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# Expert-validated CSF segmentation of MNI atlas enhances accuracy of virtual glioma growth patterns

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**Abstract.** Biomathematical modeling of glioma growth has been developed to optimize treatments delivery and to evaluate their efficacy. Simulations currently make use of anatomical knowledge from standard MRI atlases. For example, cerebrospinal fluid (CSF) spaces are obtained by automatic thresholding of the MNI atlas, leading to an approximate representation of real anatomy. To correct such inaccuracies, an expert-revised CSF segmentation map of the MNI atlas was built. Several virtual glioma growth patterns of different locations were generated, with and without using the expert-revised version of the MNI atlas. The adequacy between virtual and radiologically observed growth patterns was clearly higher when simulations were based on the expert-revised atlas. This work emphasizes the need for close collaboration between clinicians and researchers in the field of brain tumor modeling.

## 1 Introduction

Gliomas are brain tumors that remain incurable despite recent advances in treatments that combine surgery, chemotherapy and radiation therapy. Their diffuse behavior, resulting in an invasion of normal appearing parenchyma peripheral to the bulk lesion, is a major cause of treatment failure.

Biomathematical modeling of these tumors has been developed over the past two decades. The hope is that *in silico* tumor growth models could help to optimize treatments delivery [2, 5, 23, 24] and to evaluate their efficacy [34, 18, 22]. Such clinical applications require patient-specific inputs, obtained for example from pre-treatment sequential MRIs. Simulations are either performed in the patient MRI space [27] onto which anatomical knowledge of atlases can be matched (to obtain brain parenchyma segmentation and create white and gray matter segmentations), or in a reference space - usually the MNI atlas [9] - onto which all patient images are registered. Hence accurate anatomical atlases are needed in both cases.

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Advances have been made in integrating a more precise anatomy in the atlas. Whereas the very first templates in the nineties were built from a 2D CT scan [35, 6, 33], just outlining the brain surface and the ventricles, more recent works are based on 3D-MRI atlases of CSF, grey matter and white matter [28], and eventually including detailed white matter architecture via DTI sequences [12, 3, 27, 26]. CSF spaces are of utmost importance for achieving realistic glioma growth patterns, as they constitute anatomical barriers that cannot be crossed by tumor cells (a statement that is implemented in the model by a no flux boundary condition). The segmentation of CSF delineation is commonly obtained by an automated thresholding of the atlas, without any expert validation of its anatomical accuracy. For example, it has been previously shown that current templates contain unphysiological bridges of brain matter between frontal and temporal operculum, which should normally be separated by the subarachnoid spaces of the sylvian fissure [12]. As a consequence, the virtual tumor can grow directly from one operculum to the other, resulting in unrealistic growth patterns as compared to clinically reported ones [19].

In this paper, we build an expert-revised CSF segmentation map of the MNI reference brain. We then propose to analyze how these corrections influence tumor growth patterns, by comparing simulations obtained using the native and corrected templates.

## 2 Data

The MNI 152 T1 MRI, gray matter probability map, and white matter probability map are de facto registered [9] and are all downloadable from the MNI website. The MNI 152 brain segmentation was created from the threshold gray and white matter MNI 152 probability maps (process described in following section). A neurosurgeon (A. Amelot) segmented the missing sulci patterns from the T1 image to refine this baseline brain parenchyma mask (BM), creating an improved BM. For the simulations in the Experiment section, the data inputs were the white matter segmentation (WM), which was segmented from the white matter probability map, and either the MNI 152 original brain segmentation or the improved brain segmentation (see below).

## 3 Method

In this section, we describe the preprocessing of the data and the model used to simulate tumor growth.

*Preprocessing of Data:* The WM, gray matter segmentation (GM), original MNI 152 BM and improved BM were created with the following steps.

The WM and GM mark out the inhomogeneous tissue boundaries of the brain and the CSF segmentation marks out where brain tissue is not. The WM was achieved by thresholding the MNI 152 white matter probability map or a probability  $> 0.58$ . The GM was estimated by thresholding the MNI 152 gray matter

probability map for a probability  $> 0.42$  and the CSF segmentation was achieved by thresholding the MNI 152 CSF probability map for probability  $> 0.17$ . These threshold values depict the most accurate account for where the white and gray matter and CSF are according to a neurosurgeon (E. Mandonnet).

The original MNI 152 BM was created by combining the WM and GM segmentations and removing all voxels that were marked as CSF by the CSF segmentation.

It took several steps to enhance the original MNI 152 BM. First, we determined where the original MNI 152 BM was imperfect by visually inspecting each slice along the three dimensions (axial, coronal, and sagittal). In this scan, we studied all sulci, gyrus, and cerebral lobes. Second, we created an improved CSF segmentation manually by redrawing, using Slicer [8], all of the subarachnoid spaces physiologically present that were lacking in the original MNI 152 BM (Figure 1). Third, we used the improved CSF segmentation to identify additional voxels in the original MNI 152 BM to be marked as CSF instead of brain.

*The Fisher Kolmogorov (FK) Model:* The Fisher Kolmogorov (FK) equation is a type of reaction-diffusion model, which has been used extensively in tumor growth modeling [32, 21, 31, 4, 12, 16, 20, 10, 11, 26, 27]. In our work, we use the following formulation:

$$\frac{\partial u}{\partial t} = \underbrace{\nabla \cdot (D(\mathbf{x})\nabla u)}_{\text{Diffusion Term}} + \underbrace{\rho \cdot u \cdot (1 - u)}_{\text{Logistic Reaction Term}} ; \underbrace{\eta_{\partial\omega} \cdot (D\nabla u)}_{\text{Boundary Condition}} = 0, \quad (1)$$

where  $u$  is the tumor cell density,  $D$  is the diffusion tensor,  $\rho$  is the proliferation rate, and  $\eta_{\partial\omega}$  are the normal directions to the boundaries of the brain surface.

There are several tensor construction methods that have been proposed to model anisotropic diffusion [4, 12]. We used a tensor construction method, proposed by Clatz et al. [4], which uses global scaling on the DTI,

$$D(\mathbf{x}) = \begin{cases} d_g I & \text{if } \mathbf{x} \text{ is in grey matter} \\ d_w D_{water} & \text{if } \mathbf{x} \text{ is in white matter,} \end{cases} \quad (2)$$

where  $D(\mathbf{x})$  is the inhomogeneous diffusion term, which takes into account that tumor cells move faster along anisotropic white matter fiber tracts, estimated by  $d_w D_{water}$ , than in isotropic gray matter  $d_g I$ .  $d_w$  and  $d_g$  are scalars,  $D_{water}$  is the normalized water diffusion tensor in the brain measured by the DTI, and  $I$  is a 3x3 identity matrix, which can be seen as an isotropic diffusion tensor.  $D_{water}$  is normalized so that the largest eigenvalue in white matter is one.

*The Eikonal Approximation of the FK Model:* In this section we first present the mathematical model that we considered for the description of glioma growth. This model is based on a reaction-diffusion equation (nonlinear PDE) which, even though is quite precise in predicting tumor cell density concentrations in

the brain, it is computationally very expensive. Then, we show an approximation of this reaction-diffusion model by a traveling time formulation [14] which we use to estimate the proliferation and diffusivity parameters of the model by minimizing the mismatch between a simulated tumor and a real one extracted from MRIs.

As presented in [14] we can approximate the reaction-diffusion model in Equation 1 by considering that for large times with constant coefficients the FK model with constant coefficients admits a traveling wave solution in the infinite cylinder. In other words, when the change of  $u$  is nonzero in only one direction,  $\mathbf{n}$ , for extremely large times the solution of Equation 1 can be formulated as

$$u(x, t) = u(\mathbf{n} \cdot x - vt) = u(\zeta) \quad \text{as } t \rightarrow \infty, \quad (3)$$

where  $v$  is the asymptotic speed of the wave front and  $\zeta = (\mathbf{n} \cdot x - vt)$  is the moving frame of the traveling wave. Then, by substituting Equation 3 into Equation 1 and considering a constant diffusion tensor we get

$$\mathbf{n}' D \mathbf{n} \frac{d^2 u}{d\zeta^2} + v \frac{du}{d\zeta} + \rho u(1 - u) = 0, \quad (4)$$

which is a non-linear ordinary differential equation. In order to have admissible solutions, the asymptotic speed  $v$  should depend on the diffusion tensor  $D$ ,  $\rho$ , and on the shape of the initial condition  $u(x, 0)$ . When the initial condition has a compact support the asymptotic speed of the traveling wave can be given as, [21],

$$v = 2\sqrt{\rho \mathbf{n}' D \mathbf{n}}. \quad (5)$$

However, there exist a transient behavior for the traveling wave speed while it converges to the asymptotic speed in Equation 5. Ebert et al. studied this convergence behaviour and derived in [7] the following analytical time-dependent representation of the traveling wave speed:

$$v(t) = \sqrt{\mathbf{n}' D \mathbf{n}} \frac{4t\rho - 3}{2t\sqrt{\rho}}. \quad (6)$$

Now we can formulate the traveling time formulation for the tumor delimitation. Based on the concepts described in [25],  $v(t)$  can be characterized as

$$|\nabla T| = \frac{1}{v(t)} = \left( 2\sqrt{\rho \mathbf{n}' D \mathbf{n}} - \frac{3}{2T} \sqrt{\frac{\mathbf{n}' D \mathbf{n}}{\rho}} \right)^{-1}, \quad (7)$$

where  $T$  is an implicit time function such that it embeds the locations of the tumor delimitation as iso-time surfaces ( $T(x)$  is the function described as the time when the tumor delineation passes over the point  $x$ ). Thus,  $\mathbf{n}$  can be written as  $\nabla T/|\nabla T|$  resulting in the traveling wave formulation as

$$\sqrt{\nabla T^T D \nabla T} = \frac{2\sqrt{\rho T}}{4\rho T - 3}, \quad (8)$$

where the equation has the Eikonal form ( $F\sqrt{\nabla T^T D \nabla T} = 1$  with  $F$  being a general speed function). This equation by itself solely gives the relation of consecutive iso-time surfaces of  $T$ . In order to construct the solution everywhere in the domain we require a Dirichlet type boundary condition, i.e., an initial surface for which we know the  $T$  value. For the tumor growth modeling case, this surface is given by the tumor delination in the first image,i.e.,

$$T(x) = T_1 \quad \forall x \in \Gamma_1, \quad (9)$$

where  $\Gamma_1$  is the tumor delination established in the first image and  $T_1$  is the time from the origination of the tumor to the aquisition of the first image. For the asymptotic case, the traveling time formulation is given by

$$2\sqrt{\nabla T^T \rho D \nabla T} = 1. \quad (10)$$

Notice from Equation 10 that  $T_1$  is not needed for the asymptotic case and that  $\rho$  and  $D$  appear in the product form and cannot be separated. The formulation given in equations 8, and 9 is valid in the infinite cylinder where the evolution is in one direction (in this situation, the traveling wave is a plane). In the case of tumor growth, the delination is curved and consequently its evolution is not analogous to an evolution in the infinite cylinder. We can still implement the formulation obtained in the infinite cylinder to more general cases in 3D by assuming that within a voxel, the tumor delination is planar and the model coefficients are constant. Then by starting from the initial tumor delination and spweeping the domain outwards we can construct the solution. Still, such a generalization does not consider the effect of curvatuue in the more general evolutions. Following the derivations of [13], [14] proposed the following Eikonal equation to describe the evolution of the tumor delination in 3D:

$$\left( \frac{4\rho T - 3}{2\sqrt{\rho T}} - \nabla \cdot \frac{D \nabla T}{\sqrt{\nabla T^T D \nabla T}} \right) \sqrt{\nabla T^T D \nabla T} = 1, \quad (11)$$

where  $\nabla \cdot (D \nabla T / \sqrt{\nabla T^T D \nabla T})$  is the efect of the curvature. In the derivation of Equation 11 it is assumed that the surface is slightly curved which requires the effect of the curvature to be of a lower order than the term  $2\sqrt{\rho}$ . However, the value of the curvature might be higher in the general case due to the precense of anisotropy in the diffusion process. Therefore, one needs to saturate the effect of curvature to satisfy this asumption. Thus, adding saturation to the curvature effect in Equation 11 we obtain the final formulation which describes the evolution of the tumor delination in 3D based on the reaction-diffusion formalism:

$$\left( \frac{4\rho T - 3}{2\sqrt{\rho T}} - 0.3\sqrt{\rho}(1 - e^{-|K_{eff}|/0.3\sqrt{\rho}}) \right) \sqrt{\nabla T^T D \nabla T} = 1, \quad (12)$$

$$K_{eff} = \nabla \cdot \frac{D \nabla T}{\sqrt{\nabla T^T D \nabla T}}, \quad (13)$$

$$T(x) = T_1 \quad \forall x \in \Gamma_1, \quad (14)$$

Notice that Equation 12 can become negative for low values of  $T$  due to the fact that the approximation for the time convergence and curvature effects get worse for lower  $T$  values [7]. In order to overcome this approximation error, [14] prevented the speed function in Equation 12 to drop lower than  $0.1\sqrt{\rho}$ , i.e.,

$$\frac{4\rho T - 3}{2\sqrt{\rho T}} - 0.3\sqrt{\rho}(1 - e^{-1|K_{eff}|/0.3\sqrt{\rho}}) \geq 0.1\sqrt{\rho}, \quad (15)$$

which serves as the minimum threshold for the speed of the tumor. In terms of the speed of progression of the tumor delineation, this limit can be written as

$$v_{min} = 0.1\sqrt{\rho \mathbf{n}^T D \mathbf{n}}, \quad (16)$$

where  $\mathbf{n}$  in the direction of the vector  $\nabla T$ . As a result of this constraint we have a growing tumor delineation at all times, consistent with the reaction-diffusion model.

## 4 Experiment

We performed a comparison between MNI original BM and improved BM using synthetic tumor simulations. Using the traveling time formulation in equations 12, 13, and 14, we simulated four synthetic tumor evolutions using both the BMs within the simulations. Each simulation was started from a voxel with a asymptotic tumor growth speed ( $v = 2\sqrt{d_w\rho}$ ) of  $v = 24 \text{ mm/year}$ ,  $\rho = 6 \text{ 1/year}$ ,  $d_w = 24 \text{ mm}^2/\text{year}$ ,  $T_0 = 1 \text{ day}$  (tumor age), and  $d_g = d_w/10 \text{ mm}^2/\text{year}$  [14, 29, 30].

## 5 Results

A total of 111963 voxels have been redefined as CSF by the expert, representing 2% of the total number of brain voxels. Despite that this ratio is very small, we show now the importance of these corrections by comparing the growth patterns obtained with simulations using the baseline BM (original MNI 152) versus the improved BM for 4 different starting points.

We first selected a starting point in the deep white matter of the anterior middle frontal gyrus (see Figure 2). In this situation, there was no significant difference in the growth patterns between baseline BM and improved BM simulations.

In Figure 3, the tumor starting point was chosen in the right frontal operculum, pars triangularis of the right inferior frontal gyrus. When using the original MNI 152 BM, the tumor invaded the right insula in the first year of tumor growth, whereas the insula remained free of tumor after two years of growth when using our improved BM. This latter tumor growth pattern better depicts what is observed on a real patient (see Figure 3). Figure 4 illustrates tumor growth in the right temporal lobe. The starting point of the simulated tumor was set in the superior temporal gyrus. As seen in the coronal section

on the original BM, the virtual tumor started to invade the middle temporal gyrus during the first year of tumor growth, as tumor cells could find a way to go through the superior temporal sulcus. The simulated tumor using the improved BM clearly shows no tumor invasion of the middle temporal gyrus and the growth remained confined to the superior temporal gyrus as observed on a real patient (see Figure 4).

## 6 Discussion

Computational modeling of glioma growth has recently emerged as an active field of biomathematics. The aim is to build a patient-specific virtual tumor, whose evolution is as close as possible to the real patient tumor. On this perfect virtual copy, several treatment sequences could be simulated, helping to select the optimal regimen. However, there is currently a huge gap between advances in numerical simulations and their effective use in clinical practice, and actually, very few studies attempted to evaluate the veracity of virtual glioma growth patterns [12, 15].

In this paper, we showed the difference in simulated growth patterns when using two different templates of segmented CSF spaces, obtained from a baseline and an expert-revised version of the MNI 152 atlas. The mismatch between real and simulated tumors was minimal when using the expert-revised template. This result emphasizes that detailed anatomy has to be taken into account in computational models. Here, anatomical inaccuracies of sulcal anatomy in the baseline template allow virtual glioma cells to cross a sulcus - that should normally not be crossed by real glioma cells -, leading to unrealistic shapes of simulated tumors. Of course, the difference is especially great for tumors with a starting point close to important sulci. Our results reinforce the idea that glioma simulations cannot be purely based on patient images and require anatomical information from atlases. Until advances in image analysis tools enable an automated and reliable identification of gyri and sulci, it is indeed unrealistic to perform manual segmentation of CSF spaces for each patient case. The simplest way to overcome this issue is to register all patient images in the reference space, perform the simulations in the reference space, and project the results back to the patient space. However, this approach might not always produce good results due to a possible non-correspondence between the patient and atlas geometries. The reverse method of registering the atlas onto the patient space is an alternative, but it carries the risk of recreating artificial bridges of gray matter between the two flanks of sulci. Hence this paper has important consequences regarding the elaboration of an efficient pipeline for patient-specific tumor growth simulations. Moreover, previous works that did not make use of an expert-revised segmentation of CSF spaces could be of limited value. For example, it has been proposed to use the proliferation-diffusion model to determine the starting point of a patient glioma [16]. The starting point is indeed key information that can be used to find spatially distinct clusters of glioma [15] arising from different cells of origin, with distinct patterns of recurrence and prognosis [17, 1]. This paper



shows that inferring tumor starting points by solving the inverse problem of the proliferation-diffusion equation is meaningless if the CSF template has not been carefully designed to take into account precise sulcal anatomy.

## 7 Conclusion

We have shown the importance of using expert-revised templates when dealing with glioma computational simulations. We invite researchers to make use of the presented map of CSF spaces in their simulations of tumor growth, or to give in the methods section how their CSF segmentation was obtained. Clinicians will not trust biomathematical models predictions unless anatomical knowledge is adequately incorporated in the modeling processes.

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### Compare BMs

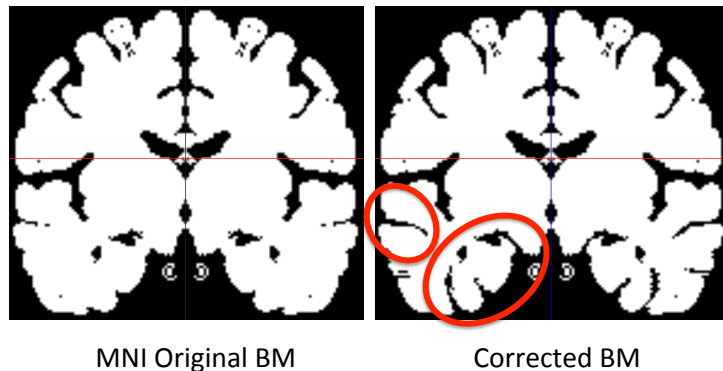


Fig. 1: MNI 152 original BM vs improved BM. Left, the MNI 152 original BM is displayed. Right, the improved BM is shown with the changes highlighted by red circles.

### Synthetic Simulation #1

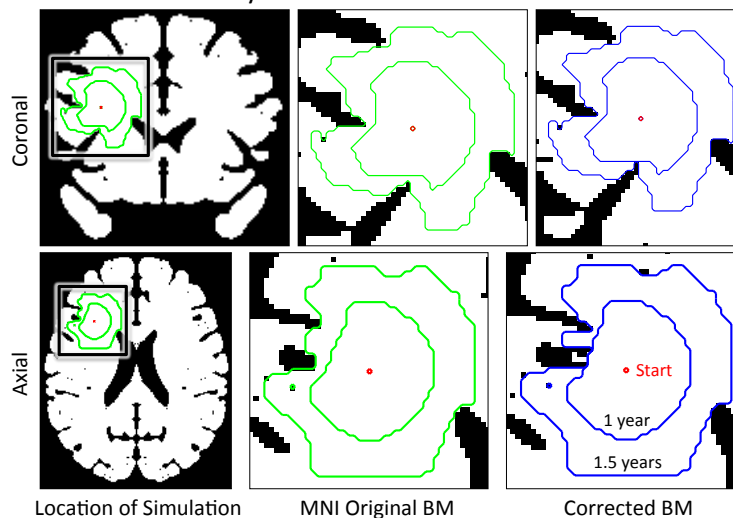


Fig. 2: Comparison between MNI 152 original BM and improved BM using synthetic tumor simulation #1. The BMs are the background of each image. Left images show the location in the BM where this synthetic tumor was simulated. On the right bottom is displayed a time map (shown for 1 and 1.5 years) for this synthetic tumor that was started from a single voxel (red). Notice that the simulations run using the original MNI 152 BM and improved MNI 152 BM are the same for a tumor growing in the white matter of anterior middle frontal gyrus (2 cm lateral to the frontal horn).

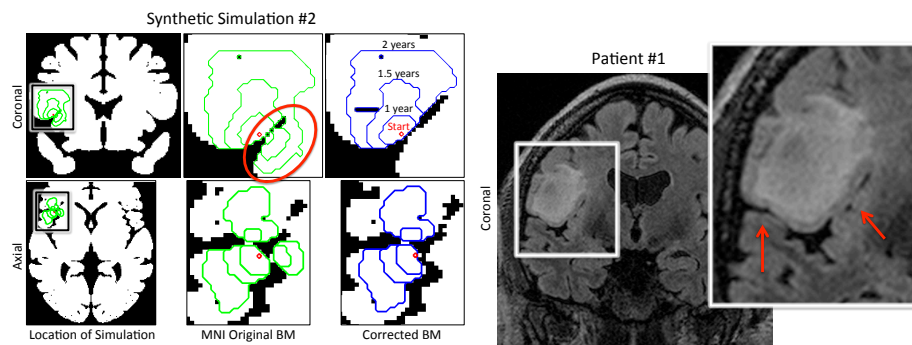


Fig. 3: Left: Comparison between MNI 152 original BM and improved BM using synthetic tumor simulation #2. The BMs are the background of each image. Left images show the location in the BM where this synthetic tumor was simulated. On the right top is displayed a time map (shown for 1, 1.5, and 2 years) for this synthetic tumor that was started from a single voxel (red). A red circle is drawn around an area where the synthetic tumor grew because the MNI 152 original BM (background) was incorrect. Right is displayed the simulation which used the improved BM where this synthetic tumor did not grow across the sylvian fissure incorrectly. Right: Patient #1 had a tumor in the same place as where the synthetic simulation #2 was grown. This demonstrates the importance of the improved BM as there was indeed no tumor growth into the insular and superior temporal gyrus (red arrows).

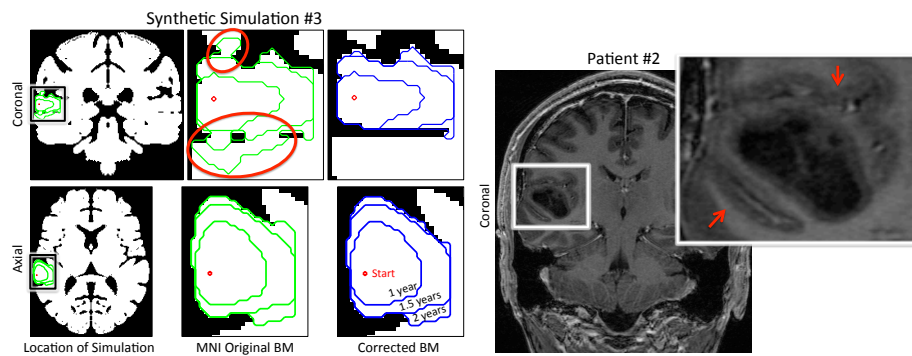


Fig. 4: Left: Comparison between MNI 152 original BM and improved BM using synthetic tumor simulation #3. The BMs are the background of each image. Left images show the location in the BM where this synthetic tumor was simulated. On the right bottom is displayed a time map (shown for 1, 1.5, and 2 years) for this synthetic tumor that was started from a single voxel (red). A red circle is drawn around an area where the synthetic tumor grew because the MNI 152 original BM (background) was incorrect. Right is displayed the simulation which used the improved BM where the synthetic tumor did not grow across the sulci incorrectly. Right: Patient #2 had a tumor in the same place as where the synthetic simulation #3 was grown. This demonstrates the importance of the improved BM in the superior temporal gyrus, as the tumor growth remained confined to the superior temporal gyrus, with no growth across the superior temporal sulcus and sylvian fissure (red arrows).