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Embedding domain technique for a fluid-structure interaction problem

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Abstract. We present a weak formulation for a steady fluid-structure interaction problem using an embedding domain technique with penalization. Except of the penalizing term, the coefficients of the fluid problem are constant and independent of the deformation of the structure, which represents an advantage of this approach. A second advantage of this model is the fact that the continuity of the stress at the fluid-structure interface does not appear explicitly. Numerical results are presented.

Keywords: fluid-structure interaction; embedding domain;

1 A steady fluid-structure interaction problem

The present paper is devoted to the study of the numerical behavior of an elastic structure immersed in a viscous incompressible fluid. We use Stokes equation to model the flow motion. The displacement of the structure under the flow motion will be modeled by linear elasticity equations, under the small deformations assumption. In this paper, we study the steady case.

Let $D \subset \mathbb{R}^2$ be a bounded open domain with boundary ∂D . Let Ω_0^S be the undeformed structure domain, and suppose that its boundary admits the decomposition $\partial\Omega_0^S = \Gamma_D \cup \Gamma_0$, where Γ_0 is a relatively open subset of the boundary. On Γ_D we impose zero displacement for the structure. We assume that $\Omega_0^S \subset D$.

Suppose that the structure is elastic and denote by $\mathbf{u} = (u_1, u_2) : \Omega_0^S \rightarrow \mathbb{R}^2$ its displacement. A particle of the structure with initial position at the point \mathbf{X} will occupy the position $\mathbf{x} = \varphi(\mathbf{X}) = \mathbf{X} + \mathbf{u}(\mathbf{X})$ in the deformed domain $\Omega_u^S = \varphi(\Omega_0^S)$.

We assume that $\Omega_u^S \subset D$ and the fluid occupies $\Omega_u^F = D \setminus \overline{\Omega_u^S}$. We set $\Gamma_u = \varphi(\Gamma_0)$ and we suppose that Γ_u does not touch the container wall, i.e. $\partial D \cap \Gamma_u = \emptyset$. We recall that Γ_0 is a relatively open subset. The boundary Γ_u represents the moving fluid-structure interface. The boundary of the deformed

structure is $\partial\Omega_u^S = \Gamma_D \cup \Gamma_u$. In the case when $\overline{\Omega}_u^S \subset D$, the fluid-structure geometrical configuration is represented in Figure 1 and the boundary of the fluid domain admits the decomposition $\partial\Omega_u^F = \partial D \cup \Gamma_D \cup \Gamma_u$.

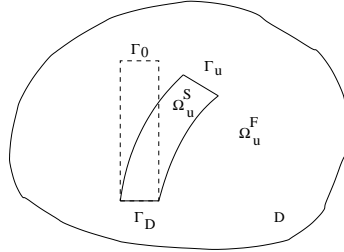


Fig. 1. Geometrical configuration.

Also, for the first numerical test, we consider the case when $\Gamma_D \subset \partial D$ as in Figure 2 and the boundary of the fluid domain admits the decomposition $\partial\Omega_u^F = (\partial D \setminus \Gamma_D) \cup \Gamma_u$.

2 Weak formulation using an embedding domain technique with penalization

We introduce the tensor $\epsilon(\mathbf{w}) = \frac{1}{2}(\nabla\mathbf{w} + (\nabla\mathbf{w})^T)$ and we assume that the fluid is Newtonian and the Cauchy stress tensor is given by $\sigma^F(\mathbf{v}, p) = -p\mathbf{I} + 2\mu^F\epsilon(\mathbf{v})$, where $\mu^F > 0$ is the viscosity of the fluid and \mathbf{I} is the unit matrix. We assume that the structure verifies the linear elasticity equation, under the assumption of small deformations. The stress tensor of the structure written in the Lagrangian framework is $\sigma^S(\mathbf{u}) = \lambda^S(\nabla \cdot \mathbf{u})\mathbf{I} + 2\mu^S\epsilon(\mathbf{u})$, where $\lambda^S, \mu^S > 0$ are the Lamé coefficients.

We present in an informal and intuitive manner the ideas behind our approximation approach using embedding domain technique with penalization. In the fluid domain, Stokes equations are solved:

$$-\nabla \cdot \sigma^F(\mathbf{v}, p) = \mathbf{f}^F, \quad \text{in } \Omega_u^F \quad (1)$$

$$\nabla \cdot \mathbf{v} = 0, \quad \text{in } \Omega_u^F \quad (2)$$

We introduce two more equations concerning the fluid fields, but written on the deformed structure domain:

$$-\nabla \cdot \sigma^F(\mathbf{v}, p) + \frac{1}{\varepsilon}\mathcal{P}(\mathbf{v}) = \mathbf{f}^F, \quad \text{in } \Omega_u^S \quad (3)$$

$$\nabla \cdot \mathbf{v} = 0, \quad \text{in } \Omega_u^S \quad (4)$$

where $\varepsilon > 0$ is a penalization parameter,

$$\mathcal{P}(\mathbf{v}) = \left(|v_1|^{\alpha-1} \operatorname{sgn}(v_1), |v_2|^{\alpha-1} \operatorname{sgn}(v_2) \right) \quad (5)$$

where $\mathbf{v} = (v_1, v_2)$ and $1 < \alpha < 2$ is a real number.

Remark 1. This choice of the penalization term is justified in [2], in order to obtain existence of the fluid-structure interaction problem. For the steady case, the role of the penalization term is to obtain very small values of the fluid velocity in the structure domain. If we take other values for α or for a H^1 penalization, we do not get more regularity of the solution.

Let χ_u^S be the characteristic function of Ω_u^S . Combining (1) and (3), it follows that

$$-\nabla \cdot \sigma^F(\mathbf{v}, p) + \frac{1}{\varepsilon} \chi_u^S \mathcal{P}(\mathbf{v}) = \mathbf{f}^F, \quad \text{in } D. \quad (6)$$

Similarly, we have from (2) and (4)

$$\nabla \cdot \mathbf{v} = 0, \quad \text{in } D. \quad (7)$$

In view of the equation (3), the ‘‘fictitious’’ fluid velocity and pressure defined on the structure domain Ω_u^S depend on ε . In the following, we denote by \mathbf{v}_ε and p_ε the fluid velocity and pressure defined all over the domain D .

Let us introduce the bi-linear forms

$$\begin{aligned} a_S(\mathbf{u}, \mathbf{w}^S) &= \int_{\Omega_0^S} (\lambda^S (\nabla \cdot \mathbf{u}) (\nabla \cdot \mathbf{w}^S) + 2\mu^S \varepsilon(\mathbf{u}) : \varepsilon(\mathbf{w}^S)) \, d\mathbf{X} \\ a_F(\mathbf{v}, \mathbf{w}) &= \int_D 2\mu^F \varepsilon(\mathbf{v}) : \varepsilon(\mathbf{w}) \, d\mathbf{x} \\ b_F(\mathbf{w}, p) &= - \int_D (\nabla \cdot \mathbf{w}) p \, d\mathbf{x} \end{aligned}$$

and the Hilbert spaces

$$\begin{aligned} W^S &= \left\{ \mathbf{w}^S \in (H^1(\Omega_0^S))^2; \mathbf{w}^S = 0 \text{ on } \Gamma_D \right\}, \\ W &= (H_0^1(D))^2, \\ Q &= L_0^2(D) = \{q \in L^2(D); \int_D q \, dx = 0\}. \end{aligned}$$

We assume for the moment that $\mathbf{f}^F \in (L^2(D))^2$, $\mathbf{f}^S \in (L^2(\Omega_0^S))^2$ and $\mathbf{g} \in (H^{1/2}(\partial D))^2$, such that $\int_{\partial D} \mathbf{g} \cdot \mathbf{n}^F \, ds = 0$.

For a given $\mathbf{u} \in (W^{1,\infty}(\Omega_0^S))^2$, such that $\|\mathbf{u}\|_{1,\infty,\Omega_0^S} < 1$ and $\mathbf{u} = 0$ on Γ_D , we define:

- fluid velocity $\mathbf{v}_\varepsilon \in (H^1(D))^2$, $\mathbf{v}_\varepsilon = \mathbf{g}$ on ∂D ,
- fluid pressure $p_\varepsilon \in Q$,

– structure displacement $\mathbf{u}_\varepsilon \in W^S$,

as the solution of the following weakly coupled system of PDE's:

$$a_F(\mathbf{v}_\varepsilon, \mathbf{w}) + b_F(\mathbf{w}, p_\varepsilon) + \frac{1}{\varepsilon} \int_D \tilde{H}_u \mathcal{P}(\mathbf{v}_\varepsilon) \cdot \mathbf{w} \, d\mathbf{x} = \int_D \mathbf{f}^F \cdot \mathbf{w} \, d\mathbf{x}, \quad \forall \mathbf{w} \in W \quad (8)$$

$$b_F(\mathbf{v}_\varepsilon, q) = 0, \quad \forall q \in Q \quad (9)$$

$$\begin{aligned} a_S(\mathbf{u}_\varepsilon, \mathbf{w}^S) &= \int_{\Omega_0^S} \mathbf{f}^S \cdot \mathbf{w}^S \, d\mathbf{X} + \int_{\Omega_0^S} J(\sigma^F(\mathbf{v}_\varepsilon, p_\varepsilon) \circ \varphi) \mathbf{F}^{-T} : \nabla_{\mathbf{X}} \mathbf{w}^S \, d\mathbf{X} \\ &\quad + \frac{1}{\varepsilon} \int_{\Omega_0^S} J \tilde{H}_u \mathcal{P}(\mathbf{v}_\varepsilon \circ \varphi) \cdot \mathbf{w}^S \, d\mathbf{X} \\ &\quad - \int_{\Omega_0^S} J(\mathbf{f}^F \circ \varphi) \cdot \mathbf{w}^S \, d\mathbf{X}, \quad \forall \mathbf{w}^S \in W^S \end{aligned} \quad (10)$$

where $\varphi(\mathbf{X}) = \mathbf{X} + \mathbf{u}(\mathbf{X})$, $\mathbf{F}(\mathbf{X}) = \mathbf{I} + \nabla_{\mathbf{X}} \mathbf{u}(\mathbf{X})$, $J(\mathbf{X}) = \det \mathbf{F}(\mathbf{X})$.

The equations (8) and (9) are obtained from (6) and (7). The coefficient \tilde{H}_u in (8) is a regularization of the characteristic function of Ω_u^S , which is necessary in order to prove the continuity of the solution with respect to the structure displacement.

Remark 2. From the structure equation $-\nabla \cdot \sigma^S(\mathbf{u}_\varepsilon) = \mathbf{f}^S$, in Ω_0^S using Green's formula, we obtain for all $\mathbf{w}^S = 0$ on Γ_D that

$$a_S(\mathbf{u}_\varepsilon, \mathbf{w}^S) = \int_{\Omega_0^S} \mathbf{f}^S \cdot \mathbf{w}^S \, d\mathbf{X} + \int_{\Gamma_0} \sigma^S(\mathbf{u}_\varepsilon) \mathbf{n}^S \cdot \mathbf{w}^S \, dS.$$

We can prove (see [2]) that the sum of the last three terms in (10) is equal to the fluid forces acting on the structure which is also equals to $\int_{\Gamma_0} \sigma^S(\mathbf{u}_\varepsilon) \mathbf{n}^S \cdot \mathbf{w}^S \, dS$. In fact, from (10) and the above weak formulation of the structure, we can get that the boundary condition at the interface concerning the continuity of the stress is verified in a weak sense (see [2]). The second boundary condition at the interface is the continuity of the velocity, i.e. $\mathbf{v} = 0$ on Γ_u in the steady case. This is obtained by using the penalization term in the structure domain.

Define the nonlinear operator

$$T_\varepsilon : \left\{ \mathbf{u} \in (W^{1,\infty}(\Omega_0^S))^2; \|\mathbf{u}\|_{1,\infty,\Omega_0^S} < 1, \mathbf{u} = 0 \text{ on } \Gamma_D \right\} \rightarrow (W^{1,\infty}(\Omega_0^S))^2$$

by $T_\varepsilon(\mathbf{u}) = \mathbf{u}_\varepsilon$. A solution of the penalized fluid-structure interaction problem will be, by definition, a fixed point of T_ε . In [2], we discuss the existence of a solution of the penalized fluid-structure interaction problem. The convergence of \mathbf{u}_ε , \mathbf{v}_ε , p_ε when ε goes to 0 is also analyzed.

3 Partitioned procedures based on fixed point iterations

The penalized term $\mathcal{P}(\mathbf{v})$ is non-linear in \mathbf{v} for $\alpha \neq 2$. But for $\alpha = 2$, we have $\mathcal{P}(\mathbf{v}) = \mathbf{v}$. Now, the fluid problem, at the **Step 2** of the algorithm below, becomes linear and, for a given \mathbf{u}_ε^k , it has a unique solution.

For $1 < \alpha < 2$, we can prove the existence of a fixed point for the nonlinear operator T_ε defined at the end of the previous section, but not for $\alpha = 2$. We can also replace \tilde{H}_u in (8) by χ_u^S the characteristic function of Ω_u^S in order to simplify the computation. The regularization of the the characteristic function was necessary in order to prove the continuity of the solution with respect to the structure displacement.

Under the assumption of small displacements for the structure, we can approach the Jacobian determinant J by 1 and the gradient of the deformation \mathbf{F} by the identity matrix \mathbf{I} . The structure problem at the **Step 3** is linear and, for given \mathbf{v}_ε^k and p_ε^k , it has a unique solution.

Algorithm

Step 1. Given the initial displacement of the structure $\mathbf{u}^0 \in W^S$, compute the characteristic function $\chi_{u^0}^S$, put $k := 0$.

Step 2. Find the velocity $\mathbf{v}_\varepsilon \in (H^1(D))^2$, $\mathbf{v}_\varepsilon = \mathbf{g}$ on ∂D and the pressure $p_\varepsilon^k \in Q$ by solving the fluid problem

$$\begin{aligned} a_F(\mathbf{v}_\varepsilon^k, \mathbf{w}) + b_F(\mathbf{w}, p_\varepsilon^k) + \frac{1}{\varepsilon} \int_D \chi_{u_\varepsilon^k}^S \mathbf{v}_\varepsilon^k \cdot \mathbf{w} \, d\mathbf{x} &= \int_D \mathbf{f}^F \cdot \mathbf{w} \, d\mathbf{x}, \quad \forall \mathbf{w} \in W \\ b_F(\mathbf{v}_\varepsilon^k, q) &= 0, \quad \forall q \in Q. \end{aligned}$$

Step 3. Find the new displacement of the structure $\mathbf{u}_\varepsilon^{k+1} \in W^S$ by solving

$$\begin{aligned} a_S(\mathbf{u}_\varepsilon^{k+1}, \mathbf{w}^S) &= \int_{\Omega_0^S} (\mathbf{f}^S - \mathbf{f}^F) \cdot \mathbf{w}^S \, d\mathbf{x} + \int_{\Omega_0^S} 2\mu^F \epsilon(\mathbf{v}_\varepsilon^k) : \epsilon(\mathbf{w}^S) \, d\mathbf{x} \\ &\quad - \int_{\Omega_0^S} (\nabla \cdot \mathbf{w}^S) p_\varepsilon^k \, d\mathbf{x} + \frac{1}{\varepsilon} \int_{\Omega_0^S} (\mathbf{v}_\varepsilon^k \circ \varphi_\varepsilon^k) \cdot \mathbf{w}^S \, d\mathbf{x} \quad \forall \mathbf{w}^S \in W^S \end{aligned}$$

where $\varphi_\varepsilon^k(\mathbf{X}) = \mathbf{X} + \mathbf{u}_\varepsilon^k(\mathbf{X})$.

Step 4. Stopping test: if $\|\mathbf{u}_\varepsilon^k - \mathbf{u}_\varepsilon^{k+1}\|_{0, \Omega_0^S} \leq tol$, then **Stop**.

Step 5. Compute the characteristic function $\chi_{u_\varepsilon^{k+1}}^S$, put $k := k + 1$ and **Go to Step 2**.

It is possible to consider Navier-Stokes equations for the fluid domain, then at the **Step 2** we have to solve a non-linear system. In this case we can use the non-linear penalization term for $\alpha \neq 2$. If we use a non-linear model for the structure, too, we have to use more accurate approximations for the the Jacobian determinant J and the gradient of the deformation \mathbf{F} .

4 Numerical tests

The numerical tests have been produced using the software *FreeFem++* [3].

4.1 Test 1. Shell in steady-state cross flow

First, we have performed numerical simulation using a 2D model adapted from [1] (see Figure 2) where we have changed the physical parameters of the fluid and of the structure.

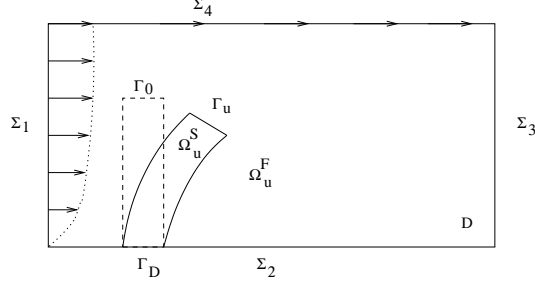


Fig. 2. Geometrical configuration for the Test 1.

The dimensions of a rectangular elastic structure are: height $\ell = 3$ m, thickness $h = 0.125$ m. The computational domain of the fluid D is a rectangle of height $H = 5$ m and length $L = 12$ m. The distance between the left side of the fluid and the left side of the structure is 2 m. The lower left corner of Figure 2 is $(x_1 = 0, x_2 = 0)$.

We denote by Σ_1, Σ_3 the left and the right vertical boundaries of D and by Σ_2, Σ_4 the bottom and the top boundaries of D , respectively.

The mechanical proprieties of the structure (polybutadiene) are: Young modulus $E^S = 1.6 \times 10^6$ N/m², Poisson's ratio $\nu^S = 0.49$, the applied volume forces on the structure $\mathbf{f}^S : \Omega_0^S \rightarrow \mathbb{R}^2$, $\mathbf{f}^S = (0, 0)$ N/m³.

The dynamic viscosity of the fluid (glycerin) is $\mu^F = 1.14$ N · s/m².

The inflow velocity profile on Σ_1 is

$$v_1(x_1, x_2) = V \times 1.5 \frac{(2Hx_2 - x_2^2)}{H^2} \text{ m/s}, \quad V = 1, \quad v_2(x_1, x_2) = 0.$$

The other boundary conditions are: $\mathbf{v} = \mathbf{0}$ (no-slip) on Σ_2 , $\mathbf{v} \cdot \mathbf{n}^F = 0$ (slip) on Σ_4 and $\mathbf{v} \times \mathbf{n}^F = 0$, $\mathbf{n}^F \cdot (\sigma^F(\mathbf{v}, p) \mathbf{n}^F) = 0$ (the tangential velocity and the normal traction are zero) on Σ_3 .

We use a fixed mesh for the fluid domain of 13096 triangles and 6719 vertices. The mesh of the structure domain has 188 triangles and 145 vertices. The fluid and structure meshes are not compatible, for example, a vertex on the structure boundary is not necessary a vertex on the fluid mesh. For the approximation of the fluid velocity and pressure we have employed the triangular finite elements $\mathbb{P}_1 + \text{bubble}$ and \mathbb{P}_1 respectively, also called “mini” finite elements. The finite element \mathbb{P}_1 was used in order to solve the structure problem. The characteristic function was approached by \mathbb{P}_0 finite elements.

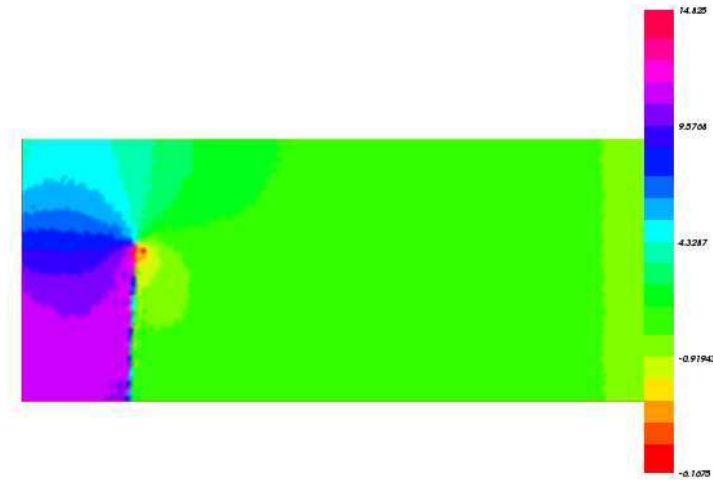


Fig. 3. The fluid pressure [Pa].

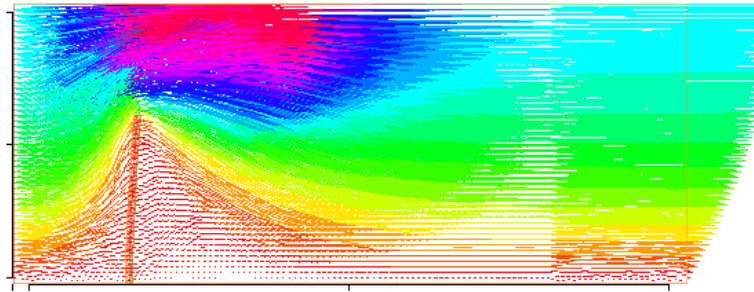


Fig. 4. The fluid velocity around the final position of the structure. In each point of the grid, there is an arrow giving the direction of the velocity and the length of the arrow is proportional to the euclidean norm of the velocity. The maximal value for the horizontal component v_1 is 2.82 m/s and for the vertical component v_2 is 1.18 m/s

We have performed the simulation using the **Algorithm** described in the previous section. For the stopping criterion at the **Step 4**, we have used the tolerance $tol = 0.2 \times 10^{-4}$. The penalization parameter is $\varepsilon = 10^{-3}$. The stopping criterion holds after 5 iterations of the fixed point algorithm. The maximal structural displacement is $0.14 m$.

The fluid velocity into the fictitious domain is very small

$$\|\mathbf{v}_\varepsilon\|_{0,\Omega_{u_\varepsilon}^S} = \sqrt{\int_D \chi_{u_\varepsilon}^S \mathbf{v}_\varepsilon \cdot \mathbf{v}_\varepsilon d\mathbf{x}} = 0.0703384.$$

4.2 Test 2. Flexible appendix in a flow

We have adapted the benchmark from [4]. Originally, the structure was placed horizontally, parallel to the flow, but the displacements in this case are very small. We have placed the structure vertically, transversely to the flow, see Figure 5.

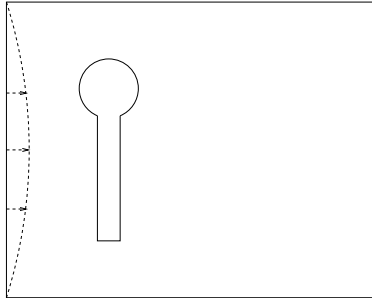


Fig. 5. Geometrical configuration.

The structure is composed by a rectangular flexible appendix attached to a fixed circle. The circle center is positioned at $(0.2, 0.2) m$ measured from the left top corner of the channel. The circle has the radius $r = 0.5 m$ and the rectangular appendix is of length $\ell = 0.35 m$, thickness $h = 0.02 m$. The Young modulus is $E^S = 1.6 \times 10^6 N/m^2$ and Poisson's ratio is $\nu^S = 0.49$ (polybutadiene).

The channel has the length $L = 2.5 m$ and the width $H = 0.75 m$. The fluid dynamic viscosity is $\mu^F = 1.420 N \cdot s/m^2$ (glycerin).

We have used the following boundary conditions: at the inflow the velocity is

$$v_1(x_1, x_2) = V \times 1.5 \frac{(H x_2 - x_2^2)}{(H/2)^2} m/s, \quad V = 1, \quad v_2(x_1, x_2) = 0;$$

at the bottom and the top we have imposed the no-slip boundary condition $\mathbf{v} = \mathbf{0}$ and at the outflow the traction free $\sigma^F(\mathbf{v}, p) \mathbf{n}^F = 0$.

We use a fixed mesh for the fluid domain of 30330 triangles and 15461 vertices and a structure mesh of 128 triangles and 97 vertices. We have employed the

same finite elements as for the Test 1. We have treated by the embedding domain technique only the flexible part of the structure.

The penalization parameter is $\varepsilon = 10^{-4}$ and for the stopping criterion $tol = 10^{-8}$. The fixed point algorithm stops after 8 iterations.

The maximal horizontal displacement of the structure is 0.10886 m . The pressure and the velocity of the fluid are presented in Figures 6 and 7. The fluid velocity in the fictitious domain is very small

$$\|\mathbf{v}_\varepsilon\|_{0,\Omega_{u_\varepsilon}^S} = \sqrt{\int_D \chi_{u_\varepsilon}^S \mathbf{v}_\varepsilon \cdot \mathbf{v}_\varepsilon \, d\mathbf{x}} = 0.080920.$$

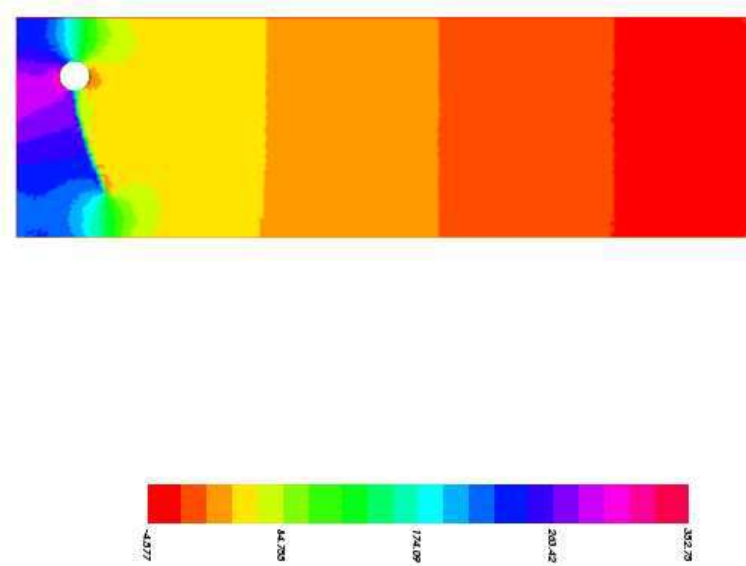


Fig. 6. The fluid pressure [Pa].

Conclusions

We have presented a fixed point algorithm for solving steady fluid-structure interaction problem. Using the embedding domain technique with penalization, the fluid equations as well as the structure equations are solved in fixed meshes. The fluid and structure meshes could be generated independently. The algorithm can be used for the three dimensions problems.

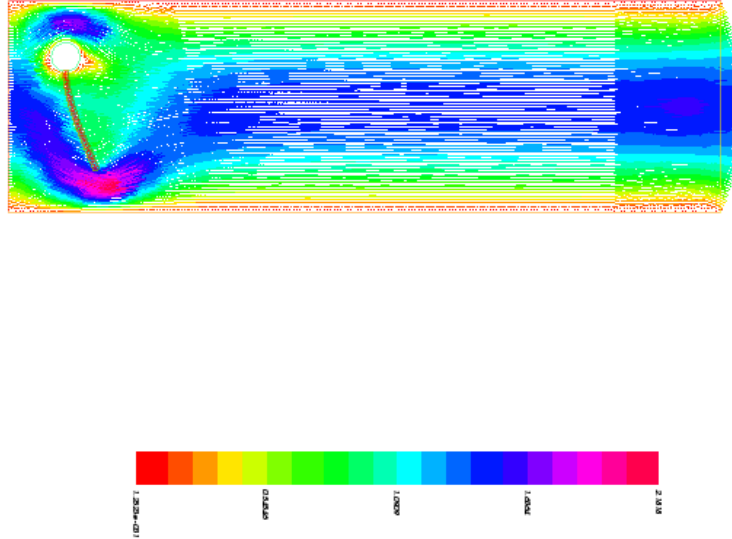


Fig. 7. The fluid velocity [m/s] around the final position of the structure. In each point of the grid, there is an arrow giving the direction of the velocity. The length of the arrow is proportional to the euclidean norm of the velocity which is represented in the color bar.

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