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Multichannel audio source separation with deep neural networks

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Abstract—This article addresses the problem of multichannel audio source separation. We propose a framework where deep neural networks (DNNs) are used to model the source spectra and combined with the classical multichannel Gaussian model to exploit the spatial information. The parameters are estimated in an iterative expectation-maximization (EM) fashion and used to derive a multichannel Wiener filter. We present an extensive experimental study to show the impact of different design choices on the performance of the proposed technique. We consider different cost functions for the training of DNNs, namely the probabilistically motivated Itakura-Saito divergence, and also Kullback-Leibler, Cauchy, mean squared error, and phase-sensitive cost functions. We also study the number of EM iterations and the use of multiple DNNs, where each DNN aims to improve the spectra estimated by the preceding EM iteration.

Finally, we present its application to a speech enhancement problem. The experimental results show the benefit of the proposed multichannel approach over a single-channel DNN-based approach and the conventional multichannel nonnegative matrix factorization based iterative EM algorithm.

Index Terms—Audio source separation, speech enhancement, multichannel, deep neural network (DNN), expectation-maximization (EM).

I. INTRODUCTION

AUDI O source separation aims to recover the signals of underlying sound sources from an observed mixture signal. Recent research on source separation can be divided into (1) speech separation, in which the speech signal is recovered from a mixture containing multiple background noise sources with possibly interfering speech; and (2) music separation, in which the singing voice and possibly certain instruments are recovered from a mixture containing multiple musical instruments. Speech separation is mainly used for speech enhancement in hearing aids or noise robust automatic speech recognition (ASR), while music separation has many interesting applications, including music editing/remixing, up-mixing, music information retrieval, and karaoke [1]–[5].

Recent studies have shown that deep neural networks (DNNs) are able to model complex functions and perform well on various tasks, notably ASR [6], [7]. More recently, DNNs have been applied to single-channel speech enhancement and shown to provide a significant increase in ASR performance compared to earlier approaches based on beamforming or non-negative matrix factorization (NMF) [8]. The DNNs typically operate on magnitude or log-magnitude spectra in the Mel domain or the short time Fourier transform (STFT) domain. Various other features have been studied in [9]–[11]. The DNNs can be used either to predict the source spectrograms [11]–[16] whose ratio yields a time-frequency mask or directly to predict a time-frequency mask [10], [17]–[21]. The estimated source signal is then obtained as the product of the input mixture signal and the estimated time-frequency mask. Various DNN architectures and training criteria have been investigated and compared [19], [21], [22]. Although the authors in [15] considered both speech and music separation, most studies focused either on speech separation [10]–[12], [14], [17]–[21] or on music separation [13], [16].

As shown in many works mentioned above, the use of DNNs for audio source separation by modeling the spectral information is extremely promising. However, a framework to exploit DNNs for multichannel audio source separation is lacking. Most of the approaches above considered single-channel source separation, where the input signal is either one of the channels of the original multichannel mixture signal or the result of delay-and-sum (DS) beamforming [19]. Efforts on exploiting multichannel data have been done by extracting multichannel features and using them to derive a single-channel mask [10], [11]. As a result, they do not fully exploit the benefits of multichannel data as achieved by multichannel filtering [1], [4].

In this article, we propose a DNN-based multichannel source separation framework where the source spectra are estimated using DNNs and used to derive a multichannel filter using an iterative EM algorithm. The framework is built upon the state-of-the-art iterative EM algorithm in [23] which integrates spatial and spectral models in a probabilistic fashion. This model was used up to some variants in [24]–[28]. We study the impact of different design choices on the performance, including the cost function used for the training of DNNs and the number of EM iterations. We also study the impact of the spatial information by varying the number of spatial parameter updates and the use of multiple DNNs to improve the spectra over the iterations. We present the application of the proposed framework to a speech enhancement problem.

This work extends our preliminary work in [29] by following the exact EM algorithm in [24], instead of its variant in [28] and by reporting extensive experiments to study the impact of different design choices not only on the speech
recognition performance, but also on the source separation performance.

The rest of this article is organized as follows. Section II describes the iterative EM algorithm for multichannel source separation, which is the basis for the proposed DNN-based iterative algorithm described in Section III. Section IV shows the effectiveness of the framework for a speech separation problem and the impact of different design choices. Finally, Section V concludes the article and presents future directions.

II. BACKGROUND

In this section, we briefly describe the problem of multichannel source separation and the iterative EM algorithm in [23], [24], which is the basis for the proposed DNN-based multichannel source separation algorithm.

A. Problem formulation

Following classical source separation terminology [5], let \( I \) denote the number of channels, \( J \) the number of sources, \( \mathbf{c}_j(t) \in \mathbb{R}^{I \times 1} \) the \( I \)-channel spatial image of source \( j \), and \( \mathbf{x}(t) \in \mathbb{R}^{I \times 1} \) the observed \( I \)-channel mixture signal. Both \( \mathbf{c}_j(t) \) and \( \mathbf{x}(t) \) are in the time domain and related by

\[
\mathbf{x}(t) = \sum_{j=1}^{J} \mathbf{c}_j(t).
\]  

(1)

Source separation aims to recover the source spatial images \( \mathbf{c}_j(t) \) from the observed mixture signal \( \mathbf{x}(t) \).

B. Model

Let \( \mathbf{x}(f, n) \in \mathbb{C}^{I \times 1} \) and \( \mathbf{c}_j(f, n) \in \mathbb{C}^{I \times 1} \) denote the short-time Fourier transform (STFT) coefficients of \( \mathbf{x}(t) \) and \( \mathbf{c}_j(t) \), respectively, for frequency bin \( f \) and time frame \( n \). Also, let \( F \) be the number of frequency bins and \( N \) the number of time frames.

We assume that \( \mathbf{c}_j(f, n) \) are independent of each other and follow a multivariate complex-valued zero-mean Gaussian distribution [23], [24], [27], [30]

\[
\mathbf{c}_j(f, n) \sim \mathcal{N}_c(0, v_j(f, n)\mathbf{R}_j(f)),
\]  

(2)

where \( v_j(f, n) \in \mathbb{R}_+ \) denotes the power spectral density (PSD) of source \( j \) for frequency bin \( f \) and time frame \( n \), and \( \mathbf{R}_j(f) \in \mathbb{C}^{I \times I} \) is the spatial covariance matrix of source \( j \) for frequency bin \( f \). This \( I \times I \) matrix represents spatial information by encoding the spatial position and the spatial width of the corresponding source [23]. Since the mixture \( \mathbf{x}(f, n) \) is the sum of \( \mathbf{c}_j(f, n) \), it is consequently distributed as

\[
\mathbf{x}(f, n) \sim \mathcal{N}_c\left(0, \sum_{j=1}^{J} v_j(f, n)\mathbf{R}_j(f)\right).
\]  

(3)

Given the PSDs \( v_j(f, n) \) and the spatial covariance matrices \( \mathbf{R}_j(f) \) of all sources, the spatial source images can be estimated in the minimum mean square error (MMSE) sense using multichannel Wiener filtering [23], [27]

\[
\hat{\mathbf{c}}_j(f, n) = \mathbf{W}_j(f, n)\mathbf{x}(f, n),
\]  

(4)

where the Wiener filter \( \mathbf{W}_j(f, n) \) is given by

\[
\mathbf{W}_j(f, n) = v_j(f, n)\mathbf{R}_j(f) \left( \sum_{j' = 1}^{J} v_{j'}(f, n)\mathbf{R}_{j'}(f) \right)^{-1}.
\]  

(5)

Finally, the time-domain source estimates \( \hat{\mathbf{c}}_j(t) \) are recovered from \( \hat{\mathbf{c}}_j(f, n) \) by inverse STFT.

Following this formulation, source separation becomes the problem of estimating the PSD and the spatial covariance matrices of each source. This can be achieved using an EM algorithm.

C. General iterative EM framework

The general iterative EM algorithm is summarized in Algorithm 1. It can be divided into the E-step and the M-step. The estimated PSDs \( v_j(f, n) \) are initialized in the spectrogram initialization step, for instance by computing the PSD of the mixture, while the estimated spatial covariance matrices \( \mathbf{R}_j(f) \) can be initialized by \( I \times I \) identity matrices. In the E-step, given the estimated parameters \( v_j(f, n) \) and \( \mathbf{R}_j(f) \) of each source, the source image estimates \( \hat{\mathbf{c}}_j(f, n) \) are obtained by multichannel Wiener filtering (4) and the posterior second-order raw moments of the spatial source images \( \hat{\mathbf{R}}_j(f, n) \) are computed as

\[
\hat{\mathbf{R}}_j(f, n) = \hat{\mathbf{c}}_j(f, n)\hat{\mathbf{c}}_j^H(f, n)
\]

\[
+ (I - \mathbf{W}_j(f, n)) v_j(f, n)\mathbf{R}_j(f),
\]  

(6)

where \( I \) denotes the \( I \times I \) identity matrix and \( \cdot^H \) is the Hermitian transposition. In the M-step, the spatial covariance matrices \( \mathbf{R}_j(f) \) are updated as

\[
\mathbf{R}_j(f) = \frac{1}{N} \sum_{n=1}^{N} \frac{1}{v_j(f, n)} \hat{\mathbf{R}}_j(f, n).
\]  

(7)

The source PSDs \( v_j(f, n) \) are first estimated without constraints as

\[
v_j(f, n) = \frac{1}{I} \text{tr}\left(\mathbf{R}_j^{-1}(f)\hat{\mathbf{R}}_j(f, n)\right),
\]  

(8)

where \( \text{tr}(\cdot) \) denotes the trace of a matrix. Then, they are updated according to a given spectral model by fitting \( v_j(f, n) \) from \( z_j(f, n) \) in the spectrogram fitting step. The spectrogram initialization and the spectrogram fitting steps depend on how the spectral parameters are modeled. Spectral models used in this context may include NMF [24], which is a linear model with nonnegativity constraints, KAM [27], which relies on the local regularity of the sources, and continuity models [31]. In this study, we propose to use DNNs for this purpose.

III. DNN-BASED MULTICHANNEL SOURCE SEPARATION

In this section, we propose a DNN-based multichannel source separation algorithm, which is based on the iterative algorithm presented in Section II. Theoretical arguments regarding the cost function for DNN training are also presented.
Algorithm 1 General iterative EM algorithm [23], [24]

Inputs:
- The STFT of mixture \( x(f, n) \)
- The number of channels \( I \)
- The number of sources \( J \)
- The number of EM iterations \( L \)
- The spectral models \( M_0, M_1, \ldots, M_J \)

1: for each source \( j \) of \( J \) do
2:   Initialize the source spectrogram:
3:     \( v_j(f, n) \leftarrow \text{spectrogram initialization} \)
4:   Initialize the source spatial covariance matrix:
5:     \( R_j(f) \leftarrow I \times I \) identity matrix
6: end for
7: for each EM iteration \( l \) of \( L \) do
8:   Compute the mixture covariance matrix:
9:     \( R_x(f, n) \leftarrow \sum_{j=1}^{J} v_j(f, n) R_j(f) \)
10:  for each source \( j \) do
11:     Compute the Wiener filter gain:
12:       \( W_j(f, n) \leftarrow \text{Eq. (5) given } v_j(f, n), R_j(f), R_x(f, n) \)
13:     Compute the spatial source image:
14:       \( \tilde{c}_j(f, n) \leftarrow \text{Eq. (4) given } x(f, n), W_j(f, n) \)
15:     Compute the posterior second-order raw moment of the spatial source image:
16:       \( R_{c_j}(f, n) \leftarrow \text{Eq. (6) given } v_j(f, n), R_j(f), W_j(f, n), \tilde{c}_j(f, n) \)
17:     Update the source spatial covariance matrix:
18:       \( R_j(f) \leftarrow \text{Eq. (7) given } v_j(f, n), R_{c_j}(f, n) \)
19:     Compute the unconstrained source spectrogram:
20:       \( z_j(f, n) \leftarrow \text{Eq. (8) given } R_j(f), R_{c_j}(f, n) \)
21:     Update the source spectrogram:
22:       \( v_j(f, n) \leftarrow \text{spectrogram fitting given } z_j(f, n), R_j(f) \)
23: end for
24: end for
25: for each source \( j \) of \( J \) do
26:   Compute the final spatial source image:
27:     \( \tilde{c}_j(f, n) \leftarrow \text{Eq. (4) given all } v_j(f, n), \text{all } R_j(f), x(f, n) \)
28: end for

Outputs:
- All spatial source images \( [\tilde{c}_1(f, n), \ldots, \tilde{c}_J(f, n)] \)

A. Algorithm

In our algorithm, DNNs are employed to model the source spectra \( v_j(f, n) \). We use them to predict the source spectra instead of the time-frequency masks because our preliminary experiments showed that the performance of both approaches was similar on our dataset. Moreover, it is more convenient to integrate DNNs that estimate spectra into Algorithm 1 because the algorithm requires PSD and the power spectrum can be viewed as an estimate of the PSD [32].

A DNN is used for spectrogram initialization and one or

Algorithm 2 DNN-based iterative algorithm

Inputs:
- The STFT of mixture \( x(f, n) \)
- The number of channels \( I \)
- The number of sources \( J \)
- The number of spatial updates \( K \)
- The number of EM iterations \( L \)
- The DNN spectral models \( DNN_0, DNN_1, \ldots, DNN_L \)

1: Compute a single-channel version of the mixture:
2: \( \bar{x}(f, n) \leftarrow \text{DS beamforming given } x(f, n) \)
3: Initialize all source spectrograms simultaneously:
4: \( [v_1(f, n), \ldots, v_J(f, n)] \leftarrow DNN_0(|\bar{x}(f, n)|)^2 \)
5: for each source \( j \) of \( J \) do
6:   Initialize the source spatial covariance matrix:
7:     \( R_j(f) \leftarrow I \times I \) identity matrix
8: end for
9: for each EM iteration \( l \) of \( L \) do
10:  for each spatial update \( k \) of \( K \) do
11:    Compute the mixture covariance matrix:
12:      \( R_x(f, n) \leftarrow \sum_{j=1}^{J} v_j(f, n) R_j(f) \)
13:  for each source \( j \) do
14:    Compute the Wiener filter gain:
15:      \( W_j(f, n) \leftarrow \text{Eq. (5) given } v_j(f, n), R_j(f), R_x(f, n) \)
16:     Compute the spatial source image:
17:       \( \tilde{c}_j(f, n) \leftarrow \text{Eq. (4) given } x(f, n), W_j(f, n) \)
18:     Compute the posterior second-order raw moment of the spatial source image:
19:       \( R_{c_j}(f, n) \leftarrow \text{Eq. (6) given } v_j(f, n), R_j(f), W_j(f, n), \tilde{c}_j(f, n) \)
20:     Update the source spatial covariance matrix:
21:       \( R_j(f) \leftarrow \text{Eq. (7) given } v_j(f, n), R_{c_j}(f, n) \)
22:     Compute the unconstrained source spectrogram:
23:       \( z_j(f, n) \leftarrow \text{Eq. (8) given } R_j(f), R_{c_j}(f, n) \)
24:     Update the source spectrogram:
25:       \( v_j(f, n) \leftarrow \text{spectrogram fitting given } z_j(f, n), R_j(f) \)
26: end for
27: end for
28: for each source \( j \) of \( J \) do
29:   Compute the final spatial source image:
30:     \( \tilde{c}_j(f, n) \leftarrow \text{Eq. (4) given all } v_j(f, n), \text{all } R_j(f), x(f, n) \)
31: end for

Outputs:
- All spatial source images \( [\tilde{c}_1(f, n), \ldots, \tilde{c}_J(f, n)] \)

more DNNs are used for spectrogram fitting. Let \( DNN_0 \) be the DNN used for spectrogram initialization and \( DNN_L \) the
ones used for spectrogram fitting. DNN₀ aims to estimate the source spectra simultaneously from the observed mixture. This usage of joint DNN is similar to the usage of DNNs in the context of single-channel source separation in [12], [14], [15]. Meanwhile, DNNᵢ aims to improve the source spectra estimated at iteration l. This usage of DNN to obtain clean spectra from noisy spectra is similar to the usage of DNNs in the context of single-channel speech enhancement in [33], [34]. Theoretically, we can train different DNNs for spectrogram fitting at different iterations. Thus, the maximum number of DNNs for spectrogram fitting is equal to the number of iterations L.

In this article, we consider magnitude STFT spectra as the input and output of DNNs. Following [19], the input and output spectra are computed from single-channel signals \( \tilde{x}(f,n) \) and \( \tilde{c}_j(f,n) \) obtained from the corresponding multichannel signals \( x(f,n) \) and \( c_j(f,n) \), respectively, by DS beamforming. All DNNs are trained with the magnitude spectra of the single-channel source images \( |\tilde{c}_j(f,n)| \) as the target.

The inputs of DNN₀ and DNNᵢ are denoted by \( |\tilde{x}(f,n)| \) and \( \sqrt{z_j(f,n)} \), respectively. The outputs of both types of DNNs for source j, frequency bin f, and frame index n are denoted by \( \sqrt{v_j(f,n)} \). DNN₀ takes the magnitude spectra \( |\tilde{x}(f,n)| \) and yields the initial magnitude spectra \( \sqrt{v_j(f,n)} \) for all sources simultaneously. DNNᵢ takes the magnitude spectra \( \sqrt{z_j(f,n)} \) of all sources and yields the improved magnitude spectra \( \sqrt{v_j(f,n)} \) for all sources simultaneously.

The proposed DNN-based iterative algorithm is described in Algorithm 2.

B. Cost functions

We are interested in the use of different cost functions for training the DNNs.

1) The Itakura-Saito (IS) divergence [35] between the target \( |\tilde{c}_j(f,n)| \) and the estimate \( \sqrt{v_j(f,n)} \) is expressed as

\[
D_{IS} = \frac{1}{JFN} \sum_{j,f,n} \left( \frac{|\tilde{c}_j(f,n)|^2}{\sqrt{v_j(f,n)}} - \log \frac{|\tilde{c}_j(f,n)|^2}{\sqrt{v_j(f,n)}} - 1 \right).
\]

(9)

It is a popular metric in the speech processing community because it yields signals with good perceptual quality. Moreover, it is desirable from a theoretical point of view because it results in maximum likelihood (ML) estimation of the spectra [35] and the whole Algorithm 2 then achieves ML estimation. While the IS divergence has become a popular choice for NMF-based audio source separation [35]–[37], its use as the cost function for DNN training is uncommon.

2) The Kullback-Leibler (KL) divergence [38] is expressed as

\[
D_{KL} = \frac{1}{JFN} \sum_{j,f,n} \left( \frac{|\tilde{c}_j(f,n)|}{\sqrt{v_j(f,n)}} \log \frac{|\tilde{c}_j(f,n)|}{\sqrt{v_j(f,n)}} - |\tilde{c}_j(f,n)| + \sqrt{v_j(f,n)} \right).
\]

(10)

It is also a popular choice for NMF-based audio source separation [35] and has been shown to be effective for DNN training [13].

3) The Cauchy cost function is expressed as

\[
D_{Cauchy} = \frac{1}{JFN} \sum_{j,f,n} \left( \frac{3}{2} \log \left( |\tilde{c}_j(f,n)|^2 + v_j(f,n) \right) - \log \sqrt{v_j(f,n)} \right).
\]

(11)

It has been proposed recently for NMF-based audio source separation and advocated as performing better than the IS divergence in some cases [39].

4) The phase-sensitive (PS) cost function is defined as

\[
D_{PS} = \frac{1}{2JFN} \sum_{j,f,n} |m_j(f,n)\tilde{x}(f,n) - \tilde{c}_j(f,n)|^2,
\]

(12)

where \( m_j(f,n) = v_j(f,n)/\sum_{j'} v_{j'}(f,n) \) is the single-channel Wiener filter [8], [22]. It minimizes the error in the complex-valued STFT domain, not in the magnitude STFT domain as the other cost functions considered here.

5) The mean squared error (MSE) [35] is expressed as

\[
D_{MSE} = \frac{1}{2JFN} \sum_{j,f,n} \left( |\tilde{c}_j(f,n)| - \sqrt{v_j(f,n)} \right)^2.
\]

(13)

It is the most widely used cost function for various optimization processes, including DNN training for regression tasks. Despite its simplicity, it works well in most cases.

IV. EXPERIMENTAL EVALUATION FOR SPEECH ENHANCEMENT

In this section, we present the application of the proposed framework for speech enhancement in the context of the CHiME-3 Challenge [40] and evaluate different design choices. We considered different cost functions, numbers of spatial updates, and numbers of spectral updates. We anticipated that these three parameters are important parameters for the proposed framework. Extensive experiments have been done to investigate the comparative importance of these three parameters. By presenting detailed descriptions, we want to boost the reproducibility of the experiments presented and the performance achieved in this article.

A. Task and dataset

The CHiME-3 Challenge is a speech separation and recognition challenge which considers the use of ASR for a multi-microphone tablet device. In this context, we consider two sources (\( J = 2 \)), namely speech and noise. The challenge provides real and simulated 6-channel microphone array data in 4 varied noise settings (bus, cafe, pedestrian area, and street junction) divided into training, development, and test sets. The training set consists of 1,600 real and 7,138 simulated utterances (tr05_real and tr05_simu), the development
set consists of 1,640 real and 1,640 simulated utterances ($dt05\_real$ and $dt05\_simu$), while the test set consists of 1,320 real and 1,320 simulated utterances ($et05\_real$ and $et05\_simu$). The utterances are taken from the 5k vocabulary subset of the Wall Street Journal corpus [41]. All data are sampled at 16 kHz. For further details, please refer to [40].

We used the source separation performance metrics defined in BSS Eval toolbox 3.0\(^1\) [42] in most of the experiments presented in this section. The metrics include signal to distortion ratio (SDR), source image to spatial distortion ratio (ISR), signal to interference ratio (SIR), and signal to artifacts ratio (SAR). In addition, at the end of this section, we use the best speech separation system as the front-end, combine it with the best back-end in [29], and evaluate the ASR performance in terms of word error rate (WER).

The ground truth speech and noise signals, which are employed as training targets for DNN-based speech enhancement, were extracted using the baseline simulation tool provided by the challenge organizers [40]. The ground truth speech and noise signals for the real data are not perfect because they are extracted based on an estimation of the impulse responses (IRs) between the close-talking microphone and the microphones on the tablet device. Hence, the resulting source separation performance metrics for the real data are unreliable. Therefore, we evaluate the separation performance on the simulated data for studying the impact of the different design choices. By contrast, since the ground truth transcriptions for ASR are reliable, we evaluate the ASR performance on real data.

### B. General system design

The proposed DNN-based speech separation framework is depicted in Fig. 1. A single-channel variant of this framework which boils down to the approach in [19] is also depicted for comparison.

The framework can be divided into three main successive steps, namely pre-processing, spectrogram initialization, and multichannel filtering. We describe each step in detail below and then provide further description of the DNNs in the following section.

1) **Preprocessing:** The STFT coefficients were extracted using a Hamming window of length 1024 and hopsize 512 resulting $F = 513$ frequency bins.

The time-varying time difference of arrivals (TDOAs) between the speaker’s mouth and each of the microphones are first measured using the provided baseline speaker localization tool [40], which relies on a nonlinear variant of steered response power using the phase transform (SRP-PHAT) [43], [44]. All channels are then aligned with each other by shifting the phase of STFT of the input noisy signal $x(f,n)$ in all time-frequency bins $(f,n)$ by the opposite of the measured delay. This preprocessing is required to satisfy the model in (2) which assumes that the sources do not move over time.

In addition, we obtain a single-channel signal by averaging the realigned channels together. The combination of time alignment and channel averaging is known as DS beamforming in the microphone array literature [45], [46].

2) **Spectrogram initialization:** The initial PSDs of speech and noise are computed from the magnitude source spectra estimated by DNN\(_0\).

3) **Multichannel filtering:** The PSDs and spatial covariance matrices of speech and noise are estimated and updated using the iterative algorithm (Algorithm 2), in which DNN\(_l\) is employed for spectrogram fitting at iteration $l$. In order to avoid numerical instabilities due to the use of single precision, the PSDs $v_j(f,n)$ are floored to $10^{-5}$ in the EM iteration.

In addition, the channels of estimated speech spatial image are averaged to obtain a single-channel signal for the ASR

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\(^1\) http://bass-db.gforge.inria.fr/bss_eval/
evaluation. Empirically, this provided better ASR performance than the use of one of the channels. The number of spatial updates \( K \) is investigated in Section IV-E and the number of iterations \( L \) in Section IV-F.

C. DNN spectral models

Three design aspects are discussed below: the architecture, the input and output, and the training.

1) Architecture: The DNNs follow a multilayer perceptron (MLP) architecture. The number of hidden layers and the number of units in each input or hidden layer may vary. The number of units in the output layer equals the dimension of spectra multiplied by the number of sources. The activation functions of the hidden and output layers are rectified linear units (ReLU) [47].

In this article, DNN\(_0\) and DNN\(_1\) have a similar architecture. They have an input layer, three hidden layers, and an output layer. Both types of DNN have hidden and output layers size of \( F \times J = 1026 \). DNN\(_0\) has an input layer sizes of \( F = 513 \) and DNN\(_1\) of \( F \times J = 1026 \).

Other network architectures, e.g. recurrent neural network (RNN) and convolutional neural network (CNN), may be used instead of the one used here. The performance comparison with different architectures is beyond the scope of this article.

2) Inputs and outputs: In order to provide temporal context, the input frames are concatenated into supervectors consisting of a center frame, left context frames, and right context frames. In choosing the context frames, we use every second frame relative to the center frame in order to reduce the redundancies caused by the windowing of STFT. Although this causes some information loss, this enables the supervectors to represent a longer context [16], [48]. In addition, we do not use the magnitude spectra of the context frames directly, but the difference of magnitude between the context frames and the center frame. These differences act as complementary features similar to delta features. Preliminary experiments (not shown here) indicated that this improves DNN training and provides a minor improvement in terms of SDR.

Let \( \tilde{x}(f,n) \) be the input frames of DNN\(_0\). The supervector can be expressed as

\[
Z_0(f,n) = \begin{bmatrix} \left| \tilde{x}(f,n-2c) \right| - \left| \tilde{x}(f,n) \right| \\ \vdots \\ \left| \tilde{x}(f,n) \right| \\ \vdots \\ \left| \tilde{x}(f,n+2c) \right| - \left| \tilde{x}(f,n) \right| \end{bmatrix}
\]  

(14)

where \( c \) is the one-sided context length in frames. The supervector for DNN\(_1\), \( Z_1(f,n) \), is constructed in a similar way where a stack of \( \sqrt{2} \) is used as input instead of \( \left| \tilde{x}(f,n) \right| \) (see Fig. 2 and 3). In this article, we considered \( c = 2 \), so the supervectors for the input of the DNNs were composed by 5 time frames (2 left context, 1 center, and 2 right context frames).

The dimension of the supervectors is reduced by principal component analysis (PCA) to the dimension of the DNN input. As shown in [49], dimensionality reduction by PCA significantly minimizes the computational cost of DNN training with a negligible effect on the performance of DNN. Standardization (zero mean, unit variance) is done element-wise before and after PCA over the training data as in [49]. The standardization factors and the PCA transformation matrix are then kept for processing of any input. Thus, strictly speaking, the inputs of DNNs are not the supervectors of magnitude spectra \( Z_0(f,n) \) and \( Z_1(f,n) \), but their transformation into reduced dimension vectors.

Fig. 2 and 3 illustrates the inputs and outputs of the DNNs for spectrogram initialization and spectrogram fitting, respectively. \( F \) denotes the dimension of the spectra, \( C = 2c + 1 \) the context length, and \( J \) the number of sources.

3) Training criterion: The cost function used for DNN training is the sum of a primary cost function and an \( \ell_2 \) regularization term. The \( \ell_2 \) regularization term [50] is used to prevent overfitting and can be expressed as

\[
D_{\ell_2} = \frac{\lambda}{2} \sum_q w_q^2
\]  

(15)

where \( w_q \) are the DNN weights and the regularization parameter is fixed to \( \lambda = 10^{-5} \). No regularization is applied to the biases.

Table I summarizes the implementation of different cost functions for the experiments. In order to avoid numerical instabilities, instead of using the original formulation of IS divergence in (9), our implementation used a regularized formulation as shown in (16). It should be noted that the use of regularization in this case is a common practice to avoid instabilities [36], [51]. For the same reason, we used regularized formulations of KL divergence and Cauchy cost function as shown in (17) and (18), respectively. For these three divergences, the regularization parameter is set to \( \delta = 10^{-3} \). In addition, geometric analysis on the PS cost function by considering that \( m_\delta(f,n) \in \mathbb{R}_{+}^{F \times N} \) leads to a simplified formula shown in (19).

4) Training algorithm: The weights are initialized randomly from a zero-mean Gaussian distribution with standard deviation of \( \sqrt{2}/n_i \), where \( n_i \) is the fan-in (the number of inputs to the neuron, which is equal to the size of the previous layer in our case) [52]. Finally, the biases are initialized to zero.

The DNNs are trained by greedy layer-wise supervised training [53] where the hidden layers are added incrementally. In the beginning, a NN with one hidden layer is trained after random weight initialization. The output layer of this trained NN is then substituted by new hidden and output layers to form a new NN, while the parameters of the existing hidden layer are kept. Thus, we can view this as a pre-training method for the training of a new NN. After random initialization for the parameters of new layers, the new NN is entirely trained. This procedure is done iteratively until the target number of hidden layers is reached.

Training is done by backpropagation with minibatch size of 100 and the ADADELTA parameter update algorithm [54]. Compared to standard stochastic gradient descent (SGD), ADADELTA employs adaptive per-dimension learning rates and does not require manual setting of the learning rate. The
Fig. 2. Illustration of the inputs and outputs of the DNN for spectrogram initialization. Input: magnitude spectrum of the mixture (left). Output: magnitude spectra of the sources (right).

Fig. 3. Illustration of the inputs and outputs of the DNNs for spectrogram fitting. Input: stack of magnitude spectra of all sources (left). Output: magnitude spectra of the sources (right).

TABLE I

IMPLEMENTATION DETAILS OF THE DNN TRAINING COST FUNCTIONS.

<table>
<thead>
<tr>
<th>Exp. label</th>
<th>Weight reg.</th>
<th>Primary cost function</th>
</tr>
</thead>
<tbody>
<tr>
<td>IS $D_{l_2}$</td>
<td>$D_{IS} = \frac{1}{JFN} \sum_{j,f,n} \left( \left</td>
<td>\tilde{c}_j(f,n) \right</td>
</tr>
<tr>
<td>KL $D_{l_2}$</td>
<td>$D_{KL} = \frac{1}{JFN} \sum_{j,f,n} \left( \left</td>
<td>\tilde{c}_j(f,n) \right</td>
</tr>
<tr>
<td>Cau $D_{l_2}$</td>
<td>$D_{Cau} = \frac{1}{2JFN} \sum_{j,f,n} \left( \frac{v_j(f,n)}{\sum_{j'} v_{j'}(f,n)} \right) \left( \left</td>
<td>\tilde{c}_j(f,n) \right</td>
</tr>
<tr>
<td>PS $D_{l_2}$</td>
<td>$D_{PS} = \frac{1}{2JFN} \sum_{j,f,n} \left( \left</td>
<td>\tilde{c}_j(f,n) \right</td>
</tr>
<tr>
<td>MSE $D_{l_2}$</td>
<td>$D_{MSE} = \frac{1}{2JFN} \sum_{j,f,n} \left( \left</td>
<td>\tilde{c}_j(f,n) \right</td>
</tr>
</tbody>
</table>
hyperparameters of ADADELTA are set to $\rho = 0.95$ and $\epsilon = 10^{-6}$ following [54]. The validation error is computed every epoch and the training is stopped after 10 consecutive epochs failed to obtain better validation error. The latest model which yields the best validation error is kept. Besides, the maximum number of training epochs is set to 100.

The DNNs for the source separation evaluation were trained on both the real and simulated training sets (tr05_real and tr05_simu) with the real and simulated development sets (dt05_real and dt05_simu) as validation data. Conversely, we trained the DNNs for the speech recognition evaluation on the real training set only (tr05_real) and validated them on the real development set only (dt05_real). The same DNNs were also used for the performance comparison to the general iterative EM algorithm. See [29] for the performance comparison between these two different settings.

**D. Impact of cost functions**

We first evaluated the impact of the cost function by setting $L = 0$ (see Algorithm 2) so that the separation relied on the PSD estimates $v_j(f, n)$ by letting the spatial covariance matrices $R_j(f)$ be the identity matrix. This is equivalent to single-channel source separation for each channel.

Fig. 4 shows the evaluation results for the resulting 6-channel estimated speech signal on the simulated test set (et05_simu).

‘KL’, ‘PS’, and ‘MSE’ have comparable performance. Among these three cost functions, ‘KL’ is shown to have the best SDR and SIR properties, while ‘PS’ and ‘MSE’ whose performance is the same follow closely behind. ‘MSE’ is shown to have the best ISR property, while ‘KL’ and ‘PS’ follow behind. For the SAR, these three cost functions have almost the same performance. Among all of the cost functions used in this evaluation, ‘IS’ almost always has the worst performance. Interestingly, ‘Cau’ outperformed the others in terms of SIR, but it has a poor SAR property. Thus, in general, ‘IS’ and ‘Cau’ should be avoided for single-channel source separation with DNN model.

In addition, it is worth mentioning that the use of flooring function (e.g. ReLU activation function for the DNN outputs) during the training with ‘IS’, ‘KL’, ‘Cau’, ‘PS’ seems to be important. We found in additional experiments (not shown here) that training failed when a linear activation function was used for the output layer with these cost functions.

**E. Impact of spatial parameters updates**

In this subsection, we investigate the impact of spatial parameters updates on the performance by setting the number of iterations to $L = 1$ and varying the number of spatial updates $K$, while ignoring the computation of $z_j(f, n)$ and the spectral parameters update (lines 16–19 of Algorithm 2). Thus, the spectral parameters $v_j(f, n)$ are only initialized by the first DNN (as in Section III-B) and kept fixed during the iterative procedure. We evaluate the different cost functions from Section III-B in this context again.

Fig. 5 shows the results for the resulting 6-channel estimated speech signal on the simulated test set (et05_simu). The x-axis of each chart corresponds to the number of spatial updates $k$. Thus, $k = 0$ is equivalent to single-channel source separation for each channel whose results are shown in Fig. 4.

In general, the performance of ‘PS’ saturated after a few updates, while the performance of other cost functions is increased with $k$ in most metrics. Interestingly, after 20 iterations, each cost function showed its best property. Among all of the cost functions, ‘KL’ has the best SDR, ‘Cau’ the best SIR, and ‘IS’ the best SAR. While for the ISR, ‘PS’, ‘MSE’, and ‘KL’ performed almost identical and better than the other two cost functions.

In summary, the proposed multichannel approach outperformed single-channel DNN-based approach even when using DNN0 only. The spatial parameters and their updates improved the enhancement performance. From the experiments using 20 spatial parameter updates, we can observe that each cost function has its own properties. ‘KL’ followed by ‘MSE’ are the most reasonable choices because they improved all of the metrics well. ‘PS’ is suitable for the tasks that put emphasis on the ISR. On the contrary, ‘Cau’ is suitable for the tasks in which the ISR is less important. Finally, ‘IS’ is suitable for the tasks that put emphasis on the SAR. Thus, the choice of the cost function should depend on the trade-off we want to achieve between these four metrics.

**F. Impact of spectral parameters updates**

In this subsection, we investigate the impact of spectral parameter updates (i.e. the spectrogram fitting) on the performance by setting the number of spatial updates to $K = 20$, varying the number of iterations $L$, and varying the DNN used for iteration $l$. We also evaluate different cost functions in this context, namely IS, KL, Cauchy, and MSE. We left the PS cost function because as shown previously, its SDR after 20 spatial updates was significantly lower than the others and the overall performance saturated already.

We trained two additional DNNs (DNN1 and DNN2) for spectrogram fitting. This allowed us to try different settings for the iterative procedure: (1) without spectral updates; (2) with spectral updates using only DNN1; and (3) with spectral updates using DNN1 and DNN2.

We present the comparison of these three settings using KL divergence as the cost function in Fig. 6. We then present the comparison of different cost functions using the third setting in Fig. 7. For both figures, the x-axis shows the index of EM iteration $l$, the update type (spatial or spectral), and the DNN index. Thus, $l = 0$ is equivalent to single-channel source separation for each channel whose results are shown in Fig. 4, while $l = 1$ with spatial updates is equivalent to the results shown in Fig. 5.

Fig. 6 shows that the use of a specific DNN for each iteration (here, DNN1 for $l = 1$ and DNN2 for $l = 2$) is beneficial. When a specific DNN is used, the spectral update provides a small improvement. Most importantly, this update allows the following spatial update to yield significant improvement. This behavior can be observed by comparing the performance of the spectral updates of EM iteration $l$ and the spatial updates of the following iteration $l + 1$. Additionally,
we can observe it by comparing the overall behavior of the “3 DNNs” curve to the “1 DNN” curve, in which no spectrogram fitting is done. Fig. 7 shows similar behavior for the other cost functions.

Fig. 6 also shows that the use of the same DNN for several iterations (here, DNN$_1$ for $l = 1$ and $l = 2$) did not improve the performance. Although the following spatial update recovered the performance, the use of a specific DNN for each iteration still provided better performance. We can observe this by comparing the “3 DNNs” curve to the “2 DNNs” curve for $l = 2$ and $l = 3$. It is understandable because there is a mismatch between the input and the training data of the DNN in this case.

Fig. 7 shows that the performance of all cost functions improves with $l$. ‘Cau’ and ‘IS’ tend to saturate more quickly than the others.

In summary, the iterative spectral and spatial updates improve the enhancement performance. The performance saturates after few EM iteration. ‘KL’ and ‘MSE’ perform better than the other cost functions. Although the use of IS divergence for DNN training is theoretically motivated, the resulting performance is lower than the others for most metrics.

G. Comparison to NMF-based iterative EM algorithm

In this subsection, we compare the best system of the proposed framework to the NMF-based iterative EM algorithm [24] in terms of source separation performance. We used the algorithm implementation in the Flexible Audio Source Separation Toolbox (FASST)$^2$ and followed the settings used in [55]. The speech spectral and spatial models were trained on

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$^2$http://bass-db.gforge.inria.fr/fasst
the real training set (tr05_real). Meanwhile, the noise spectral and spatial models were initialized for each mixture using 5 seconds of background noise context based on its annotation. By doing so, the comparison is not completely fair since the proposed framework does not use this context information. However, this setting is favourable for the NMF-based iterative algorithm. As described in Section IV-C, the DNNs used in this evaluation were also trained on the real training set only. However, this setting is favourable for the NMF-based iterative algorithm. As described in Section IV-C, the DNNs used in this evaluation were also trained on the real training set only. The separation results from this evaluation were then used for the speech recognition evaluation in Section IV-H.

Table II shows the performance of the NMF-based iterative EM algorithm after 50 EM iterations and the performance of the proposed framework after the spatial update of the EM iteration \( l = 3 \). The proposed framework was clearly better than the NMF-based iterative EM algorithm for all metrics.

<table>
<thead>
<tr>
<th>Enhancement method</th>
<th>SDR (dB)</th>
<th>ISR (dB)</th>
<th>SIR (dB)</th>
<th>SAR (dB)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proposed: KL (3 DNNs)</td>
<td>13.23</td>
<td>24.25</td>
<td>15.58</td>
<td>18.23</td>
</tr>
</tbody>
</table>

This confirms that DNNs are able to model spectral parameters much better than NMF does.

H. Speech recognition

In this subsection, we evaluate the use of our best system as the front-end of a speech recognition system. We did a speech recognition evaluation by following the Kaldi setup distributed...
by the CHiME-3 challenge organizers\textsuperscript{3} [40], [56]. The evaluation includes the uses of (a) feature-space maximum likelihood regression (fMLLR) features [57]; (b) acoustic models based on Gaussian Mixture Model (GMM) and DNN trained with the cross entropy (CE) criterion followed by state-level minimum Bayes risk (sMBR) criterion [58]; and (c) language models with 5-gram Kneser-Ney (KN) smoothing [59] and rescoring using recurrent neural network-based language model (RNN-LM) [60]. The acoustic models are trained on enhanced multi-condition real and simulated data. The evaluation results are presented in terms of word error rate (WER). The optimization of the speech recognition back-end is beyond the scope of this article. Please refer to [56] for the further details of the methods used in the evaluation.

The evaluation results include the baseline performance (observed), DS beamforming, and NMF-based iterative EM algorithm [24]. The baseline performance was measured using only channel 5 of the observed signal. This channel is considered as the most useful channel because the corresponding microphone faces the user and is located at the bottom-center of the tablet device. DS beamforming was performed on the 6-channel observed signal as described in Section IV-B. For the NMF-based iterative EM algorithm and the proposed framework, we simply average over channels the separation results from the evaluation described in Section IV-G.

Table III shows the performance comparison using the GMM back-end retrained on enhanced multi-condition data. Table IV shows the performance comparison using the DNN+sMBR back-end trained with enhanced multi-condition data followed by 5-gram KN smoothing and RNN-LM rescoring. Both tables show the performance on the real development set (dt05\_real) and the real test set (et05\_real). Boldface numbers show the best performance for each dataset.

For the single-channel enhancement (see EM iteration $l = 0$), the WER on the real test set decreases by 22% and 21% relative using the GMM and the DNN+sMBR backends, respectively, w.r.t. the observed WER. Interestingly, this single-channel enhancement which is done after DS beamforming did not provide better performance compared to the DS beamforming alone. It indicates that proper exploitation of multichannel information is crucial.

The proposed multichannel enhancement then decreases the WER on the real test set up to 25% and 33% relative using the GMM and the DNN+sMBR backends, respectively, w.r.t. the corresponding single-channel enhancement. It decreases the WER up to 25% and 26% relative w.r.t. the DS beamforming alone. It also decreases the WER up to 16% and 24% relative w.r.t. the NMF-based iterative EM algorithm [24].

\section*{V. Conclusion}

In this article, we presented a DNN-based multichannel source separation framework where the multichannel filter is derived from the source spectra, which are estimated by DNNs, and the spatial covariance matrices, which are updated iteratively in an EM fashion. Evaluation has been done for a speech enhancement task. The experimental results show that the proposed framework works well. It outperforms single-channel DNN-based enhancement and the NMF-based iterative EM algorithm [24]. The use of a single DNN to estimate the source spectra from the mixture already suffices to observe an improvement. Spectral updates by employing additional DNNs moderately improve the performance themselves, but they allow the following spatial updates to provide further significant improvement. We also demonstrate that the use of a specific DNN for each iteration is beneficial. The use of KL divergence as the DNN training cost function is shown to provide the best performance. The widely used MSE is also shown to perform very well.

Future directions concern alternative training targets for DNNs, the use of spatial features [9]–[11] as additional inputs, the incorporation of prior information about the source position, the use of more advanced network architectures, such as RNN [8] and CNN, and the use of more advanced training techniques, such as dropout.

\section*{Acknowledgment}

The authors would like to thank the developers of Theano [61] and Kaldi [62]. Experiments presented in this article were carried out using the Grid’5000 testbed, supported by a scientific interest group hosted by Inria and including CNRS, RENATER and several Universities as well as other organizations (see https://www.grid5000.fr).

\footnotesize

\begin{table}[h]
\centering
\caption{Average WERs ($\%$) using the GMM back-end retrained on enhanced multi-condition data. The evaluation was done on the real sets. Lower is better.}
\begin{tabular}{|c|c|c|c|c|}
\hline
Enhancement method & EM iter. & Update type & Dev & Test \\
\hline
Observed & - & - & 18.32 & 33.02 \\

DS beamforming & - & - & 14.07 & 25.86 \\


Proposed: KL (3 DNNs) & 0 & - & 13.56 & 25.90 \\

& 1 & spatial & 11.17 & 20.42 \\

& 2 & spectral & 11.25 & 20.67 \\

& 3 & spatial & 11.00 & 19.72 \\

\hline
\end{tabular}
\end{table}

\begin{table}[h]
\centering
\caption{Average WERs ($\%$) using the DNN+sMBR back-end trained with enhanced multi-condition data followed by 5-gram KN smoothing and RNN-LM rescoring. The evaluation was done on the real sets. Lower is better.}
\begin{tabular}{|c|c|c|c|c|}
\hline
Enhancement method & EM iter. & Update type & Dev & Test \\
\hline
Observed & - & - & 9.65 & 19.28 \\

DS beamforming & - & - & 6.35 & 13.70 \\


Proposed: KL (3 DNNs) & 0 & - & 6.64 & 15.18 \\

& 1 & spatial & 5.37 & 11.46 \\

& 2 & spectral & 5.19 & 11.46 \\

& 3 & spatial & 4.87 & 10.79 \\

& & & 4.99 & 11.12 \\

\hline
\end{tabular}
\end{table}

\textsuperscript{3}https://github.com/kaldi-asr/kaldi/tree/master/egs/chime3


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