Bridging High-Level Synthesis and Application-Specific Arithmetic: The Case Study of Floating-Point Summations

Yohann Uguen
Univ Lyon, INSA Lyon, Inria, CITI
F-69621 Villeurbanne, France
Yohann.Uguen@insa-lyon.fr

Florent de Dinechin
Univ Lyon, INSA Lyon, Inria, CITI
F-69621 Villeurbanne, France
Florent.de-Dinechin@insa-lyon.fr

Steven Derrien
University Rennes 1, IRISA
Rennes, France
Steven.Derrien@univ-rennes1.fr

Abstract—FPGAs are well known for their ability to perform non-standard computations not supported by classical microprocessors. Many libraries of highly customizable application-specific IPs have exploited this capability. However, using such IPs usually requires handcrafted HDL, hence significant design efforts. High Level Synthesis (HLS) lowers the design effort thanks to the use of C/C++ dialects for programming FPGAs. However, high-level 
language becomes a hindrance when one wants to express non-standard computations: this language was designed for programming microprocessors and carries with it many restrictions due to this paradigm. This is especially true when computing with floating-point, whose datatypes and evaluation semantics are defined by the IEEE-754 and C11 standards. If the high-level specification was a computation on the reals, then HLS imposes a very restricted implementation space.

This work attempts to bridge FPGA application-specific efficiency and HLS ease of use. It specifically targets the ubiquitous floating-point summation-reduction pattern. A source-to-source compiler transforms selected floating-point additions into sequences of simpler operators using non-standard arithmetic formats. This improves performance and accuracy for several benchmarks, while keeping the ease of use of a high-level 

I. INTRODUCTION

Many case studies have demonstrated the potential of Field-Programmable Gate Arrays (FPGAs) as accelerators for a wide range of applications, from scientific or financial computing to signal processing and cryptography. FPGAs offer massive parallelism and programmability at the bit level. These FPGAs characteristics enables programmers to exploit a range of techniques that avoid many bottlenecks of classical von Neumann computing: dataflow operation without the need of instruction decoding; massive register and memory bandwidth, without contention on a register file and single memory bus; operators and storage elements tailored to the application in nature, number and size.

However, to unleash this potential, development costs for FPGAs are orders of magnitude higher than classical programming. High performance and high design costs are the two faces of the same coin.

Hardware design flow and High-level synthesis: To address this, languages such as C or Java are increasingly being considered as hardware description languages. This has many advantages. The language itself is more widely known than any HDL. The sequential execution model makes designing and debugging much easier. One can even use software execution on a processor for simulation. All this drastically reduces development time.

The process of compiling a software program into hardware is called High-Level Synthesis (HLS), with tools such as Vivado HLS [11] or Catapult C 1 among others [18]. These tools are in charge of turning a C description into a circuit. This task requires to extract parallelism from sequential programs constructs (e.g. loops) and expose this parallelism in the target design. Today’s HLS tools are reasonably efficient at this task, and can automatically synthesize highly efficient pipelined dataflow architectures.

They however miss one important feature: they are not able to tailor operators to the application in size, and even less in nature. This comes from the C language itself: its high-level datatypes and operators are limited to a small number (more or less matching the hardware operators present in mainstream processors). Indeed, such high-level languages were designed to be compiled and run on hardware, not to describe hardware.

However, HLS tool know a lot about the context of each operator. This should allow them to transform these simple operators into application-specific ones, thus exploiting FPGAs to their full potential. The broader objective of this work is to demonstrate this opportunity. For this purpose, we envision a compilation flow involving one or several source-to-source transformations, as illustrated by Figure 1.

Arithmetic in HLS: To better exploit the freedom offered by hardware and FPGAs, HLS vendors have enriched the C language with integer and fixed-point types of arbitrary size 2. However the operations on these types remain limited to the basic arithmetic and logic ones. Exotic or complex operators (for instance for finite fields) may be encapsulated in a C function that is called to instantiate the operator.

2Arbitrary-size floating-point should follow some day, it is well supported by mature libraries and tools
The proposed approach uses number formats that are larger or smaller than the standard ones. These, and the corresponding operators, are presented in Section II. The contribution of this paper, which are compiler transformations to generate C description of these operators in a HLS workflow, is presented in Section III. Section IV evaluates our approach on the FPMark benchmark suite.

II. THE ARITHMETIC SIDE: AN APPLICATION-SPECIFIC ACCUMULATOR IN VIVADO HLS

The accumulator that we used for this paper is based on a more general idea developed by Kulisch. He advocated a very large floating-point accumulator [14] whose 4288 bits would cover the entire range of double precision floating-point. Such an accumulator would remove rounding errors from all the possible floating-point additions and sums of products, with the added bonus that addition would become associative.

A parallel execution with the sequential semantics is also possible, but very expensive [13].
So far, Kulisch’s full accumulator has proven too costly to appear in mainstream processors. However, in the context of application acceleration with FPGAs, it can be tailored to the accuracy requirements of applications. Its cost then becomes comparable to classical floating point operators, although it vastly improves accuracy [6]. This operator can be found in the FloPoCo [5] generator and in Altera DSP Builder Advanced. Its core idea, illustrated on Figure 2, is to use a large fixed-point register into which the mantissas of incoming floating-point summands are shifted (top) then accumulated (middle). A third component (bottom) converts the content of the accumulator back to the floating-point format. The sub-blocks visible on this figure (shifter, adder, and leading zero counter) are essentially the building blocks of a classical floating-point adder.

The accumulator used here slightly improves the one offered by FloPoCo [6]:

- It supports subnormal numbers [17].
- In FloPoCo, FloatToFix and Accumulator form a single component, which restricts its application to simple accumulations similar to Listing 1. The two components of Figure 2 enable a generalization to arbitrary summations within a loop, as Section III will show.

The parameters of a large accumulator

The main feature of this approach is that the internal fixed-point representation is configurable in order to control accuracy. It has two parameters:

- MSBA is the weight of the most significant bit of the accumulator. For example, if MSBA = 20, the accumulator can accommodate values up to a magnitude of $2^{20} \approx 10^{6}$.
- LSBA is the weight of the least significant bit of the accumulator. For example, if LSBA = −50, the accumulator can hold data accurate to $2^{-50} \approx 10^{-15}$.

Such a fixed-point format is illustrated in Figure 3. The accumulator width $w_a$ is then computed as MSBA − LSBA + 1, for instance 71 bits in the previous example. 71 bits represents a wide range and high accuracy, and still additions on this format will have one-cycle latency for practical frequencies on recent FPGAs. If this is not enough the frequency can be improved thanks to partial carry save [6] but this was not useful in the present work. For comparison, for the same frequency, a floating-point adder has a latency of 7 to 10 cycles, depending on the target.

In the following, the latency of a circuit denotes the number of cycles needed for the entire application to complete.

Implementation within a HLS tool

This accumulator has been implemented in C, using arbitrary-precision fixed point types (ap_int). The leading zero count, bit range selections and other operations are implemented using Vivado HLS built-in functions. For modularity purposes, the FloatToFix and FixToFloat are wrapped into C functions (respectively 28 and 22 lines of code). Their calls are inlined to enable HLS optimizations.

Because the internal accumulation is performed on a fixed-point integer representation, the combinational delay between two accumulations is lower compared to a full floating point addition. HLS tools can take advantage of this delay reduction by more aggressive loop pipelining (with shorter Initiation Interval), resulting in a design with a shorter overall latency.

Validation

To evaluate and refine this implementation, we used Listing 3, which we compared to Listings 1 and 2. In the latter, the loop was unrolled by a factor 7, as it is the latency of a floating-point adder on our target FPGA (Kintex-7).
For test data, we use as in Muller et al. [17] the input values $c[i] = (\text{float}) \cos (i)$, where $i$ is the input array’s index. Therefore the accumulation computes $\sum_i c[i]$.

The parameters chosen for the accumulator are:
- MSBA = 17. Indeed, as we are adding $\cos(i)$ 100K times, an upper bound is 100K, which can be encoded in 17 bits.
- MaxMSBX = 1 as the maximum input value is 1.
- LSBA = -50: the accumulator itself will be accurate to the 50th fractional bit. Note that a float input will see its mantissa rounded by FloatToFix only if its exponent is smaller than $2^{-25}$, which is very rare. In other words, this accumulator is much more accurate than the data that is thrown to it.

The results are reported in Table I for simple and double precision. The Accuracy line of the table reports the number of correct bits of each implementation, after the result has been rounded to a float. All the data in this table was obtained by generating VHDL from C synthesis using Vivado HLS followed by place and route from Vivado v2015.4, build 1412921. This table also reports synthesis results for the corresponding FloPoCo-generated VHDL, which doesn’t include the array management.

Vivado HLS uses DSPs to implement the shifts in its floating-point adders. Even if the shifts were implemented in LUTs, the first column would remain well below 500 LUTs: it has the best resource usage. However the latency of one iteration is 7 cycles, hence 100K iterations takes 700K cycles. When unrolling the loop, Vivado HLS is using almost 4 times more LUTs for floats, and 3 times more for doubles. The unrolled versions improves latency over naive versions. Nevertheless, the proposed approach gets even better latencies for a reasonable LUT usage. It also achieves maximum accuracy for the float format, which caps at 24 bits (the internal representations of the double, unrolled double and proposed approach have a higher accuracy than 24 bits, but their result is then rounded to a float). Finally, our results are very close to FloPoCo ones, both in terms of LUT usage, DPSS and latency.

### Table I: Synthesis results of different accumulators using Vivado HLS for Kintex 7.

<table>
<thead>
<tr>
<th>Listing</th>
<th>Listing 2</th>
<th>Listing 1</th>
<th>Listing 2</th>
<th>Listing 3</th>
<th>FloPoCo VHDL</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>(float)</td>
<td>(float)</td>
<td>(double)</td>
<td>(double)</td>
<td>(71 bits)</td>
</tr>
<tr>
<td>LUTs</td>
<td>266</td>
<td>907</td>
<td>801</td>
<td>2193</td>
<td>736</td>
</tr>
<tr>
<td>DSPs</td>
<td>2</td>
<td>4</td>
<td>3</td>
<td>6</td>
<td>0</td>
</tr>
<tr>
<td>Latency</td>
<td>100K</td>
<td>142K</td>
<td>700K</td>
<td>142K</td>
<td>100K</td>
</tr>
<tr>
<td>Accuracy</td>
<td>17 bits</td>
<td>17 bits</td>
<td>24 bits</td>
<td>24 bits</td>
<td>24 bits</td>
</tr>
</tbody>
</table>

Using this implementation method, we also created an exact floating-point multiplier with the final rounding removed as in [6]. This function is called ExactProduct and represents 44 lines of code. Due to lack of space we do not present it in detail. As the output of this multiplier is not standard, we also created an adapted Float-to-fix block called ExactProductFloatToFix (21 lines of code).

### III. THE COMPILER SIDE: GeCoS source-to-source transformations

The previous section has shown that Vivado HLS can be used to synthesize very efficient specialized floating point operators which rival in quality with those generated by FloPoCo. Our goal is now to study how such optimization can be automated. More precisely, we aim at automatically optimizing Listing 1 into Listing 3, and generalizing this transformation to many more situations.

For convenience, this optimization was developed as a source-to-source transformation implemented within the open source GeCoS compiler framework [8]. It is publicly available with GeCoS. Source-to-source compiler are very convenient in an HLS context, since they can be used as optimization front-ends on top of closed-source commercial tools.

This work focuses on two computational patterns, namely the accumulation and the sum of product. Both are specific instances of the reduction pattern, which can be optimized by many compilers or parallel run-time environments. Reduction pattern are exposed to the compiler/runtime either though user directives (e.g. #pragma reduce in openMP), or automatically inferred using static analysis techniques [19], [7].

As the problem of detecting reductions is not the main focus on this work, our tool uses a straightforward solution to the problem using a combination of user directive and (simple) program analysis. More specifically, the user must identify a target accumulation variable through a pragma, and provide additional information such as the dynamic range of the accumulated data along with the target accuracy. In the future, we expect to improve the program analysis, so that the two later parameter could be omitted in some situations.

We found this approach easier, more general and less invasive than those attempting to convert a whole floating-point program into a fixed-point implementation [20].

#### A. Proposed compiler directive

In imperative languages such as C, reductions are implemented using for or while loop constructs. Our compiler directive must therefore appear right outside such a construct. Listing 4 illustrates its usage on the code of Listing 1.

Listing 3: Sum of floats using the large fixed-point accumulator

```c
#define N 100000
float acc = 0; ap_int<68> long_accumulator = 0;
for(int i = 0; i < N; i++) {
    long_accumulator += FloatToFix(in[i]);
}
acc = FixToFloat(long_accumulator);
```
The \texttt{pragma} must contain the following information:

- The keyword \texttt{FPacc}, which triggers the transformations.
- The name of the variable in which the accumulation is performed, preceded with the keyword \texttt{VAR}. In the example, the accumulation variable is \texttt{acc}.
- The maximum value that can be reached by the accumulator through the use of the \texttt{MaxAcc} keyword. This value is used to determine the weight MSBA.
- The desired accuracy of the accumulator using the \texttt{epsilon} keyword. This value is used to determine the weight LSBA.
- Optional: The maximum value among all inputs of the accumulator in the \texttt{MaxInput} field. This value is used to determine the weight MaxMSBX. If this information is not provided, then MaxMSBX is set to MSBA.

\textbf{Listing 4: Illustration of the use of a} \texttt{pragma} \textbf{for the naive accumulation}

\begin{verbatim}
#define N 100000
float accumulation(float in[N]){
    float acc = 0;
    #pragma FPacc VAR=acc MaxAcc=100000.0 epsilon=1E-15 MaxInput=1.0
    for(int i=0; i<N; i++){
        acc+=in[i];
    }
    return acc;
}
\end{verbatim}

In the case when no size parameters are given, a full Kulisch accumulator is currently produced. Note that the user can quietly overestimate the maximum value of the accumulator without major impact on area. For instance, overestimating \texttt{MaxAcc} by a factor 10 only adds 3 bits to the accumulator width.

\textbf{B. Proposed code transformation}

The proposed transformation operates on the compiler program intermediate representation (IR), and rely on the ability to identify loops constructs and expose def/use relations between instructions of a same basic block in the form of an operation dataflow graph (DFG).

\textbf{Listing 5: Simple reduction with multiple accumulation statements}

\begin{verbatim}
#define N 100000
float computeSum(float in1[N], float in2[N]){
    float sum = 0;
    #pragma FPacc VAR=sum MaxAcc=300000.0 epsilon=1e-15 MaxInput=3.0
    for(int i=1; i<N-1; i++){
        sum+=in1[i]*in2[i-1];
        sum+=in1[i];
        sum+=in2[i+1];
    }
    return sum;
}
\end{verbatim}

To illustrate the transformation, consider the toy but non-trivial program of Listing 5. This program performs a reduction into the variable \texttt{sum}, involving both sums and sums of product operations. Figure 4a shows the operation dataflow graph for the loop body of this program. In this Figure, dotted arrows represent loop-carried dependencies between operations belonging to distinct loop iterations. Such loop-carried dependencies have a very negative impact on the kernel latency as they prevent loop pipelining. For example, when using a pipelined floating-point adder with a seven cycle latency, the HLS tool will schedule a new iteration of the loop at best every seven cycles.

As illustrated in Figure 5a, the proposed transformation hoists the floating-point normalization step out of the loop, and performs the accumulation using fixed point arithmetic. Since integer add operations can generally be implemented with a 1-cycle delay, the HLS tool may now be able to initiate a new iteration every cycle, improving the overall latency by a factor of 7.

The code transformation first identifies all relevant basic blocks (i.e those associated to the \texttt{pragma} directive). It then
performs a backward traversal of the dataflow graph, starting from a Float Add node that writes to the accumulation variable identified by the #pragma.

During this traversal, the following actions are performed depending on the visited nodes:
- A node with the summation variable is ignored.
- A Float Add node is transformed to an accurate fixed-point adder. The analysis is then recursively launched on that node.
- A Float Mul node is replaced with a call to the ExactProduct function followed by a call to ExactProdFloatToFix.
- Any other node has a call to FloatToFix inserted.

This algorithm rewrites the DFG from Figure 4a into the new DFG shown on Figure 5a. In addition, a new basic block containing a call to FixToFloat is inserted immediately after the transformed loop, in order to expose the floating point representation of the results to the remainder of the program.

Figure 5: DFG of the loop body from Listing 5 (top) and its corresponding architecture (bottom) after transformations

From there, it is then possible to regenerate the corresponding C code. As an illustration of the whole process, Figures 4b and 5b describe the architectures corresponding to the code before and after the transformation.

C. Evaluation of the toy example of Listing 5

The proposed transformations work on non-trivial examples such as the one represented in Listing 5. Table II shows how resource consumption depends on epsilon, all the other parameters being those given in the pragma of Listing 5. All these versions where synthesised for 100 MHz.

Compared to the classical IEEE-754 implementation, the transformed code uses more LUTs for less DSPs. This is due to Vivado implementing shifters using DSPs within the floating-point IP, but not in the transformed code. In all cases, on this example, the transformed code has its latency reduced by a factor 20.

IV. Evaluation on FPMark benchmarks

In order to evaluate the relevance of the proposed transformations on real-life programs, we used the EEMBC FPMark benchmark suite [1].

This suite consists of 10 programs. A first result is that half of these programs contain visible accumulations:
- Enhanced Livermore Loops (1/16 kernels contains one accumulation)
- LU Decomposition (multiple accumulations)
- Neural Net (multiple accumulations)
- Fourier Coefficients (one accumulation)
- Black Scholes (one accumulation)

The following focuses on these, and ignores the other half (Fast Fourier Transform, Horner’s method, Linpack, ArcTan, Ray Tracer).

Most benchmarks come in single-precision and double-precision versions. We focus here on the single-precision. Double-precision benchmarks lead to the same conclusions.

A. Benchmarks and accuracy: methodology

Each benchmark comes with a golden reference against which the computed results are compared. As the proposed transformations are controlled by the accuracy, it may happen that the transformed benchmark is less accurate than the original. In this case, it will not pass the benchmark verification test, and rightly so.

A problem is that the transformed code will also fail the test if it is more accurate than the original. Indeed, the golden reference is the result of a certain combination of rounding

<table>
<thead>
<tr>
<th></th>
<th>Naive</th>
<th>Transformed LSBA = (-14)</th>
<th>Transformed LSBA = (-20)</th>
<th>Transformed LSBA = (-50)</th>
</tr>
</thead>
<tbody>
<tr>
<td>LUTs</td>
<td>538</td>
<td>693</td>
<td>824</td>
<td>1400</td>
</tr>
<tr>
<td>DSPs</td>
<td>5</td>
<td>2</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>Latency</td>
<td>200K</td>
<td>100K</td>
<td>100K</td>
<td>100K</td>
</tr>
</tbody>
</table>

Table II: Comparison between the naive code from Listing 5 and its transformed equivalent. All these versions run at 100MHz.
errors using the standard FP formats, which we do not attempt
to replicate.

To work around this problem, each benchmark was first
transformed into a high-precision version where the accumu-
lation variable is a 10,000-bit floating-point numbers using
the MPFR library. We used the result of this highly-accurate
version as a “platinum” reference, against which we could
measure the accuracy of the benchmark’s golden reference.
This allowed us to choose our epsilon parameter such that
the transformed code would be at least as accurate as the
golden reference. This way, the epsilon of the following
results is obtained through profiling. The accuracy of the
obtained results are computed as the number of correct bits of
the result.

We first present the benchmarks that are improved by our
approach before discussing the reasons why we can’t prove
that the others are.

B. Benchmarks improved by the proposed transformation

Enhanced Livermore Loops: This program contains 16
kernels of loops that compute numerical equations. Among
these kernels, there is one that performs a sum-of-product
(banded linear equations). This kernel computes 20000 sums-
of-products. The values accumulated are pre-computed. This
is a perfect candidate for the proposed transformations.

For this benchmark, the optimal accumulation parameters
were found as:
MaxAcc=50000.0 epsilon=1e-5
MaxInput=22000.0

Synthesis results of both codes (before and after transforma-
tion) are given in Table III. As in the previous toy examples,
laten
cy and accuracy are vastly improved for comparable area.

<table>
<thead>
<tr>
<th>Benchmark</th>
<th>Type</th>
<th>LUTs</th>
<th>DSPs</th>
<th>Latency</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Livermore</td>
<td>Original</td>
<td>384</td>
<td>5</td>
<td>80K</td>
<td>11 bits</td>
</tr>
<tr>
<td></td>
<td>Transformed</td>
<td>576</td>
<td>2</td>
<td>20K</td>
<td>13 bits</td>
</tr>
<tr>
<td>LU-8</td>
<td>Original</td>
<td>809</td>
<td>5</td>
<td>82</td>
<td>8-23 bits</td>
</tr>
<tr>
<td></td>
<td>Transformed</td>
<td>1007</td>
<td>2</td>
<td>17</td>
<td>23 bits</td>
</tr>
<tr>
<td>LU-45</td>
<td>Original</td>
<td>819</td>
<td>5</td>
<td>452</td>
<td>8-23 bits</td>
</tr>
<tr>
<td></td>
<td>Transformed</td>
<td>1034</td>
<td>2</td>
<td>54</td>
<td>23 bits</td>
</tr>
<tr>
<td>Scholes</td>
<td>Original</td>
<td>15640</td>
<td>175</td>
<td>N/A</td>
<td>19 bits</td>
</tr>
<tr>
<td></td>
<td>Transformed</td>
<td>15923</td>
<td>175</td>
<td>N/A</td>
<td>23 bits</td>
</tr>
<tr>
<td>Fourier</td>
<td>Original</td>
<td>34396</td>
<td>64</td>
<td>N/A</td>
<td>6 bits</td>
</tr>
<tr>
<td></td>
<td>Transformed</td>
<td>34681</td>
<td>59</td>
<td>N/A</td>
<td>11 bits</td>
</tr>
</tbody>
</table>

Table III: Synthesis results of benchmarks before and after
transformations

LU Decomposition and Neural Net: Both the LU decom-
position and the neural net programs contain multiple nested
small accumulations. In the LU decomposition program, an
inner loop accumulates between 8 and 45 values. Such accu-
mulations are performed more than 7M times. In the neural
net program, inner loops accumulate between 8 and 35 values,
and such accumulations are performed more than 5K times.

Both of these programs accumulate values from registers or
memory that are already computed. It makes these programs
good candidates for the proposed transformations.

Vivado HLS is unable to predict a latency for these designs
due to their non-constant loop trip counts. As a consequence,
instead of presenting results for the complete benchmark,
we restrict ourselves to the LU innermost loops. Table III
shows the results obtained for the smallest (8 terms) and the
largest (45 terms) sums-of-products in lines LU-8 and LU-
45 respectively. The latency is vastly improved even for the
smallest one. The accuracy results of the original code here
varies from 8 to 23 bits between different instances of the
loops. To have a fair comparison, we generated a conservative
design that performs 23 bits accuracy on all loops, using a
sub-optimal amount of resources.

C. Benchmarks that exposed the limitations of HLS tools

Black Scholes: This program contains an accumulation that
sums 200 terms. The result of this computation is divided by
a constant (that could be optimized by using transformations
based on [3]). This process is performed 5000 times.

Here the optimal accumulator parameters are the following:
MaxAcc=245000.0 epsilon=1e-4
MaxInput=278.0
This gives us an accumulator that uses 19 bits for the integer
part and 10 bits for the fractional part. The result of the
synthesis are provided in Table III.

For comparable area, accuracy is vastly improved but
latency could not be obtained from Vivado HLS. Indeed,
the Black Scholes algorithm uses the mathematical function
power. Such a function is not natively supported by Vi-
vado HLS, and was therefore implemented by hand using a
data dependant trip count loop. Because of this, the tool cannot
statically derive the execution latency of the benchmark.

Fourier Coefficients: The Fourier coefficients program,
which computes the coefficients of a Fourier series, contains an
accumulation which is performed in single precision. This pro-
cram comes in three different configurations: small, medium
and big. Each of them computes the same algorithm but with a
different amount of iterations. The big version is supposed to
compute the most accurate answer. We obtain similar results
for the three versions of this program, as a consequence we
only present the big version here. In this version, there are
multiple instances of 2K terms accumulations. The accumula-
tor is reset at every call.

The parameters determined for this benchmark were the
following:
MaxAcc=6000.0 epsilon=1e-7 MaxInput=10.0
This results in an accumulator using 14 bits for the integer
part and 24 bits for the fractional part. The synthesis results
obtained for the original and transformed codes are given in
Table III.

Here again, area cost is comparable, while accuracy is
improved by 5 bits (which represents one order of magnitude).
As for Black Scholes, Vivado HLS cannot compute the overall
latency due to the power function. However, since our oper-
ators have a shorter latency by design, we expect the circuits
to also have a shorter latency.
The power operator could be implemented such as in [4] in the near future. This would allow us to obtain the latency of the two last benchmarks.

V. CONCLUSION

The main outcome of this work is an evidence that HLS tools have the potential to generate efficient designs for handling floating-point computations in a completely non-standard way. Our results show that the use of application-specific intermediate formats can provide both performance and accuracy at a competitive cost. To achieve this, we have to sacrifice the strict respect of the IEEE-754 and C11 standards. It is replaced by the strict respect of a high-level specification.

Classically, designers face a trade-off between performance and cost. Our approach brings computation accuracy to this trade-off. Some designers may not like this. To convince them, consider that established performance benchmarks compute results which are accurate only to a few bits. If only a few bits are important, do we really need to instantiate 32-bit or 64-bit floating-point operators to compute them? Isn’t this accuracy information worth investigating and exploiting?

This work also provides a practical tool that improves a given C program. The input to the tool is application-specific information representing high-level domain knowledge such as the range and desired accuracy of a variable. The resulting code is compatible with Vivado HLS.

The proposed transformation already works very well on all the FPMarks that contains a reduction where it improves both latency and accuracy by an order of magnitude for comparable area.

In the longer term, we believe there is much more to come. The arithmetic optimizations that a classical compiler can do are very limited by the fixed hardware of classical processors. With compilers of high-level software to hardware, there is much more freedom, hence many more opportunities to build application-specific arithmetic operators.

Future work will attempt to explore this new realm, starting with operator specialization; operator fusion such as in [21] but at a more coarse grain allowing more aggressive fusion; compile-time generation of application-specific cores; error analysis such as in [15] benefiting from compilers static analysis and more generally building upon compiler progresses in program analysis.

REFERENCES