sampling from different locations of the same tumor we infer a relation between D values vs. 3d cell density and area fraction, respectively, for one single tumor alone, that span a surprisingly large range of values hence displaying a significant degree of heterogeneity. The findings suggest that tumor heterogeneity in individual patients can be detected non-invasively.

In summary, the novelties of this work comprise: study in human lung tumor with large heterogeneity; efficient algorithm for nuclei detection and application to tumor cells; proposed ellipsoid model based algorithm for 3d cell density estimation; cancer and non-cancer cell-count on 350 whole histology slides; investigation of heterogeneity within an individual tumor from DWI; correlation between diffusion coefficient assessed by the IVIM model in DWI and cell density; counting of total cell number of tumor based on this correlation. The findings suggest that tumor heterogeneity in individual patients can be detected non-invasively.

II. DATA ACQUISITION

A. Patient Selection and Tissue matching

Primary human NSCLC tissue was obtained from a patient as part of a patient cohort who underwent a lobar resection for lung cancer at the Department of Thoracic Surgery, Thoraklinik Heidelberg-Rohrbach (Germany). Informed consent was obtained from the patient (Appendix-A). After tumor resection the patient underwent adjuvant radiation therapy.

The tumor was selected for the following reasons. It showed invasion into the pericardial fat, which made it immobile during breathing excursions, thus reducing the effects of respiratory motion during cross-sectional imaging and avoided difficulties in the identification of tumor sub-volume locations. Centrally the contact between the tumor and the large bronchial structures (diameter of about 5-6mm) could be used to reliably and easily orient the tumor after resection. The bronchial structures were located within the axial planes of the CT and MRI (Fig. 1(a), (b)), to co-register the different imaging modalities (CT and MRI).

Further serial sections were performed in parallel to the axial cut with thickness of each section of approximately 1 cm. The tumor tissue slice (Fig. 1(c)) selected for further work-up, was the one above the central cutting line of the tumor, and contained all relevant tissue and cell types of the tumor such as normal lung tissue, vital tumor tissue, and surrounding adipose tissue. Relevant MRIs were acquired in axial plane identical to the selected tumor slice (Fig. 2), based on which the tumor tissue was classified. Identification of central necrosis was based on DCE-dynamics and Ktrans (volume transfer coefficient reflecting vascular permeability) value from DCE-MRI (Fig. 2(a)) which has the same coordinate system and structural images as the other MRIs. The functionally identified borders of the necrosis (the central area being not perfused) were transferred to the high resolution T1-contrast image (Fig. 2(b)). The outer border of the tumor (Fig. 2(b)) was manually segmented based on contrast differences.

Fig. 1. Selection of patient tumor. (a) CT slice; (b) Corresponding T1-weighted MRI slice; (c) Tumor tissue slices, the one which was selected for further analysis is highlighted. The chronic inflammation is indicated by the enlarged diameter of the bronchial structures up to the periphery (white arrow on (b)).

For further analysis, the tumor slice was cut into smaller pieces. Seven tissue samples were cut from the tumor strip delineated by a white rectangle as shown in Fig. 1(c) and Fig. 10(a). The cutting line (Fig. 1(c)) was drawn from the extension of bronchus III through the center of the necrosis towards the most distant part of the adipose tissue invasion by the tumor. Based on the cutting line, histological samples were visually matched to fit the structures identified in MR/CT. Fine calibration was done by careful evaluation of the multimodal contrast with regard to specific tissue types in the MRI to select the pixels that correspond to the histological specimens. This procedure was several times repeated ensuring reproducibility.

Fig. 2. Tissue classification based on functional MRI: (a) Perfusion kinetics of DCE-MRI (the colorbar indicates the Ktrans values displayed in the tumor region); (b) Necrotic tumor contour (necrosis from (a)) overlaid on T1-CEFS-MRI. The outer thin line delineates the tumor region. The vital tumor is in-between.
**B. DWI**

Within a clinical standard thorax MRI [34] including a tumor perfusion contrast dynamic MR-image [35] a navigated diffusion echo-planar imaging sequence was used acquiring 6 b-values above zero = 50, 100, 150, 200, 400, and 800 s/mm². The diffusion-encoding gradients were applied in three orthogonal directions; therefore the diffusion tensor is assumed isotropic. The sequence used the following parameters: TE 75 ms, TR 8364 ms, SL 6 mm. Imaging was performed on a 1.5 T MRI (Avanto, Siemens, Erlangen). The DWI voxel resolution is 2.1 mm × 2.1 mm × 6 mm. The D value of each voxel was obtained by fitting the voxel signal S/S₀ vs. the b-value to the above signal attenuation model (1) using the freely available software MITK Diffusion [36]. For the determination of the tissue diffusion coefficient, all above b-values were taken into account.

**C. Materials**

1) **Tissue sampling and processing**

After fixation of the tissue slice (about 7 cm × 5 cm × 0.5 cm) in 4% buffered formalin overnight, the sample was cut in smaller pieces (about 1 cm × 1 cm × 0.5 cm), transferred in paraffin, and systematically cut in 1-2 µm thick sections using a microtome (HM 355, Microm, Thermo Scientific, Braunschweig, Germany). Selected samples were stained with hematoxylin/eosin (H&E) and carefully reviewed by the study pathologist (A.W.) to determine the proportion of viable tumor cells, stromal cells, normal lung cell content, infiltrating lymphocytes, and necrotic areas.

2) **Sample staining**

Sections were stained using hematoxylin/eosin (H&E) and acid fuchsin orange G (AFOG) standard protocols. In addition, an anti-pan cytokeratin antibody (clone KL1, Abcam, Cambridge, UK) was used for epitope-specific stain. In brief, staining was performed using the Dako Autostainer (Dako, Hamburg, Germany) and the following protocol: tissue slides were air-dried in an incubator at 42°C overnight and deparaffinized in xylene (2 × 10 min). After rehydration in graded ethanol, the slides were pretreated with 0.01 M sodium citrate (pH 6.0) in a pressure cooker for 10 min. Afterwards, primary antibodies in PBS/Tween were added for 30 min at room temperature and slides were washed with PBS/Tween for 5 min before the secondary antibody was applied for 20 minutes (1:1.000 in PBS/Tween). The samples were then incubated with 1% hydrogen peroxide diluted in PBS/Tween (5 min). After signal detection using amino-ethyl-carbazol (AEC, 2 × 7 min) nuclei were stained using hematoxylin.

3) **Image acquisition**

Glass slides were automatically scanned in bright-field mode at a 40-fold magnification (0.23 µm/pixel) with the Hamamatsu NanoZoomer 2.0-HT Scan System (Hamamatsu Photonics, Hamamatsu, Japan). The imaging system consists of three 4096x64 pixel TDI-CCD sensors (sensor pixel size: 8 µm²), providing manual/automatic adjustments of the number of focus points and multiple plane digitization [37]. For the scanning of the object slides, the slide scanner automatically detects the ROI that contains the tissue and also determines automatically a valid focal plane for scanning. Resulting virtual slides have an average compressed file size of 1 GB (JPEG, Q = 90) and un compressed of about 25 GB, depending on the scanned area.

**III. DATA ANALYSIS METHODS**

Based on the tumor DWI and histology data, we developed a processing pipeline for tumor cellularity estimation. The pipeline includes:

1. 2d cell density estimation based on histological image analysis. A segmentation algorithm is proposed to detect cell nuclei in histological images. Each cell is assumed to have only one nucleus, and the 2d cell density is obtained by dividing the number of detected nuclei by the area of the tissue slide. The analysis tool enables the automated quantification of cellularity in large histological samples with high accuracy.

2. 3d cell density estimation in a two-step process. The first step involves the computation of 3d cell densities from 2d segmentations separately for cancer and non-cancer cells based on a model that approaches cell nuclei shapes by ellipsoids. Next the total 3d cell density is computed involving both cancer and non-cancer cells. This is necessary to estimate the tumor cell load for the entire tumor as well as on a voxel-wise basis.

3. Correlation of the DWI-images and tumor cellularity in both 2d and 3d by comparison of diffusion coefficients and cell densities of seven selected tumor tissue samples. The correlation is used to calculate the tumor cell load in each voxel of the DWI data for analysis of tumor heterogeneity, which includes calculation of the cell distribution in tumor regions for which no histology data is present as well as for cell load estimation of the entire tumor.

4. Cell number estimation of the whole tumor. The tumor contour and volume are obtained by tumor segmentation in DWI data. The 3d cellular distribution of the tumor can be estimated from the D value distribution based on the relationship between D value and cell density in step 3. The total cell number is finally obtained by summing up the cell numbers in all those voxels of the DWI data that belong to the tumor.

**A. Histological image analysis**

We propose an automated algorithm for the detection and classification of cells in tumor tissue based on H&E staining for all nuclei, and KL1 staining for cancer cytoplasm. The algorithm depicted in the flowchart of Fig. 3 was tested on digitized histological slides.

1) **Pre-processing**

The original histological image is at 40-fold magnification with file size of larger than 1 GB. To trade-off visible details and computation time, a magnification of 20-fold was chosen (0.455 µm/pixel) for all images for histology analysis. In the cutting process, the spatial correspondence between neighbor tissue slides is lost and information from different slides is difficult to compare. Before analyzing the data quantitatively, the scanned histology slides were preprocessed once with, once...
without image registration [38] (see Table I). The Gaussian blur was applied to reduce the noise in both cases. Data represented below are for registered images.

![Flowchart of the image analysis algorithm for automatic histology study](image)

**Fig. 3.** Flowchart of the image analysis algorithm for automatic histology study, from serial histology slides to 2d cell density evaluation. The left column indicates the corresponding sub-sections in Section III. A.

2) **Color deconvolution**

An automated color deconvolution [39] was performed in the histological image after pre-processing to split the color image into hematoxylin and KL1 channels. The KL1 channel image was used to generate a mask image, which separated the cancer sensitive region from the background. The final detected nuclei were then classified into cancer and non-cancer nuclei based on the mask image. From the hematoxylin channel image, we then implemented an automatic cell segmentation algorithm.

The color deconvolution method assumes that a pixel is a weighted sum of 3 stains, the two stains hematoxylin and KL1, and the background. Each stain $j$ has its own characteristic absorbance for light in each of the three RGB channels $i = \{r, g, b\}$. For channel $i$, based on Lambert-Beers law, Rufrok et al. [40] proposed for the intensity of light after passing a tissue sample in a bright field micrograph the relation

$$I_i = I_{0,i}e^{-\sum_j A_{i,j}C_j},$$

where $I_{0,i}$ is the intensity of light entering the specimen in color channel $i = \{r, g, b\}$; $A_{i,j}$ is the corresponding absorption factor, and $C_j$ is the concentration of the stain $j$. With incident white light $I_{0,i} = 255$ for each channel $i = \{r, g, b\}$ the optical density reads

$$\Delta_i = \sum_j A_{i,j}C_j = -\ln \left( \frac{I_i}{I_{0,i}} \right).$$

The optical density of the color image is expressed as $\Delta = AC$, where $A$ is a three-element vector denoting the optical density of each of the RGB channels. $A$ is a three-by-three absorption matrix, of which the rows indicate the different RGB channels and columns indicate the different stains. $C$ is a three-element vector representing the concentration of each stain. Once $A$ is determined, the color deconvolution scheme is applied according to

$$C = A^{-1} \Delta.$$  

In our study, there are two principal stains, hematoxylin and KL1. The optical densities of the specific stains were obtained by an automatic singular value decomposition (SVD) method, based on which the absorption matrix $A$ was created following the process detailed in [39]. The color deconvolution was then performed to separate the hematoxylin and KL1 channels as shown in Fig. 4(b), (c).

3) **Cell nuclei segmentation**

To segment cells on histological images with high accuracy is a big challenge, since cells have high variance in size and shape. In addition, artifacts coming from the histological image preparation (tissue slice cutting and staining) further impede cell segmentation. In this paper, we implemented a seed based automatic and robust cell segmentation algorithm which is composed of two steps. The first step was to automatically locate the center of each cell using local intensity minimum and gradient information [26]. Cell centers detected in the first step were then used as initial positions for the second step for nucleus segmentation and nucleus contour extraction.

To determine the seed points, only the hematoxylin channel (Fig. 4(b)) extracted above by color deconvolution from the color image (Fig. 4(a)) was used, as including KL1 staining reduced contrast. The hematoxylin channel was converted into a gray scale field $I(x, y)$ (Fig. 4(d)). The image gradient was computed with the Sobel operator. Its direction is from the center of a nucleus to the outside. The gradient for each pixel was used to compute a voting area (Fig. 4(f)) denoting the most probable (candidate) nuclei region as follows: for each pixel $(x, y)$, the “voting direction" $a(x, y)$ is defined as

$$a = \frac{-\nabla I(x, y)}{||\nabla I(x, y)||} = -\left( \cos(\theta(x, y)), \sin(\theta(x, y)) \right),$$

where $\nabla I(x, y)$ is the gradient, $||\nabla I(x, y)||$ is the gradient magnitude, and $\theta$ is the angle of the gradient direction with respect to x-axis. The voting area $A_{vot}(x, y; l_{\text{min}}, l_{\text{max}})$ of each pixel is defined by an annular sector with its vertex at $(x, y)$ as illustrated in Fig. 4(f). Based on the approximated mean nuclei diameter (5 μm), $l_{\text{min}}$ was set to 1.25 μm, and $l_{\text{max}}$ was set to 3.75 μm. $\beta$ is the angular range and set to 30°. Those regions where voting regions of different pixels overlap are likely to be nuclear center regions (Fig. 4(f)). A region overcoming a certain threshold was considered as center region, whereby the threshold was chosen to ensure one center region per nucleus. We defined the nucleus seed point as centroid of the region. The final nuclei segmentation was obtained by an active contour method [41] using the detected nuclei seed points (Fig.4(g)).

**B. 3d cell density estimation with an ellipsoid model**

The 3d cell density is estimated in a two-step process. First, we analyze how 2d and 3d cell densities relate for a given cell type (cancer vs. non-cancer cells). Second, based on these relationships, the total 3d cell density is computed combining the number of cancer and non-cancer cells (this will lead to (7) in Section IV.D). The first step is the focus of this section, while the results for the two steps are given in Sections IV B, D.

An iterative optimization method is proposed to estimate the nuclei distribution in 3d using the 2d nuclei features of a given cell type. Our method estimates a statistical distribution of cells in 3d space but cannot give their true 3d spatial distribution.
Fig. 5 illustrates the 3D density estimation algorithm that will be applied in section IV.B.

Our method is based on the observation that the shape of a cell nucleus in 2D is approximately elliptical [27], [28], [42]. Accordingly, we assumed that nuclei in 3D are ellipsoids [43], [44] (Fig. 5(a)).

The 2D cell density and nuclei size distribution are calculated based on the 2D nuclei segmentation results on the histological images. The 2D contours of detected nuclei are fitted by ellipses with semi-major axis \( a \) and semi-minor axis \( b \). As nuclei contours are of different size, this leads to nuclei size distributions \( f(a) \), \( h(b) \), respectively. We assume that the 2D contours emerge from cross sections of ellipsoidal shaped nuclei in 3D whereby the ellipsoids have semi-axes \( a' \), \( b' \) and \( c' \) (Fig. 5(a)). The axes are determined empirically requiring that: (i) the density of objects in virtual 2D cross sections through a 3D volume (Fig. 5(b)), into which the ellipsoids were homogeneously distributed and isotropically oriented, shall reproduce the 2D density in the data (Fig. 5(b),(c)); (ii) the distribution of semi-major and semi-minor axes in the virtual 2D cross sections should statistically reproduce the expectation values \( \langle \delta a \rangle^2 \) and \( \langle \delta b \rangle^2 \) obtained from the data. For this, an iterative procedure is used (Algorithm 1) where the ellipsoid axes are drawn from normal distributions:

\[
\begin{align*}
  a' & \sim N(r_{maj}, \sigma_{maj}) \\
  b' & \sim N(r_{min}, \sigma_{min}) \\
  c' & \sim N\left(\sqrt{r_{maj}r_{min}}, \sqrt{\sigma_{maj}\sigma_{min}}\right)
\end{align*}
\]  

As starting values of the iteration, values \( r_{maj} = \langle a \rangle, r_{min} = \langle b \rangle \), \( \sigma_{maj} = \langle \delta a \rangle^2 \), and \( \sigma_{min} = \langle \delta b \rangle^2 \) are used and stepwise adjusted until the upper conditions (i) and (ii) are fulfilled. Notice that this choice is neither unique, nor compulsory. For example, it neglects a possible correlation between major and minor axes in 2D section and in 3D (through the nucleus volume for which we do not have data). However, we validated the algorithm with liver tissue for which we could reconstruct the 3D volume data from optical sections of confocal laser scanning micrographs, and we verified the algorithm with synthetic data on elongated cell nuclei shapes, with both homogeneous and inhomogeneous distributions of cell nuclei (Supplementary1-A).

**Algorithm 1: 3D cell density estimation**

**Input parameter:**
- \( \rho_T \): target nuclei density in 2D measured by image analysis
- \( \Delta \rho_T \): target accuracy of result. (Choose e.g. \( \Delta \rho_T = 0.1 \times \rho_T \))
- Semi-axes distribution of cell nuclei in 2D

**Algorithm:**
1. Define a cube with a given volume \( V \)
2. Distribute \( N \) cells (ellipsoids) in the cube
   - Axes of ellipsoids are determined by 2D axes distribution; adjusted to meet condition (ii)
   - Prevent nuclei overlapping
3. Obtain resulting average 2D cut cell density \( \rho_N \)
4. If \( |\rho_N - \rho_T| < \Delta \rho_T \)
   - Meet condition (i) and compute resulting 3D density:

\(^1\) Supplementary materials are available in the supplementary files /multimedia tab.
Cell segmentation and classification evaluation

The proposed automatic cell segmentation algorithm performs high detection accuracy (Fig. 7); this was confirmed by the study pathologist whose evaluation served as ‘diagnostic standard’. For this, we selected 20 representative histological images, and then compared the detected results by the proposed method with the manual results. First we validated the cell segmentation, and then among the detected cells, the cell classification in cancer versus non-cancer cells. The TP, TN, FP, and FN \((T = \text{true}, F = \text{false}, N = \text{negative}, P = \text{positive})\) of cell segmentation are defined in Supplementary1-B. Fig. 7(a) shows the ROC graph for the cell segmentation (blue solid triangles) and classification performance of identifying cell types (red solid circles) while low D value corresponds to high cell density (densely distributed nuclei) and high D value corresponds to low cell density (sparsely distributed nuclei) with a symbol). The results indicate high sensitivity \((=\frac{TP}{TP+FN}}\) and specificity \(=\frac{TN}{TN+FP}\) \(\) in all cases. Table I lists the corresponding mean values and the variances of sensitivity, specificity, and accuracy \(\) for all blocks obtaining the distributions in Fig. 8. The pooling from all slices is justified, as not only the intra-block but also the inter-block variability of the ellipse axes is small (see Supplementary1-C). The average values and the variances of semi-axes over all the blocks were used for computation of the parameters \(a’, b’\) and \(c’\) as explained in Section III.B.

To probe the relationship between 2d and 3d cell densities for the selected tumor, we mimicked the cell distribution in the tumor volume and the tissue cuts. We assumed the 2d cell density for each cell type (cancer or non-cancer cells) increasing from 1 cell/mm² to 6000 cell/mm² by step 1 cell/mm². For each of the given 2d cell density value, we estimated the corresponding 3d cell density according to Algorithm1. We defined a cube \(V\) with edge length of 1 mm, and then distributed a number of ellipsoids in \(V\) in random locations and orientations, according to distributions \(a’, b’\) and \(c’\). The estimated 2d cell density is defined as the number of ellipsoid sections on the virtual cutting plane (Fig. 5(c)) divided by the area of the cutting cross-section. The estimated 3d cell density equals the number of ellipsoids divided by the volume \(V\). The

\[
\rho_0(3D) = N/V \quad \text{(End result of computation)}
\]

Else if \((\phi_n < \phi_f)\)

\[
\{ \begin{align*}
\text{Increase } N & \quad \text{(N = N + } \Delta N) \\
\text{Remove existing nuclei and restart with } 2. \\
\text{Else} & \\
\text{Decrease } N & \quad \text{(N = N – } \Delta N) \\
\text{Remove existing nuclei and restart with } 2. 
\end{align*}
\]

C. Cell number estimation by correlation between diffusion and cellularity

The tumor cell number was calculated based on tumor voxels’ D values and the identified correlation between diffusion and cellularity. Fig. 6 illustrates the mapping from D value to local cell density: the high D value voxel has low cell density, while the low D voxel has high cell density. The correlation and cell number counting scheme are explained in detail in Section IV.

Fig. 6. Mapping from D value to local cell density. T1-MRI overlaid with the D parametric map of the selected tumor (left), the color bar indicates the D values displayed in the tumor region; high D value corresponds to low cell density (sparsely distributed nuclei) while low D value corresponds to high cell density (densely distributed nuclei)

IV. ANALYSIS RESULTS

A. Cell segmentation and classification evaluation

B. 3d cell density estimation: cancer vs. non-cancer cells

First, in order to investigate the 3d cell density, we fitted ellipses to the segmented nuclei in the histological images and computed the semi-major and semi-minor axes in the 2D slices for all blocks obtaining the distributions in Fig. 8. The pooling from all slices is justified, as not only the intra-block but also the inter-block variability of the ellipse axes is small (see Supplementary1-C). The average values and the variances of semi-axes over all the blocks were used for computation of the parameters \(a’, b’\) and \(c’\) as explained in Section III.B.

To probe the relationship between 2d and 3d cell densities for the selected tumor, we mimicked the cell distribution in the tumor volume and the tissue cuts. We assumed the 2d cell density for each cell type (cancer or non-cancer cells) increasing from 1 cell/mm² to 6000 cell/mm² by step 1 cell/mm². For each of the given 2d cell density value, we estimated the corresponding 3d cell density according to Algorithm1. We defined a cube \(V\) with edge length of 1 mm, and then distributed a number of ellipsoids in \(V\) in random locations and orientations, according to distributions \(a’, b’\) and \(c’\). The estimated 2d cell density is defined as the number of ellipsoid sections on the virtual cutting plane (Fig. 5(c)) divided by the area of the cutting cross-section. The estimated 3d cell density equals the number of ellipsoids divided by the volume \(V\). The

<table>
<thead>
<tr>
<th>Performance</th>
<th>Sensitivity</th>
<th>Specificity</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cell segmentation</td>
<td>0.954 ± 0.026</td>
<td>0.946 ± 0.042</td>
<td>0.953 ± 0.017</td>
</tr>
<tr>
<td>Classification</td>
<td>0.947 ± 0.030</td>
<td>0.968 ± 0.022</td>
<td>0.963 ± 0.017</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Performance</th>
<th>Sensitivity</th>
<th>Specificity</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cell segmentation</td>
<td>0.950 ± 0.023</td>
<td>0.943 ± 0.029</td>
<td>0.947 ± 0.016</td>
</tr>
<tr>
<td>Classification</td>
<td>0.956 ± 0.056</td>
<td>0.952 ± 0.026</td>
<td>0.954 ± 0.032</td>
</tr>
</tbody>
</table>
estimation was repeated for 10 times for each of the given 2d cell density. Finally, by plotting the estimated 3d cell density against the given 2d cell density for each estimation, a linear relationship was indicated for each cell type, \( \rho_{3D} = m^c \rho_{2D}^c \) with \( k \in \{c, nc\} \) for cancer and non-cancer cells, respectively (Fig. 9, showing the data points with 3d density ranging from about 1000 to 320,000 cell/mm\(^3\)). The least-square regression lines were drawn for both cancer and non-cancer cases. For cancer cells the slope \( m^c = 96/\text{mm} \) (goodness of fit: \( R^2 = 0.9997 \)), while for non-cancer cells \( m^{nc} = 115/\text{mm} \) (\( R^2 = 0.9996 \)).

**Fig. 8.** Elliptical semi-major (left) and semi-minor (right) axes distributions in 2d histological images for cancer cells (in red) and non-cancer cells (in blue). For cancer cells, the average semi-major axis is 4.38 μm (SD = 1.62 μm); the average semi-minor axis is 2.68 μm (SD = 0.9 μm). For non-cancer cells, the average semi-major axis is 3.85 μm (SD = 1.92 μm); the average semi-minor axis is 2.05 μm (SD = 0.66 μm).

**C. Tumor homogeneity analysis: cell density distribution and cancer region fraction**

The representative tumor samples (Fig. 10(a)) are selected for the study of the tumor homogeneity and cellularity. The 2d cell density was tested for significant differences among the selected tumor samples (S1-S7) with the Kruskal-Wallis test [45]. For each tumor sample, 50 histological slides uniformly distributed through the tumor block were selected for the statistical test. The null hypothesis (H\( _0 \)) is that there is no significant difference of cell density among tumor samples (the tumor is homogeneous). The hypothesis was rejected, as the difference is statistically significant (\( p \ll 0.001 \)). The tumor is thus heterogeneous.

The cancer region area fraction of tumor samples is presented by plotting the cancer (KL1 positive) region area against the non-cancer (non-KL1 positive) region area as shown in Fig. 10(b). The tumor sample S3, which is the closest to the necrosis region, has the highest cancer region fraction, while the tumor samples with lung tissue S1 and with fat tissue S7 have lower cancer region fractions. In case of a homogeneous tumor, all points on Fig. 10(b) would be on one straight line.

**Fig. 10.** Heterogeneity of the tumor: (a) overview of the tumor samples (S1-S7); (b) comparison of the cancer region fraction between different tumor samples by plotting the cancerous (KL1 positive) region area against the non-cancerous (non-KL1) region area, for 50 slides per tumor block. The yellow solid point denotes the average for the respective tumor sample.

**D. Correlation between D value and cell density**

To investigate the correlation between diffusion and cellularity, we performed quantitative analyses of D values and cell densities of the selected tumor samples (Fig. 10(a)). Table II lists the D values of different tumor samples, which were calculated by performing IVIM estimation on the ROIs of the tumor samples on DWI (Fig. 11). The values of the fitted f and \( D^* \) are given in Supplementary1-D. The average goodness of fit (\( R^2 \)) of (1) to our data is 0.91, and the corresponding standard deviation is 0.06. The 2d cell density (cancer and non-cancer cells together) of each tumor sample is the mean cell density of the 50 histological slides uniformly distributed through the tumor block.
TABLE II
D VALUES (MEAN AND STANDARD DEVIATION (SD) IN (10⁻³mm²/s)) OF THE DIFFERENT TUMOR SAMPLES DEFINED IN FIG. 10(a)

<table>
<thead>
<tr>
<th>Blocks</th>
<th>S1</th>
<th>S2</th>
<th>S3</th>
<th>S4</th>
<th>S5</th>
<th>S6</th>
<th>S7</th>
</tr>
</thead>
<tbody>
<tr>
<td>D</td>
<td>2.985</td>
<td>1.632</td>
<td>1.095</td>
<td>1.809</td>
<td>1.963</td>
<td>2.064</td>
<td>2.404</td>
</tr>
<tr>
<td>SD of D</td>
<td>0.328</td>
<td>0.122</td>
<td>0.079</td>
<td>0.027</td>
<td>0.018</td>
<td>0.050</td>
<td>0.037</td>
</tr>
</tbody>
</table>

Fig. 11. ROIs on DWI corresponding to the seven tumor samples (Fig. 10(a)). The shapes of the histological specimens were translated back to the DWI data by manual co-registration. Necrosis has been identified from T1-CEFS-MRI (Fig. 2(b)).

Drawing the 2d cell densities of tumor samples against the corresponding D values exhibits a strong negative linear correlation (Fig. 12). The Pearson product-moment correlation test was performed to evaluate the linear correlation. The tumor sample S3 is next to the necrosis region (Fig. 10(a)), which has the highest tumor cell density with lowest diffusion coefficient. S1 includes part of healthy lung tissue. Because of the alveoli of lung tissue, there are cell-free regions in S1; this reduces the cell density and allows high mobility of water molecules (high diffusion). S7 is located at the tumor boundary where it has grown into the pericardial fat. A typical fat cell is quite big. For example, the white fat cell is 0.1 mm in diameter [46], which is the major form of adipose tissue in mammals.

A negative linear correlation is also observed between 3d cell density and D value (Fig. 13). The 3d cell density ρ_{3d} was computed based on the cancer region fraction φ_{c} and the intrinsic cell density slope factor m_{c} (for cancer cell) and m_{nc} (for non-cancer cell) from 2d to 3d (Fig. 9):

\[ ρ_{3d} = φ_{c} * ρ_{2d}^{c} + m_{c} + (1 - φ_{c}^{c}) * ρ_{2d}^{nc} * m_{nc}, \]

where φ_{c} is the ratio between the cancer area (KL1 stained tissue area) and the tumor area (total tissue area). The intrinsic cancer cell density ρ_{2d}^{c} equals the number of cancer cells divided by the cancer region (KL1) area, and the intrinsic non-cancer cell density ρ_{2d}^{nc} equals the number of non-cancer cells divided by the non-cancer region area (non-KL1).

E. Tumor cell count estimation

Given the D value of each voxel in the tumor DWI data, the 3d cell density corresponding to each voxel is obtained by the mapping from the D value to the local cell density. We exclude the necrotic volume in the calculation of cell number. The cell number of the whole tumor is the sum of the local cell numbers of vital tumor voxel volumes (excluding necrosis),

\[ N_{tumor} = \sum_{i} N(i) = \sum_{i} ρ_{3d}(i) \times v(i) = \sum_{i} g(D(i)) \times v(i). \]

Here N(i) is the cell number of voxel i, ρ_{3d}(i) is the voxel 3d cell density, and v(i) is the voxel volume, v(i) = 2.1 mm × 2.1 mm × 6 mm = 26.46 mm³. The linear mapping g(D(i)) is defined above (see Fig. 13). The total cell number of the lung tumor in this study is estimated as 2.57 × 10^{10}.

The average cell density of the whole tumor is 5.9 × 10⁵ cell/mm³ computed by dividing the total cell number by the vital tumor volume. It is comparable to the average density of the tumor samples (S1-S7) 6.28 × 10⁵ cell/mm³. If we compute the total tumor cell number by multiplying the vital tumor volume in the T1-weighted MRI data with the average cell density of the tumor samples, the cell count is 4.52 × 10⁹ mm³ × 6.28 × 10⁵ cell/mm³ = 2.84 × 10^{10}.

T1-weighted MRI seems to lead to a larger total tumor volume than DWI (4.35 × 10^{⁷}mm³), but the difference between tumor cell load estimations through both methods is not large.
V. DISCUSSION AND CONCLUSION

Exemplified for a NSCLC patient, we here present a new pipeline for the estimation of tumor cell load in solid tumors based on the fusion of image processing techniques. As a result, tumor cell numbers may directly be inferred from the non-invasive DWI data, which is routinely available for cancer patients. The main novelties include: adaptive cell nuclei segmentation; model-based 3d cell nuclei density estimation from 2d cell nuclei data; cell number calculation based on the correlation between diffusion coefficient (D value) obtained from the DWI data and 3d cell densities. The inference of 3d nuclei density from 2d sections is crucial to estimate tumor cell load in each voxel of the DWI as well as the whole tumor. Despite the algorithm is simple and approaches nuclei shapes by simple ellipsoids, it could be validated using confocal micrographs of liver tissue to give reliable values, and verified with synthetic data (Supplementary 1-A). The inference algorithm could further be refined by taking into account the nucleus volume distribution, permitting to identify correlations between the ellipsoid axes. However, we do not expect major differences for the questions studied in this paper.

The representative tumor samples were separated from the tumor mass after surgical resection. The automatic histology evaluation was successfully validated by a pathologist, showing high accuracy of the algorithm. The radiologist localized the representative tumor sample, defined the tumor borders in the DWI, and calculated for each tumor sample its corresponding D value by averaging over all voxels belonging to the respective sample. Knowing the D values of the whole tumor and the relationship between the D values and cell densities, the total tumor cell number was finally obtained.

For the histological study of the selected tumor, the digital cell segmentation successfully distinguished cancer cells from non-cancer cells, and their respective fractions revealed tumor heterogeneity. The segmentation and classification perform very well (Table 1), but might be further improved by applying an image-specific color deconvolution method [47]. Heterogeneity was also indicated by the inter tumor samples cell density standard deviation SD_inter = 1700 cell/mm^2 having been more than five times the standard deviation of the intra sample density SD_intra = 330 cell/mm^2. The tumor region close to the necrosis part has much higher cell densities than the region merged with the lung tissue or pericardial fat. In DWI, a high D value was obtained in tumor regions with low cell density, while low D value was obtained for high cellularity region. The D value of the tumor samples ranges between 1.09 and 2.98 × 10^{-3}mm^2/s with mean value 1.99 × 10^{-3}mm^2/s. The D value differences in DWI indicate the variation of local cell density of tumor samples, which ranges between 2917 cell/mm^2 and 7684 cell/mm^2. The model-based computed 3d tumor densities varying within the tumor by a factor of about 2 were within the range denoted in [48]. Moreover this spatial organization of cell densities in a tumor is coherent with classical solid tumor descriptions [49]. DWI may thus provide a non-invasive indicator of such microscale structure.

Our study may help to refine and adjust the patient-specific development of therapeutic strategies. This holds true for conventional cytostatic drugs (e.g. platin based regimens) and for highly selective enzyme inhibitors (e.g. the epidermal growth factor inhibitor erlotinib), which are currently used in the treatment of lung cancer. In addition, this algorithm may be beneficial for the personalized adjustment of novel therapeutic approaches such as bi-specific monoclonal antibodies (BITE) or immunotherapeutic therapies. Here the knowledge of cell numbers (cancer and non-cancer), as well as vessel density (which is key for pharmacokinetics) may allow the precise fitting of drug concentrations and application modes in order to reduce side effects and to increase the drugs anti-tumor efficiency. Thus, differences in the diffusion coefficient (D value) could not only aid the diagnosis but also guide the therapeutic intervention. Our procedure, tested for one selected NSCLC patient, might straightforwardly be applied to other cancer types, for which specific biomarkers for cancer cells exist. Stains used in tissue preparation other than KL1, will also be successful as long as individual cell types (cancer and non-cancer) can be identified based on the morphology or epitope-based approaches.

Potential errors of our study may include a mis-fusion of the MRI imaging and pathology processing of tissue specimens. For example, the shrinkage of tissue samples after formalin fixation [50] (around 10% [51]), may affect the tumor size measurement and must be considered in the future for tumor volume and 2d/3d cell density estimations. The tissue deformation caused by cutting artifacts may be corrected by image registration [38], however, as was shown in this paper, the registration step is not compulsory (see Table 1). Limitations of the anatomical MRI planning, such as tilts of less than 5° of the DWI plane vs. the histology plane, increase the difficulty of the co-registration of the histological tumor slide and MRI data; however, by slight variation of the included DWI voxels we verified the robustness of the obtained D values. The reproducibility of DWI in lung tumor is still under investigation, but the DWI data is reproducible in many organs and different tumor types [52]–[54].

Concerning the time-consumption of the different steps: the histological data generation is the most tedious part, whereas its automated image analysis does not require much man-time (and even computational time: 1 slide takes about ~1h on a 10-core computer). The DWI data acquisition and parameter estimation are both much shorter than for histology (~1h).

A further question remains of how this finding might be applied in the clinics. If the relation of D value and 3d density is sufficiently general it could be applied to different tissues. However, as the D value reflects the sum of interactions with macromolecules, fibers, desmoplastic reaction and vascularization, differences would be expected for different tissues, even if the qualitative behavior should not change as indicated by the negative correlation between cell density and ADC (D value in our notion) observed in different tumors and patients in literature [55]. To further test its validity, the proposed method must be tested on patients with different subtypes of NSCLC tumors (e.g. squamous cell carcinoma and adenocarcinoma) to study how far the relation changes. For application in the clinics, one solution, even if labor-intense, would therefore be to systematically explore the correlation between cell density and D value for different tumor types (including origin at different organs) to obtain calibration
curves that could be used for patients after identification of their tumor subtype. As an alternative applicable approach in the clinics, latest results indicate that the relation between D-value and cell density might be inferred from biopsies, that in case of NSCLC patients are routinely taken for diagnosis guided by non-invasive imaging techniques. The biopsies should be sampled from regions of different D-values.

APPENDIX

A. Surgery protocol

The study protocol was approved by the local Ethics Committee of the University of Heidelberg (approval number S-249/2010). In our study, the tumor tissue (6.5 cm in diameter) was taken from a 72 year old patient with a NSCLC that was treated with an upper left lobe en-block resection including pericardial and mediastinal invaded parts (Fig. 1). Initial histology had been sampled by means of trans bronchial biopsy. The patient tumor, which was poorly differentiated squamous cell carcinoma, was classified as pT4 pN0 (0/27) pL2 G3 R2 (details given in Supplementary[1-G]) according to TNM cancer staging system [56].

ACKNOWLEDGMENT

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REFERENCES
