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Possible improvements of the method of fundamental solution to solve the **ECGI problem**



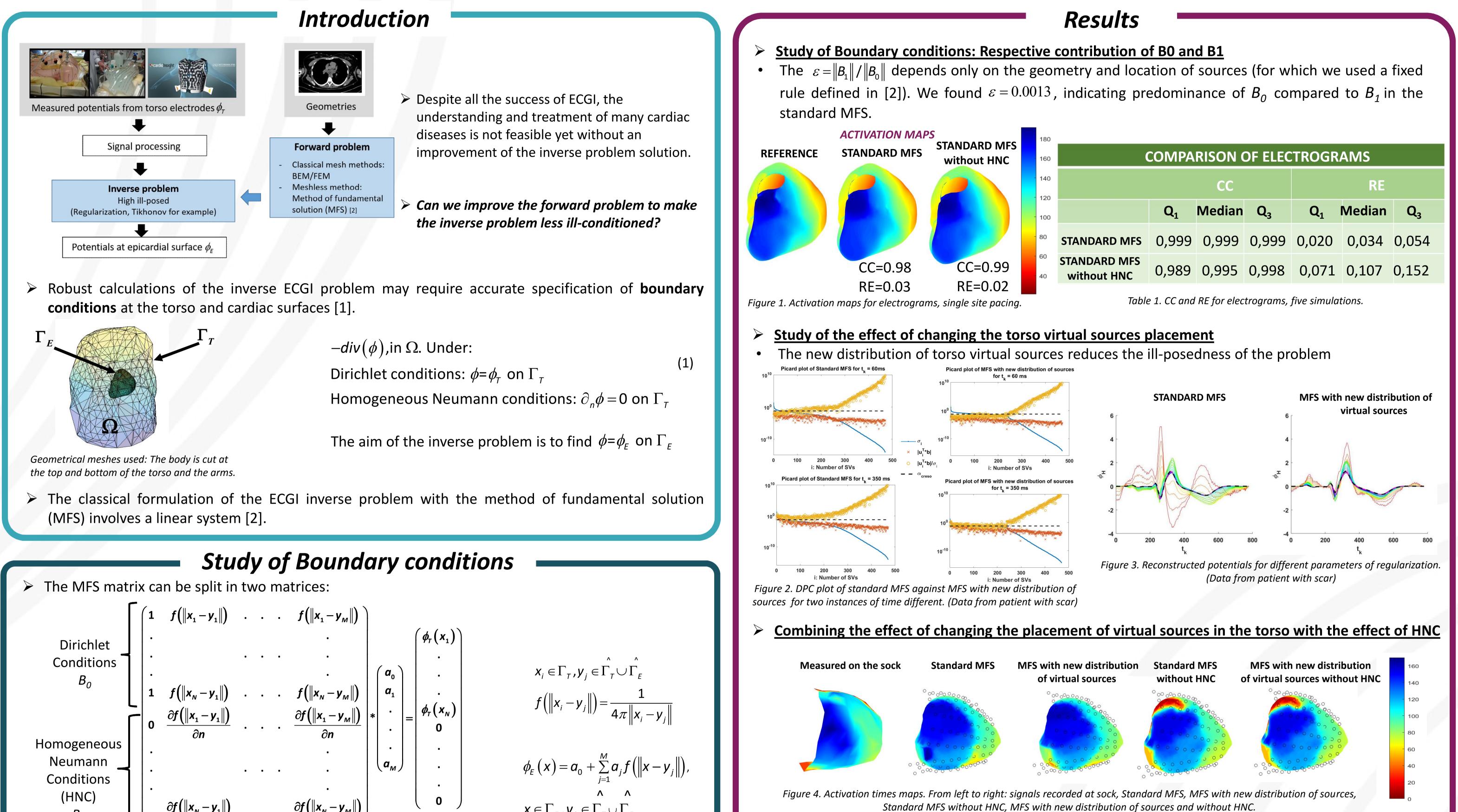
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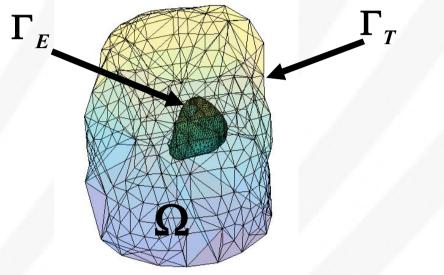
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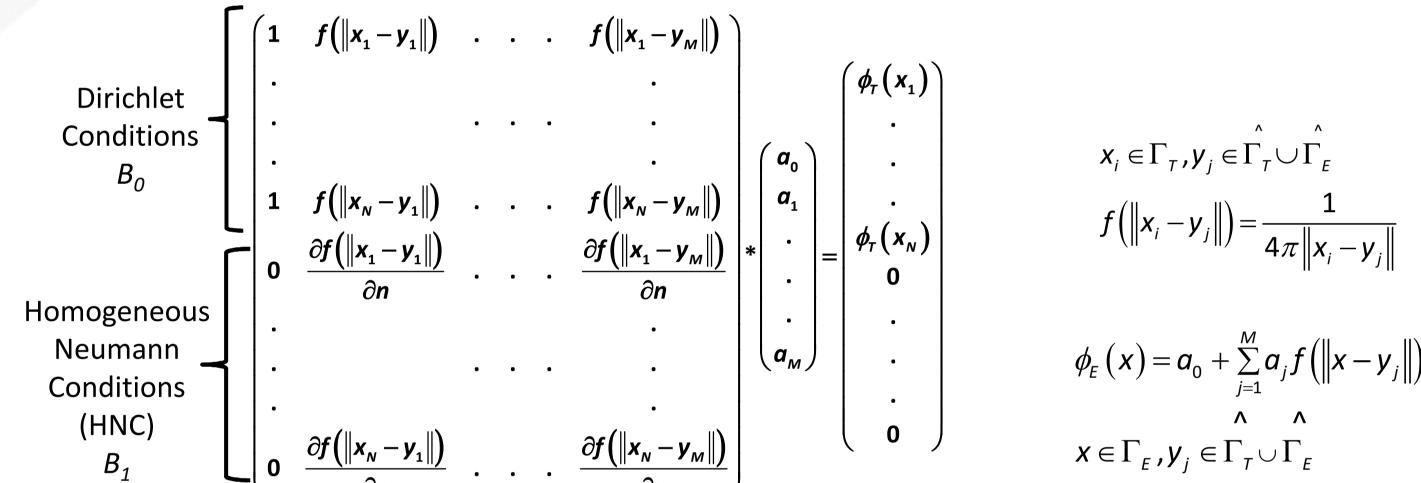


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- We can remark that:
- The contribution of the submatrices B_1 and B_0 in the whole solution is related to their respectives norms.
- Due to the meshing of the torso, non-physiological conditions are applied to the top, bottom of the torso and the arms.
- Accurate computation of the normals at torso surface is required.

Do we need to enforce the homogeneous Neumann conditions in the MFS inverse problem? •To evaluate the contribution of both **boundary conditions**:

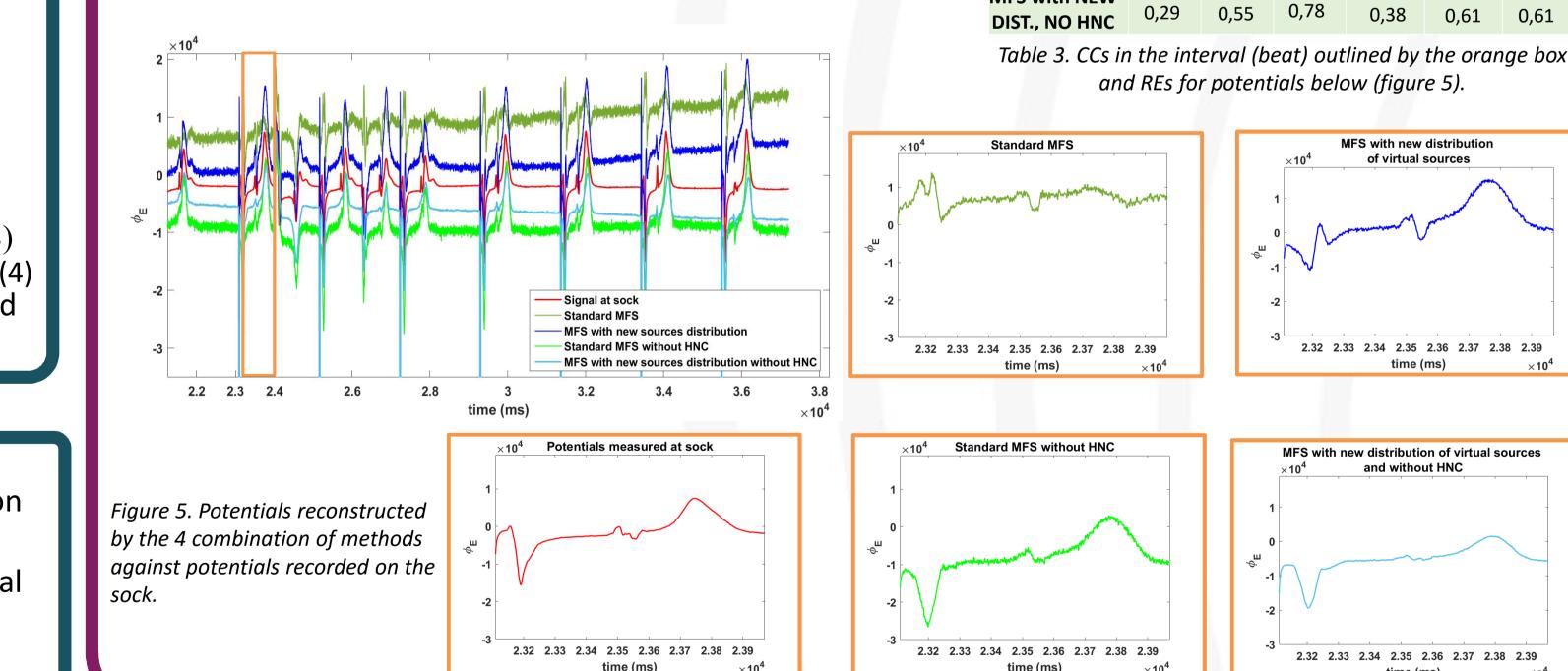
 $J_{\lambda}(a) = \frac{1}{2} \left(\left(1 - \lambda \right)^2 \left\| B_0 a - \phi_T \right\|_2^2 + \lambda \left\| B_1 a \right\|_2^2 + \alpha \left\| a \right\|_2^2 \right), \text{ for } \lambda = 0 \text{ (MFS without HNC) and } \lambda = 0.5 \text{ (Standard MFS)}$ The solution of (4) was found by using Tikhonov regularization and α was chosen by using Creso method as in [2].

Study of placement of virtual sources

- > In other fields it has been shown that the ill-posedness of MFS problem and the efficacy of its solution depends on the placement of the virtual sources [3].
- > The center of the heart used in [2] to inflate the torso surface (in order to place its respective virtual sources) can be a misfit reference, for example when structural diseases are present.
- Therefore, we studied the effect of changing the torso virtual placement: For each electrode on the torso, we find the location of closest point on the heart surface $h_{d_{\min}}$ s.t. $d_{\min} = \min(\|x_i - h_k\|_2), k = 1, \dots, M_H$ ii. We construct the location of virtual source y_i related to the torso electrode x_i as $y_i = x_i + R_T (x_i - h_{d_{min}})$
- iii. We use SVA to find the ratio R_{τ} that makes our problem better

COMPARISON OF ATs					
	СС	RE			
STANDARD MFS	0,57	0,37			
STANDARD MFS, NO HNC	0,66	0,34			
MFS with NEW DIST.	0,61	0,35			
MFS with NEW DIST., NO HNC	0,58	0,38			

Table 2. CCs and REs for Ats maps above (figure 4).



Conclusions

- Removing the Neumann conditions reduces the forward and inverse computational cost.
- MFS with new distribution of sources made the problem less ill-conditioned and less sensitive to the choice of the regularization parameter.

COMPARISON OF ELECTROGRAMS								
	СС			RE				
	Q1	Median	Q3	Q1	Median	Q3		
NDARD MFS	0,32	0,41	0,68	0,54	0,78	1,03		
NDARD MFS, NO HNC	0,28	0,5	0,77	0,57	0,75	0,96		
S with NEW DIST.	0,24	0,49	0,75	0,58	0,74	0,95		

0,38 0,61 0,61

MFS with new distributio

232 233 234 235 236 23

MFS with new distribution of virtual source and without HNC

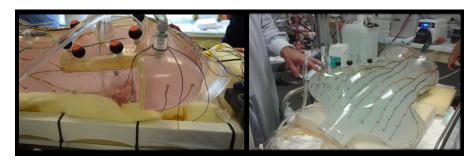
2.32 2.33 2.34 2.35 2.36 2.37 2.38 2.3

MFS with NEW

Conditioned, i.e. that improves the SV decay.

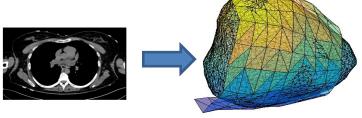
Method of evaluation

- To test the effect of HNC Five activation patterns (1 single site pacing and 4 single spiral waves) were **simulated** using [4]:
 - The currents from the monodomain problem are used to compute the BSPM. The simulations provide both the theoretical, *in-silico* ϕ_{τ} and ϕ_{E} every 1ms.
 - ϕ_{τ} were computed by solving a static bidomain problem in a realistic, heterogeneous torso model. ii.
- To test the ill-posedness of the problem with standard and new distribution of sources Real data from a patient presenting scar was employed.
- > To compare the four combinations: Standard MFS, Standard MFS without HNC, MFS with new distribution of sources, and MFS with new distribution of sources and without HNC – Experimental data (LBBB) from:



256 electrodes at torso(128 obtained) Sinus rhythm pacing for epi /endo surfaces





108 electrodes at sock Heart and sock meshes

- The HNC are related with the small SVs, i.e. with higher frequencies, this can be seen in the respective noisy reconstructed potentials.
- MFS with new distribution of virtual sources and without HNC has better CC and less REs. However, the REs are still high. This indicates that a good similarity of the potential pattern is achieved but not a good amplitude. Finally, best ATs maps were achieved by standard MFS without HNC.
- Future work: The amplitude can be improved with better choice of the regularization parameter according to the distance of the virtual sources and/or by using spatio-temporal regularization.

Acknowledgements

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