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Possible improvements of the method of fundamental solution to solve the ECGI problem



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Inserm

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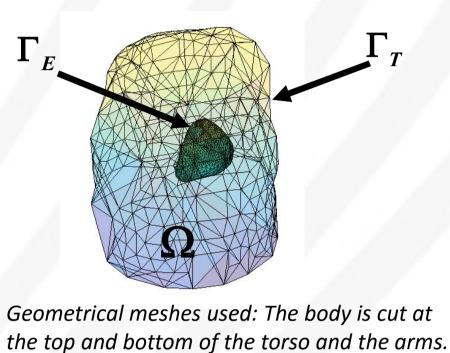
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Introduction > Despite all the success of ECGI, the Measured potentials from torso electrodes ϕ_{τ} understanding and treatment of many cardiac diseases is not feasible yet without an Forward problem Signal processing

(Regularization, Tikhonov for example) Potentials at epicardial surface

Inverse problem

> Robust calculations of the inverse ECGI problem may require accurate specification of **boundary** conditions at the torso and cardiac surfaces [1].



 $-div(\phi)$, in Ω . Under:

Dirichlet conditions: $\phi = \phi_{\tau}$ on Γ_{τ}

Homogeneous Neumann conditions: $\partial_n \phi = 0$ on Γ_{τ}

improvement of the inverse problem solution.

> Can we improve the forward problem to make

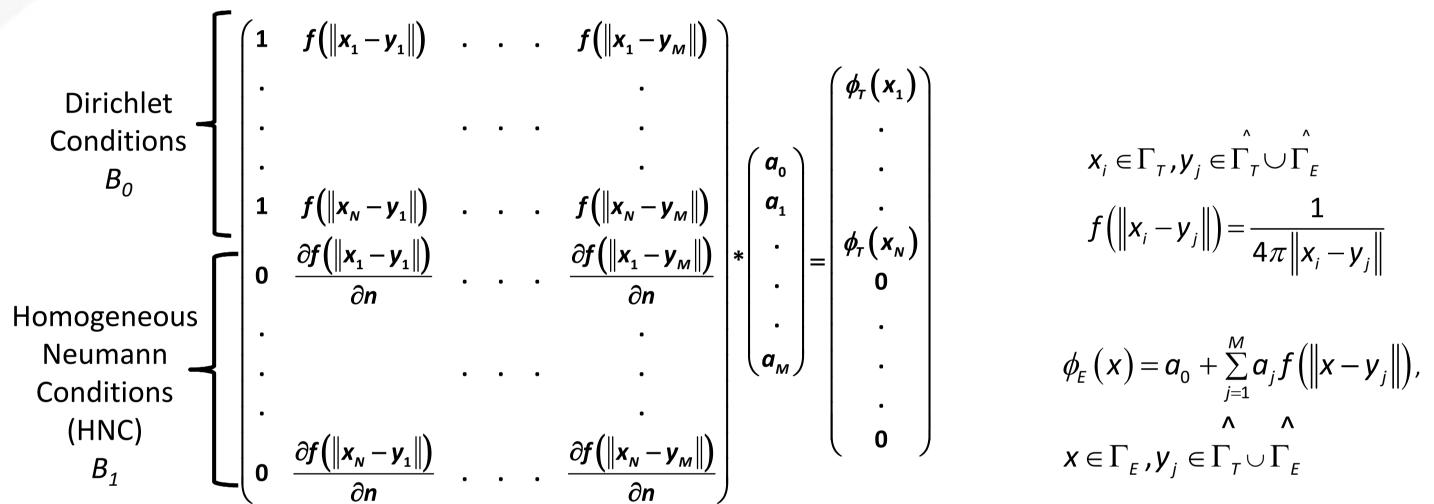
the inverse problem less ill-conditioned?

The aim of the inverse problem is to find $\phi = \phi_E$ on Γ_E

> The classical formulation of the ECGI inverse problem with the method of fundamental solution (MFS) involves a linear system [2].

Study of Boundary conditions

The MFS matrix can be split in two matrices:



- We can remark that:
- The contribution of the submatrices B_1 and B_0 in the whole solution is related to their respectives norms.
- Due to the meshing of the torso, non-physiological conditions are applied to the top, bottom of the torso and the arms.
 - Accurate computation of the normals at torso surface is required.

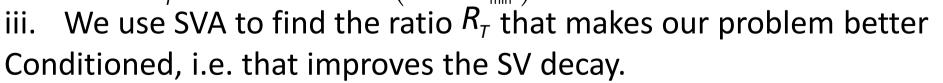
Do we need to enforce the homogeneous Neumann conditions in the MFS inverse problem? •To evaluate the contribution of both **boundary conditions**:

 $J_{\lambda}(a) = \frac{1}{2} \left((1 - \lambda)^{2} \| B_{0} a - \phi_{T} \|_{2}^{2} + \lambda \| B_{1} a \|_{2}^{2} + \alpha \| a \|_{2}^{2} \right), \text{ for } \lambda = 0 \text{ (MFS without HNC) and } \lambda = 0.5 \text{ (Standard MFS)}$

The solution of (4) was found by using Tikhonov regularization and lpha was chosen by using Creso method as in [2].

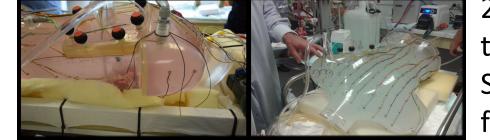
Study of placement of virtual sources

- > In other fields it has been shown that the ill-posedness of MFS problem and the efficacy of its solution depends on the placement of the virtual sources [3].
- > The center of the heart used in [2] to inflate the torso surface (in order to place its respective virtual sources) can be a misfit reference, for example when structural diseases are present.
- Therefore, we studied the effect of changing the torso virtual placement:
- For each electrode on the torso, we find the location of closest point
- on the heart surface $h_{d_{\min}}$ s.t. $d_{\min} = \min(\|x_i h_k\|_2), k = 1, \dots, M_H$
- ii. We construct the location of virtual source y_i related to the torso electrode x_i as $y_i = x_i + R_T (x_i - h_{d_{min}})$



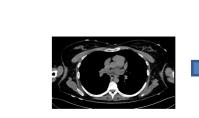
Method of evaluation

- To test the effect of HNC Five activation patterns (1 single site pacing and 4 single spiral waves) were **simulated** using [4]:
 - The currents from the monodomain problem are used to compute the BSPM. The simulations provide both the theoretical, in-silico ϕ_{τ} and ϕ_{ε} every 1ms.
- $\phi_{\!\scriptscriptstyle T}$ were computed by solving a static bidomain problem in a realistic, heterogeneous torso model.
- To test the ill-posedness of the problem with standard and new distribution of sources Real data from a patient presenting scar was employed.
- > To compare the four combinations: Standard MFS, Standard MFS without HNC, MFS with new distribution of sources, and MFS with new distribution of sources and without HNC – Experimental data (LBBB) from:



256 electrodes at torso(128 obtained) Sinus rhythm pacing for epi /endo surfaces



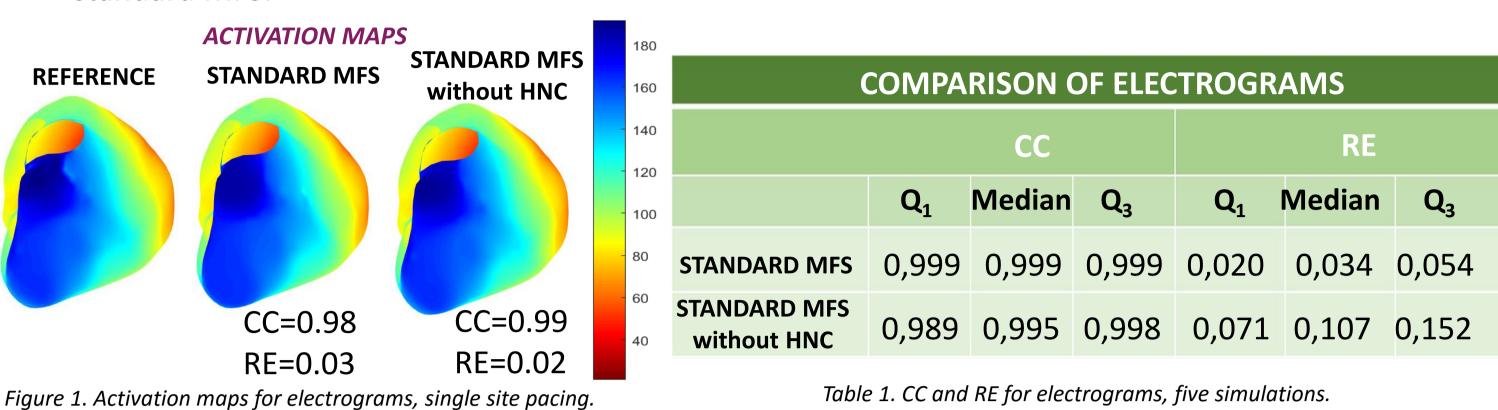


Heart and sock meshes

2011; 19(3): 309-336.

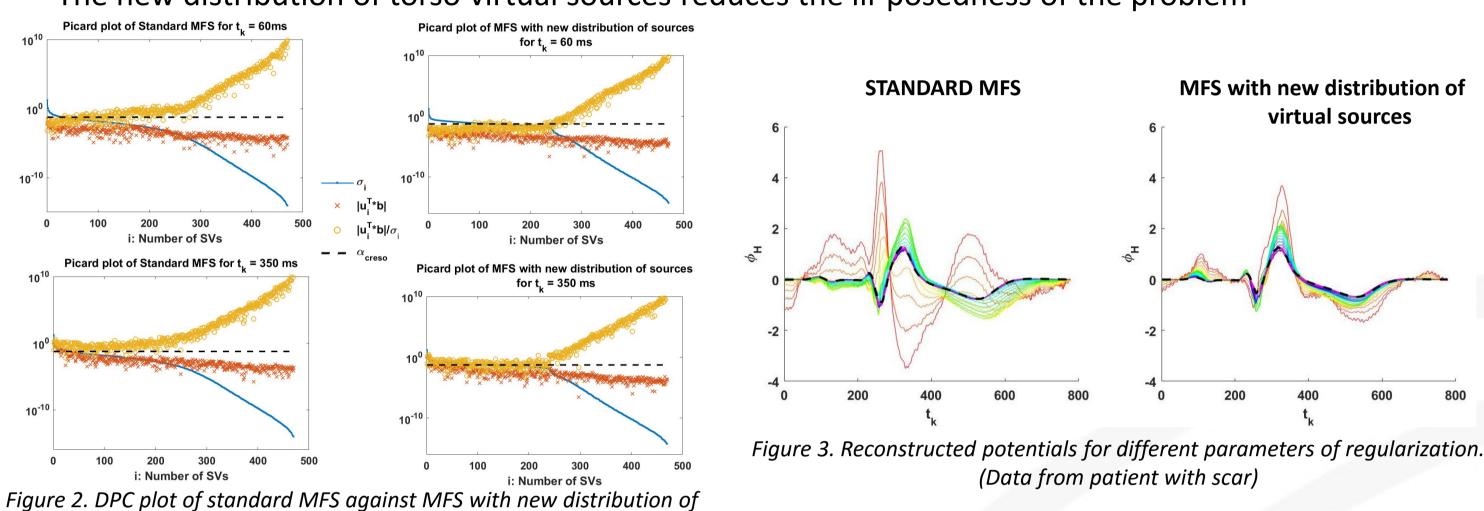
Results

- Study of Boundary conditions: Respective contribution of B0 and B1
- The $\varepsilon = ||B_1|| / ||B_0||$ depends only on the geometry and location of sources (for which we used a fixed rule defined in [2]). We found $\varepsilon = 0.0013$, indicating predominance of B_0 compared to B_1 in the standard MFS.

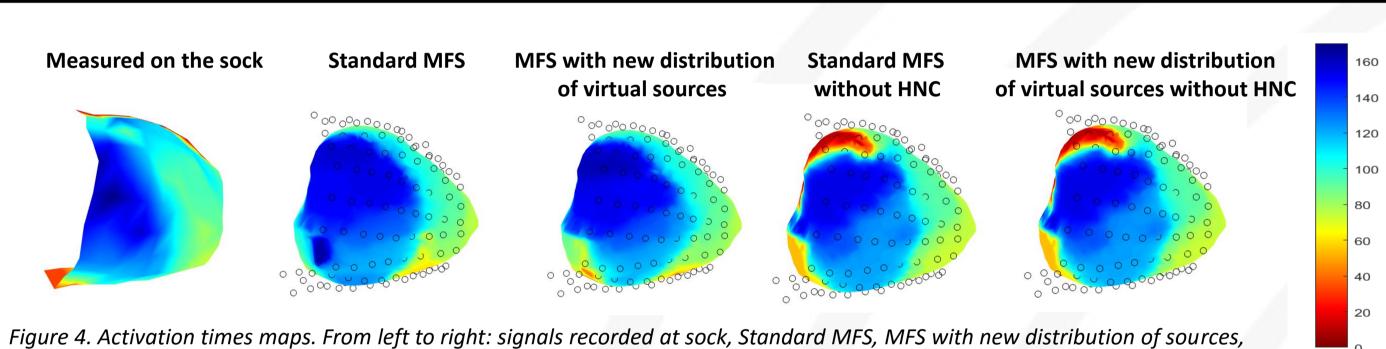


Study of the effect of changing the torso virtual sources placement

The new distribution of torso virtual sources reduces the ill-posedness of the problem



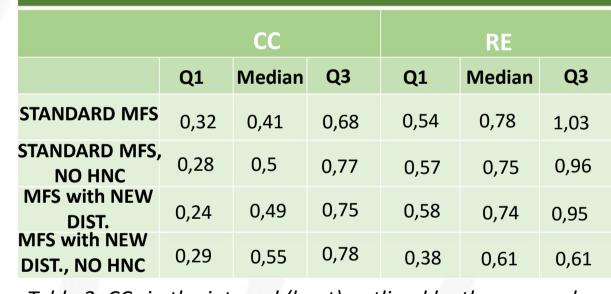
Combining the effect of changing the placement of virtual sources in the torso with the effect of HNC



Standard MFS without HNC, MFS with new distribution of sources and without HNC.

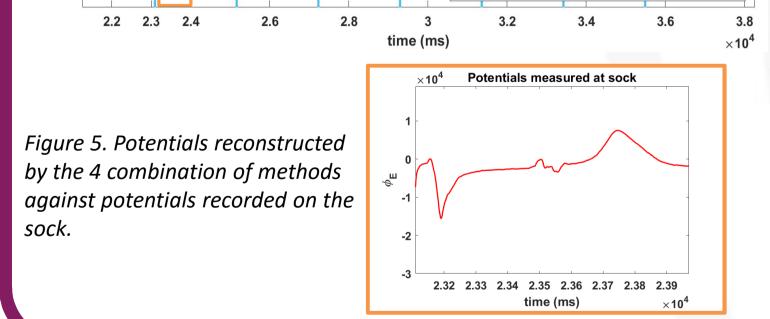
COMPARISON OF ATS STANDARD MFS 0,37 0,57 STANDARD MFS, NO HNC MFS with NEW DIST. 0,61 MFS with NEW DIST., NO HNC 0,58 0,38 Table 2. CCs and REs for Ats maps above (figure 4).

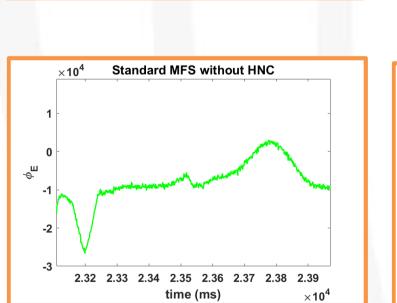
sources for two instances of time different. (Data from patient with scar)



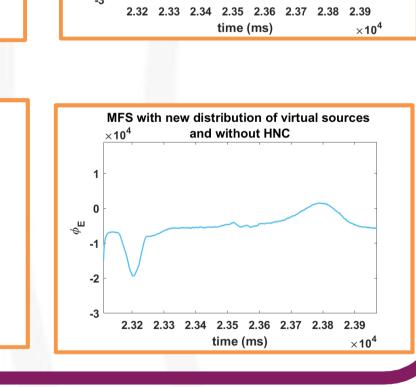
COMPARISON OF ELECTROGRAMS

Table 3. CCs in the interval (beat) outlined by the orange box and REs for potentials below (figure 5).





2.32 2.33 2.34 2.35 2.36 2.37 2.38 2.39



Conclusions

- Removing the Neumann conditions reduces the forward and inverse computational cost.
- MFS with new distribution of sources made the problem less ill-conditioned and less sensitive to the choice of the regularization parameter.
- The HNC are related with the small SVs, i.e. with higher frequencies, this can be seen in the respective noisy reconstructed potentials.
- MFS with new distribution of virtual sources and without HNC has better CC and less REs. However, the REs are still high. This indicates that a good similarity of the potential pattern is achieved but not a good amplitude. Finally, best ATs maps were achieved by standard MFS without HNC.
- Future work: The amplitude can be improved with better choice of the regularization parameter according to the distance of the virtual sources and/or by using spatio-temporal regularization.

Acknowledgements

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