

Boundary conditions control in ORCA2

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Boundary conditions control in ORCA2

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Journée thématique "Que peuvent attendre les modélisateurs de l'assimilation de données ?" Paris, le 12 février 2013

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ORCA-2 configuration of NEMO

- $182 \times 149 \times 31$ nodes in curvilinear (x, y) coordinates;
- z levels with partial steps at the bottom;
- leap-frog scheme with Asselin filter;
- implicit surface pressure gradient with External Gravity Waves filter;
- implicit vertical diffusion with TKE Turbulent Closure Scheme;
- Solar Radiation + Geothermal Heating + BBL + Surface evaporation/precipitation;
- surface wind stress.

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$$\begin{split} \frac{\partial u}{\partial t} &= \left(S_x S_y v\right) S_y(\omega + f) - D_x \frac{S_x u^2 + S_y v^2}{2} - S_z \left(S_x w D_z u\right) + D_x A_u^h \xi + D_y A_u^h \omega + \\ &+ g \int_0^z D_x S_z \rho(x, y, \zeta) d\zeta + D_{zz} (A_u^z u) + g D_x (\eta + T_c \phi) \\ \frac{\partial T}{\partial t} &= -D_x (u S_x T) - D_y (v S_y T) - D_z (w S_z T) + A_T^h \left(D_x D_x T + D_y D_y T\right) + \\ &+ D_{zz} (A_T^z T) + \text{Solar Radiation} + \text{Geothermal Heating} + \text{BBL} \\ \xi &= D_x u + D_y v, \quad \omega = D_y u - D_x v, \quad w = \int_H^z \xi(x, y, \zeta) d\zeta; w(x, y, H) = 0 \end{split}$$

Interpolations and Derivatives

$$(Sw)_{k+1/2} = \frac{w_{k+1} + w_k}{2} \ k = 1, \dots, K-1$$
$$(DT)_k = \frac{T_{k+1/2} - T_{k-1/2}}{h} \ k = 1, \dots, K-1$$

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$$\begin{aligned} \frac{\partial u}{\partial t} &= \left(S_x S_y v\right) S_y(\omega + f) - D_x \frac{S_x u^2 + S_y v^2}{2} - S_z \left(S_x w D_z u\right) + D_x A_u^h \xi + D_y A_u^h \omega + \\ &+ g \int_0^z D_x S_z \rho(x, y, \zeta) d\zeta + D_{zz} (A_u^z u) + g D_x (\eta + T_c \phi) \\ \frac{\partial T}{\partial t} &= -D_x (u S_x T) - D_y (v S_y T) - D_z (w S_z T) + A_T^h \left(D_x D_x T + D_y D_y T\right) + \\ &+ D_{zz} (A_T^z T) + \text{Solar Radiation} + \text{Geothermal Heating} + \text{BBL} \\ \xi &= D_x u + D_y v, \quad \omega = D_y u - D_x v, \quad w = \int_H^z \xi(x, y, \zeta) d\zeta; w(x, y, H) = 0 \end{aligned}$$

Interpolations and Derivatives Modified Near the boundary

$$(Sw)_{k+1/2} = \frac{w_{k+1} + w_k}{2}, \ k = 1, \dots, K-2, \ (Sw)_{1/2} = \alpha_0^S + \alpha_1^S w_0 + \alpha_2^S w_1$$

$$(DT)_k = \frac{T_{k+1/2} - T_{k-1/2}}{h}, \ i = 2, \dots, K-2, \ (DT)_1 = \alpha_0^D + \frac{\alpha_1^D T_{1/2} + \alpha_2^D T_{3/2}}{h}$$

$$\underbrace{\begin{array}{c} T_{1/2} & T_{3/2} & T_{5/2} & T_{7/2} \\ w_0 & w_1 & w_2 & w_3 \end{array}}_{W_K - 3} \cdots \underbrace{\begin{array}{c} T_{K-5/2} & T_{K-3/2} & T_{K-1/2} \\ w_{K-3} & w_{K-2} & w_{K-1} & w_K \\ w_{K-3} & w_{K-2} & w_{K-1} & w_K \end{array}}$$

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Boundary conditions control for ORCA2

$$\begin{aligned} \frac{\partial u}{\partial t} &= \left(S_x S_y v\right) S_y(\omega + f) - D_x \frac{S_x u^2 + S_y v^2}{2} - S_z \left(S_x w D_z u\right) + D_x A_u^h \xi + D_y A_u^h \omega + \\ &+ g \int_0^z D_x S_z \rho(x, y, \zeta) d\zeta + D_{zz} (A_u^z u) + g D_x (\eta + T_c \phi) \\ \frac{\partial T}{\partial t} &= -D_x (u S_x T) - D_y (v S_y T) - D_z (w S_z T) + A_T^h \left(D_x D_x T + D_y D_y T\right) + \\ &+ D_{zz} (A_T^z T) + \text{Solar Radiation} + \text{Geothermal Heating} + \text{BBL} \\ \xi &= D_x u + D_y v, \quad \omega = D_y u - D_x v, \quad w = \int_H^z \xi(x, y, \zeta) d\zeta; w(x, y, H) = \alpha_0(x, y) \end{aligned}$$

Vertical velocity

$$\begin{split} w_{i,j,K-1} &= \alpha_0^{w^b} - \alpha_1^{w^b} h z_{i,j,K-1/2} \xi_{i,j,K-1/2} \\ w_{i,j,k-1} &= w_{i,j,k} - h z_{i,j,k-1/2} \xi_{i,j,k-1/2} \quad \forall k : 2 \le k \le K-1 \\ w_{i,j,0} &= w_{i,j,1} + \alpha_0^{w^s} - \alpha_1^{w^s} h z_{i,j,1/2} \xi_{i,j,1/2} \end{split}$$



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Vertical diffusion

$$\frac{\partial}{\partial z} A_{u}^{z} \frac{\partial u}{\partial z} \quad \text{is replaced by} \\ \left(D_{zz}u \right)_{i,j,1/2} = \frac{(A_{u}^{2})_{1}}{hz_{1}hz_{1/2}} (\alpha_{2}^{DzzU^{S}} u_{3/2} - \alpha_{1}^{DzzU^{S}} u_{1/2}) \\ \left(D_{zz}u \right)_{i,j,k-1/2} = \frac{1}{hz_{k-1/2}} \left(\frac{(A_{u}^{z})_{k}}{hz_{k}} (u_{k+1/2} - u_{k-1/2}) - \frac{(A_{u}^{z})_{k-1}}{hz_{k-1}} (u_{k-1/2} - u_{k-3/2}) \right) \\ \left(D_{zz}u \right)_{i,j,K-1/2} = \frac{1}{hz_{K-1/2}} \left[\alpha_{2}^{DzzU^{b}} \frac{(A_{u}^{z})_{K-1}}{hz_{K-1}} u_{K-1/2} - \alpha_{1}^{DzzU^{b}} \left(\frac{(A_{u}^{z})_{K}}{hz_{K}} + \frac{(A_{u}^{z})_{K-1}}{hz_{K-1}} \right) u_{K-3} \right] \\ \frac{\partial u}{\partial z} \Big|_{w_{0}} = \alpha_{0}^{DzzU^{S}} + \frac{\tau_{x}}{hz_{1}\rho_{0}}, \quad \frac{\partial v}{\partial z} \Big|_{w_{0}} = \alpha_{0}^{DzzU^{S}} + \frac{\tau_{y}}{hz_{1}\rho_{0}}, \quad \frac{\partial T}{\partial z} \Big|_{w_{0}} = \frac{\partial DzzT^{S}}{\partial z} \Big|_{w_{0}} = \alpha_{0}^{DzzT^{S}} \right] \\ u_{bottom} = v \Big|_{bottom} = \alpha_{0}^{DzzU^{b}} T \Big|_{bottom} = S \Big|_{bottom} = \alpha_{0}^{DzzT^{b}} \right)$$
(1)

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The models solution depend on initial and boundary conditions :

$$\frac{\partial T}{\partial t} = -D_x(uS_xT) - D_y(vS_yT) - \frac{D_z^{(\alpha)}}{D_z^{(\alpha)}}(wS_z^{(\alpha)}T) + A_T^h\left(D_{xx}T + D_{yy}T\right) + \frac{Dzz^{(\alpha)}}{D_z^{(\alpha)}}(A_T^z)T$$

• The model $x(t) = \mathcal{M}_{0,t}(x_0, \alpha)$

We calculate the derivatives and their adjoints with respect to

 x_0, α

by TAPENADE 3.6 (Tropics team, INRIA) that allows us

- to avoid a HUGE development/coding (a double of the classical one, at least)
- to obtain immediately the derivative with respect to any parameter we want.

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Adjoint

TAPENADE 3.6 (Tropics team, INRIA) with the Memory Usage Optimization:

search for push/pop

replace by

CALL PUSHREAL8ARRAY(sold, nx*ny*nz) CALL PUSHREAL8ARRAY(told, nx*ny*nz) CALL PUSHREAL8ARRAY(vold, nx*ny*nz) CALL PUSHREAL8ARRAY(uold, nx*ny*nz) CALL PUSHREAL8ARRAY(uold, nx*ny*nz) CALL PUSHREAL8ARRAY(sh, nx*ny) CALL PUSHREAL8ARRAY(sh, nx*ny*nz) CALL PUSHREAL8ARRAY(th, nx*ny*nz) CALL PUSHREAL8ARRAY(vh, nx*ny*nz) CALL PUSHREAL8ARRAY(vh, nx*ny*nz) CALL PUSHREAL8ARRAY(uh, nx*ny*nz) $call push_uvts(u,v,t,s,ssh)$

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 $Procedure \ push/pop_uvts(u,v,t,s,ssh):$

- does not push n 1 step and pops appropriate values (divides the required memory by 2)
- does not push u, v, t, s in lower level routines
- does not push values on continents (divides by 2)
- pushes values in Real*4 format (divides by 2)
- eventually pushes only odd timesteps and interpolate when poping (divides by 2)

Total reduction of required memory is up to 25 times.

10 hours window \implies 10 days window.

ECMWF data issued from Jason-1 and Envisat altimetric missions and ENACT/ENSEMBLES data banque.



The model: $x_N = \mathcal{M}_{0,N}(x_0, \alpha)$ with $x = (u, v, T, S, ssh)^T$

Cost function ${\cal J}$

$$U = ||x_0 - x_{bgr}||_{B^{-1}}^2 + ||\alpha - \alpha_{bgr}||_{B^{-1}}^2 + \sum_{n=0}^N t_n ||\mathcal{HM}_{0,n}(x_0, \alpha) - y_n||_{R^{-1}}^2$$

Matrices: $B^{-1} = diag(10^{-4})$, $R^{-1} = diag(1/\sigma_u, 1/\sigma_v, 1/\sigma_T, 1/\sigma_S, 1/\sigma_{ssh})$ where $\sigma_u^2 = \frac{1}{N_{obs}} \sum (u_{obs} - u_{bgr})^2$ Minimization is performed by M1QN3 (JC Gilbert, C.Lemarechal)

Data Assimilation – Forecast

Assimilation window — 10 days (Jan. 1-10, 2006), Test time — 20 or 30 days (Jan. 1-31, 2006).

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Distance Model-Observations

The model: $x(t) = \mathcal{M}_{0,t}(x_0, \alpha)$ with $x = (u, v, T, S, ssh)^T$

Distance:
$$\xi(t) = \sum_{n=0}^{t} \|\mathcal{HM}_{0,n}(x_0, \alpha) - y_n\|_{R^{-1}}$$

Convergence of J and evolution of ξ



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Modified formula

$$\begin{aligned} w_{i,j,K-1} &= \alpha_0^{w^b} - \alpha_2^{w^b} h z_{i,j,K-1/2} \xi_{i,j,K-1/2} \\ w_{i,j,k-1} &= w_{i,j,k} - h z_{i,j,k-1/2} \xi_{i,j,k-1/2} \quad \forall k : 1 \le k \le K-2 \\ w_{i,j,0} &= w_{i,j,1} + \alpha_0^{w^s} - \alpha_2^{w^s} h z_{i,j,1/2} \xi_{i,j,1/2} \end{aligned}$$

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BC for the vertical velocity

α for the vertical velocity w. North Atlantic.



α_0 on the surface





α_2 on the surface



α_2 on the bottom Boundary conditions control for ORCA2

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North Atlantic, January, 30, 2006, surface



Vertical velocity



North Atlantic, January, 30, 2006, y - z section



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Vertical velocity



North Atlantic, January, 30, 2006, x - z section



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Tourbillon

Levels z = 28 and z = 29



Velocity u



Velocity u



Velocity v



Velocity w



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$$\begin{array}{lll} \left. \frac{\partial u}{\partial z} \right|_{w_0} &=& \left. \alpha_0^{DzzU^s} + \frac{\tau_x}{hz_1\rho_0}, \quad \left. \frac{\partial v}{\partial z} \right|_{w_0} = \alpha_0^{DzzU^s} + \frac{\tau_y}{hz_1\rho_0}, \\ \\ u|_{bottom} &=& v|_{bottom} = \alpha_0^{DzzU^b} \end{array}$$

North Atlantic



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Velocity components



North Atlantic, January, 30, 2006, Velocity u, y - z section



North Atlantic

Modification of the SSH in the North Atlantic is strongly related to the boundary conditions of u and v especially on the bottom.

Only α_0 on the Bottom for u and v, only in the Vertical diffusion

$$\begin{aligned} \frac{\partial}{\partial z} A_{u}^{z} \frac{\partial u}{\partial z} & \text{ is replaced by} \\ \left(D_{zz} u \right)_{i,j,1/2} &= \frac{(A_{u}^{z})_{1}}{hz_{1}hz_{1/2}} (u_{3/2} - u_{1/2}) \\ \left(D_{zz} u \right)_{i,j,k-1/2} &= \frac{1}{hz_{k-1/2}} \left(\frac{(A_{u}^{z})_{k}}{hz_{k}} (u_{k+1/2} - u_{k-1/2}) - \frac{(A_{u}^{z})_{k-1}}{hz_{k-1}} (u_{k-1/2} - u_{k-3/2}) \right) \\ \left(D_{zz} u \right)_{i,j,K-1/2} &= \frac{1}{hz_{K-1/2}} \left[\frac{(A_{u}^{z})_{K-1}}{hz_{K-1}} u_{K-1/2} - \left(\frac{(A_{u}^{z})_{K}}{hz_{K}} + \frac{(A_{u}^{z})_{K-1}}{hz_{K-1}} \right) u_{K-3/2} \right] \\ & u|_{bottom} = \alpha_{0}^{u} \quad v|_{bottom} = \alpha_{0}^{v} \end{aligned}$$
(2)

Control space dimensionInitial conditions:1 707 245Full vertical boundary:1 197 792Only bottom:33 272

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SSH in the restrained control experiment

North Atlantic



SSH in the restrained control experiment

North Pacific



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Boundary conditions control for ORCA2

Extending the set of control parameters we can

- find a way to compensate model errors
- showing the most influent parameter and the most important geographical regions.

Automatic adjoint code generation helps us

- to generate TLM/AM almost immediately,
- to avoid a HUGE development/coding,
- to obtain immediately the derivative with respect to any parameter we want.

http://www-ljk.imag.fr/membres/Kazantsev/orca2/index.html

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