Abstract

Alias analysis is one of the most fundamental techniques that compilers use to optimize languages with pointers. However, in spite of all the attention that this topic has received, the current state-of-the-art approaches inside compilers still face challenges regarding precision and speed. In particular, pointer arithmetic, a key feature in C and C++, is yet to be handled satisfactorily. This paper presents a new alias analysis algorithm to solve this problem. The key insight of our approach is to combine alias analysis with symbolic range analysis. This combination lets us disambiguate fields within arrays and structs, effectively achieving more precision than traditional algorithms. To validate our technique, we have implemented it on top of the LLVM compiler. Tests on a vast suite of benchmarks show that we can disambiguate several kinds of C idioms that current state-of-the-art analyses cannot deal with. In particular, we can disambiguate 1.35x more queries than the alias analysis currently available in LLVM. Furthermore, our analysis is very fast: we can go over one million assembly instructions in 10 seconds.

Categories and Subject Descriptors D - Software [D.3 Programming Languages]: D.3.4 Processors - Compilers

General Terms Languages, Experimentation

Keywords Alias analysis, range analysis, speed, precision

1. Introduction

Pointer analysis is one of the most fundamental compiler technologies. This analysis lets the compiler distinguish one memory location from others; hence, it provides the necessary information to transform code that manipulates memory. Given this importance, it comes as no surprise that pointer analysis has been one of the most researched topics within the field of compiler construction [12]. This research has contributed to make the present algorithms more precise [10, 28], and faster [11, 22]. Nevertheless, one particular feature of imperative programming languages remains to be handled satisfactorily by the current state-of-the-art approaches: the disambiguation of pointer intervals.

Mainstream compilers still struggle to distinguish intervals within the same array. In other words, state-of-the-art pointer analyses often fail to disambiguate regions addressed from a common base pointer via different offsets, as explained by Yong and Horwitz [27]. Field-sensitive pointer analysis, provide a partial solution to this problem. These analyses can distinguish different fields within a record, such as a struct in C [17], or a class in Java [26]. However, they rely on syntax that is usually absent in the low level program representations adopted by compilers. Shape analyses [13, 21] can disambiguate subparts of data-structures such as arrays, yet their scalability remains an issue to be solved. Consequently, many compiler optimizations, such as...
loop transformations, tiling, fission, skewing and interchanging \cite{25} Ch.09, are very limited in practice. Therefore, we claim that, to reach their full potential, compilers need to be provided with more effective alias analyses.

This paper describes such an analysis. We introduce an abstract domain that associates pointers with symbolic ranges. In other words, for each pointer \( p \) we conservatively estimate the range of memory slots that can be addressed as an offset of \( p \). We let \( GR(p) \) be the global abstract address set associated with pointer \( p \), such that if \( lci \in GR(p) \) then \( p \) may dereference any address from \( lci + [l,u] \in @\{lci\}+u \), where \( loc_i \) is a program site that contains a memory allocation call, and \( @\{lci\} \) is the actual return address of the malloc at runtime. We let \( \{l,u\} \) be two symbols defined within the program code. Like the vast majority of pointer analyses available in the compiler literature, from Andersen’s work \cite{2} to the more recent technique of Zhang et al. \cite{23}, our method is correct if the underlying program is also correct. In other words, our results are sound with respect to the semantics of the program if this program has no undefined behavior, such as out-of-bounds accesses.

The key insight of this paper is the combination of pointer analysis with range analysis on the symbolic interval lattice. In a symbolic range analysis, ranges are defined as expressions of the program symbols, a symbol being either a constant or the name of a variable. There exist many approaches to symbolic range analyses in the literature \cite{4} \cite{15} \cite{19}. The algorithms that we present in this paper do not depend on any particular implementation. Nevertheless, the more precise the range analysis that we use, the more precise the analysis facts that we produce. In this work we have adopted the symbolic range analysis proposed in 1994 by William Blume and Rudolf Eigenmann \cite{4}.

To validate our ideas, we have implemented them in the LLVM compilation infra-structure \cite{14}. We have tested our pointer analysis onto three different benchmarks used in previous work related to pointer disambiguation: Prolangs \cite{20}, PrtDist \cite{29} and MallocBench \cite{9}. As we show in Section 4 our analysis is linear on the size of programs. It can go over one-million assembly instructions in approximately 10 seconds. Furthermore, we can disambiguate 1.35x more queries than the alias analysis currently available in LLVM.

2. Overview

We have two different ways to answer the following question: “do pointers \( tmp_i \) and \( tmp_j \) alias?” These tests are called global and local. In this section, we will use two different examples to illustrate situations in which each query is more effective. These distinct strategies are complementary: one is not a superset of the other.

Global pointer disambiguation. Figure 1 illustrates our first approach to disambiguate pointers. The figure shows a pattern typically found in distributed systems implemented in C. Messages are represented as arrays of bytes. In this particular example, messages have two parts: an identifier, which is stored in the beginning of the array, and a payload, which is stored right after. The loops in lines 5-8 and 9-12 fill up each of these parts with data. If a compiler can prove that the stores at lines 6 and 10 are always independent, then it can perform optimizations that would not be possible otherwise. For instance, it can parallelize the loops, or switch them, or merge them into a single body.

No alias analysis currently available in either gcc or LLVM is able to disambiguate the stores at lines 6 and 10. These analyses are limited because they do not contain range information. The range interval \([l,u]\) associated with a variable \( i \) is an estimate of the lowest \( (l) \) and highest \( (u) \) values that \( i \) can assume throughout the execution of the program. In this paper, we propose an alias analysis that solves this problem. To achieve this goal, we couple this alias analysis with range analysis on symbolic intervals \cite{4}. Thus, we will say that the store at line 6 might modify any address from \( p + 0 \) to \( p + N - 1 \), and that the store at line 10 might write on any address from \( p + N \) to \( p + N + strlen(m) - 1 \). For this purpose, we will use an abstract address that encodes the actual value(s) of \( p \) inside the prepare function. These memory addresses are depicted in Figure 2 where each \( \square \) represents a memory slot.

Whole program analysis reveals that there are two candidate locations that any pointer in the program may refer to. These locations have been created at lines 17 and 18 of Figure 1 and we represent them abstractly as loc17 and loc18. These names are unique across the entire program.


![Figure 2. Array p in the routine prepare seen in Fig.1. Lines 6 and 10 represent the different stores in the figure.](image)

1. **void accelerate**
2. 
3. 
4. 
5. 
6. 
7. 
8. 
9. 
10. 

Figure 3. Program that shows the need to assign common names to addresses that spring from the same base pointer.

1. **void accelerate**
2. 
3. 
4. 
5. 
6. 
7. 
8. 
9. 
10. 

Figure 4. Program from Figure 3 after pointer is renamed within loop.

After running our analysis, we find out that the abstract state (GR) of i at line 6 is GR(\(i_{f_{6,i}}\)) = \(\{loc_{i7} + [0, N - 1]\) and that the abstract state of i at line 10 is GR(\(i_{f_{10,n}}\)) = \(\{loc_{i7} + [N, N + strlen(m) - 1]\). Given that these two abstract ranges do not intersect, we know that the two stores update always different locations. We call this check the **global disambiguation criterion**.

**Local pointer disambiguation.** Figure 3 shows a program in which the simple intersection of ranges would not let us disambiguate pointers temp0 and tmp1. After solving global range analysis for that program, we have that GR(temp0) = \(\{loc_{0} + [0, N + 1]\) and that GR(tmp1) = \(\{loc_{0} + [1, N + 2]\), where loc0 defines the abstract address of the function parameter p. The intersection of these ranges is non-empty for \(N \geq 1\). Thus, the global check that we have used to disambiguate locations in Figure 1 does not work in Figure 3. Notwithstanding this fact, we know that temp0 and tmp1 will never point to a common location. In fact, these pointers constitute different offsets from the same base address. To deal with this imprecision of the global check, we will be also discussing a local disambiguation criterion.

3. Combining Range and Pointer Analyses

We perform our pointer analysis in several steps. Figure 5 shows how each of these phases relates to each other. Our final product is a function that, given two pointers, \(p_0\) and \(p_1\), tells if they may point to overlapping areas or not. An invocation of this function is called a **query**. We use an off-the-shelf symbolic range analysis, e.g., à la Blume [4], to bootstrap our pointer analysis. By inferring the symbolic ranges of pointers, we have two alias tests: the global and the local approach. In the rest of this section we describe each one of these contributions.

3.1 A Core Language

We solve range analysis through abstract interpretation. To explain how we abstract each instruction in our intermediate representation, we shall use the language seen in Figure 6 henceforth, we shall call this syntax our **core language**. We shall be working on programs in Extended Static Single Assignment (e-SSA) form [5]. E-SSA form is a flavor of Static Single Assignment (SSA) [6] form, with variable renaming after inequalities. Thus, our core language contains \(\phi\)-functions to ensure the single definition (SSA) property, and intersections to rename variables after conditionals. We assume that \(\phi\)-functions have only two arguments. Generalizing this notation to \(n\)-ary functions is immediate.
Figure 6. The syntax of our language of pointers.

Figure 7. Control flow graph of program seen in Figure 1.

The implementation of the analysis that we shall present in this paper is interprocedural, albeit not context-sensitive. To achieve interprocedurality, we associate actual parameters with formal parameters of functions. In the example of Figure 1, pointer \( b \) – an actual parameter – is linked with \( p \) – a formal parameter – through a \( \phi \)-function.

The e-SSA format lets us implement our analysis sparsely, e.g., we can assign information directly to variables, instead of pairs of variables and program points. As demonstrated by Choi et al. [6], the main advantage of a sparse analysis is efficiency: the product of the analysis - the information that is bound to each variable - requires \( O(N) \) space, where \( N \) is the number of variable names in the program. Furthermore, as we shall explain in the rest of this section, our analysis can be computed in \( O(N) \) time.

Key to these good properties is the fact that we create new variable names at each program point where our analysis can infer new information. This knowledge appears due to memory allocation (malloc), deallocation (free), pointer arithmetic, intersections and \( \phi \)-functions. Each of these instructions defines new variables, whose names are associated with information. For instance, the instruction \( p_0 = \text{free}(p_1) \) copies \( p_1 \) to \( p_0 \), and binds \( p_0 \) to a memory chunk of size 0. As we will show in Section 3.4, our abstract interpreter associates with \( p_0 \) a new abstract state which indicates that \( p_0 \) is not a valid reference to any location.

3.3 Symbolic Range Analysis.

We start our pointer analysis by running an off-the-shelf range analysis parameterized on symbols. For the sake of completeness, we shall revisit the main notions associated with range analysis, which we borrow from Nazaré et al. [15]. We say that \( E \) is a symbolic expression, if and only if, \( E \) is defined by the grammar below. In this definition, \( s \) is a symbol and \( n \in \mathbb{N} \). The set of symbols \( s \) in a program form its symbolic kernel. The symbolic kernel is formed by names that cannot be represented as function of other names in the program text. Concretely, this set contains the names of global variables and variables assigned with values returned from library functions.

\[
E ::= n \mid s \mid \min(E, E) \mid \max(E, E) \mid E - E \mid E + E \mid E/E \mid E \mod E \mid E \times E
\]

We shall be performing arithmetic operations over the partially ordered set \( S = S_E \cup \{-\infty, +\infty\} \), where \( S_E \) is the set of symbolic expressions. The partial ordering is given by \(-\infty < \ldots < -2 < -1 < 0 < 1 < 2 < \ldots +\infty \). There exists no ordering between two distinct elements of the symbolic kernel of a program. For instance, \( N < N + 1 \) but there is no relationship between an expression containing \( N \) and another expression containing \( M \).

A symbolic interval is a pair \( R = [l, u] \), where \( l \) and \( u \) are symbolic expressions. We denote by \( R_l \) the lower bound \( l \) and \( R_r \) the upper bound \( u \). We define the partially ordered set of (symbolic) intervals \( S^2 = (S \times S, \sqsubseteq) \), where the ordering operator is defined as:

\[
[l_0, u_0] \sqsubseteq [l_1, u_1], \text{ if } l_1 \leq l_0 \wedge u_1 \geq u_0
\]

From the previous definitions, we define the semi-lattice \( \text{SymbRanges} \) of symbolic intervals as \((S^2, \sqsubseteq, \sqcup, \emptyset, [-\infty, +\infty])\), where the join operator “\( \sqcup \)” is defined as:

\[
[a_1, a_2] \sqcup [b_1, b_2] = [\min(a_1, b_1), \max(a_2, b_2)]
\]

Our lattice has a least element \( \emptyset \), such that:

\[
\emptyset \sqcup [l, u] = [l, u] \sqcup \emptyset = [l, u]
\]
and a greatest element \([-\infty, +\infty]\), such that:
\[
[-\infty, +\infty] \sqcup [l, u] = [l, u] \sqcup [-\infty, +\infty] = [-\infty, +\infty]
\]

For sake of clarity, we also define the intersection operator \(\sqcap\):
\[
[a_1, a_2] \sqcap [b_1, b_2] = \begin{cases} 
\emptyset, & \text{if } a_2 < b_1 \text{ or } b_2 < a_1 \\
\{ \min(a_1, b_1), \max(a_2, b_2) \}, & \text{otherwise}
\end{cases}
\]

\([-\infty, +\infty]\) is absorbant and \(\emptyset\) is neutral for \(\sqcap\).

The result of range analysis is a function \(R : V \mapsto S^2\), that maps each integer variable \(i\) in a program to an interval \([l, u], l \leq u\), e.g., \(R(i) = [l, u]\). The more precise the technique we use to produce this result, the more precise our results will be. Nevertheless, the exact implementation of the range analysis is immaterial for the formalization that follows. In this paper, we are using the following widening operator on \(\text{SymbRanges}\):
\[
[l, u] \vee [l', u'] = \begin{cases} 
[l, u'] & \text{if } l = l' \text{ and } u = u' \\
[l, +\infty) & \text{if } l = l' \text{ and } u' > u \\
[l', u] & \text{if } l < l' \text{ and } u = u' \\
[-\infty, u] & \text{if } l < l' \text{ and } u' > u \\
[-\infty, +\infty] & \text{if } l' < l \text{ and } u' > u
\end{cases}
\]

The only requirement that we impose on the implementation of range analysis is that it exists over \(\text{SymbRanges}\), our lattice of symbolic intervals. We denote by \((\text{\alpha(SymbRanges)}, \text{\gamma(SymbRanges)})\) the underlying galois connection.

**Example 2.** A range analysis such as Nazaré et al.’s \([13]\), if applied onto the program seen in Figure 3, will give us that \(R(i_{\text{line} \ 3}) = [0, 0], R(i_{\text{line} \ 5}) = [0, N - 1], R(i_{\text{line} \ 7}) = [0, N + 1].\)

### 3.4 Global Range Analysis of Pointers

As we have mentioned in Section 2 we use two different strategies to disambiguate pointers: the global and the local test. Our global pointer analysis goes over the entire code of the program, associating variables that have the pointer type with elements of an abstract domain that we will define soon. The local analysis, on the other hand, works only for small regions of the program text. We shall discuss the local test in Section 3.5. In this section, we focus on the global test, which is an abstract-interpretation based algorithm.

**An Abstract Domain of Pointer Locations.** We associate pointers with tuples of size \(n\) of \(\text{SymbRanges} \cup \bot^n\); \(n\) being the number of program sites where memory is allocated (the cardinal of \(\text{Loc}\)) and \(\bot\) is the disjoint union.

Let \(\text{\@}(\text{loc}_i)\) denotes the actual address value returned by the \(i^{th}\) malloc of the program. By construction, all actual addresses are supposed to be offsets of a given \(\text{\@}(\text{loc}_i)\). The abstract value \(\text{GR}(p) = (p_0, \ldots, p_{n-1})\) represents (an abstract version) of the set of memory locations that pointer variable \(p\) can address throughout the execution of a program:

**Definition 1 (Abstraction).** A set of actual addresses, \(S = \{ s \mid \exists i \in \mathbb{N}, d \in \mathbb{Z}, s = \text{\@}(\text{loc}_i) + d \}\) is abstracted by \(\text{GR}(S) = (p_0, p_1, \ldots, p_{n-1}) \) where:

- \(p_i = \bot\) if there is no address in \(S\) which is an offset of \(\text{\@}(\text{loc}_i)\)
- \(p_i = \alpha \text{SymbRanges}(\{ d \in \mathbb{Z} \mid s = \text{\@}(\text{loc}_i) + d \in S \})\), otherwise. The offsets from a given pointer are abstracted altogether in the \(\text{SymbRanges}\) lattice.

The goal of our GR analysis is to compute such an abstract value for each pointer of the program. Some elements in a tuple \(\text{GR}(p)\) are bound to the undefined location, e.g., \(\bot\). These elements are not interesting to us, as they do not encode any useful information. Thus, to avoid keeping track of them, we rely on the concept of support, which we state in Definition 2.

**Definition 2 (Support).** We denote by \(\text{supp}_{\text{GR}}(p)\) the set of indexes for which \(p_i\) is not \(\bot\):

\[
\text{supp}_{\text{GR}}(p) = \{ i \mid p_i \neq \bot \}.
\]

For sake of readability, let us denote for instance \(\text{GR}(p) = (\bot, [1, u_1], \bot, [l_3, u_3], \bot)\), by the set \(\text{GR}(p) = \{ \text{loc}_1 + [l_1, u_1], \text{loc}_3 + [l_3, u_3] \}\). In the concrete world, this notation will mean that pointer \(p\) can address any memory location from \(\text{\@}(\text{loc}_1) + l_1\) to \(\text{\@}(\text{loc}_1) + u_1\), and from \(\text{\@}(\text{loc}_3) + l_3\) to \(\text{\@}(\text{loc}_3) + u_3\).

For instance, consider that \(l_1 = 3, u_1 = 5, l_3 = 3\) and \(u_3 = 8\). \(\text{GR}(p) = \{ \text{loc}_1 + [3, 5], \text{loc}_3 + [3, 8] \}\) is then depicted in Figure 8.

Now for the abstract operations: \((\bot, \ldots, \bot)\) is the least element of our lattice, and \(([-\infty, \infty], \ldots, [-\infty, \infty])\) the greatest one.

Given the two abstract values \(\text{GR}(p^1) = (p_0^1, \ldots, p_{n-1}^1)\) and \(\text{GR}(p^2) = (p_0^2, \ldots, p_{n-1}^2)\), the union \(\text{GR}(p^1) \sqcup \text{GR}(p^2)\) is the tuple \((q_0, \ldots, q_{n-1})\) where:

\[
q_i = \begin{cases} 
\bot & \text{if } p_i^1 = p_i^2 = \bot \\
 p_1 \sqcup p_2 & \text{else}
\end{cases}
\]

and \(\text{GR}(p^1) \subseteq \text{GR}(p^2)\) if an only if all involved (symbolic) intervals of \(p^1\) are included in the ones of \(p^2\); \(\forall i \in [0, (n - 1)], p_i^1 \subseteq p_i^2\) (considering \(\bot \subseteq R\) and \(\bot \sqcup R = R\) for all non-empty intervals \(R\)). We call this structure, formed by \((\text{SymbRanges} \cup \bot)^n\) plus its partial ordering the lattice MemLocs.
Example 3. For the example depicted in Figure 7 where we only have two malloc sites denoted by $\text{loc}_0$ and $\text{loc}_1$, we will obtain the following results: $\text{GR}(p) = \text{GR}(b) = (\{\text{loc}_0 + [0, 0]\}, \{\text{loc}_1 + [0, 0]\})$. $\text{GR}(m_0) = \text{GR}(s) = (\{\text{loc}_1 + [0, 0]\})$. $\text{GR}(e) = \{\text{loc}_0 + [N, N]\}$, $\text{GR}(m_1) = \{\text{loc}_1 + [1, +\infty]\}$, $\text{GR}(i_7) = \{\text{loc}_0 + [N + \text{strlen}(m_0), N + \text{strlen}(m_0) + 1]\}$. How this mapping is found is discussed in the rest of this section.

Abstract semantics for GR, and concretisation. The abstract semantics of each instruction in our core language is given by Figure 9. Abstract semantics for GR, and concretisation. The abstract interpretation framework, we solve our system of constraints by computing for each pointer a growing set of abstract values until convergence. However, as the underlying lattice SymbRanges has infinite height, widening is necessary to ensure that these sequence of iterations actually terminate. Our widening operation on pointers generalizes the widening operation on ranges. It is defined as follows:

\[ \text{GR}(p) \downarrow \text{GR}(p') \subseteq \text{GR}(p) \]

where $\downarrow$ denotes the widening on SymbRanges, extended with $\bot$ and $\bot$.

As usual, we only apply the widening operator on a cut set of the control flow graphs (here, only on $\phi$ functions).

Widening may lead our interpreter to produce very imprecise results. To recover part of this imprecision, we use a descending sequence of finite size: after convergence, we redo a step of symbolic evaluation of the program, starting from the value obtained after convergence. One example of analysis will be detailed later, in Section 3.9.

The abstract interpretation of loads and stores. In Figure 9 we chose not to track precisely the intervals associated with pointers stored in memory. In other words, when interpreting stores, e.g., $q = *p$, we assign the top value of our lattice to $q$. This decision is pragmatic. As we shall explain in Section 4, a typical compilation infrastructure already contains analyses that are able to track the propagation of pointer information throughout memory. Our goal is not to solve this problem. We want to deliver a fast analysis that is precise enough to handle C-style pointer arithmetic.

3.5 Answering GR Queries

Our queries are based on the following result, that is an immediate consequence of the fact our analysis is an abstract interpretation:

Proposition 2 (Correctness). Let $p$ and $p'$ be two pointers in a given program then:

\[ \text{if } \supp_{\text{GR}}(p) \cap \supp_{\text{GR}}(p') = \emptyset \]

\[ \text{or } \forall i \in \supp_{\text{GR}}(p) \cap \supp_{\text{GR}}(p'), p_i \cap p'_i = \emptyset \]

While speaking about symbolic ranges, we also have to concretize the values involved in the bounds of $p_i$, that is we shall use the actual values between $S(p_i)$ and $S(p'_i)$.
3.6 Local Range Analysis of Pointers

The global pointer analysis is not path sensitive. As a consequence, this analysis cannot, for instance, distinguish the effects of different iterations of a loop upon the actual value of a pointer, or the effects of different branches of a conditional test on that very pointer. The program in Figure 10 illustrates this issue. Pointers  and  do not alias. Yet, their abstract states have non-empty intersections for pointers .

To solve this problem, we have developed a local version of our pointer analysis. We call it local because it creates new locations for every of our pointer analysis. We call it local because it creates new locations for every

instructions of our core language. Instructions are evaluated

then  .

In other words, if the abstract values of two different pointers of the program have a null intersection, then the two concrete pointers do not alias. This result is directly implied by the abstract interpretation framework. Thanks to this result, we implement the query as:

- If  and  have an empty intersection, then “they do not alias”.
- Else “they may alias”.

3.7 Answering LR Queries

The correction for the local analysis is stated by the following proposition:

PROPOSITION 3 (Correctness). Let  and  be two pointers in a given program, and  be the concretization of the abstract map LR, which we state like in Definition 3. If

then . In other words,  and  never alias.

Thanks to this result, we implement the query as:

- If  and  have a common base pointer with ranges that do not intersect, then “they do not alias”.
- Else “they may alias”.

3.8 Complexity

The e-SSA representation ensures that we can implement our analysis sparsely. Sparsity is possible because the e-SSA form renames variables at each program point, where new abstract information, e.g., ranges of integers and pointers, arises. According to Tavares et al. [24], this property – single information – is sufficient to enable sparse implementation of non-relational static analyses [24]. Therefore, the abstract state of each variable is invariant along the entire live range of that variable. Consequently, the space complexity of our static analysis is , where  is the set of names of variables in the program in e-SSA form, and  is a measure of the size of the information that can be bound to each variable.

We apply widening after one iteration of abstract interpretation. Thus, we let the state of a variable to change first
from \([\bot, \bot]\) to \([s_l, s_u]\), where \(s_l \neq -\infty\), and \(s_u \neq +\infty\). From there, we can reach either \([-\infty, s_u]\) or \([s_l, +\infty]\). And, finally, this abstract state can jump to \([-\infty, +\infty]\). Hence, our time complexity is \(O(3 \times |V|) = O(|V|)\). This observation also prevents our algorithm from generating expressions with very long chains of “min” and “max” expressions. Therefore, \(I\), the amount of information associate with a variable, can be represented with \(O(1)\) space. As a consequence of this fragility, our static analysis runs in \(O(|V|)\) time, and requires \(O(|V|)\) space.

### 3.9 A wrap-up Example

Example 4 shows how our analysis works on the program seen in Figure 1.

**Example 4.** Figure 7 shows the control flow graph (CFG) of the program in Figure 1. Our graph is in e-SSA form. Figure 7 shows the result of widening ranges after one round of abstract interpretation (stabilization achieved), and a descending sequence of size two. Our system stabilizes after each instruction is visited four times. The first visit does initialization, the second widening (and stabilization check), and the last two build the descending sequence.

This example illustrates the need of widening to ensure termination. Our program has a cycle of dependencies between pointers \(i_1\), \(i_2\), and \(i_3\). If not for widening, pointer \(i_3\), incremented in line 5 of Figure 1, would grow forever. Thus, as in Abstract Interpretation, we must break the cyclic dependencies between our pointers under analysis, by means of insertion of widening points (identify points in the CFG where to apply widening to insure convergence).

Returning to our example of Figure 1, we are interested in knowing, for instance, that the memory access at line 6 is independent on the accesses that happen at line 10. To achieve this goal, we must bound the memory regions covered by pointers \(i_3\) and \(i_7\). A cyclic dependence happens at the operation \(i++\), because in this case, we have a pointer being used as both, source and destination of the update. Thus, we should have inserted a widening point at stores and load instructions. However, in the Abstract Interpreter depicted in Figure 2, it was sufficient to insert widening points at \(\phi\) functions (as we already said before) because:

- heads of loops are \(\phi\) functions (thus dependencies between variables of different iteration of loops are broken).
- we are working on (e-)SSA form programs; thus, the only inter-loop dependencies are successive stores to the same variable: \(*q=\ldots, *q=\ldots\). The value \(GR(q)\) is the union of all information gathered inside the loop. (In essence, memory addresses are not in static single assignment form, i.e., we could have the same address being used as the target of a store multiple times). This information might grow forever; hence, we would have inserted a widening point on the last write. In our case, the information we store is already the top of our lattice; hence, there is no need for widening.

### 4. Experiments

We have implemented our range analysis in the LLVM compiler, version 3.5. In this section, we show a few numbers that we have obtained with this implementation. All our experiments have been performed on an Intel i7-4770K, with 8GB of memory, running Ubuntu 14.04.2. Our goal with these experiments is to show: (i) that our alias analysis is more precise than other alternatives of practical runtime; and (ii) that it scales up to large programs.

**On the Precision of our Analysis.** In this section, we compare our analysis against the other pointer analyses that are available in LLVM 3.5, namely basic and SCEV. The first of them, although called “basic”, is currently the most effective alias analysis in LLVM, and is the default choice at the -O3 optimization level. It relies on a number of heuristics to disambiguate pointer.

![Figure 12. Abstract interpretation of CFG seen in Figure 7](http://llvm.org/docs/AliasAnalysis.html)
• Distinct globals, stack allocations, and heap allocations can never alias.
• Globals, stack allocations, and heap allocations never alias the null pointer.
• Different fields of a structure do not alias.
• Indexes into arrays with statically differing subscripts cannot alias.
• Many common standard C library functions never access memory or only read memory.
• Function calls cannot reference stack allocations which never escape from the function that allocates them.

As we see from the above list, the basic alias analysis has some of the capabilities of the technique that we present in this paper, namely the ability to distinguish fields and indices within aggregate types. In this case, such disambiguation is only possible when the aggregates are indexed with constants known at compilation time. For situations when these indices are symbols, LLVM relies on a second kind of analysis to perform the disambiguation: the "scalar-evolution-based" (SCEV) alias analysis. This analysis tries to infer closed-form expressions to the induction variables used in loops. For each loop such as:

\[
\text{for (i = B; i < N; i += S) \{ ... a[i] ... \}}
\]

this analysis associates variable \(i\) with the expression \(i = B + \text{iter} \times S, i \leq N\). The parameter \text{iter}\ represents the current iteration of the loop. With this information, SCEV can track the ranges of indices which dereference array within the loop. Contrary to our analysis, SCEV is only effective to disambiguate pointers accessed within loops and indexed by variables in the expected closed-form.

Figure 13 shows how the three different analyses fare when applied on larger benchmarks. For this experiment we have chosen three benchmarks that have been used in previous work that compares pointer analyses: Prolangs \[20\], PrrDist \[29\] and MalloclBench \[9\]. We first notice that in general all the pointer analyses in LLVM disambiguate a relatively low number of pointers. This happens because many pointers are passed as arguments of functions, and, not knowing if these functions will be called from outside the program, the analyses must, conservatively, assume that these parameters may alias. Second, we notice that our pointer analysis is one order of magnitude more precise than the scalar-evolution based implementation available in LLVM. Finally, we notice that we are able to disambiguate more queries than the basic analysis. Furthermore, our results complements it in non-trivial ways. In total, we tried to disambiguate 3.093 million pairs of pointers. Our analysis found out that 1.29 million pairs reference non-overlapping regions; however, not at the same moment during the execution of the program. The two columns \textit{noalias} of Figure 14 correspond to the percentage of queries that have disambiguated and the \textit{basic} alias analysis of LLVM. Numbers in \textit{scev}, \textit{basic}, \textit{rbaa} and \textit{r+b} show percentage of queries that answer "no-alias".
5. Related Work

The contribution of this work is a new representation of pointers, based on the SymbRanges lattice, and an algorithm to reach a fixed point in this lattice, based on abstract interpretation. This contribution complements classic work on pointer analysis. In other words, our representation of pointers can be used to enhance the precision of algorithms such as Steensgaard’s [23], Andersen’s [2], or even the state-of-the-art technique of Hardekopf and Lin [11]. These techniques map pointers to sets of locations, but they could be augmented to map pointers to sets of locations plus ranges. Furthermore, the use of our approach does not prevent the employment of acceleration techniques such as lazy cycle detection [10], or wave propagation [18].

There exist previous work that used similar lattices as ours, albeit different resolution algorithms. For instance, much of the work on automatic parallelization has some way to associate symbolic offsets, usually loop bounds, with pointers. Michael Wolfe [25, Ch.7] and Aho et al. [1, Ch.11] have entire chapters devoted to this issue. The key difference between our work and this line of research is the algorithm to solve pointer relations: they resort to integer linear programming (ILP) or the Greatest Common Divisor test to solve diophantine equations, whereas we do abstract interpretation. Even Rugina and Rinard [19], who we believe is the state-of-the-art approach in the field today, use integer linear programming to solve symbolic relations between variables. We speculate that the ILP approach is too expensive to be used in large programs; hence, concessions must be made for the sake of speed. For instance, whereas the previous literature that we know restrict their work to pointers within loops, we can analyze programs with over one million assembly instructions in a few seconds.

There exist work that, like ours, also associates intervals with pointers, and solves static analysis via abstract interpretation techniques. However, to the best of our knowledge, these approaches have a fundamental difference to our work: they use integer intervals à la Cousot [7], whereas we use symbolic intervals. The inspiration for much of this work springs from Balakrishnan and Reps notion of Value Set Analysis [3]. Integer intervals have also being used by Yong et al. [27] and, more recently, by Oh et al. [16]. In the latter case, Oh et al. use pointer disambiguation incidentally, to demonstrate their ability to implement efficiently static analyses in a context-sensitive way. Even though integer ranges fit well the need of machine code, as demonstrated by Balakrishnan and Reps, we believe that further precision requires more expressive lattices. We have not implemented value set analysis, but we have tried a simple experiment: we counted the number of pointers that have integer ranges, and compared this number against the quantity of pointers that have symbolic ranges. We found out that 20.47% of the pointers in our three benchmark suites have exclusively symbolic ranges. Classic range analysis would not be able to distinguish them. Notice that numeric ranges are more common among pointer variables than among integer, because fields within structs – a very common construct in C – are indexed through integers. Finally, the fact that we use...
Bodik’s e-SSA form \[5\] distinguish our abstract interpretation algorithm from previous work. This representation lets us solve our analysis sparsely, whereas Balakrishnan’s algorithm works on a dense representation that associates facts with pairs formed by variables and program points.

6. Conclusion

In this paper we have presented a new alias analysis technique that handles, within the same theoretical framework, the subtleties of pointer arithmetic and memory indexation. Our technique can disambiguate regions within arrays and C-like structs using the same abstract interpreter. We have achieved precision in our algorithm by combining alias analysis with classic range analysis on the symbolic domain. Our analysis is fast, and handles cases that the implementations of pointer analyses currently available in LLVM cannot deal with. In future work, we plan to investigate better splitting strategies and other more expressive lattices to improve the global precision of our analyses.

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