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What Makes a Distributed Problem Truly Local?*

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Abstract

In this talk we attempt to identify the characteristics of a task of distributed network computing, which make it easy (or hard) to solve by means of fast local algorithms. We look at specific combinatorial tasks within the local model of distributed computation, and rephrase some recent algorithmic results in a framework of constraint satisfaction. Finally, we discuss the issue of efficient computability for relaxed variants of the local model, involving the so-called non-signaling property.

In distributed network computing, autonomous computational entities are represented by the nodes of an undirected system graph, and exchange information by sending messages along its edges. A major line of research in this area concerns the notion of locality, and asks how much information about its neighborhood a node needs to collect in order to solve a given computational task. In particular, in the seminal local model [19], the complexity of a distributed algorithm is measured in term of number of rounds, where in each round all nodes synchronously exchange data along network links, and subsequently perform individual computations. A t-round algorithm is thus one in which every node exchanges data with nodes at distance at most t (i.e., at most t hops away) from it.

Arguably, the most important class of local computational tasks concerns symmetry breaking, and several forms of such tasks have been considered, including the construction of proper graph colorings [3–9, 11, 15, 17, 18, 22], of maximal independent sets (MIS) [1, 4, 5, 14, 16, 18], as well as edge-based variants of these problems (cf. e.g. [21]). In this talk we address the following question: What makes some symmetry-breaking problems in the local model easier than others?

We note that the local model has two flavors, involving the design of deterministic and randomized algorithms, which are clearly distinct [8]. When considering randomized algorithms, for n-node graphs of maximum degree Δ, a hardness separation between the randomized complexities of the specific problems of MIS and (Δ + 1)-coloring has recently been observed [11, 14]. No analogous separation is as yet known when considering deterministic solutions to these problems. We look at some partial evidence in this direction, making use of the recently introduced framework of conflict coloring representations [9].

*This talk includes results of joint work with: P. Fraigniaud, C. Gavoille, M. Heinrich, and M. Markiewicz.
for local combinatorial problems. A conflict coloring representation captures a distributed task through a set of local constraints on edges of the system graph, thus constituting a special case of the much broader class of constraint satisfaction problems (CSP) with binary constraints. Whereas all local tasks are amenable to a conflict coloring formulation, one may introduce a natural constraint density parameter, which turns out to be inherently smaller for some problems than for others. For example, for the natural representation of the $(\Delta + 1)$-coloring task, the constraint density is $1/(\Delta + 1)$, while for any accurate representation of MIS, the constraint density is at least $1/2$. We discuss implications of how low constraint density (notably, much smaller than $1/\Delta$) may be helpful when finding solutions to a distributed task, especially when applying the so-called shattering method [20] in a randomized setting, and more directly, when designing faster deterministic algorithms through a direct attack on the conflict coloring representation of the task [9].

We close this talk with a discussion of relaxed variants of the LOCAL model, inspired by the physical concept of non-signaling. In a computational framework, the non-signaling property can be stated as the following necessary (but not sufficient) property of the LOCAL model: for any $t > 0$, given two subsets of nodes $S_1$ and $S_2$ of the system graph, such that the distance between the nearest nodes of $S_1$ and $S_2$ is greater than $t$, in any $t$-round LOCAL algorithm, the outputs of nodes from $S_1$ must be (probabilistically) independent of the inputs of nodes from $S_2$. We point out that for a number of symmetry breaking tasks in the LOCAL model, the currently best known asymptotic lower bounds can be deduced solely by exploiting the non-signaling property. This is the case for problems such as MIS [10][14] or $2$-coloring of the ring [10]. On the other hand, such an implication is not true for, e.g., the $\Omega(\log^* n)$ lower bound on the number of rounds required to $3$-color the ring [15] — this lower bound follows from different (stronger) properties of the LOCAL model [12][13]. This leads us to look at the converse question: How to identify conditions under which non-signaling solutions to a distributed task can be converted into an algorithm in the LOCAL model? We note some progress in this respect for quantum analogues of the LOCAL model [2].

References


