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Chapter 3

Time Granularity

Jérôme Euzenat & Angelo Montanari

A temporal situation can be described at different levels of abstraction depending on the accuracy required or the available knowledge. Time granularity can be defined as the resolution power of the temporal qualification of a statement. Providing a formalism with the concept of time granularity makes it possible to model time information with respect to differently grained temporal domains. This does not merely mean that one can use different time units, e.g., months and days, to represent time quantities in a unique flat temporal model, but it involves more difficult semantic issues related to the problem of assigning a proper meaning to the association of statements with the different temporal domains of a layered temporal model and of switching from one domain to a coarser/finer one. Such an ability of providing and relating temporal representations at different “grain levels” of the same reality is both an active research theme and a major requirement for many applications (e.g., integration of layered specifications and agent communication).

After a presentation of the general requirements of a multi-granular temporal formalism, we discuss the various issues and approaches to time granularity proposed in the literature. We focus our attention on the main existing formalisms for representing and reasoning about quantitative and qualitative time granularity: the set-theoretic framework developed by Bettini et al. [Bettini *et al.*, 2000] and the logical approach systematically investigated by Montanari et al. [Montanari, 1996; Franceschet, 2002] for quantitative time granularity, and Euzenat’s relational algebra granularity conversion operators [Euzenat, 2001] for qualitative time granularity. We present in detail the achieved results, we outline the open issues, and we point out the links that connect the different approaches. In the last part of the chapter, we describe some applications exploiting time granularity, and we briefly discuss related work in the areas of formal methods, temporal databases, and data mining.

3.1 Introduction

The usefulness of the addition of a notion of time granularity to representation languages is widely recognized. As an example, let us consider the problem of providing a logical specification of a wide-ranging class of real-time reactive systems whose components have dynamic behaviors regulated by very different — even by orders of magnitude — time constants (*granular systems* for short) [Montanari, 1996]. This is the case, for instance, of a pondage power station that consists of a reservoir, with filling and emptying times of days or weeks, generator units, possibly changing state in a few seconds, and electronic control

devices, evolving in milliseconds or even less [Corsetti *et al.*, 1991a]. A complete specification of the power station must include the description of these components and of their interactions. A natural description of the temporal evolution of the reservoir state will probably use days: “During rainy weeks, the level of the reservoir increases 1 meter a day”. The description of the control devices behavior may use microseconds: “When an alarm comes from the level sensors, send an acknowledge signal in 50 microseconds”. We say that systems of such a type have *different time granularities*. It is not only somewhat unnatural, but also sometimes impossible, to compel the specifier of these systems to use a unique time granularity, microseconds in the previous example, to describe the behavior of all the components. For instance, the requirement that “the filling of the reservoir must be completed within m days” can be hardly assumed to be equivalent to the requirement that “the filling of the reservoir must be completed within n microseconds”, for a suitable n (we shall discuss in detail the problems involved in such a rewriting in the next section). Since a good language must allow the specifier to easily and precisely describe all system requirements, different time granularities must be a feature of a specification language for granular systems.

A complementary point of view on time granularity is also possible: besides an important feature of a representation language, time granularity can be viewed as a formal tool to investigate the definability of meaningful timing properties, such as density and exponential grow/decay, as well as the expressiveness and decidability of temporal theories [Montanari *et al.*, 1999]. In this respect, the number and organization of layers (single vs. multiple, finite vs. infinite, upward unbounded vs. downward unbounded) of the underlying temporal structure plays a major role: certain timing properties can be expressed using a single layer; others using a finite number of layers; others only exploiting an infinite number of layers. In particular, finitely-layered metric temporal logics can be used to specify timing properties of granular systems composed by a finite number of differently-grained temporal components, which have been fixed once and for all (n -layered temporal structures). Furthermore, if provided with a rich enough layered structure, they suffice to deal with conditions like “ p holds at all even times of a given temporal domain” that cannot be expressed using flat propositional temporal logics [Emerson, 1990] (as a matter of fact, a 2-layered structure suffices to capture the above condition). ω -layered metric temporal logics allow one to express relevant properties of infinite sequences of states over a single temporal domain that cannot be captured by using flat or finitely-layered temporal logics. This is the case, for instance, of conditions like “ p holds at all times 2^i , for all natural numbers i , of a given temporal domain”.

The chapter is organized as follows. In Section 3.2, we introduce the general requirements of a multi-granular temporal formalism, and then we discuss the different issues and approaches to time granularity proposed in the literature. In Sections 3.3 and 3.4, we illustrate in detail the two main existing formal systems for representing and reasoning about quantitative time granularity: the set-theoretic framework for time granularity developed by Bettini *et al.* [Bettini *et al.*, 2000] and the logical approach systematically explored by Montanari *et al.* [Montanari, 1996; Franceschet, 2002]. In Section 3.5, we present the relational algebra granularity conversion operators proposed by [Euzenat, 2001] to deal with qualitative time granularity and we briefly describe the approximation framework outlined by Bittner [Bittner, 2002]. In Section 3.6, we describe some applications exploiting time granularity, while in Section 3.7 we briefly discuss related work. The concluding remarks provide an assessment of the work done in the field of time granularity and give an indication

of possible research directions.

3.2 General setting for time granularity

In order to give a formal meaning to the use of different time granularities in a representation language, two main problems have to be solved: the qualification of statements with respect to time granularity and the definition of the links between statements associated with a given time granularity, e.g., *days*, and statements associated with another granularity, e.g., *microseconds* [Montanari, 1996]. Sometimes, these problems have an obvious solution that consists in using *different time units* — say, months and minutes — to measure time quantities in a *unique model*. In most cases, however, the treatment of different time granularities involves more difficult semantic problems. Let consider, for instance, the sentence: “every month, if an employee works, then he gets his salary”. It could be formalized, in a first-order language, by the following formula:

$$\forall t_m, emp(work(emp, t_m) \rightarrow get_salary(emp, t_m)),$$

with an obvious meaning of the used symbols, once it is stated that the subscript m denotes the fact that t is measured by the time unit of *months*.

Another requirement can be expressed by the sentence: “an employee must complete every received job within 3 days”. It can be formalized by the formula:

$$\forall t_d, emp, job(get_job(emp, job, t_d) \rightarrow job_done(emp, job, t_d + 3)),$$

where the subscript d denotes that t is measured by the time unit of *days*.

Assume now that the two formulas are part of the specification of the same office system. We need a *common model* for both formulas. As done before, we could choose the finest temporal domain, i.e., the set of (times measured by) *days*, as the common domain. Then, a term labeled by m would be translated into a term labeled d by multiplying its value by 30. However, the statement “every month, if an employee works, then he gets his salary” is clearly different from the statement “every day, if an employee works, then he gets his salary”. In fact, working for a month means that one works for 22 days in the month, whereas getting a monthly salary means that there is one day when one gets the salary for the month. Similarly, stating that “every day of a given month it rains” does not mean, in general, that “it rains for all seconds of all days of the month”. On the contrary, if one states that “a car has been moving for three hours at a speed greater than 30 km per hour”, he usually means that for all seconds included in the considered three hours the car has been moving at the specified speed. The above examples show that the interpretations of temporal statements are likely to change when switching from one time granularity to another one. The addition of the concept of time granularity is thus necessary to allow one to build granular temporal models by referring to the natural scale in any component of the model and by properly constraining the interactions between differently-grained components.

Further difficulties arise from the *synchronization problem* of temporal domains [Corsetti *et al.*, 1991a]. Such a problem can be illustrated by the following examples. Consider the sentence “tomorrow I will eat”. If one interprets it in the domain of hours, its meaning is that there will be several hours, starting from the next midnight until the following one, when it will be true that I eat, *no matter in which hour of the present day this sentence is claimed*.

Thus, if the sentence is claimed at 1 a.m., it will be true that “I eat” at some hours t whose distance d from the current hour is such that $23 \leq d < 47$. Instead, if the same sentence is claimed at 10 p.m. of the same day, d will be such that $2 \leq d < 26$. Consider now the sentence “dinner will be ready in one hour”. If it is interpreted in the domain of minutes, its meaning is that dinner will be ready in 60 minutes *starting from the minute when it is claimed*. Therefore, if the sentence is claimed at minute, say, 10, or 55, of a given hour, it will be always true that “dinner is ready” at a minute t whose distance d from the current minute is *exactly* 60 minutes. Clearly, the two examples require two different semantics.

Thus, when the granularity concept is applied to time, we generally assume a set of differently-grained domains (or layers) with respect to which the situations are described and some operators relating the components of the multi-level description. The resulting system will depend on the language in which situations are modeled, the properties of the layers, and the operators. Although these elements are not fully independent, we first take into consideration each of them separately.

3.2.1 Languages, layers, operators

The distinctive features of a formal system for time granularity depend on some basic decisions about the way in which one models the relationships between the representations of a given situation with respect to different granularity layers.

Languages. The first choice concerns the language. One possibility is to use the same language to describe a situation with respect to different granularity layers. As an example, the representations associated with the different layers can use the same temporal logic or the same algebra of relations. In such a way, the representations of the same situation at different abstraction levels turn out to be *homogeneous*. Another possibility is to use different languages at different levels of abstraction, thus providing a set of *hybrid* representations of the same situation. As an example, one can adopt a metric representation at the finer layers and a qualitative one at the coarser ones.

Layers. Any formal system for time granularity must feature a number of different (granularity) layers. They can be either explicitly introduced by means of suitable linguistic primitives or implicitly associated with the different representations of a given situation.

Operators. Another choice concerns the operators that the formal system must encompass to deal with the layered structure. In this respect, one must make provision for at least two basic operators:

contextualization to select a layer;

projection to move across layers.

These operators are independent of the specific formalism one can adopt to represent and to reason about time granularity, that is, each formalism must somehow support such operators. They are sufficient for expressing fundamental questions one would like to ask to a granular representation:

- converting a representation from a given granularity to another one (how would a particular representation appear under a finer or coarser granularity?);
- testing the compatibility of two representations (is it possible that they represent the same situation under different granularities?);
- comparing the relative granularities of two representations (which is the coarser/finer representation of a given situation?).

Internal vs. external layers. Once the relevance of these operators is established, it must be decided if the granularity applies within a formalism or across formalisms. In other terms, it must be decided if an existing formalism will be extended with these new operators or if these operators will be defined and applied from the outside to representations using existing formalisms. Both these alternatives have been explored in the literature:

- Some solutions propose an internal extension of existing formalisms to explicitly introduce the notion of granularity layer in the representations (see Sections 3.4.1 and 3.4.2 [Ciapessoni *et al.*, 1993; Montanari, 1996; Montanari *et al.*, 1999]), thus allowing one to express complex statements combining granularity with other notions. The representations of a situation with respect to different granularity layers in the resulting formalism are clearly homogeneous.
- Other solutions propose an external apprehension which allows one to relate two descriptions expressed in the same formalism or in different formalisms (see Sections 3.3, 3.4.3, and 3.5 [Euzenat, 1995b; Fiadeiro and Maibaum, 1994; Franceschet, 2002; Franceschet and Montanari, 2004]). This solution has the advantage of preserving the usual complexity of the underlying formalism, as far as no additional complexity is introduced by granularity.

3.2.2 Properties of languages

The whole spectrum of languages for representing time presented in this book is available for expressing the sentences subject to granularity. Here we briefly point out some alternatives that can affect the management of granularity.

Qualitative and quantitative languages. There can be many structures on which a temporal representation language is grounded. These structures can be compared with that of mathematical spaces:

set-theory when the language takes into account containment (i.e. set-membership);

topology when the language accounts for connexity and convexity;

metric spaces when the language takes advantage of a metric in order to quantify the relationship (distance) between temporal entities.

vector spaces when the language considers alignment and precedence (with regard to an alignment). As far as time is considered as totally ordered, the order comes naturally.

A quantitative representation language is generally a language which embodies properties of metric and vector spaces. Such a language allows one to precisely define a displacement operator (of a particular distance along an axis). A qualitative representation language does not use a metric and thus one cannot precisely state the position of objects. For instance, Allen’s Interval Algebra (see Chapter 1) considers notions from vector (before) and topological (meets) spaces.

Expressive power. The expressive power of the languages can vary a lot (this is true in general for classical temporal representation languages, see Chapter 6). It can roughly be:

exact and conjunctive when each temporal entity is localized at a particular known position (a is ten minutes after b) and a situation is described by a conjunction of such sentences;

propositional when the language allows one to express conjunction and disjunction of propositional statements (a is before or after b); this also applies to constrained positions of entities (a is between ten minutes and one hour after b);

first-order when the language contains variables which allow one to quantify over the entities (there exists time lap x in between a and b);

“second-order” when the language contains variables which allow one to quantify over layers (there exists a layer g under which a is after b).

3.2.3 Properties of layers

As it always happens when time information has to be managed by a system, the properties of the adopted model of time influence the representation. The distinctive feature of the models of time that incorporate time granularity is the coexistence of a set \mathcal{T} of temporal domains. Such a set is called *temporal universe* and the temporal domains belonging to it are called (temporal) *layers*. Layers can be either overlapping, as in the case of `Days` and `Working Days`, since every working day is a day (cf. Section 3.3), or disjoint, as in the case of `Days` and `Weeks` (cf. Section 3.4).

Structure of time. It is apparent that the temporal structure of the layers influences the semantics of the operators. Different structures can obviously be used. Moreover, one can either constrain the layers to share the same structure or to allow different layers to have different structures.

For each layer $T \in \mathcal{T}$, let $<$ be a linear order over the set of time points in T . We confine our attention to the following temporal structures:

continuous T is isomorphic to the set of real numbers (this is the usual interpretation of time);

dense between every two different points there is a point

$$\forall x, y \in T \exists z \in T (x < y \rightarrow x < z < y);$$

discrete every point having a successor (respectively, a predecessor) has an immediate one

$$\forall x \in T((\exists y \in T(x < y) \rightarrow \exists z \in T(x < z \wedge \forall w \in T \neg(x < w < z))) \wedge (\exists y \in T(y < x) \rightarrow \exists z \in T(z < x \wedge \forall w \in T \neg(z < w < x))))).$$

Most formal systems for time granularity assume layers to be discrete, with the possible exception of the most detailed layer, if any, whose temporal structure can be dense, or even continuous (an exception is [Endriss, 2003]). The reason of this choice is that each dense layer is already at the finest level of granularity, and it allows any degree of precision in measuring time. As a consequence, for dense layers one must distinguish granularity from metric, while, for discrete layers, one can define granularity in terms of set cardinality and assimilate it to a natural notion of metric. Mapping, say, a set of rational numbers into another set of rational numbers would only mean changing the unit of measure with no semantic effect, just in the same way one can decide to describe geometric facts by using, say, kilometers or centimeters. If kilometers are measured by rational numbers, indeed, the same level of precision as with centimeters can be achieved. On the contrary, the key point in time granularity is that saying that something holds for all days in a given interval does not imply that it holds at every second belonging to the interval [Corsetti *et al.*, 1991a]. For the sake of simplicity, in the following we assume each layer to be discrete.

Global organization of layers. Further conditions can be added to constrain the global organization of the set of layers. So far, layers have been considered as independent representation spaces. However, we are actually interested in comparing their grains, that is, we want to be able to establish whether the grain of a given layer is finer or coarser than the grain of another one. It is thus natural to define an order relation \prec , called *granularity* relation, on the set of layers of \mathcal{T} based on their grains: we say that a layer T is finer (resp. coarser) than a layer T' , denoted by $T \prec T'$ (resp. $T' \prec T$), if the grain of T is finer (resp. coarser) than that of T' . There exist at least three meaningful cases:

partial order \prec is a reflexive, transitive, and anti-symmetric relation over layers;

(semi-)lattice \prec is a partial order such that, given any two layers $T, T' \in \mathcal{T}$, there exists a layer $T \wedge T' \in \mathcal{T}$ such that $T \wedge T' \prec T$ and $T \wedge T' \prec T'$, and any other layer T'' with the same property is such that $T'' \prec T \wedge T'$;

total order \prec is a partial order such that, for all $T, T' \in \mathcal{T}$, either $T = T'$ or $T \prec T'$ or $T' \prec T$.

We shall see that the set of admissible operations on layers depends on the structure of \prec .

Beside the order relation \prec , one must consider the cardinality of the set \mathcal{T} . Even though a finite number of layers suffices for many applications, there exist significant properties that can be expressed only using an infinite number of layers (cf. Section 3.4.2). As an example, an infinite number of arbitrarily fine (discrete) layers makes it possible to express properties related to temporal density, e.g., the fact that two states are distinct, but arbitrarily close.

Pairwise organization of layers. Even in the case in which layers are totally ordered, their organization can be made more precise. For instance, consider the case of a situation described with respect to the totally ordered set of granularities including *years*, *months*, *weeks*, and *days*. The relationships between these layers differ a lot. Such differences can be described through the following notions:

homogeneity when the (temporal) entities of the coarser layer consist of the same number of entities of the finer one;

alignment when the entities of the finer layer are mapped in only one entity of the coarser one.

These two notions allow us to distinguish four different cases:

year-month the situation is very neat between years and months since each year contains the same number of months (homogeneity) and each month is mapped onto only one year (alignment);

year-week a year contains a various number of weeks (non homogeneity) and a week can be mapped into more than one year (non alignment);

month-day while every day is mapped into exactly one month (alignment), the number of days in a month is variable (non homogeneity);

working week-day one can easily imagine working weeks beginning at 5 o'clock on Mondays (this kind of weeks exists in industrial plants): while every week is made of the same duration or amount of days (homogeneity), some days are mapped into two weeks (non alignment).

How the objects behave. There are several options with regard to the behavior of the objects considered by the theories. The objects can

persist when they remain the same across layers (in the logical setting, this is modeled by the Barcan formula);

change category when, moving from one layer to another one, they are transformed into objects of different size (e.g., transforming intervals into points, or vice versa, or changing an object into another of a bigger/lower dimension, see Section 3.6.4);

vanish when an object associated with a fine layer disappears in a coarser one.

3.2.4 Properties of operators

The operator that models the change of granularity is the *projection* operator. It relates the temporal entities of a given layer to the corresponding entities of a finer/coarser layer. In some formal systems, it also models the change of the interpretation context from one layer to another. The projection operator is characterized by a number of distinctive properties, including:

reflexivity (see Section 3.5.2 self-conservation p. 105 and Section 3.4.1 p. 85) constrains an entity to be able to be converted into itself;

symmetry (see Section 3.5.2 inverse compatibility p. 106 and Section 3.4.1 p. 85) states that if an entity can be converted into another one, then this latter entity can be converted back into the original one;

order-preservation (for vectorial systems, see Section 3.3 p. 69, Section 3.5.2 p. 105, and Section 3.4.1 p. 86) constrains the projection operators to preserve the order of entities among layers;

transitivity (see below) constrains consecutive applications of projection operators in any “direction” to yield the same result as a direct projection;

oriented transitivity (see Section 3.5.2 p. 106 and Section 3.4.1 downward transitivity p. 85 and upward transitivity p. 86) constrains successive applications of projection operators in the same “direction” to yield the same result as a direct projection;

downward/upward transitivity (see Section 3.4.1 pp. 85-86 and [Euzenat, 1993]) constrains two consecutive applications of the projection operators (first downward, then upward) to yield the same result as a direct downward or upward projection;

Some properties of projection operators are related to pairwise properties of layers:

contiguity (see Section 3.4.1 p. 86), or “contiguity-preservation”, constrains the projections of two contiguous entities to be either two contiguous (sets of) entities or the same entity (set of entities);

total covering (see Section 3.3 p. 69 and Section 3.4.1 p. 86) constrains each layer to be totally accessible from any other layer by projection;

convexity (see Section 3.4.1 p. 86) constrains the coarse equivalent of an entity belonging to a given layer to cover a convex set of entities of such a layer;

synchronization (see Sections 3.3 and 3.4.1), or “origin alignment”, constrains the origin of a layer to be projected on the origin of the other layers. It is called synchronization because it is related to “synchronicity” which binds all the layers to the same clock;

homogeneity (see Section 3.4.1 p. 86) constrains the temporal entities of a given layer to be projected on the same number of entities of a finer layer;

Such properties are satisfied when they are satisfied by all pairs of layers.

3.2.5 Quantitative and qualitative models

In the following we present in detail the main formal systems for time granularity proposed in the literature. We found it useful to make a distinction between quantitative and qualitative models of time granularity. Quantitative models are able to position temporal entities (or occurrences) within a metric frame. They have been obtained following either a set-theoretic approach or a logical one. In contrast, qualitative models characterize the position of temporal entities with respect to each other. This characterization is often topological or vectorial. The main qualitative approach to granularity is of algebraic nature.

The set-theoretic approach is based upon naive set theory and algebra. According to it, the single temporal domain of flat temporal models is replaced by a temporal universe, which is defined as a set of inter-related temporal layers, which is built upon its finest layer. The finest layer is a totally ordered set, whose elements are the smallest temporal units relevant to the considered application (*chronons*, according to the database terminology [Dyreson and

Snodgrass, 1994; Jensen *et al.*, 1994]); any coarser layer is defined as a suitable partition of this basic layer. To operate on elements belonging to the same layer, the familiar Boolean algebra of subsets suffices. Operations between elements belonging to different layers require a preliminary mapping to a common layer. Such an approach, originally proposed by Clifford and Rao in [Clifford and Rao, 1988], has been successively refined and generalized by Bettini *et al.* in a number of papers [Bettini *et al.*, 2000]. In Section 3.3, we shall describe the evolution of the set-theoretic approach to time granularity from its original formulation up to its more recent developments.

According to the logical approach, the single temporal domain of (metric) temporal logic is replaced by a temporal universe consisting of a possibly *infinite* set of inter-related differently-grained layers and logical tools are provided to qualify temporal statements with respect to the temporal universe and to switch temporal statements across layers. Logics for time granularities have been given both non-classical and classical formalizations. In the non-classical setting, they have been obtained by extending metric temporal logics with operators for temporal contextualization and projection [Ciapessoni *et al.*, 1993; Montanari, 1996; Montanari and de Rijke, 1997], as well as by combining linear and branching temporal logics in a suitable way [Franceschet, 2002; Franceschet and Montanari, 2003; Franceschet and Montanari, 2004]. In the classical one, they have been characterized in terms of (extensions of) the well-known monadic second-order theories of k successors and of their fragments [Montanari and Policriti, 1996; Montanari *et al.*, 1999; Franceschet *et al.*, 2003]. In Section 3.4, we shall present in detail both approaches.

The study of granularity in a qualitative context is presented in Section 3.5. It amounts to characterize the variation of relations between temporal entities that are induced by granularity changes. A number of axioms for characterizing granularity conversion operators have been provided in [Euzenat, 1993; Euzenat, 1995a], which have been later shown to be consistent and independent [Euzenat, 2001]. Granularity operators for the usual algebras of temporal relations have been derived from these axioms. Another approach to characterizing granularity in qualitative relations, associated with a new way of generating systems of relations, has recently come to light [Bittner, 2002]. The relations between two entities are characterized by the relation (in a simpler relation set) between the intersection of the two entities and each of them. Temporal locations of entities are then approximated by subsets of a partition of the temporal domain, so that the relation between the two entities can itself be approximated by the relation holding between their approximated locations. This relation (that corresponds to the original relation under the coarser granularity) is obtained directly by maximizing and minimizing the set of possible relations.

3.3 The set-theoretic approach

In this section, we present several contributions to the development of a general framework for time granularity coming from both the area of knowledge-based systems and that of database systems. We qualify their common approach as set-theoretic because it relies on a temporal domain defined as an ordered set, it builds granularities by grouping subsets of this domain, and it expresses their properties through set relations and operations over sets. In the area of knowledge representation and reasoning, the addition of a notion of time granularity to knowledge-based systems has been one of the most effective attempts at dealing with the widely recognized problem of managing periodic phenomena. Two relevant set-theoretic ap-

proaches to time granularity are the formalism of collection expressions proposed by Leban et al. [Leban *et al.*, 1986] and the formalism of slice expressions developed by Niezette and Stevenne [Niezette and Stevenne, 1992]. In the database area, time granularity emerged as a formal tool to deal with the intrinsic characteristics of calendars in a principled way. The set-theoretic approach to time granularity was originally proposed by Clifford and Rao [Clifford and Rao, 1988] as a suitable way of structuring information with a temporal dimension, independently of any particular calendric system, and, later, it has been systematically explored by Bettini et al. in a series of papers [Bettini *et al.*, 1998a; Bettini *et al.*, 1998b; Bettini *et al.*, 1996; Bettini *et al.*, 1998c; Bettini *et al.*, 1998d; Bettini *et al.*, 2000]. As a matter of fact, the set-theoretic framework developed by Bettini et al. subsumes all the other ones. In the following, we shall briefly describe its distinctive features. A comprehensive presentation of it is given in [Bettini *et al.*, 2000]

3.3.1 Granularities

The basic ingredients of the set-theoretic approach to time granularity have been outlined in Clifford and Rao's work. Even though the point of view of the authors has been largely revised and extended by subsequent work, most of their original intuitions have been preserved.

The temporal structure they propose is a temporal universe consisting of a finite, totally ordered set of temporal domains built upon some base discrete, totally ordered, infinite set which represents the smallest observable/interesting time units.

Let T^0 be the chosen base temporal domain. A temporal universe \mathcal{T} is a finite sequence $\langle T^0, T^1, \dots, T^m \rangle$ such that, for $i, j = 0, 1, \dots, m$, if $i \neq j$, then $T^i \cap T^j = \emptyset$, and, for $i = 0, 1, \dots, m-1$, T^{i+1} is a constructed intervallic partition of T^i . We say that T^{i+1} is a constructed intervallic partition of T^i if there exists a mapping $\psi_i^{i+1} : T^{i+1} \rightarrow 2^{T^i}$ which satisfies the following two properties: (i) $\psi_i^{i+1}(x)$ is a (finite) convex subset of T^i (convexity), and (ii) $\bigcup_{x \in T^{i+1}} \psi_i^{i+1}(x) = T^i$ (total covering). If we add the conditions that, for each $x \in T^{i+1}$, $\psi_i^{i+1}(x) \neq \emptyset$ and, for every pair $x, y \in T^{i+1}$, with $x \neq y$, $\psi_i^{i+1}(x) \cap \psi_i^{i+1}(y) = \emptyset$, the temporal domain T^{i+1} , under the mapping ψ_i^{i+1} , can be viewed as a partition of T^i . Furthermore, the resulting mapping ψ_i^{i+1} allows us to inherit a total order of T^{i+1} from the total order of T^i as follows (order-preservation). Given a finite closed interval S of T^i , let $first(S)$ and $last(S)$ be respectively the first and the last element of S with respect to the total order of T^i . A total order of T^{i+1} can be obtained by stating that, for all $x, y \in T^{i+1}$, $x < y$ if and only if $last(\psi_i^{i+1}(x)) < first(\psi_i^{i+1}(y))$.

In [Bettini *et al.*, 1998c; Bettini *et al.*, 1998d; Bettini *et al.*, 2000], Bettini et al. have generalized that simple temporal structure for time granularity. The framework they propose is based on a *time domain* $\langle T, \leq \rangle$, that is, a totally ordered set, which can be dense or discrete. A *granularity* g is a function from an index set I_g to the powerset of T such that:

$$\begin{aligned} \forall i, j, k \in I_g (i < k < j \wedge g(i) \neq \emptyset \wedge g(j) \neq \emptyset \Rightarrow g(k) \neq \emptyset) & \quad (\text{conservation}) \\ \forall i, j \in I_g (i < j \Rightarrow \forall x \in g(i) \forall y \in g(j) x < y) & \quad (\text{order preservation}) \end{aligned}$$

Typical examples of granularities are the business weeks which map week numbers to sets of five days (from Monday to Friday) and ignore completely Saturday and Sunday. I_g can be any discrete ordered set. However, for practical reasons, and without loss of generality, we shall consider below that it is either \mathbb{N} or an interval of \mathbb{N} .

The *origin* of a granularity is $g_0 = g(\min_{<}(I_g))$ and its *anchor* is $a \in g_0$ such that $\forall x \in g_0(a \leq x)$. The *image* of a granularity g is $Im(g) = \cup_{i \in I_g} g(i)$ and its *extent* is $Ext(g) = \{x \in T : \exists a, b \in Im(g)(a \leq x \leq b)\}$. Two granules $g(i)$ and $g(j)$ are said to be *contiguous* if and only if $\nexists x \in T(g(i) \leq x \leq g(j))$.

3.3.2 Relations between granularities

One of the important aspects of the work by Bettini et al. is the definition of many different relationships between granularities:

$$\begin{aligned}
g \trianglelefteq h &\equiv \forall j \in I_h, \exists S \subseteq I_g(h(j) = \cup_{i \in S} g(i)) && (g \text{ groups into } h) \\
g \preceq h &\equiv \forall i \in I_g, \exists j \in I_h(g(i) \subseteq h(j)) && (g \text{ is finer than } h) \\
g \sqsubseteq h &\equiv \forall i \in I_g, \exists j \in I_h(g(i) = h(j)) && (g \text{ is a subgranularity of } h) \\
g \leftrightarrow h &\equiv \exists k \in \mathbb{N} \forall i \in I_g(g(i) = h(i+k)) && (g \text{ is shift-equivalent to } h) \\
g \trianglelefteq h \text{ and } g \preceq h &&& (g \text{ partitions } h) \\
g \widehat{\sqsubseteq} h &\equiv Im(g) \subseteq Im(h) && (g \text{ is covered by } h) \\
g \trianglelefteq h \text{ and } \exists r, p \in \mathbb{Z}^+(r \leq |I_h| \wedge \forall i \in I_h(h(i) = \cup_{x=0}^k g(j_x) \\
&\quad \wedge h(i+r) \neq \emptyset \Rightarrow h(i+r) = \cup_{x=0}^k g(j_x+p))) && (g \text{ groups periodically into } h)
\end{aligned}$$

Apart from the case of shift-equivalence, all these definitions state, in different ways, that g is a more precise granularity than h . As an example, the groups into relation groups together intervals of g . In fact, it can group a subset of the elements within the interval, but in such a case the excluded elements cannot belong to any other granule of the less precise granularity. Finer than requires that all the granules of g are covered by a granule of h . So h can group granules of g , but never forget one. However, it can introduce granules that were not taken into account by g (between two g -granules). Sub-granularity can only do exactly that (i.e., it cannot group g -granules). Shift-equivalence is, in spirit, the relation holding between two granularities that are equivalent up to index renaming. It is here restricted to integer increment. Partition, as we shall see below, is the easy-behaving relationship in which the less precise granularity is just a partition of the granules of the more precise one.

It is noteworthy that all these relationships consider only aligned granularities, that is, the granules of the more precise granularity are either preserved or forgotten, but never broken, in the less precise one.

These relations are ordered by strength as below.

Proposition 3.3.1. $\forall h, g(g \sqsubseteq h \Rightarrow g \preceq h \Rightarrow g \widehat{\sqsubseteq} h)$

It also appears that the shift-equivalence is indeed the congruence relation induced by the subgranularity relation.

Proposition 3.3.2. $\forall h, g(g \leftrightarrow h \text{ iff } g \sqsubseteq h \text{ and } h \sqsubseteq g)$

It is an equivalence relation and if we consider the quotient set of granularity modulo shift-equivalence, then \sqsubseteq but also \preceq and \trianglelefteq define partial orders (and thus partition as well) and $\widehat{\sqsubseteq}$ is still a pre-order.

3.3.3 Granularity systems and calendars

For the purpose of using the granularities, it is more convenient to study granularity systems, i.e., sets of granularities related by different constraints.

A *calendar* is a set S of granularities over the same time domain that includes a granularity g such that $\forall h \in S (g \preceq h)$. Considering sets of granularities in which items can be converted, there are four important design choices:

The choice of the absolute time set \mathcal{A} dense, discrete or continuous.

Restriction on the use of the index set if it is common to all granularities, otherwise, the restriction hold between them; the authors offer the choice between \mathbb{N} or \mathbb{N}^+ . More generally, the choice can be done among index sets isomorphic to these.

Constraints on the granularities no gaps within a granule, no gaps between granules, no gaps on left/right (i.e., the granularity covers the whole domain), with uniform extent.

Constraints between granularities which can be expressed through the above-defined relationships.

They define, as their reference granularity frame, the *General Granularity on Reals* by:

- Absolute time is the set \mathbb{R} ;
- index set is \mathbb{N}^+ ;
- no restrictions on granules;
- no two granularities are in shift-equivalent.

Two particular units g_{\top} and g_{\perp} can be defined such that:

$$\forall i \in \mathbb{N}^+, g_{\perp}(i) = \emptyset \text{ and } g_{\top}(i) = \begin{cases} T & \text{if } i = 1; \\ \emptyset & \text{otherwise.} \end{cases}$$

It is shown [Bettini *et al.*, 1996] that under sensible assumptions (namely, order-preservation or convexity-contiguity-totality), the set of units is a lattice with respect to \preceq in which g_{\top} (resp. g_{\perp}) is the greatest (resp. lowest) element. In [Bettini *et al.*, 2000], it is proved that this applies to any granularity system having no two granularity shift-equivalence (i.e., $\leftrightarrow = \emptyset$). This is important because any granularity system can be quotiented by shift-equivalence.

Finally, two conversion operators on the set of granularities are defined. The *upward conversion* between granularities is defined as:

$$\forall i \in I_g, \uparrow_g^h i = \begin{cases} j & \text{if } \exists j \in I_h (g(i) \subseteq h(j)); \\ \text{undefined} & \text{otherwise.} \end{cases}$$

Notice that the upward operator is thus only defined in the aligned case expressed by the “finer than” relationship.

Proposition 3.3.3. *if $g \preceq h$, then \uparrow_g^h is always defined.*

The *downward conversion* between granularities is defined as:

$$\forall j \in I_h, \downarrow_g^h j = \begin{cases} \langle i, k \rangle & \text{if } h(j) = \cup_{x=i}^{i+k-1} g(x); \\ \text{undefined} & \text{otherwise.} \end{cases}$$

The result is thus the set of elements covered by $h(j)$. Obviously, here the ‘‘groups into’’ relation between the granularities ensures the totality of the downward conversion.

Proposition 3.3.4. *if $g \trianglelefteq h$, then \downarrow_g^h is always defined.*

3.3.4 Algebra for generating granularities

As it is usual in the database tradition, the authors investigate the many ways in which granularities can be freely generated by applying operations to other granularities. This can be used for defining the free generated system from a set of base granularities over the same temporal domain and a set of operations. With these operations will naturally come corresponding conversion operators.

Two set of operations are identified: grouping (or group-oriented) operations, which create a granularity by grouping granules of another granularity, and selection (or granule-oriented) operations, which create a granularity by selecting granules of another granularity.

These operations are informally described below. Interested readers must refer to [Bettini *et al.*, 2000] which adds new notions (label-aligned subgranularities) for facilitating their introduction.

Grouping operations are the following:

$group_m(g)$ groups m granules of a granularity g into one granule of granularity $group_m(g)$;

$alter_{i,k}^m(g, g')$ modifies granularity g such that any l^{th} granule having k additional granules of g' (g' must partition g , k can be negative);

$shift_m(g)$ creates a granularity shift-equivalent to g modulo m ;

$combine(g, h)$ creates a new granularity whose granules group granules of h belonging to the same granule of g ;

$anchor - group(g, h)$ creates a new granularity by adding to each granule of h all following granules of g before the next granule of h .

Selection operations are the following:

$subset_m^n(g)$ selects the granules of g whose index are between m and n ;

$select - up(g, h)$ selects the granules of g that contain at least one granule of h ;

$select - down_k^l(g, h)$ selects the l granules of g starting with the k^{th} in each granule of h ;

$select - by - intersect_k^l(g, h)$ selects the k granules of g starting with the l^{th} in each ordered set of granules intersecting any granule of h ;

$union(g, h)$, $intersection(g, h)$, $difference(g, h)$ are defined as the corresponding operations on the set of granules of two subgranularities of the same reference granularity.

A consequence of the choice of these operations is that the operators never create finer granularities from coarser ones (they either group granules for a coarser granularity or select a subset of the granules of one existing granularity). This can be applied, for instance, generating many granularities starting with the second granularity (directly inspired from [Bettini *et al.*, 2000]):

```

minute = group60(second)
hour = group60(minute)
USEasthour = shift-5(hour)
day = group24(hour)
week = group7(day)
busi-day = select - down15(day, week)
month = alter2+12*399,112*400(day, alter2+12*99,-112*100(day, alter2+12*3,112*4(day,
    alter11,-112(day, alter9,-112(day, alter6,-112(day, alter4,-112(day,
    alter2,-312(day, group31(day))))))
year = group12(month)
academicyear = anchor - group(day,
    select - by - intersect11(busi-day, select - down91(month)

```

As a matter of fact, these granularities can be generated in a more controlled way. Indeed, the authors distinguish three layers of granularities:

- L_1 containing the bottom granularity and all the granularities obtained by applying *group*, *alter*, and *shift* on granularities of this layer;
- L_2 including L_1 and containing all the granularities obtained by applying *subset*, *union*, *intersection*, and *difference* on granularities of this layer and selections with first operand belonging to this layer;
- L_3 including L_2 and containing all the granularities obtained by applying *combine* on granularities of this layer and *anchor - group* with the second operand on granularities of this layer.

Granularities of L_1 are full-integer labelled granularities, those of L_2 may not be labelled by all integers, but they contain no gaps within granules. These aspects, as well as the expressiveness of the generated granularities, are investigated in depth in [Bettini *et al.*, 2000].

3.3.5 Constraint solving and query answering

Wang et al. [Wang *et al.*, 1995] have proposed an extension of the relational data model which is able to handle granularity. The goal of this work is to take into account possible granularity mismatch in the context of federated databases.

An extended temporal model is a relational database in which each tuple is timestamped under some granularity. Formally, it is a set of tables such that each table is a quadruple

$\langle R, \phi, \tau, g \rangle$ such that R is a set of tuples (a relational table), g is a granularity, $\phi : \mathbb{N} \longrightarrow 2^R$ maps granules to tuples, $\tau : R \longrightarrow 2^{\mathbb{N}}$ maps tuples to granules such that $\forall t \in R, t \in \phi(i) \Rightarrow i \in \tau(t)$ and $\forall i \in \mathbb{N}, i \in \tau(t) \Rightarrow t \in \phi(i)$.

In [Bettini *et al.*, 2000], the authors develop methods for answering queries in database with granularities. The answers are computed with regard to hypotheses tied to the databases. These hypotheses allow the computation of values between two successive timestamps. The missing values can, for instance, be considered constant (persistence) or interpolated with a particular interpolation function. These hypotheses also apply to the computation of values between granularity.

The hypotheses (H) provide the way to compute the closure (\overline{D}^H) of a particular database (D). Answering a query q against a database with granularities D and hypotheses H consists in answering the query against the closure of the database ($\overline{D}^H \models q$). Instead of computing this costly closure, the authors proposes to *reduce* the database with regard to the hypotheses (i.e., to find the minimal database equivalent to the initial one modulo closure) and to add to the query formulas allowing the computation of the hypotheses.

The authors also define quantitative temporal constraint satisfaction problems under granularity whose variables correspond to points and arcs are labelled by an integer interval and a granularity. A pair of points $\langle t, t' \rangle$ satisfies a constraint $[m, n]g$ (with $m, n \in \mathbb{Z}$ and g a granularity) if and only if $\uparrow^g t$ and $\uparrow^g t'$ are defined and $m \leq \uparrow^g t - \uparrow^g t' \leq n$. These constraints cannot be expressed as a classical TCSP (see Chapter 7). As a matter of fact, if the constraint $[0 0]$ is set on two entities under the hour granularity, two points satisfy it if they are in the same hour. In terms of seconds, the positions should differ from 0 to 3600. However, $[0 3600]$ under the second granularity does not corresponds to the original constraint since it can be satisfied by two points in different hours.

The satisfaction problem for granular constraint satisfaction is NP-hard (while STP is polynomial) [Bettini *et al.*, 1996]. Indeed the modulo operation involved in the conversions can introduce disjunctive constraints (or non convexity). For instance, next business day is the convex constraint $[1 1]$, which converted in hours can yield the constraint $[1 24] \vee [49 72]$ which is dependent on the exact day of the week.

The authors propose an arc-consistency algorithm complete for consistency checking when the granularities are periodical with regard to some common finer granularity. They also propose an approximate (i.e., incomplete) algorithm by iterating the saturation of the networks of constraints expressed under the same granularity and then converting the new values into the other granularities.

The work described above mainly concerns aligned systems of granularity (i.e., systems in which the upward conversion is always defined). This is not always the case, as the week/month example illustrates it. Non-aligned granularity has been considered by several authors. Dyreson and collaborators [Dyreson and Snodgrass, 1994] define comparison operators across granularities and their semantics (this covers the extended comparators of [Wang *et al.*, 1995]): comparison between entities of different granularities can be considered under the coarser granularity (here coarser is the same as ‘‘groups into’’ above and thus requires alignment) or the finer one. They define upward and downward conversion operators across comparable granularities and the conversion across non-comparable granularities is carried out by first converting down to the greatest lower bound and then up (assuming the greatest lower bound exists and thus that the structure is a lower semi-lattice): $\downarrow_{g \wedge g'}^g \uparrow_{g \wedge g'}^{g'} x$. Comparisons across granularities (with both semantics) are implemented in terms of the

conversion operators.

3.3.6 Alternative accounts of time granularity

The set-theoretic approach has been recently revisited and extended in several directions. In the following, we briefly summarize the most promising ones.

An alternative string-based model for time granularities has been proposed by Wijzen [Wijzen, 2000]. It models (infinite) granularities as (infinite) words over an alphabet consisting of three symbols, namely, \blacksquare (filler), \square (gap), and \wr (separator), which are respectively used to denote time points covered by some granule, to denote time points not covered by any granule, and to delimit granules. Wijzen focuses his attention on (infinite) periodical granularities, that is, granularities which are left bounded and, ultimately, periodically groups time points of the underlying temporal domain. Periodical granularities can be identified with ultimately periodic strings, and they can be finitely represented by specifying a (possibly empty) finite prefix and a finite repeating pattern. As an example, the granularity *BusinessWeek* $\blacksquare\blacksquare\blacksquare\blacksquare\blacksquare\blacksquare\blacksquare\blacksquare\wr\blacksquare\blacksquare\blacksquare\blacksquare\blacksquare\blacksquare\wr\dots$ can be encoded by the empty prefix ε and the repeating pattern $\blacksquare\blacksquare\blacksquare\blacksquare\blacksquare\blacksquare\wr$. Wijzen shows how to use the string-based model to solve some fundamental problems about granularities, such as the equivalence problem (to establish whether or not two given representations define the same granularity) and the minimization problem (to compute the most compact representation of a granularity). In particular, he provides a straightforward solution to the equivalence problem that takes advantage of a suitable *aligned form* of strings. Such a form forces separators to occur immediately after an occurrence of \blacksquare , thus guaranteeing a one-to-one correspondence between granularities and strings.

The idea of viewing time granularities as ultimately periodic strings establishes a natural connection with the field of formal languages and automata. An automaton-based approach to time granularity has been proposed by Dal Lago and Montanari in [Dal Lago and Montanari, 2001], and later revisited by Bresolin et al. in [Bresolin et al., 2004; Dal Lago et al., 2003a; Dal Lago et al., 2003b]. The basic idea underlying such an approach is simple: we take an automaton \mathcal{A} recognizing a *single* ultimately periodic word $u \in \{\square, \blacksquare, \blacktriangleleft\}^\omega$ and we say that \mathcal{A} represents the granularity G if and only if u represents G . The resulting framework views granularities as strings generated by a specific class of automata, called Single-String Automata (SSA), thus making it possible to (re)use well-known results from automata theory. In order to compactly encode the redundancies of the temporal structures, SSA are endowed with counters ranging over discrete finite domains (Extended SSA, ESSA for short). Properties of ESSA have been exploited to efficiently solve the equivalence and the granule conversion problems for single time granularities [Dal Lago et al., 2003b]. The relationships between ESSA and Calendar Algebra have been systematically investigated by Dal Lago et al. in [Dal Lago et al., 2003a], where a number of algorithms that map Calendar Algebra expressions into automaton-based representations of time granularities are given. Such an encoding allows one to reduce problems about Calendar Algebra expressions to equivalent problems for ESSA. More generally, the operational flavor of ESSA suggests an alternative point of view on the role of automaton-based representations: besides a formalism for the direct specification of time granularities, automata can be viewed as a low-level formalism into which high-level time granularity specifications, such as those of Calendar Algebra, can be mapped. This allows one to exploit the benefits of both formalisms, using a high level language to define granularities and their properties in a natural and flexible

way, and the automaton-based one to efficiently reason about them. Finally, a generalization of the automaton-based approach from single periodical granularities to (possibly infinite) sets of granularities has been proposed by Bresolin et al. in [Bresolin *et al.*, 2004]. To this end, they identify a proper subclass of B uchi automata, called Ultimately Periodic Automata (UPA), that captures regular sets consisting of only ultimately periodic words. UPA allow one to encode single granularities, (possibly infinite) sets of granularities which have the same repeating pattern and different prefixes, and sets of granularities characterized by a finite set of non-equivalent patterns, as well as any possible combination of them.

The choice of Propositional Linear Temporal Logic (Propositional LTL) as a logical tool for granularity management has been recently advocated by Combi et al. in [Combi *et al.*, 2004]. Time granularities are defined as models of Propositional LTL formulas, where suitable propositional symbols are used to mark the endpoints of granules. In this way, a large set of regular granularities, such as, for instance, repeating patterns that can start at an arbitrary time point, can be captured. Moreover, problems like checking the consistency of a granularity specification or the equivalence of two granularity expressions can be solved in a uniform way by reducing them to the validity problem for Propositional LTL, which is known to be in PSPACE. An extension of Propositional LTL that replaces propositional variables by first-order formulas defining integer constraints, e.g., $x \equiv_k y$, has been proposed by Demri in [Demri, 2004]. The resulting logic, denoted by PLTL^{mod} (Past LTL with integer periodicity constraints), generalizes both the logical framework proposed by Combi et al. and the automaton-based approach of Dal Lago and Montanari, and it allows one to compactly define granularities as periodicity constraints. In particular, the author shows how to reduce the equivalence problem for ESSA to the model checking problem for PLTL^{mod} (-automata), which turns out to be in PSPACE, as in the case of Propositional LTL. The logical approach to time granularity is systematically analyzed in the next section, where various temporal logics for time granularity are presented.

3.4 The logical approach

A first attempt at incorporating time granularity into a logical formalism is outlined in [Corsetti *et al.*, 1991a; Corsetti *et al.*, 1991b]. The proposed logical system for time granularity has two distinctive features. On the one hand, it extends the syntax of temporal logic to allow one to associate different granularities (temporal domains) with different subformulas of a given formula; on the other hand, it provides a set of translation rules to rewrite a subformula associated with a given granularity into a corresponding subformula associated with a finer granularity. In such a way, a model of a formula involving different granularities can be built by first translating everything to the finest granularity and then by interpreting the resulting (flat) formula in the standard way.

A major problem with such a method is that there exists no a standard way to define the meaning of a formula when moving from a time granularity to another one. Thus, more information is needed from the user to drive the translation of the (sub)formulas. The main idea is that when we state that a predicate p holds at a given time point x belonging to the temporal domain T , we mean that p holds in a subset of the interval corresponding to x in the finer domain T' . Such a subset can be the whole interval, a scattered sequence of smaller intervals, or even a single time point. For instance, saying that “the light has been switched on at time x_{min} ”, where x_{min} belong to the domain of minutes, may correspond to state

that a predicate *switching_on* is true at the minute x_{min} and exactly at one second of x_{min} . Instead, saying that an employee works at the day x_d generally means that there are several minutes, during the day x_d , where the predicate *work* holds for the employee. These minutes are not necessarily contiguous. Thus, the logical system must provide the user with suitable tools that allow him to qualify the subset of time intervals of the finer temporal domain that correspond to the given time point of the coarser domain.

A substantially different approach is proposed in [Ciapessoni *et al.*, 1993; Montanari, 1994; Montanari, 1996], where Montanari et al. show how to extend syntax and semantics of temporal logic to cope with metric temporal properties possibly expressed at different time granularities. The resulting metric and layered temporal logic is described in detail in Subsection 3.4.1. Its distinctive feature is the coexistence of three different operators: a contextual operator, to associate different granularities with different (sub)formulas, a displacement operator, to move within a given granularity, and a projection operator, to move across granularities.

An alternative logical framework for time granularity has been developed in the classical logic setting [Montanari, 1996; Montanari and Policriti, 1996; Montanari *et al.*, 1999]. It imposes suitable restrictions to languages and structures for time granularity to get decidability. From a technical point of view, it defines various theories of time granularity as suitable extensions of monadic second-order theories of k successors, with $k \geq 1$. Monadic theories of time granularity are the subject of Subsection 3.4.2.

The temporal logic counterparts of the monadic theories of time granularity, called temporalized logics, are briefly presented in Subsection 3.4.3. This way back from the classical logic setting to the temporal logic one passes through an original class of automata, called temporalized automata.

A coda about the relationships between logics for time granularity and interval temporal logics concludes the section.

3.4.1 A metric and layered temporal logic for time granularity

Original metric and layered temporal logics for time granularity have been proposed by Montanari et al. in [Ciapessoni *et al.*, 1993; Montanari, 1994; Montanari, 1996]. We introduce these logics in two steps. First, we take into consideration their purely metric fragments in isolation. To do that, we adopt the general two-sorted framework proposed in [Montanari, 1996; Montanari and de Rijke, 1997], where a number of metric temporal logics, having a different expressive power, are defined as suitable combinations of a temporal component and an algebraic one. Successively, we show how flat metric temporal logic can be generalized to a many-layer metric temporal logic, embedding the notion of time granularity [Montanari, 1994; Montanari, 1996]. We first identify the main functionalities a logic for time granularity must support and the constraints it must satisfy; then, we axiomatically define metric and layered temporal logic, viewed as the combination of a number of differently-grained (single-layer) metric temporal logics, and we briefly discuss its logical properties.

The basic metric component

The idea of a logic of positions (topological, or metric, logic) was originally formulated by Rescher and Garson [Rescher and Garson, 1968; Rescher and Urquhart, 1971]. In [Rescher

and Garson, 1968], the authors define the basic features of the logic and they show how to give it a temporal interpretation. Roughly speaking, metric (temporal) logic extends propositional logic with a parameterized operator Δ_α of positional realization that allows one to constrain the truth value of a proposition at position α . If we interpret the parameter α as a displacement with respect to the current position, which is left implicit, we have that $\Delta_\alpha q$ is true at a position x if and only if q is true at a position y at distance α from x . Metric temporal logics can thus be viewed as two-sorted logics having both formulas and parameters; formulas are evaluated at time points while parameters take values in a suitable algebraic structure of temporal displacements. In [Montanari and de Rijke, 1997], Montanari and de Rijke start with a very basic system of metric temporal logic, and they build on it by adding axioms and/or by enriching the underlying structures. In the following, we describe the metric temporal logic of two-sorted frames with a linear temporal order (*MTL*); we also briefly consider general metric temporal logics allowing quantification over algebraic and temporal variables and free mixing of algebraic and temporal formulas (*Q-MTL*).

The *two-sorted temporal language* for *MTL* has two components: the algebraic component and the temporal one. Given a non-empty set A of constants, let $T(A)$ be the set of terms over A , that is, the smallest set such that $A \subseteq T(A)$, and if $\alpha, \beta \in T(A)$ then $\alpha + \beta, -\alpha, 0 \in T(A)$. The first-order (algebraic) component is built up from $T(A)$ and the predicate symbols $=$ and $<$. The temporal component of the language is built up from a non-empty set \mathcal{P} of proposition letters. The set of formulas over \mathcal{P} and A , $F(\mathcal{P}, A)$, is the smallest set such that $\mathcal{P} \subseteq F(\mathcal{P}, A)$, and if $\phi, \psi \in F(\mathcal{P}, A)$ and $\alpha \in T(A)$, then $\neg\phi, \phi \wedge \psi, \top$ (true), \perp (false), and $\Delta_\alpha\phi$ (and its dual $\nabla_\alpha\phi := \neg\Delta_\alpha\neg\phi$) belong to $F(\mathcal{P}, A)$. Δ_α is called the (parameterized) *displacement operator*.

A *two-sorted frame* is a triple $\mathbf{F} = (T, \mathbf{D}; \text{DIS})$, where T is the set of (time) points over which temporal formulas are evaluated, \mathbf{D} is the algebra of metric displacements in whose domain D terms take their values, and $\text{DIS} \subseteq T \times D \times T$ is an accessibility relation, called displacement relation, relating pairs of points and displacements. The components of two-sorted frames satisfy the following properties. First, \mathbf{D} is an ordered Abelian group, that is, a structure $\mathbf{D} = (D, +, -, 0, <)$, where $+$ is a binary function of displacement composition, $-$ is a unary function of inverse displacement, and 0 is the zero displacement constant, such that:

- (i) $\alpha + \beta = \beta + \alpha$ (commutativity of $+$);
- (ii) $\alpha + (\beta + \gamma) = (\alpha + \beta) + \gamma$ (associativity of $+$);
- (iii) $\alpha + 0 = \alpha$ (zero element of $+$);
- (iv) $\alpha + (-\alpha) = 0$ (inverse),

and $<$ is an irreflexive, asymmetric, transitive, and linear relation that satisfies the comparability property (viii) below:

- (v) $\neg(\alpha < \alpha)$;
- (vi) $\neg(\alpha < \beta \wedge \beta < \alpha)$;
- (vii) $\alpha < \beta \wedge \beta < \gamma \rightarrow \alpha < \gamma$;
- (viii) $\alpha < \beta \vee \alpha = \beta \vee \beta < \alpha$.

Furthermore, there are two conditions expressing the relations between $+$ and $-$, and $<$:

- (ix) $\alpha < \beta \rightarrow \alpha + \gamma < \beta + \gamma$;
- (x) $\alpha < \beta \rightarrow -\beta < -\alpha$.

As for the displacement relation, we first require DIS to respect the converse operation of the Abelian group in the following sense:

Symmetry: $\forall i, j, \alpha (\text{DIS}(i, \alpha, j) \rightarrow \text{DIS}(j, -\alpha, i)).$

Furthermore, we require DIS to be reflexive, transitive, quasi-functional (q-functional for short) with respect to both its third and second argument, and totally connected:

Reflexivity: $\forall i \text{DIS}(i, 0, i);$

Transitivity: $\forall i, j, k, \alpha, \beta (\text{DIS}(i, \alpha, j) \wedge \text{DIS}(j, \beta, k) \rightarrow \text{DIS}(i, \alpha + \beta, k));$

Q-functionality - 1: $\forall i, j, j', \alpha (\text{DIS}(i, \alpha, j) \wedge \text{DIS}(i, \alpha, j') \rightarrow j = j');$

Q-functionality - 2: $\forall i, j, \alpha, \beta (\text{DIS}(i, \alpha, j) \wedge \text{DIS}(i, \beta, j) \rightarrow \alpha = \beta);$

Total connectedness: $\forall i, j \exists \alpha \text{DIS}(i, \alpha, j).$

From the ordering $<$ on the algebraic component of the frames, an ordering \ll on the temporal component can be defined as follows:

$$i \ll j \text{ iff for some } \alpha > 0, \text{DIS}(i, \alpha, j). \quad (3.1)$$

According to Definition 3.1, we have that i and j are \ll -related if there exists a positive displacement between them. It is possible to show that \ll is a strict linear order [Montanari and de Rijke, 1997] (it is worth noting that, without the properties of quasi-functionality with respect to the second argument and total connectedness, Definition 3.1 does not produce a strict linear order).

The interpretation of the language for *MTL* on two-sorted frames based on an ordered Abelian group is fairly straightforward: the first-order (algebraic) component is interpreted on the ordered Abelian group, and the temporal component on the temporal domain. Basically, a two-sorted frame \mathbf{F} can be turned into a *two-sorted model* by adding an interpretation for the algebraic terms and a valuation for proposition letters. An interpretation for algebraic terms is given by a function $g : A \rightarrow D$ that is automatically extended to all terms from $T(A)$. A valuation is simply a function $V : \mathcal{P} \rightarrow 2^T$. We say that $\alpha = \beta$ (resp. $\alpha < \beta$) is *true* in a model $\mathbf{M} = (T, \mathbf{D}; \text{DIS}; V, g)$ whenever $g(\alpha) = g(\beta)$ (resp. $g(\alpha) < g(\beta)$). *Truth* of temporal formulas is defined by means of the standard semantic clauses for proposition letters and Boolean connectives, plus the following clause for the displacement operator:

$$\mathbf{M}, i \Vdash \Delta_\alpha \phi \text{ iff there exists } j \text{ such that } \text{DIS}(i, g(\alpha), j) \text{ and } \mathbf{M}, j \Vdash \phi.$$

Let Γ denote a set of formulas. To avoid messy complications we only consider one-sorted consequences $\Gamma \models \phi$; for algebraic formulas ' $\Gamma \models \phi$ ' means 'for all models \mathbf{M} , if $\mathbf{M} \models \Gamma$, then $\mathbf{M} \models \phi$ '; for temporal formulas it means 'for all models \mathbf{M} , and time points i , if $\mathbf{M}, i \Vdash \Gamma$, then $\mathbf{M}, i \Vdash \phi$ '.

The following example shows that the language of *MTL* allows one to express meaningful temporal conditions.

Example 3.4.1. *Let us consider a communication channel C that collects messages from n different sources S_1, \dots, S_n and outputs them with delay δ . To exclude that two input events can occur simultaneously, we add the constraint (notice that preventing input events from occurring simultaneously also guarantees that output events do not occur simultaneously):*

$$\forall i, j \neg(\text{in}(i) \wedge \text{in}(j) \wedge i \neq j),$$

which is shorthand for:

$$\neg(\text{in}(1) \wedge \text{in}(2)) \wedge \dots \wedge \neg(\text{in}(n-1) \wedge \text{in}(n)).$$

The behavior of C is specified by the formula:

$$\forall i (\text{out}(i) \leftrightarrow \Delta_{-\delta} \text{in}(i)),$$

which is shorthand for a finite conjunction.

Validity in MTL can be axiomatized as follows. For the displacement component, one takes the axioms and rules of identity, ordered Abelian groups, and strict linear order, together with any complete calculus for first-order logic. For the temporal component, one takes the usual axioms of propositional logic plus the axioms:

- (AxND) $\nabla_{\alpha}(p \rightarrow q) \rightarrow (\nabla_{\alpha}p \rightarrow \nabla_{\alpha}q)$ (normality);
- (AxSD) $p \rightarrow \nabla_{\alpha}\Delta_{-\alpha}p$, (symmetry);
- (AxRD) $\nabla_0p \rightarrow p$ (reflexivity);
- (AxTD) $\nabla_{\alpha+\beta}p \rightarrow \nabla_{\alpha}\nabla_{\beta}p$ (transitivity);
- (AxQD) $\Delta_{\alpha}p \rightarrow \nabla_{\alpha}p$ (q-functionality - 1).

Its rules are modus ponens and

- (D-NEC) $\vdash \phi \implies \vdash \nabla_{\alpha}\phi$ (necessitation rule for ∇_{α});
- (REP) $\vdash \phi \leftrightarrow \psi \implies \vdash \chi(\phi/p) \leftrightarrow \chi(\psi/p)$ (replacement),
where (ϕ/p) denotes substitution of ϕ for the variable p ;
- (LIFT) $\vdash \alpha = \beta \implies \vdash \nabla_{\alpha}\phi \leftrightarrow \nabla_{\beta}\phi$ (transfer of identities).

Axiom (AxN) is the usual distribution axiom; axiom (AxS) expresses that a displacement α is the converse of a displacement $-\alpha$; axioms (AxR), (AxT), and (AxQ) capture reflexivity, transitivity, and quasi-functionality with respect to the third argument, respectively. A suitable adaptation of two truth preserving constructions from standard modal logic to the MTL setting allows one to show there are no MTL formulas that express total connectedness and quasi-functionality with respect to the second argument of the displacement relation [Montanari and de Rijke, 1997]. The rules (D-NEC) and (REP) are familiar from modal logic. Finally, the rule (LIFT) allows one to transfer provable algebraic identities from the displacement domain to the temporal one.

A *derivation in MTL* is a sequence of formulas $\sigma_1, \dots, \sigma_n$ such that each σ_i , with $1 \leq i \leq n$, is either an axiom or obtained from $\sigma_1, \dots, \sigma_{n-1}$ by applying one of the derivation rules of MTL . We write $\vdash_{MTL} \sigma$ to denote that there is a derivation in MTL that ends in σ . It immediately follows that $\vdash_{MTL} \alpha = \beta$ iff $\alpha = \beta$ is provable from the axioms of the algebraic component only: whereas we can lift algebraic information from the displacement domain to the temporal domain using the (LIFT) rule, there is no way in which we can import temporal information into the displacement domain. As with consequences, we only consider one-sorted inferences ' $\Gamma \vdash \phi$ '.

Theorem 3.4.1. *MTL is sound and complete for the class of all transitive, reflexive, totally-connected, and quasi-functional (in both the second and third argument of their displacement relation) frames.*

The proof of soundness is trivial. The completeness proof is much more involved [Montanari and de Rijke, 1997]. It is accomplished in two steps: first, one proves completeness with respect to totally connected frames via some sort of generated submodel construction; then, a second construction is needed to guarantee quasi-functionality with respect to the second argument.

Propositional variants of *MTL* are studied in [Montanari and de Rijke, 1997]. As an example, one natural specialization of *MTL* is obtained by adding discreteness. As in the case of the ordering, the discreteness of the temporal domain necessarily follows from that of the domain of temporal displacements, which is expressed by the following formula:

$$\forall \alpha \exists \beta, \beta' (\alpha < \beta \wedge \forall \gamma (\alpha < \gamma \rightarrow (\beta = \gamma \vee \beta < \gamma)) \wedge \beta' < \alpha \wedge \forall \delta (\delta < \alpha \rightarrow (\beta' = \delta \vee \beta' < \delta)))$$

Proposition 3.4.1. *Let $\mathbf{F} = (T, \mathbf{D}; \text{DIS})$ be a two-sorted frame based on a discrete ordered Abelian group \mathbf{D} . For all $i, j \in T$, there exist only finitely many k such that $i \ll k \ll j$.*

For some applications, both *MTL* and its propositional variants are not expressive enough, and thus they must be extended. In particular, they lack quantification and constrain displacements to occur as parameters of the displacement operator only. The following example shows how the ability of freely mixing temporal and displacement formulas enables one to exploit more complex ways of interaction between the two domains, rather than to only lift information from the algebraic domain to the temporal one.

Example 3.4.2. *Let us consider the operation of a traffic light controller C [Henzinger et al., 1994]. When the request button is pushed, the controller makes a pedestrian light turn green within a given time bound after which the light remains green for a certain amount of time. Moreover, assume that C takes a unit of time to switch the light and that the time needed for its internal operations is negligible.*

We require that C satisfies the following conditions:

- (i) *whenever a pedestrian pushes the request button ('request is true'), then the light is green within 5 time units and remains green for at least 10 time units (this condition guarantees that no pedestrian waits for more than 5 time units, and that he or she is given at least 10 time units to cross the road);*
- (ii) *whenever request is true, then it is false within 20 time units (this condition ensures that the request button is reset);*
- (iii) *whenever request has been false for 20 time units, the light is red (this condition should prevent the light from always being green).*

By taking advantage of the possibility of quantifying displacement variables and of using displacement formulas, the behavior of C can be specified by the conjunction of the following formulas:

$$\begin{aligned} \text{request} &\rightarrow \exists x(0 < x \leq 5 \wedge \forall y(x \leq y < x + 10 \rightarrow \nabla_y \text{lightIsGreen}); \\ \text{request} &\rightarrow \exists z(0 \leq z \leq 20 \wedge \Delta_z \neg \text{request}); \\ \forall x(0 \leq x < 20 &\rightarrow \nabla_x \neg \text{request}) \rightarrow \nabla_{20} \text{lightIsRed}, \end{aligned}$$

together with a formula stating that at each time point the traffic light is either red or green:

$$\text{lightIsGreen} \leftrightarrow \neg \text{lightIsRed}.$$

Different implementations of C , all satisfying the given specification, can be obtained by making different assumptions about the value of temporal parameters, e.g., by varying the delay between requests and resets. It is worth noting that, even if there are no restrictions on the frequency of requests, the above specification is appropriate only if that frequency is low; otherwise, it may happen that switching the light to red is delayed indefinitely. A solution to this problem is discussed in [Montanari, 1996].

Systems of quantified metric temporal logic (Q - MTL for short) are developed in [Montanari and de Rijke, 1997]. The language of Q - MTL extends that of MTL by adding algebraic variables (and, possibly, temporal variables) and by allowing quantification over algebraic (and temporal) variables and free mixing of algebraic formulas and temporal propositional symbols. Q - MTL models can be obtained from ordered two-sorted frames $\mathbf{F} = (T, \mathbf{D}; \text{DIS})$ by adding an interpretation function g for the algebraic terms and a valuation V for proposition letters, and by specifying the way one evaluates mixed formulas at time points. An axiomatic system for Q - MTL (we refer to the simplest system of quantified metric temporal logic; other cases are considered in [Montanari and de Rijke, 1997]) is obtained from that for MTL by adding a number of axiom schemata governing the behavior of quantifiers and substitutions:

- (AxF) $\forall x (\phi \rightarrow \psi) \leftrightarrow (\forall x \phi \rightarrow \forall x \psi)$ (functionality);
 (AxEVQ) $\phi \rightarrow \forall x \phi$, for x not in ϕ
 (elimination of vacuous quantifiers);
 (AxUI) $\forall x \phi \rightarrow \phi(\alpha/x)$, with α free for x in ϕ
 (universal instantiation),

the Barcan formula for the displacement operator:

- (AxBFD) $\forall x \nabla_\alpha \phi \rightarrow \nabla_\alpha \forall x \phi$, with $x \notin \alpha$ (Barcan formula for ∇_α),
 where $x \notin \alpha$ stands for $x \neq \alpha$ and x does not occur in α ,

the axioms relating the algebraic terms and the displacement operator (axiom (AxAD4) can actually be derived from the other axioms):

- (AxAD1) $\alpha = \beta \rightarrow \forall x \nabla_x \alpha = \beta$; (AxAD2) $\alpha \neq \beta \rightarrow \forall x \nabla_x \alpha \neq \beta$;
 (AxAD3) $\alpha < \beta \rightarrow \forall x \nabla_x \alpha < \beta$; (AxAD4) $\alpha \not< \beta \rightarrow \forall x \nabla_x \alpha \not< \beta$,

and the rule:

- (UG) $\vdash \phi \implies \vdash \forall x \phi$ (universal generalization).

The completeness of Q - MTL can be proved by following the general pattern of the completeness proof for MTL , but the presence of mixed formulas complicates some of the details. Basically, it makes use of a variant of Hughes and Cresswell's method for proving axiomatic completeness in the presence of the Barcan formula [Hughes and Cresswell, 1968].

The addition of time granularity

Metric and Layered Temporal Logic ($MLTL$ for short) is obtained from MTL by adding a notion of time granularity [Ciapessoni *et al.*, 1993; Montanari, 1994; Montanari, 1996]. In

the following, we first show how to extend two-sorted frames to incorporate granularity; then, we present syntax, semantics, and axiomatization of *MLTL*; finally, we briefly describe the way in which the synchronization problem (cf. Section 3.2) can be dealt with in *MLTL*.

The main change to make to the model of time when moving from *MTL* to *MLTL* is the replacement of the temporal domain T by a temporal universe \mathcal{T} consisting of a set of *disjoint* linear temporal domains/layers, that share the same displacement domain D . Formally, $\mathcal{T} = \{T^i : i \in M\}$, where M is an initial segment of \mathbb{N} , possibly equal to \mathbb{N} . The set $\bigcup_{i \in M} T^i$ collects all time points belonging to the different layers of \mathcal{T} . \mathcal{T} is assumed to be *totally ordered* by the granularity relation \prec . As an example, if $\mathcal{T} = \{\text{years}, \text{months}, \text{weeks}, \text{days}\}$, we have that $\text{days} \prec \text{weeks} \prec \text{months} \prec \text{years}$. A finer characterization of the relations among the layers of a temporal universe is provided by the *disjointedness* relation, denoted by \subset , which is quite similar to the *groups-into* relation defined in Section 3.3. It defines a partial order over \mathcal{T} that rules out pairs of layers like weeks and months for which a point of a finer layer (weeks) can be astride two points of the coarser one (months). As an example, given $\mathcal{T} = \{\text{years}, \text{months}, \text{weeks}, \text{days}\}$, we have that $\text{months} \subset \text{years}$, $\text{days} \subset \text{months}$, and $\text{days} \subset \text{weeks}$. This means that years are pairwise disjoint when viewed as sets of months ; the same holds for months when viewed as sets of days .

The links between points belonging to the same layer are expressed by means of (a number of instances of) the *displacement* relation, while those between points belonging to different layers are given by means of a *decomposition* relation that, for every pair $T^i, T^j \in \mathcal{T}$, with $T^j \prec T^i$, associates each point of T^i with the set of points of T^j that compose it. We assume that the decomposition relation turns every point $x \in T^i$ into a set of contiguous points (decomposition interval) of T^j (*convexity*). This condition excludes the presence of ‘temporal gaps’ within the set of components of a given point, as it happens, for instance, when business months are mapped on days . In general, the cardinalities of the sets of components of two distinct points $x, y \in T^i$ with respect to T^j may be different (*non homogeneity*). This is the case, for instance, with pairs of layers like real months and days : different months can be mapped on a different number of days (28, 29, 30, or 31). In some particular contexts, however, it is convenient to work with temporal universes where, for every pair of layers T^i, T_j , with $T^j \prec T^i$, the decomposition intervals have the same cardinality (*homogeneity*). For instance, this is the case of temporal universes that replace real months by legal months , which, conventionally, are 30-days long. We constrain the decomposition relation to respect the ordering of points within layers (*order preservation*). If $T^j \subset T^i$, e.g., seconds and minutes , then the intervals are disjoint; otherwise, the intervals can possibly meet at their endpoints, e.g., weeks and months . We further require that the union of the intervals of T^j associated with the points of T^i covers the whole T^j (*total covering*). From order preservation and total covering, it follows that, for all pairs of layers T^i, T^j , with $T^j \prec T^i$, the decomposition relation associates contiguous points of T^i with contiguous sets of points of T_j (*contiguity*). This excludes the presence of ‘temporal gaps’ between the decomposition intervals of consecutive points of the coarser layer, as it happens, for instance, when business weeks are mapped on days . Finally, we require that, for every i, j, k , if $T^j \subset T^k \subset T^i$, then the decomposition of T^i into T^j can be obtained from the decomposition of T^i into T^k and that of T^k into T^j (*downward transitivity*). The same holds for $T^k \subset T^j \subset T^i$ (*downward/upward transitivity*). In the following, we shall also consider the inverse relation of *abstraction*, that, for every pair $T^i, T^j \in \mathcal{T}$, with

$T^j \prec T^i$, associates a point $x \in T^j$ with a point $y \in T^i$ if x belongs to the decomposition of y with respect to T^j . Every point $x \in T^j$ can be abstracted into either one or two adjacent points of T^i . If $T^j \subset T^i$, x is abstracted into a unique point y , which is called the *coarse grain equivalent* of x with respect to T^i .

Besides the algebraic and temporal components, the *temporal language* for *MLTL* includes a *context sort*. Moreover, the displacement operator is paired with a contextual operator and a projection operator. Formally, given a non-empty set C of context constants, denoting the layers of the temporal universe, and a set Y of context variables, the set $T(C \cup Y)$ of context terms is equal to $C \cup Y$. The set $T(A \cup X)$ of algebraic terms denoting temporal displacements is built up as follows. Let A be a set of algebraic constants and X be a set of algebraic variables. $T(A \cup X)$ is the smallest set such that $A \subseteq T(A \cup X)$, $X \subseteq T(A \cup X)$, and if $\alpha, \beta \in T(A \cup X)$ then $\alpha + \beta, -\alpha, 0 \in T(A \cup X)$. Finally, given a non-empty set of proposition letters \mathcal{P} , the set of formulas $F(\mathcal{P}, A, X, C, Y)$ is the smallest set such that $\mathcal{P} \in F(\mathcal{P}, A, X, C, Y)$, if $\phi, \psi \in F(\mathcal{P}, A, X, C, Y)$, $x \in X, y \in Y, c, c', c'' \in T(C \cup Y)$, and $\alpha, \beta \in T(X \cup A)$, then $\alpha = \beta, \alpha < \beta, c' \prec c'', c' \subset c'', \neg\phi, \phi \wedge \psi, \Delta_\alpha\phi$ (and $\nabla_\alpha\phi$), $\Delta^c\phi$ (and its dual $\nabla^c\phi := \neg\Delta^c\neg\phi$), $\diamond\phi$ (and its dual $\square\phi := \neg\diamond\neg\phi$), $\forall x\phi$, and $\forall y\phi$ belong to $F(\mathcal{P}, A, X, C, Y)$. Δ^c is called the (parameterized) *contextual operator*. When applied to a formula ϕ , it restricts the evaluation of ϕ to the time points of the layer denoted by c . The combined use of Δ_α and Δ^c makes it possible to define a derived operator Δ_α^c of *contextualized* (or *local*) *displacement*: $\Delta_\alpha^c\phi := \Delta^c\Delta_\alpha\phi$ (and its dual $\nabla_\alpha^c\phi := \nabla^c\nabla_\alpha\phi$). In such a case, the context term c can be viewed as the sort of the algebraic term α (*multi-sorted algebraic terms*). \diamond is called the *projection operator*. When applied to a formula ϕ , it allows one to evaluate ϕ at time points which are descendants (decomposition) or ancestors (abstraction) of the current one. Restrictions to specific sets of descendants or ancestors can be obtained by pairing the projection operator with the contextual one.

The *two-sorted frame* for time granularity is a tuple

$$\mathbf{F} = ((\mathcal{T}, \prec, \subset), \mathbf{D}; \text{DIS}, \text{CONT}, \updownarrow)$$

where \mathcal{T} is the temporal universe, \prec and \subset are the granularity and disjointedness relations, respectively, \mathbf{D} is the algebra of metric displacements, $\text{DIS} = \bigcup_{i \in M} \text{DIS}_i$ is the displacement relation, $\text{CONT} \subseteq \bigcup_{i \in M} T^i \times \mathcal{T}$ is the relation of contextualization, and $\updownarrow \subseteq \bigcup_{i \in M} T^i \times \bigcup_{i \in M} T^i$ is the projection relation. \mathcal{T} is totally (resp. partially) ordered by \prec (resp. \subset). For every layer T^i , the ternary relation $\text{DIS}_i \subseteq T^i \times D \times T^i$ relates pairs of time points in T^i to a displacement in D . We assume that all DIS_i satisfy the same properties. The relation CONT associates each time point with the layer it belongs to. In its full generality, such a relation allows one point to belong to more than one layer (overlapping layers). However, since we restricted ourselves to the case in which \mathcal{T} is totally ordered by “ \prec ”, we assume that \mathcal{T} defines a partition of $\bigcup_{i \in M} T^i$. This amounts to constrain CONT to be a total function with range equal to \mathcal{T} . The projection relation \updownarrow associates each point with its direct or indirect descendants (downward projection) and ancestors (upward projection). More precisely, for any pair of points x, y , $\updownarrow(x, y)$ means that either x downward projects on y or x upward projection on y . Different temporal structures for time granularity can be obtained by imposing different conditions on the projection relation. Here is the list of the basic properties of the projection relation, where we assume variables x, y, z to take value over (subsets of) $\bigcup_{i \in M} T^i$ and variables α, β to take value over D :

reflexivity every point x projects on itself

$$\forall x \downarrow(x, x)$$

uniqueness the projection relation does not link distinct points belonging to the same layer

$$\forall x, y, T^i ((x \in T^i \wedge y \in T^i \wedge x \neq y) \rightarrow \neg \downarrow(x, y))$$

refinement - case 1 for any pair of layers T^i, T^j , with $T^j \prec T^i$, any point of T^i projects on at least two points of T^j

$$\forall T^i, T^j, x \exists y, z ((T^j \prec T^i \wedge x \in T^i) \rightarrow (y \in T^j \wedge z \in T^j \wedge y \neq z \wedge \downarrow(x, y) \wedge \downarrow(x, z)))$$

refinement - case 2 for any pair of layers T^i, T^j , with $T^j \prec T^i$, and every point $x \in T^i$, there exists at least one point $y \in T^j$ such that x projects on y and no other point $z \in T^i$ projects on it

$$\forall T^i, T^j, x \exists y ((T^j \prec T^i \wedge x \in T^i) \rightarrow (y \in T^j \wedge \downarrow(x, y) \wedge \forall z ((z \in T^i \wedge z \neq x) \rightarrow \neg \downarrow(z, y))))$$

separation for any pair of layers T^i, T^j , with $T^j \subset T^i$, the decomposition intervals of distinct points of T^i are disjoint

$$\forall T^i, T^j, x, y, x', y' ((T^j \subset T^i \wedge x \in T^i \wedge y \in T^i \wedge x \neq y \wedge x' \in T^j \wedge y' \in T^j \wedge \downarrow(x, x') \wedge \downarrow(y, y')) \rightarrow x' \neq y')$$

symmetry if x downward (resp. upward) projects on y , then y upward (resp. downward) projects on x

$$\forall x, y (\downarrow(x, y) \rightarrow \uparrow(y, x))$$

By pairing symmetry and separation, it easily follows that, whenever $T^j \subset T^i$, each point of the finer layer is projected on a unique point of the coarser one (*alignment*).

downward transitivity if $T^k \subset T^j \subset T^i$, $x \in T^i$ projects on $y \in T^j$, and y projects on $z \in T^k$, then x projects on z

$$\forall T^i, T^j, T^k, x, y, z ((T^k \subset T^j \subset T^i \wedge x \in T^i \wedge y \in T^j \wedge z \in T^k \wedge \downarrow(x, y) \wedge \downarrow(y, z)) \rightarrow \downarrow(x, z))$$

Notice that we cannot substitute \prec for \subset in the above formula. Consider a temporal universe consisting of months, weeks, and days. The week from December 29, 2003, to January 4, 2004, belongs to the decomposition of December 2003 (as well as of January 2004) and the 3rd of January 2003 belongs to the decomposition of such a week, but not to that of December 2003.

downward/upward transitivity - case 1 if $T^j \subset T^k \subset T^i$, $x \in T^i$ projects on $y \in T^j$, and y projects on $z \in T^k$, then x projects on z

$$\forall T^i, T^j, T^k, x, y, z ((T^j \subset T^k \subset T^i \wedge x \in T^i \wedge y \in T^j \wedge z \in T^k \wedge \downarrow(x, y) \wedge \downarrow(y, z)) \rightarrow \downarrow(x, z))$$

As in the case of downward transitivity, we cannot substitute \prec for \subset in the above formula. Consider a temporal universe consisting of `years`, `months`, and `weeks`. The week from December 29, 2003, to January 4, 2004, belongs both to the decomposition of the year 2003 (as well as of the year 2004) and to the decomposition of the month of January 2004, but such a month does not belong to the decomposition of the year 2003.

order preservation the linear order of layers is preserved by the projection relation. For every pair T^i, T^j , the projection intervals are ordered, but they can possibly meet (weak order preservation)

$$\forall T^i, T^j, x, y, x', y' ((x \in T^i \wedge y \in T^i \wedge x' \in T^j \wedge y' \in T^j \wedge \downarrow(x, x') \wedge \downarrow(y, y') \wedge x \ll y) \rightarrow (x' \ll y' \vee x' = y'))$$

where $x \ll y$ iff for some $i \in M$ and $\alpha > 0$, $\text{DIS}_i(x, \alpha, y)$. Weak order preservation encompasses both the case of two months that share a week and the case of two months that belong to the same year.

From refinement (cases 1 and 2), symmetry and weak order preservation, it follows that, for any pair of layers T^i, T^j , with $T^j \prec T^i$, any point of T^j projects on either one or two points of T^i (*abstraction*). Moreover, from refinement (case 2), symmetry, and weak order preservation, it follows that it is never the case that, given any pair of layers T^i, T^j , with $T^j \prec T^i$, two consecutive points of T^j are both projected on the same two points of T^i .

If $T^j \subset T^i$, the projection intervals of the elements of T^i over T^j are ordered and disjoint, that is, we must substitute $x' \ll y'$ for $x' \ll y' \vee x' = y'$ (*strong order preservation*).

convexity for any ordered pair of layers T^i, T^j (either $T^i \prec T^j$ or $T^j \prec T^i$), the projection relation associates any point of T^i with an interval of contiguous points of T^j

$$\forall T^i, T^j, x, y, w, z ((x \in T^i \wedge y \in T^j \wedge z \in T^j \wedge w \in T^j \wedge y \ll w \wedge w \ll z \wedge \downarrow(x, y) \wedge \downarrow(x, z)) \rightarrow \downarrow(x, w))$$

In some situations, the layers of the temporal universe can be assumed to (pairwise) satisfy the property of homogeneity.

homogeneity for every pair of (discrete) layers ordered by granularity, the projection relation associates the same number of points of the finer layer with every point of the coarser one

$$\forall T^i, T^j, x, y, x', x'' \exists y', y'' ((T^j \prec T^i \wedge x \in T^i \wedge y \in T^i \wedge x' \in T^j \wedge x'' \in T^j \wedge x' \neq x'' \wedge \downarrow(x, x') \wedge \downarrow(x, x'')) \rightarrow (y' \in T^j \wedge y'' \in T^j \wedge y' \neq y'' \wedge \downarrow(y, y') \wedge \downarrow(y, y'')))$$

and

$$\forall T^i, T^j, x, y, y' \exists x' ((T^j \prec T^i \wedge x \in T^i \wedge y \in T^i \wedge y' \in T^j \wedge \downarrow(y, y')) \rightarrow (x' \in T^j \wedge \downarrow(x, x')))$$

Other interesting properties of the projection relation can be derived from the above ones, including *total covering*, *contiguity*, *seriality* (any point x can be projected on any layer T^i), *upward transitivity* (if $T^k \subset T^j \subset T^i$, $x \in T^k$ projects on $y \in T^j$, and y projects on $z \in T^i$, then x projects on z), and *downward/upward transitivity - case 2* (if $T^j \subset T^i \subset T^k$, $x \in T^i$ projects on $y \in T^j$, and y projects on $z \in T^k$, then x projects on z).

To turn a two-sorted frame \mathbf{F} into a *two-sorted model* \mathbf{M} , we first add the interpretations for context and algebraic terms, and the valuation for atomic temporal formulas. The interpretation for context terms is given by a function $h : C \cup Y \rightarrow \mathcal{T}$; that for algebraic terms

is given by a function $g : A \cup X \rightarrow D$, which is automatically extended to all terms from $T(A \cup X)$. The valuation V for propositional variables is defined as in *MTL*. An atomic formula of the form $\alpha = \beta$ (resp. $\alpha < \beta$) is *true* in a model $\mathbf{M} = (\mathbf{F}; V, g, h)$ whenever $g(\alpha) = g(\beta)$ (resp. $g(\alpha) < g(\beta)$). Analogously, $c \prec c'$ (resp. $c \subset c'$) is *true* in \mathbf{M} whenever $h(c) \prec h(c')$ (resp. $h(c) \subset h(c')$). Next, the *truth* of the temporal formulas $\Delta_\alpha \phi$, $\Delta^c \phi$, and $\diamond \phi$ is defined by the following clauses:

- $$\begin{aligned} \mathbf{M}, i \Vdash \Delta_\alpha \phi & \text{ iff } \text{there exists } j \text{ such that } \text{DIS}(i, g(\alpha), j) \text{ and } \mathbf{M}, j \Vdash \phi; \\ \mathbf{M}, i \Vdash \Delta^c \phi & \text{ iff } \text{CONT}(i, h(c)) \text{ and } \mathbf{M}, i \Vdash \phi; \\ \mathbf{M}, i \Vdash \diamond \phi & \text{ iff } \text{there exists } j \text{ such that } \uparrow(i, j) \text{ and } \mathbf{M}, j \Vdash \phi. \end{aligned}$$

The semantic clauses for the dual operators ∇_α , ∇^c , and \diamond , as well as for the derived operator Δ_α^c , can be easily derived from the above ones. Note that $\Delta^c \phi$ (resp. $\nabla^c \phi$) conventionally evaluates to false (resp. true) outside the context c . Finally, to evaluate the quantified formula $\forall x \phi$, with $x \in X$ (resp. $\forall y \phi$, with $y \in Y$), at a point i , we write $g =_x g'$ (resp. $h =_y h'$) to state that the assignments g and g' (resp. h and h') agree on all variables except maybe x (resp. y). We have that $(\mathbf{F}; V, g, h), i \Vdash \forall x \phi$ iff $(\mathbf{F}; V, g', h), i \Vdash \phi$, for all assignments g' such that $g =_x g'$. Analogously for $\forall y \phi$.

The notions of satisfiability, validity, and logical consequence given for *MTL* can be easily generalized to *MLTL*. Furthermore, the layered structure of *MLTL*-frames makes it possible to define the notions of *local* satisfiability, validity, and logical consequence by restricting the general notions of satisfiability, validity, and logical consequence to a specific layer.

The following examples show how *MLTL* allows one to specify temporal conditions involving different time granularities (the application of *MLTL* to the specification of complex real-time systems is discussed in [Montanari, 1996]). In the simplest case (case (i)), *MLTL* specifications are obtained by contextualizing formulas and composing them by means of logical connectives. The projection operator is needed when displacements over different layers have to be composed (case (ii)). Finally, contextual and projection operators can be paired to specify nested quantifications (cases (iii)-(vi)).

Example 3.4.3. Consider the temporal conditions expressed by the following sentences:

- (i) *men work every month and eat every day;*
- (ii) *in 20 seconds 5 minutes will have passed from the occurrence of the fault;*
- (iii) *some days the plant works every hour;*
- (iv) *some days the plant remains inactive for several hours;*
- (v) *every day the plant is in production for some hours;*
- (vi) *the plant is monitored by the remote system every minute of every hour.*

They can be expressed in *MLTL* by means of the following formulas:

- (i) $\forall x_{man} (\forall \alpha \nabla_\alpha^{month} \text{work}(x_{man}) \wedge \forall \beta \nabla_\beta^{day} \text{eat}(x_{man}));$
- (ii) $\Delta_{20}^{second} \diamond \Delta_{-5}^{minute} \text{fault};$

- (iii) $\exists\alpha\Delta_\alpha^{day}\Box\nabla^{hour}\text{work}(\text{plant});$
- (iv) $\exists\alpha\Delta_\alpha^{day}\Diamond\Delta^{hour}\text{inactive}(\text{plant});$
- (v) $\forall\alpha\nabla_\alpha^{day}\Diamond\Delta^{hour}\text{in_production}(\text{plant});$
- (vi) $\forall\alpha\nabla_\alpha^{hour}\Box\nabla^{minute}\text{monitor}(\text{remote-system}, \text{plant}).$

As a matter of fact, it is possible to give a stronger interpretation of condition (ii), which is expressed by the formula:

$$(ii') \Delta_{20}^{second}\Diamond\Delta_{-5}^{minute}\text{fault} \wedge \forall\alpha(0 \leq \alpha < 20 \rightarrow \neg\Delta_\alpha^{second}\Diamond\Delta_{-5}^{minute}\text{fault}).$$

The problem of finding an axiomatization of validity in *MLTL* is addressed in [Ciapessoni *et al.*, 1993; Montanari, 1996]. The idea is to pair axioms and rules of (*Q*-)MTL, which are used to express the properties of the displacement operator with respect to every context, with additional axiom schemata and rules governing the behavior of the contextual and projection operators as well as the relations between these operators and the displacement one. First, the axiomatic system for *MLTL* must constrain \prec to be a total order and \subset to be a partial order that refines \prec , that is, for every pair of contexts c, c' we have that if $c \subset c'$, then $c \prec c'$, but not necessarily vice versa. Moreover, it must express the basic logical properties of the contextual and projection operators:

- | | | |
|---------|---|---|
| (AxNC) | $\nabla^c(\phi \rightarrow \psi) \rightarrow (\nabla^c\phi \rightarrow \nabla^c\psi)$ | (normality of ∇^c); |
| (AxNP) | $\Box(\phi \rightarrow \psi) \rightarrow (\Box\phi \rightarrow \Box\psi)$ | (normality of \Box); |
| (AxNEC) | $\Delta^c\phi \rightarrow \phi$ | (“necessity” for Δ^c); |
| (AxIC) | $\nabla^c\nabla^c\phi \equiv \nabla^c\phi$ | (idempotency of ∇^c); |
| (AxCCD) | $\nabla^c\nabla_\alpha\phi \equiv \nabla_\alpha\nabla^c\phi$ | (commutativity of ∇^c and ∇_α), |

together with the rules:

- | | | |
|---------|---|---------------------------------------|
| (C-NEC) | $\vdash \phi \longrightarrow \vdash \nabla^c\phi$ | (necessitation rule for ∇^c); |
| (P-NEC) | $\vdash \phi \longrightarrow \vdash \Box\phi$ | (necessitation rule for \Box). |

Notice that the projection operators \Diamond and \Box behave as the usual modal operators of possibility and necessity, while the contextual operators Δ^c and ∇^c are less standard (a number of theorems that account for the behavior of the contextual operators are given in [Montanari, 1996]). The set of axioms must also include the Barcan formula for the contextual and projection operators:

- | | | |
|---------|---|-----------------------------------|
| (AxBFC) | $\forall x\nabla^c\phi \rightarrow \nabla^c\forall x\phi$, with $x \neq c$ | (Barcan formula for ∇^c); |
| (AxBFP) | $\forall x\Box\phi \rightarrow \Box\forall x\phi$ | (Barcan formula for \Box), |

as well as the counterparts of axioms (AxAD1)-(AxAD4) for the contextual operator. Similar axioms must be used to constrain the relationships between context terms, ordered by \prec or \subset , and the displacement and contextual operators. Finally, we add a number of axioms that express the properties of the temporal structure, that is, the structural properties of the contextualization and projection relations. As an example, the axiom $\forall c_1, c_2, c_3((c_3 \subset c_2 \subset c_1 \wedge \nabla^{c_1}\Box\nabla^{c_3}\phi) \rightarrow \nabla^{c_1}\Box\nabla^{c_2}\Box\nabla^{c_3}\phi)$ can be added to constrain the projection relation to be downward transitive. Different classes of structures (e.g., homogeneous and non-homogeneous) can be captured by different sets of axioms. A sound axiomatic system

for *MLTL* is reported in [Montanari *et al.*, 1992]. No completeness proof is given. In principle, one can try to directly prove it by building a canonical model for *MLTL*. However, even though there seem to be no specific technical problems to solve, the process of canonical model construction is undoubtedly very demanding in view of the size and complexity of the *MLTL* axiom system. As a matter of fact, one can follow an alternative approach, based on the technique proposed by Finger and Gabbay in [Finger and Gabbay, 1996], which views temporal logics for time granularity as combinations of simpler temporal logics, and specifies what constraints such combinations must satisfy to guarantee the transference of logical properties (including completeness results) from the component logics to the combined ones. In Section 3.4.3 we shall present temporal logics for time granularity which are obtained as suitable combinations of existing linear and branching temporal logics.

We conclude the section with a discussion of two classical problems about granularity conversions. The first problem has already been pointed out at the beginning of the section: given the truth value of a formula with respect to a certain layer, can we constrain (and how) its truth value with respect to the other layers? In [Montanari and Policriti, 1996], Montanari and Policriti give an example of a proposition which is true at every point of a given layer, and false with respect to every point of another one. It follows that, in general, we can record the links explicitly provided by the user, but we cannot impose any other constraint about the truth value of a formula with respect to a layer different from the layer it is associated with. Accordingly, *MLTL* makes it possible to write formulas involving granularity changes, but the proposed axiomatic systems do not impose any general constraint on the relations among the truth values of a formula with respect to different layers. Nevertheless, from a practical point of view, it makes sense to look for general rules expressing *typical* relations among truth values. In [Ciapessoni *et al.*, 1993], Ciapessoni *et al.* introduce two consistency rules that respectively allow one to project simple *MLTL* formulas, that is, *MLTL* formulas devoid of any occurrence of the displacement, contextual, and projection operators, from coarser to finer layers (downward temporal projection) and from finer to coarser ones (upward temporal projection). For any given pair of layers T^i, T^j , with $T^j \prec T^i$, any point $x \in T^i$, and any simple formula ϕ , *downward temporal projection* states that if ϕ holds at x , then there exists at least one $y \in T^j$ such that $\downarrow(x, y)$ and ϕ holds at y , while *upward temporal projection* states that if ϕ holds at every $y \in T^j$ such that $\downarrow(x, y)$, then ϕ holds at x . Formally, downward temporal projection is defined by the formula $\forall c_1, c_2 (c_2 \subset c_1 \rightarrow \nabla^{c_1}(\phi \rightarrow \diamond \Delta^{c_2} \phi))$, while upward temporal projection is defined by the formula $\forall c_1, c_2 (c_2 \subset c_1 \rightarrow \nabla^{c_1}(\Box \nabla^{c_2} \phi \rightarrow \phi))$. It is not difficult to show that the two formulas are *inter-deducible* [Montanari, 1996]. (Downward) temporal projection captures the *weakest semantics* that can be attached to a statement with respect to a layer finer than the original one, provided that the statement is not wholistic. In most cases, however, such semantics is too weak, and additional user qualifications are needed. Various domain-specific categorizations of statements have been proposed in the literature [Roman, 1990; Shoham, 1988], which allow one to classify statements according to their behavior under temporal projection, e.g., events, properties, facts, and processes. In [Montanari, 1994], Montanari proposes some specializations of the *MLTL* projection operator \diamond that allow one to define different types of temporal projection, distinguishing among statements that hold at one and only one point of the decomposition interval (*punctual*), statements that hold at every point of such an interval (*continuous and pervasive*), statements that hold over a scattered sequence of sub-intervals of the decomposition interval (*bounded sequence*), and so on.

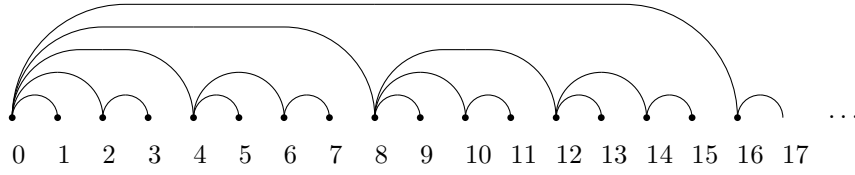
The second problem is the synchronization problem. We introduced this problem in Section 3.2, where we showed that the interpretations of the statements ‘‘tomorrow I will eat’’ and ‘‘dinner will be ready in one hour’’ with respect to a layer finer than the layer they explicitly refer to differ a lot. It is not difficult to show that even the same statement may admit different interpretations with respect to different finer layers (a detailed example can be found in [Montanari, 1996]). In general, the synchronization problem arises when logical formulas which state that a given fact holds at a point y of a layer T^i at distance α from the current point x need to be interpreted with respect to a finer layer T^j . There exist at least two possible interpretations for the original formula with respect to T^j (for the sake of simplicity, we restrict our attention to facts encoded by simple *MLTL* formulas, with a punctual interpretation under temporal projection, and we assume the temporal universe to be homogeneous). The first interpretation maps x (resp. y) into an arbitrary point x' (resp. y') of its decomposition interval, thus allowing the distance α' between x' and y' to vary. If x precedes y , we get the minimum (resp. maximum) value for α' when x' is the last (resp. first) element of the decomposition interval for x and y' is the first (resp. last) element of the decomposition interval for y . The second interpretation forces the mapping for y to conform to the mapping for x . As an example, if x is mapped into the first element of its decomposition interval, then y is mapped into the first element of its decomposition interval as well. As a consequence, there exists only one possible value for the distance α' . The first interpretation can be easily expressed in *MLTL* (it is the interpretation underlying the semantics of the projection operator). In order to enable *MLTL* to support the second interpretation, two extensions are needed: (i) we must replace the notion of current point by the notion of *vector* of current points (one for each layer); (ii) we must define a new projection operator that maps the current point of T^i into the current point of T^j , for every pair of layers T^i, T^j . Such extensions are accomplished in [Montanari, 1994]. In particular, it is possible to show that the new projection operator is second-order definable in terms of the original one, and that both projection operators are (second-order) definable in terms of a third simpler projection operator that maps every point into the first elements of its decomposition (and abstraction) intervals.

3.4.2 Monadic theories of time granularity

We move now from the temporal logic setting to the classical one, focusing our attention on monadic theories of time granularity. First, we introduce the relational structures for time granularity; then we present the theories of such structures and we analyze their decision problem. At the end, we briefly study the definability and decidability of meaningful binary predicates for time granularity with respect to such theories and some fragments of them.

Relational structures for time granularity

We begin with some preliminary definitions about finite and infinite sequences and trees (we assume the reader to be familiar with the notation and the basic notions of the theory of formal languages). Let A be a finite set of symbols and A^* be its Kleene closure. The length of a string $x \in A^*$, denoted by $|x|$, is defined in the usual way: $|\epsilon|=0$, $|xa|=|x|+1$. For any pair $x, y \in A^*$, we say that x is a *prefix* of y , denoted by $x <_{pre} y$, if $xw = y$ for some $w \in A^+ (= A^* \setminus \{\epsilon\})$. The *prefix* relation $<_{pre}$ is a partial ordering over A^* . If A is totally ordered, a total ordering over A^* can be obtained from the one over A as follows. Let $<$ be

Figure 3.1: The structure of the relation flip_2 .

the total ordering over A . For every $x, y \in A^*$, we say that x lexicographically precedes y with respect to $<$, denoted $x <_{lex} y$, if either $x <_{pre} y$ or there exist $z \in A^*$ and $a, b \in A$ such that $za \leq_{pre} x$, $zb \leq_{pre} y$, and $a < b$. The *lexicographical* relation $<_{lex}$ is a total ordering over A^* .

A *finite sequence* is a relational structure $s = \langle I, < \rangle$, where I is an initial segment of the natural numbers \mathbb{N} and $<$ is the usual ordering over \mathbb{N} . Given a *finite* set of monadic predicate symbols \mathcal{P} , a \mathcal{P} -labeled finite sequence is a relational structure $s_{\mathcal{P}} = \langle s, (\overline{P})_{P \in \mathcal{P}} \rangle$, where $s = \langle I, < \rangle$ and, for every $P \in \mathcal{P}$, $\overline{P} \subseteq I$ is the set of elements labeled with P (note that $\overline{P} \cap \overline{Q}$, with $P, Q \in \mathcal{P}$, can obviously be nonempty). An *infinite sequence* (ω -sequence for short) is a relational structure $s = \langle \mathbb{N}, < \rangle$ and a \mathcal{P} -labeled ω -sequence $s_{\mathcal{P}}$ is an ω -sequence s expanded with the sets \overline{P} , for $P \in \mathcal{P}$. For the sake of simplicity, hereafter we shall use the symbol P to denote both a monadic predicate and its interpretation; accordingly, we shall rewrite $s_{\mathcal{P}}$ as $\langle s, (P)_{P \in \mathcal{P}} \rangle$. In the following, we shall take into consideration three binary relations over \mathbb{N} , namely, flip_k , adj , and $2 \times$. Let $k \geq 2$. The binary relation flip_k is defined as follows. Given $x, y \in \mathbb{N}$, $\text{flip}_k(x, y)$, also denoted $\text{flip}_k(x) = y$, if $y = x - z$, where z is the least power of k with non-null coefficient in the k -ary representation of x . Formally, $\text{flip}_k(x) = y$ if $x = a_n \cdot k^n + a_{n-1} \cdot k^{n-1} + \dots + a_m \cdot k^m$, $0 \leq a_i \leq k-1$, $a_m \neq 0$, and $y = a_n \cdot k^n + a_{n-1} \cdot k^{n-1} + \dots + (a_m - 1) \cdot k^m$. For instance, $\text{flip}_2(18, 16)$, since $18 = 1 \cdot 2^4 + 1 \cdot 2^1$, $m = 1$, and $16 = 1 \cdot 2^4 + 0 \cdot 2^1$, while $\text{flip}_2(16, 0)$, since $16 = 1 \cdot 2^4$, $m = 4$, and $0 = 0 \cdot 2^4$. Note that there exists no y such that $\text{flip}_2(0, y)$. The structure of flip_2 is depicted in Figure 3.1. The relation adj is defined as follows: $\text{adj}(x, y)$, also denoted $\text{adj}(x) = y$, if $x = 2^{k_n} + 2^{k_{n-1}} + \dots + 2^{k_0}$, with $k_n > k_{n-1} > \dots > k_0 > 0$, and $y = x + 2^{k_0} + 2^{k_0-1}$. For instance, $\text{adj}(12, 18)$, since $12 = 2^3 + 2^2$, $k_0 = 2$, and $18 = 12 + 2^2 + 2^1$, while there exists no y such that $\text{adj}(13, y)$, since $13 = 2^3 + 2^2 + 2^0$ and $k_0 = 0$. Finally, for any pair $x, y \in \mathbb{N}$, it holds that $2 \times (x, y)$ if $y = 2x$.

Finite and infinite (k -ary) trees are defined as follows. Let $k \geq 2$ and T_k be the set $\{0, \dots, k-1\}^*$. A set $D \subseteq T_k$ is a (k -ary) *tree domain* if:

1. D is *prefix closed*, that is, for every $x, y \in T_k$, if $x \in D$ and $y <_{pre} x$, then $y \in D$;
2. for every $x \in T_k$, either $xi \in D$ for every $0 \leq i \leq k-1$ or $xi \notin D$ for every $0 \leq i \leq k-1$.

Note that, according to the definition, the whole T_k is a tree domain. A *finite tree* is a relational structure $\kappa = \langle D, (\downarrow_i)_{i=0}^{k-1}, <_{pre} \rangle$, where D is a finite tree domain, for every $0 \leq i \leq k-1$, \downarrow_i is the i -th *successor relation* over D such that $\downarrow_i(x, y)$, also denoted $\downarrow_i(x) = y$, if $y = xi$, and $<_{pre}$ is the prefix ordering over D defined as above. The elements of D are

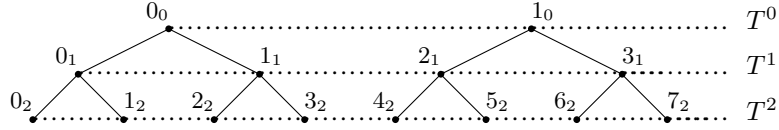


Figure 3.2: The 2-refinable 3-layered structure.

called *nodes*. If $\downarrow_i(x) = y$, then y is said the i -th *son* of x . The lexicographical ordering $<_{lex}$ over D is defined with respect to the natural ordering $<$ over $\{0, \dots, k-1\}$ such that $0 < 1 < \dots < k-1$. A *path* P in κ is a subset of D whose nodes can be written as a sequence x_0, x_1, \dots such that, for every $i > 0$, there exists $0 \leq j \leq k-1$ with $x_i = \downarrow_j(x_{i-1})$. We shall denote by $P(i)$ the i -th element x_i of the path P . A *full path* is a maximal path with respect to set inclusion. A *chain* is any subset of a path. The *root* of κ is the node ϵ . A *leaf* of κ is an element $x \in D$ devoid of sons. A node which is not a leaf is called an *internal node*. The *depth* of a node $x \in D$ is the length of the (unique) path from the root ϵ to x . The *height* of κ is the maximum of the depths of the nodes in D . κ is *complete* if every leaf has the same depth. A \mathcal{P} -labeled finite tree is a relational structure $\kappa = \langle D, (\downarrow_i)_{i=0}^{k-1}, <_{pre}, (P)_{P \in \mathcal{P}} \rangle$, where the tuple $(D, (\downarrow_i)_{i=0}^{k-1}, <_{pre})$ is a finite tree and, for every $P \in \mathcal{P}$, $P \subseteq D$ is the set of nodes labeled with P . As for infinite trees, we are interested in *complete* infinite trees over the tree domain T_k . The complete *infinite tree* over T_k is the tuple $\kappa = \langle T_k, (\downarrow_i)_{i=0}^{k-1}, <_{pre} \rangle$. Paths, full paths, and chains are defined as for finite trees. A \mathcal{P} -labeled infinite tree is an expansion of the complete infinite tree over T_k with monadic predicates P , for $P \in \mathcal{P}$.

Relational structures for time granularity consists of a (possibly infinite) number of distinct layers/domains (we shall use the two terms interchangeably). We focus our attention on n -layered structures, which include a fixed finite number n of layers, and ω -layered structures, which feature an infinite number of layers.

Let $n \geq 1$ and $k \geq 2$. For every $0 \leq i < n$, let $T^i = \{j_i \mid j \geq 0\}$. The n -layered *temporal universe* is the set $\mathcal{U}_n = \bigcup_{0 \leq i < n} T^i$. The $(k$ -refinable) n -layered *structure* (n -LS for short) is the relational structure $\langle \mathcal{U}_n, (\downarrow_j)_{j=0}^{k-1}, < \rangle$. Such a structure can be viewed as an infinite sequence of complete (k -ary) trees of height $n-1$, each one rooted at a point of the coarsest layer T^0 (see Figure 3.2). The sets T^i , with $0 \leq i < n$, are the layers of the trees. For every $0 \leq j \leq k-1$, \downarrow_j is the j -th *successor relation* over \mathcal{U}_n such that $\downarrow_j(x, y)$ (also denoted $\downarrow_j(x) = y$) if y is the j -th son of x . Hereafter, to adhere to the common terminology in the field, we shall substitute the term *projection* for the term *successor*. Note that for all x belonging to the finest layer T^{n-1} there exist no $0 \leq j \leq k-1$ and $y \in \mathcal{U}_n$ such that $\downarrow_j(x) = y$. Finally, $<$ is a total ordering over \mathcal{U}_n given by the *pre-order* (root-left-right in the binary trees) visit of the nodes (for elements belonging to the same tree) and by the total linear ordering of trees (for elements belonging to different trees). Formally, for any pair $a_b, c_d \in \mathcal{U}_n$, we have that $\downarrow_j(a_b) = c_d$ if $b < n-1$, $d = b+1$, and $c = a \cdot k + j$. The total ordering $<$ is defined as follows:

1. if $x = a_0, y = b_0$, and $a < b$ over \mathbb{N} , then $x < y$;

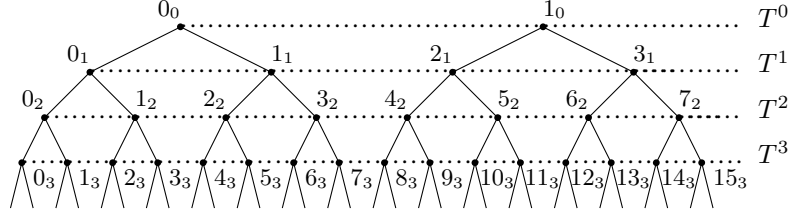


Figure 3.3: The 2-refinable downward unbounded layered structure.

2. for all $x \in \mathcal{U}_n \setminus T^{n-1}$, $x < \downarrow_0(x)$, and $\downarrow_j(x) < \downarrow_{j+1}(x)$, for all $0 \leq j < k-1$;
3. if $x \in \mathcal{U}_n \setminus T^{n-1}$, $x < y$, and not $\text{ancestor}(x, y)$, then $\downarrow_{k-1}(x) < y$;
4. if $x < z$ and $z < y$, then $x < y$,

where $\text{ancestor}(x, y)$ if there exists $0 \leq j \leq k-1$ such that $\downarrow_j(x) = y$ or there exist $0 \leq j \leq k-1$ and z such that $\downarrow_j(z) = y$ and $\text{ancestor}(x, z)$. A *path* over the n -LS is a subset of the domain whose elements can be written as a sequence x_0, x_1, \dots, x_m , with $m \leq n-1$, in such a way that, for every $i = 1, \dots, m$, there exists $0 \leq j < k$ for which $x_i = \downarrow_j(x_{i-1})$. A *full path* is a maximal path with respect to set inclusion. A *chain* is any subset of a path. A \mathcal{P} -labeled n -LS is a relational structure $\langle \mathcal{U}_n, (\downarrow_i)_{i=0}^{k-1}, <, (P)_{P \in \mathcal{P}} \rangle$, where the tuple $(\mathcal{U}_n, (\downarrow_i)_{i=0}^{k-1}, <)$ is the n -LS and, for every $P \in \mathcal{P}$, $P \subseteq \mathcal{U}_n$ is the set of points labeled with P .

As for ω -layered structures, we focus our attention on the (k -refinable) downward unbounded layered structure (DULS for short), which consists of a coarsest domain together with an infinite number of finer and finer domains, and the (k -refinable) upward unbounded layered structure (UULS for short), which consists of a finest temporal domain together with an infinite number of coarser and coarser domains. Let $\mathcal{U} = \bigcup_{i \geq 0} T^i$ be the ω -layered temporal universe. The DULS is a relational structure $\langle \mathcal{U}, (\downarrow_i)_{i=0}^{k-1}, < \rangle$. It can be viewed as an infinite sequence of complete (k -ary) infinite trees, each one rooted at a point of the coarsest domain T^0 (see Figure 3.3). The sets T^i , with $i \geq 0$, are the layers of the trees. The definitions of the projection relations \downarrow_j , with $0 \leq j \leq k-1$, and the total ordering $<$ over \mathcal{U} are close to those for the n -LS. Formally, for any pair $a_b, c_d \in \mathcal{U}$, we have that $\downarrow_j(a_b) = c_d$ if and only if $d = b+1$ and $c = a \cdot k + j$, while the total ordering $<$ is defined as follows:

1. if $x = a_0, y = b_0$, and $a < b$ over \mathbb{N} , then $x < y$;
2. for all $x \in \mathcal{U}$, $x < \downarrow_0(x)$, and $\downarrow_j(x) < \downarrow_{j+1}(x)$, for all $0 \leq j < k-1$;
3. if $x < y$ and not $\text{ancestor}(x, y)$, then $\downarrow_{k-1}(x) < y$;
4. if $x < z$ and $z < y$, then $x < y$.

A *path* over the DULS is a subset of the domain whose elements can be written as an infinite sequence x_0, x_1, \dots such that, for every $i \geq 1$, there exists $0 \leq j < k$ for which $x_i = \downarrow_j(x_{i-1})$. A *full path* is a maximal (infinite) path with respect to set inclusion. A *chain* is

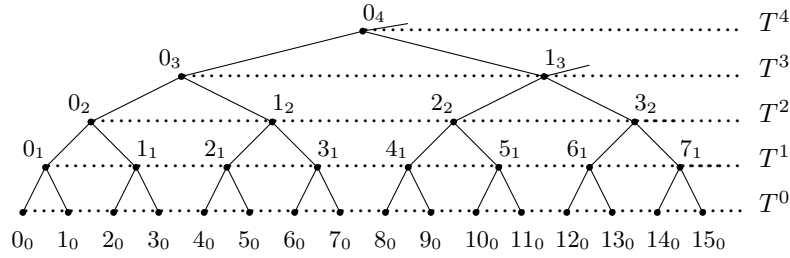


Figure 3.4: The 2-refinable upward unbounded layered structure.

any subset of a path. A \mathcal{P} -labeled DULS is a relational structure $\langle \mathcal{U}, (\downarrow_i)_{i=0}^{k-1}, <, (P)_{P \in \mathcal{P}} \rangle$, where the tuple $(\mathcal{U}, (\downarrow_i)_{i=0}^{k-1}, <)$ is the DULS and, for every $P \in \mathcal{P}$, $P \subseteq \mathcal{U}$ is the set of points labeled with P .

The UULS is a relational structure $\langle \mathcal{U}, (\downarrow_i)_{i=0}^{k-1}, < \rangle$. It can be viewed as a complete (k -ary) infinite tree generated from the leaves (Figure 3.4). The sets T^i , with $i \geq 0$, are the layers of the tree. For every $0 \leq j \leq k-1$, \downarrow_j is the j -th *projection relation* over \mathcal{U} such that $\downarrow_j(x, y)$ (also denoted by $\downarrow_j(x) = y$) if y is the j -th son of x . The total ordering $<$ over \mathcal{U} is induced by the *in-order* (left-root-right in the binary tree) visit of the treelike structure. Formally, for every $a_b, c_d \in \mathcal{U}$, $\downarrow_j(a_b) = c_d$ if $b > 0$, $d = b - 1$, and $c = a \cdot k + j$. The total ordering $<$ is defined as follows:

1. for all $x \in \mathcal{U} \setminus T^0$, $\downarrow_0(x) < x$, $x < \downarrow_1(x)$, and $\downarrow_j(x) < \downarrow_{j+1}(x)$, for every $0 < j < k - 1$;
2. if $x < y$ and not $\text{ancestor}(x, y)$, then $\downarrow_{k-1}(x) < y$;
3. if $x < y$ and not $\text{ancestor}(y, x)$, then $x < \downarrow_0(y)$;
4. if $x < z$ and $z < y$, then $x < y$.

A *path* over the UULS is a subset of the domain whose elements can be written as an infinite sequence x_0, x_1, \dots such that, for every $i \geq 1$, there exists $0 \leq j < k$ such that $x_{i-1} = \downarrow_j(x_i)$. A *full path* is a maximal (infinite) path with respect to set inclusion. A *chain* is any subset of a path. It is worth noting that every pair of paths over the UULS may differ on a finite prefix only. A \mathcal{P} -labeled UULS is obtained by expanding the UULS with a set $P \subseteq \mathcal{U}$, for any $P \in \mathcal{P}$.

Theories of time granularity

We are now ready to introduce the theories of time granularity. They are systems of monadic second-order (MSO for short) logic that allow quantification over arbitrary sets of elements. We shall study the properties of the full systems as well as of some meaningful fragments of them. We shall show that some granularity theories can be reduced to well-know classical MSO theories, such as the MSO theory of one successor and the MSO theory of two successors, while other granularity theories are proper extensions of them.

Definition 3.4.1. (*The language of monadic second-order logic*)

Let $\tau = c_1, \dots, c_r, u_1, \dots, u_s, b_1, \dots, b_t$ be a finite alphabet of symbols, where c_1, \dots, c_r (resp. $u_1, \dots, u_s, b_1, \dots, b_t$) are constant symbols (resp. unary relational symbols, binary relational symbols), and let \mathcal{P} be a finite set of uninterpreted unary relational symbols. The second-order language with equality $\text{MSO}[\tau \cup \mathcal{P}]$ is built up as follows:

1. atomic formulas are of the forms $x = y$, $x = c_i$, with $1 \leq i \leq r$, $u_i(x)$, with $1 \leq i \leq s$, $b_i(x, y)$, with $1 \leq i \leq t$, $x \in X$, $x \in P$, where x, y are individual variables, X is a set variable, and $P \in \mathcal{P}$;
2. formulas are built up from atomic formulas by means of the Boolean connectives \neg and \wedge , and the quantifier \exists ranging over both individual and set variables.

In the following, we shall write $\text{MSO}_{\mathcal{P}}[\tau]$ for $\text{MSO}[\tau \cup \mathcal{P}]$; in particular, we shall write $\text{MSO}[\tau]$ when \mathcal{P} is meant to be the empty set. The first-order fragment of $\text{MSO}_{\mathcal{P}}[\tau]$ will be denoted by $\text{FO}_{\mathcal{P}}[\tau]$, while its path (resp. chain) fragment, which is obtained by interpreting second-order variables over paths (resp. chains), will be denoted by $\text{MPL}_{\mathcal{P}}[\tau]$ (resp. $\text{MCL}_{\mathcal{P}}[\tau]$). We focus our attention on the following theories:

1. $\text{MSO}_{\mathcal{P}}[<]$ and its first-order fragment interpreted over finite and ω -sequences;
2. $\text{MSO}_{\mathcal{P}}[<, \text{flip}_k]$ (as well as its first-order fragment), $\text{MSO}_{\mathcal{P}}[<, \text{adj}]$, and $\text{MSO}_{\mathcal{P}}[<, 2\times]$ interpreted over ω -sequences;
3. $\text{MSO}_{\mathcal{P}}[<_{pre}, (\downarrow_i)_{i=0}^{k-1}]$ and its first-order, path, and chain fragments interpreted over finite and infinite trees;
4. $\text{MSO}_{\mathcal{P}}[<, (\downarrow_i)_{i=0}^{k-1}]$ and its first-order, path, and chain fragments interpreted over the n -LS, the DULS, and the UULS.

We preliminarily introduce some notations and basic properties that will help us in comparing the expressive power and logical properties of the various theories. Most definitions and results are given for full MSO theories with uninterpreted unary relational symbols, but they immediately transfer to their fragments, possibly devoid of uninterpreted unary relational symbols.

Let $\mathcal{M}(\varphi)$ be the set of models of the formula φ . We say that $\text{MSO}_{\mathcal{P}}[\tau_1]$ can be *embedded* into $\text{MSO}_{\mathcal{P}}[\tau_2]$, denoted $\text{MSO}_{\mathcal{P}}[\tau_1] \rightarrow \text{MSO}_{\mathcal{P}}[\tau_2]$, if there is an *effective* translation tr of $\text{MSO}_{\mathcal{P}}[\tau_1]$ -formulas into $\text{MSO}_{\mathcal{P}}[\tau_2]$ -formulas such that, for every formula $\varphi \in \text{MSO}_{\mathcal{P}}[\tau_1]$, $\mathcal{M}(\varphi) = \mathcal{M}(tr(\varphi))$. For instance, it is easy to prove that $\text{FO}_{\mathcal{P}}[<_{pre}, (\downarrow_i)_{i=0}^{k-1}] \rightarrow \text{MPL}_{\mathcal{P}}[<_{pre}, (\downarrow_i)_{i=0}^{k-1}] \rightarrow \text{MCL}_{\mathcal{P}}[<_{pre}, (\downarrow_i)_{i=0}^{k-1}] \rightarrow \text{MSO}_{\mathcal{P}}[<_{pre}, (\downarrow_i)_{i=0}^{k-1}]$ (the same holds for their counterparts devoid of \mathcal{P}), where all theories are interpreted over trees. The condition ‘ X is a path’ can indeed be written in the monadic chain logic, and the condition ‘ X is a chain’ can be expressed in the MSO logic. It is also easy to show that the monadic path logic over paths is as expressive as the monadic path logic over full paths. Moreover, we say that $\text{MSO}_{\mathcal{P}}[\tau_1]$ is *as expressive as* $\text{MSO}_{\mathcal{P}}[\tau_2]$, written $\text{MSO}_{\mathcal{P}}[\tau_1] \rightleftharpoons \text{MSO}_{\mathcal{P}}[\tau_2]$, if both $\text{MSO}_{\mathcal{P}}[\tau_1] \rightarrow \text{MSO}_{\mathcal{P}}[\tau_2]$ and $\text{MSO}_{\mathcal{P}}[\tau_2] \rightarrow \text{MSO}_{\mathcal{P}}[\tau_1]$. It is immediate to see that if $\text{MSO}_{\mathcal{P}}[\tau_1] \rightarrow \text{MSO}_{\mathcal{P}}[\tau_2]$ and $\text{MSO}_{\mathcal{P}}[\tau_2]$ is decidable (resp. $\text{MSO}_{\mathcal{P}}[\tau_1]$ is undecidable), then $\text{MSO}_{\mathcal{P}}[\tau_1]$ is decidable (resp. $\text{MSO}_{\mathcal{P}}[\tau_2]$ is undecidable) as well.

Besides decidability issues, we are interested in definability ones. Let β be a relational symbol. We say that β is *definable* in $\text{MSO}_{\mathcal{P}}[\tau]$ if $\text{MSO}_{\mathcal{P}}[\tau \cup \{\beta\}] \rightarrow \text{MSO}_{\mathcal{P}}[\tau]$. If the

addition of β to a decidable theory $\text{MSO}_{\mathcal{P}}[\tau]$ makes the resulting theory $\text{MSO}_{\mathcal{P}}[\tau \cup \{\beta\}]$ undecidable, we can conclude that β is not definable in $\text{MSO}_{\mathcal{P}}[\tau]$. The opposite does not hold in general: the predicate β may not be definable in $\text{MSO}_{\mathcal{P}}[\tau]$, but the extension of $\text{MSO}_{\mathcal{P}}[\tau]$ with β may preserve decidability. In such a case, we obviously cannot reduce the decidability of $\text{MSO}_{\mathcal{P}}[\tau \cup \{\beta\}]$ to that of $\text{MSO}_{\mathcal{P}}[\tau]$.

The decidability of $\text{MSO}_{\mathcal{P}}[<]$ over finite sequences has been proved in [B chi, 1960; Elgot, 1961], while its decidability over ω -sequences has been shown in [B chi, 1962] ($\text{MSO}_{\mathcal{P}}[<]$ over ω -sequences is the well-known MSO theory of one successor $S1S$).

Theorem 3.4.2. (*Decidability of $\text{MSO}_{\mathcal{P}}[<]$ over sequences*)

$\text{MSO}_{\mathcal{P}}[<]$ over finite (resp. infinite) sequences is non-elementarily decidable.

The theory $\text{MSO}_{\mathcal{P}}[<, \text{flip}_k]$ ($S1S^k$ for short), interpreted over ω -sequences, has been studied by Monti and Peron in [Monti and Peron, 2000]. Such a theory properly extends $S1S$. Moreover, the unary predicate pow_k such that $\text{pow}_k(x)$ if x is a power of k can be easily expressed as $\text{flip}_k(x) = 0$. Hence, $S1S^k$ is at least as expressive as the well-known (decidable) extension of $\text{MSO}_{\mathcal{P}}[<]$ with the predicate pow_k [Elgot and Rabin, 1966]. The decidability of $S1S^k$ has been proved by showing that it is the logical counterpart of the class of ω -sequences languages (ω -languages for short) recognized by systolic (k -ary) tree automata. The class of the languages of finite sequences recognized by systolic tree automata was originally investigated by Culik II et al. in [Culik II et al., 1984]. In [Monti and Peron, 2000], Monti and Peron extend the notion of systolic tree automaton to deal with ω -languages. They prove that the class of systolic tree ω -languages is a proper extension of the class of regular ω -languages (that is, ω -languages recognized by B chi automata), that maintains the closure properties of regular ω -languages as well as the decidability of the emptiness problem. The correspondence between systolic tree ω -languages and $S1S^k$ is established by means of a generalization of B chi's Theorem.

Theorem 3.4.3. (*Decidability of $\text{MSO}_{\mathcal{P}}[<, \text{flip}_k]$ over ω -sequences*)

$\text{MSO}_{\mathcal{P}}[<, \text{flip}_k]$ over ω -sequences is non-elementarily decidable.

The theories $\text{MSO}_{\mathcal{P}}[<, \text{adj}]$ and $\text{MSO}_{\mathcal{P}}[<, 2\times]$, interpreted over ω -sequences, have been investigated in [Monti and Peron, 2001]. $\text{MSO}_{\mathcal{P}}[<, \text{adj}]$ is a proper extension $\text{MSO}_{\mathcal{P}}[<, \text{flip}_2]$. Unfortunately, unlike $\text{MSO}_{\mathcal{P}}[<, \text{flip}_2]$, it is undecidable.

Theorem 3.4.4. (*Undecidability of $\text{MSO}_{\mathcal{P}}[<, \text{adj}]$ over ω -sequences*)

$\text{MSO}_{\mathcal{P}}[<, \text{adj}]$ over infinite sequences is undecidable.

Since $\text{MSO}_{\mathcal{P}}[<, 2\times]$ is at least as expressive as $\text{MSO}_{\mathcal{P}}[<, \text{adj}]$, its decision problem is undecidable as well.

Theorem 3.4.5. (*Undecidability of $\text{MSO}_{\mathcal{P}}[<, 2\times]$ over ω -sequences*)

$\text{MSO}_{\mathcal{P}}[<, 2\times]$ over ω -sequences is undecidable.

The theories $\text{MSO}_{\mathcal{P}}[<_{pre}, (\downarrow_i)_{i=0}^{k-1}]$, interpreted over infinite (k -ary) trees, are the well-known MSO theories of k successors (SkS for short). The decidability of SkS over finite trees has been shown in [Doner, 1970; Thatcher and Wright, 1968]. The decidability of the MSO theory of the infinite binary tree $S2S$ has been proved in [Rabin, 1969]. Such a result can be easily generalized to the MSO theory of the infinite k -ary tree SkS , for any $k > 2$ (and even to $S\omega S$ over countably branching trees) [Thomas, 1990].

Theorem 3.4.6. (*Decidability of $\text{MSO}_{\mathcal{P}}[\prec_{pre}, (\downarrow_i)_{i=0}^{k-1}]$ over trees*)

$\text{MSO}_{\mathcal{P}}[\prec, (\downarrow_i)_{i=0}^{k-1}]$ over finite (resp. infinite) trees is non-elementarily decidable.

The decidability of $\text{MSO}_{\mathcal{P}}[\prec, (\downarrow_i)_{i=0}^{k-1}]$ over the n -LS has been proved in [Montanari and Policriti, 1996] by reducing it to $S1S$. Such a reduction is accomplished in two steps. First, the n -layered structure is flattened by embedding all its layers into the finest one; then, metric temporal information is encoded by means of a finite set of unary relations. This second step is closely related to the technique exploited in [Alur and Henzinger, 1993] to prove the decidability of a family of real-time logics*. It relies on the *finite-state character* of the involved metric temporal information, which can be expressed as follows: every temporal property that partition an infinite set of states/time points into a finite set of classes can be finitely modeled and hence it is decidable.

Theorem 3.4.7. (*Decidability of $\text{MSO}_{\mathcal{P}}[\prec, (\downarrow_i)_{i=0}^{k-1}]$ over the n -LS*)

$\text{MSO}_{\mathcal{P}}[\prec, (\downarrow_i)_{i=0}^{k-1}]$ over the n -LS is non-elementarily decidable.

The decidability of $\text{MSO}_{\mathcal{P}}[\prec, (\downarrow_i)_{i=0}^{k-1}]$ over both the DULS and the UULS has been shown in [Montanari et al., 1999]. The decidability of the theory of the DULS has been proved by embedding it into SkS . The infinite sequence of infinite trees of the k -refinable DULS can indeed be appended to the rightmost full path of the infinite k -ary tree. The encoding of the 2-refinable DULS into the infinite binary tree is shown in Figure 3.5. Suitable definable predicates are then used to distinguish between the nodes of the infinite tree that correspond to elements of the original DULS, and the other nodes. As an example, in the case depicted in Figure 3.5 we must differentiate the auxiliary nodes belonging to the rightmost full path of the tree from the other ones. Finally, for $0 \leq j \leq k-1$, the j -th projection relation \downarrow_j can be interpreted as the j -th successor relation and the total order \prec can be naturally mapped into the lexicographical ordering \prec_{lex} (it is not difficult to show that \prec_{lex} can be defined in SkS).

Theorem 3.4.8. (*Decidability of $\text{MSO}_{\mathcal{P}}[\prec, (\downarrow_i)_{i=0}^{k-1}]$ over the DULS*)

$\text{MSO}_{\mathcal{P}}[\prec, (\downarrow_i)_{i=0}^{k-1}]$ over the DULS is non-elementarily decidable.

The decidability of the theory of the UULS has been proved by reducing it to $S1S^k$. For the sake of simplicity, we describe the basic steps of this reduction in the case of the 2-refinable UULS (the technique can be generalized to deal with any $k > 2$). An embedding of $\text{MSO}[\prec, \downarrow_0, \downarrow_1]$ into $S1S^2$ can be obtained as follows. First, we replace the 2-refinable UULS by the so-called *concrete* 2-refinable ULLS, which is defined as follows:

- for all $i \geq 0$, the i -th layer T^i is the set $\{2^i + n2^{i+1} : n \geq 0\} \subseteq \mathbb{N}$;

*The relationships between the theories of n - and ω -layered structures and real-time logics have been explored in detail by Montanari et al. in [Montanari et al., 2000]. Logic and computer science communities have traditionally followed a different approach to the problem of representing and reasoning about time and states. Research in logic resulted in a family of (metric) tense logics that take *time* as a primitive notion and define (*timed*) states as sets of atomic propositions which are true at given time points, while research in computer science concentrated on the so-called (real-time) temporal logics of programs that take *state* as a primitive notion, and define *time* as an attribute of states. Montanari et al. show that the theories of time granularity provide a unifying framework within which the two approaches can be reconciled. States and time-points can indeed be uniformly referred to as elements of the (decidable) theories of the DULS and the UULS. In particular, they show that the theory of timed state sequences, underlying real-time logics, can be naturally recovered as an abstraction of such theories.

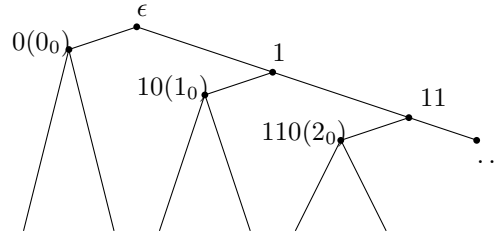
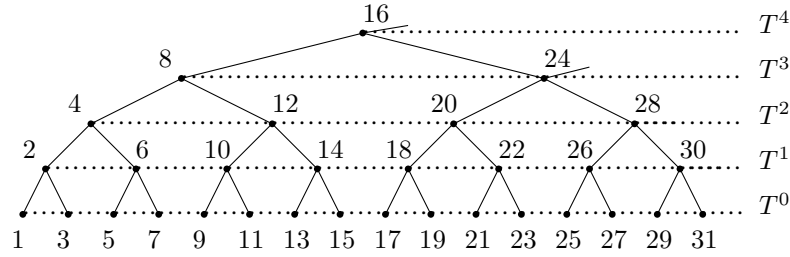
Figure 3.5: The encoding of the 2-refinable DULS into $\{0, 1\}^*$.

Figure 3.6: The concrete 2-refinable UULS.

- for every element $x = 2^i + n2^{i+1}$ belonging to T^i , with $i \geq 1$, $\downarrow_0(x) = 2^i + n2^{i+1} - 2^{i-1} = 2^{i-1} + 2n2^i$ and $\downarrow_1(x) = 2^i + n2^{i+1} + 2^{i-1} = 2^{i-1} + (2n+1)2^i$;
- $<$ is the usual ordering over \mathbb{N} .

A fragment of this concrete structure is depicted in Figure 3.6. Notice that all odd numbers are associated with layer T^0 , while even numbers are distributed over the remaining layers. Notice also that the labeling of the concrete structure does not include the number 0^* . It is easy to show that the two structures are isomorphic by exploiting the obvious mapping that associates each element of the 2-refinable UULS with the corresponding element of the concrete structure, preserving projection and ordering relations. Hence, the two structures satisfy the same $MSO[<, \downarrow_0, \downarrow_1]$ -formulas. Next, we can easily encode the concrete 2-refinable UULS into \mathbb{N} . Both relations \downarrow_0 and \downarrow_1 can indeed be defined in terms of flip_2 as follows. For any given even number x ,

$$\begin{aligned} \downarrow_0(x) = y & \quad \text{iff} \quad y < x \wedge \text{flip}_2(y) = \text{flip}_2(x) \wedge \\ & \quad \neg \exists z (y < z \wedge z < x \wedge \text{flip}_2(z) = \text{flip}_2(x)); \\ \downarrow_1(x) = y & \quad \text{iff} \quad \text{flip}_2(y) = x \wedge \neg \exists z (y < z \wedge \text{flip}_2(z) = x). \end{aligned}$$

By exploiting such a correspondence, it is possible to define a translation τ of $MSO[<, \downarrow_0, \downarrow_1]$ formulas (resp. sentences) into $S1S^2$ formulas (resp. sentences) such that, for any formula

*In [Montanari et al., 2002a], Montanari et al. show that it is convenient to consider 0 as the label of the first node of an imaginary additional finest layer, whose remaining nodes are not labeled. In such a way the node with label 0 turns out to be the left son of the node with label 1.

(resp. sentence) $\phi \in \text{MSO}[\langle, \downarrow_0, \downarrow_1]$, ϕ is satisfiable by (resp. true in) the UULS if and only if $\tau(\phi) \in S1S^2$ is satisfiable by (resp. true in) $\langle \mathbb{N}, <, \text{flip}_2 \rangle$.

Theorem 3.4.9. (*Decidability of $\text{MSO}_{\mathcal{P}}[\langle, (\downarrow_i)_{i=0}^{k-1}]$ over the UULS*)

$\text{MSO}_{\mathcal{P}}[\langle, (\downarrow_i)_{i=0}^{k-1}]$ over the UULS is non-elementarily decidable.

In [Montanari and Puppis, 2004b], Montanari and Puppis deal with the decision problem for the MSO logic interpreted over an ω -layered temporal structure devoid of both a finest layer and a coarsest one (we call such a structure totally unbounded, TULS for short). The temporal universe of the TULS is the set $\mathcal{U}_n = \bigcup_{i \in \mathbb{Z}} T^i$, where \mathbb{Z} is the set of integers; the layer T^0 is a distinguished intermediate layer of such a structure. It is not difficult to show that $\text{MSO}_{\mathcal{P}}[\langle, (\downarrow_i)_{i=0}^{k-1}]$ over both the DULS and the UULS can be embedded into $\text{MSO}_{\mathcal{P}}[\langle, (\downarrow_i)_{i=0}^{k-1}, L_0]$ over the TULS (L_0 is a unary relational symbol used to identify the elements of T^0). The solution to the decision problem for $\text{MSO}_{\mathcal{P}}[\langle, (\downarrow_i)_{i=0}^{k-1}, L_0]$ proposed by Montanari and Puppis extends Carton and Thomas' solution to the decision problem for the MSO theories of residually ultimately periodic words [Carton and Thomas, 2002]. First, they provide a tree-like characterization of the TULS and, taking advantage of it, they define a non-trivial encoding of the TULS into a vertex-colored tree that allows them to reduce the decision problem for the TULS to the problem of determining, for any given Rabin tree automaton, whether it accepts such a vertex-colored tree. Then, they reduce this latter problem to the decidable case of regular trees by exploiting a suitable notion of tree equivalence [Montanari and Puppis, 2004a].

Theorem 3.4.10. (*Decidability of $\text{MSO}_{\mathcal{P}}[\langle, (\downarrow_i)_{i=0}^{k-1}, L_0]$ over the TULS*)

$\text{MSO}_{\mathcal{P}}[\langle, (\downarrow_i)_{i=0}^{k-1}, L_0]$ over the TULS is non-elementarily decidable.

Notice that, taking advantage of the above-mentioned embedding, such a result provides, as a by-product, an alternative (uniform) decidability proof for the theories of the DULS and the UULS.

The definability and decidability of a set of binary predicates in monadic languages interpreted over the n -LS, the DULS, and the UULS have been systematically explored in [Franceschet *et al.*, 2003]. The set of considered predicates includes the equi-level (resp. equi-column) predicate constraining two time points to belong to the same layer (resp. column) and the horizontal (resp. vertical) successor predicate relating a time point to its successor within a given layer (resp. column), which allow one to express meaningful properties of time granularity [Montanari, 1996]. The authors investigate definability and decidability issues for such predicates with respect to $\text{MSO}[\langle, (\downarrow_i)_{i=0}^{k-1}]$ and its first-order, chain, and path fragments $\text{FO}[\langle, (\downarrow_i)_{i=0}^{k-1}]$, $\text{MPL}[\langle, (\downarrow_i)_{i=0}^{k-1}]$, and $\text{MCL}[\tau]$ of $\text{MSO}[\langle, (\downarrow_i)_{i=0}^{k-1}]$ (as well as their \mathcal{P} -variants $\text{FO}_{\mathcal{P}}[\langle, (\downarrow_i)_{i=0}^{k-1}]$, $\text{MPL}_{\mathcal{P}}[\langle, (\downarrow_i)_{i=0}^{k-1}]$, and $\text{MCL}_{\mathcal{P}}[\langle, (\downarrow_i)_{i=0}^{k-1}]$). Figure 3.7 summarizes the relationships between the expressive powers of such formal systems (an arrow from \mathcal{T} to \mathcal{T}' stands for $\mathcal{T} \rightarrow \mathcal{T}'$). From Theorems 3.4.7, 3.4.8, 3.4.9, and 3.4.10, it immediately follows that all the formalisms in Figure 3.7, when interpreted over the n -LS, the DULS, the UULS, and the TULS are decidable.

The outcomes of the analysis of the equi-level, equi-column, horizontal successor, and vertical successor predicates can be summarized as follows. First, the authors show that all these predicates are not definable in the MSO language over the DULS and the UULS, and that their addition immediately leads the MSO theories of such structures to undecidability.

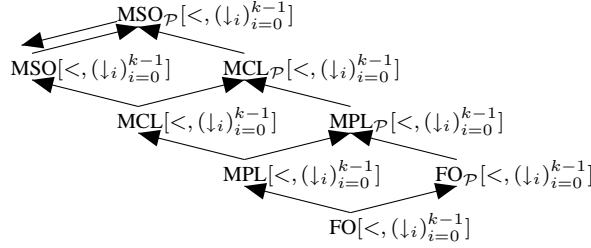


Figure 3.7: A hierarchy of monadic formalisms over layered structures.

As for the n -LS, the status of the horizontal (equi-level and horizontal successor) and vertical (equi-column and vertical successor) predicates turns out to be quite different: while horizontal predicates are easily definable, vertical ones are undefinable and their addition yields undecidability. Then, the authors study the effects of adding the above predicates to suitable *fragments* of the MSO language, such as its first-order, path, and chain fragments, possibly admitting uninterpreted unary relational symbols. They systematically explore all the possibilities, and give a number of positive and negative results. From a technical point of view, (un)definability and (un)decidability results are obtained by reduction from/to a wide spectrum of undecidable/decidable problems. Even though the complete picture is still missing (some decidability problems are open), the achieved results suffice to formulate some general statements. First, all predicates can be added to monadic first-order, path, and chain fragments, devoid of uninterpreted unary relational symbols, over the n -LS and the UULS preserving decidability. In the case of the DULS, they prove the same result for the equi-level and horizontal successor predicates, while they do not establish whether the same holds for the equi-column and vertical successor predicates. Moreover, they prove that the addition of the equi-column or vertical successor predicates to monadic first-order fragments over the ω -layered structures, with uninterpreted unary relational symbols, makes the resulting theories undecidable. The effect of such additions to the n -layered structure is not known. As for the equi-level predicate, they only prove that adding it to the monadic path fragment over the DULS, with uninterpreted unary relational symbols, leads to undecidability. Finally, as far as the MSO language over the UULS is concerned, they establish an interesting connection between its extension with the equi-level (resp. equi-column) predicate and systolic ω -languages over Y -trees (resp. trellis) [Gruska, 1990].

3.4.3 Temporalized logics and automata for time granularity

In the previous section, we have shown that monadic theories of time granularity are quite expressive, but they have not much computational appeal because their decision problem is *non-elementary*. This roughly means that it is possible to algorithmically check the truth of sentences, but the complexity of the algorithm grows very rapidly and it cannot be bounded. Moreover, the corresponding automata (Büchi sequence automata for the theory of the n -LS, Rabin tree automata for the theory of the DULS, and systolic tree automata for the theory of the UULS) do not directly work over layered structures, but rather over collapsed structures into which layered structures can be encoded. Hence, they are not natural and intuitive tools to specify and check properties of time granularity. In this section, we outline a different approach that connects monadic theories of time granularity back

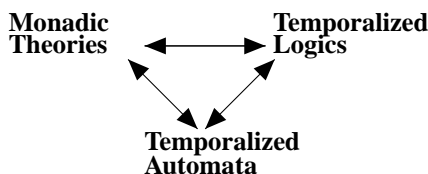


Figure 3.8: From monadic theories to temporalized logics via temporalized automata.

to temporal logic [Franceschet and Montanari, 2001a; Franceschet and Montanari, 2001b; Franceschet and Montanari, 2004]. Taking inspiration of methods for logic combinations (a short description of these methods can be found in [Franceschet *et al.*, 2004]), Franceschet and Montanari reinterpret layered structures as *combined structures*. This allows them to define suitable combined temporal logics and combined automata over layered structures, respectively called temporalized logics and temporalized automata, and to study their expressive power and computational properties by taking advantage of the transfer theorems for combined logics and combined automata. The outcome is rewarding: the resulting combined temporal logics and automata directly work over layered structures; moreover, they are expressively equivalent to monadic systems, and they are elementarily decidable.

Finding the temporal logic counterpart of monadic theories is a difficult task, involving a non-elementary blow up in the length of formulas. Ehrenfeucht games have been successfully exploited to deal with such a correspondence problem for first-order theories [Immerman and Kozen, 1989] and well-behaved fragments of second-order monadic ones, e.g., the path fragment of the monadic second-order theory of infinite binary trees [Hafer and Thomas, 1987]. As for the theories of time granularity, in [Franceschet and Montanari, 2003] Franceschet and Montanari show that an expressively complete and elementarily decidable combined temporal logic counterpart of the path fragment of the MSO theory of the DULS can be obtained by means of suitable applications of Ehrenfeucht games. Ehrenfeucht games have also been used by Montanari *et al.* to extend Kamp's theorem to deal with the first-order fragment of the MSO theory of the UULS [Montanari *et al.*, 2002a]. Unfortunately, these techniques produce rather involved proofs and they do not naturally lift to the full second-order case. A little detour is needed to deal with such a case. Instead of trying to establish a direct correspondence between MSO theories of time granularity and temporal logics, Franceschet and Montanari connect them via automata [Franceschet and Montanari, 2004] (cf. Figure 3.8). Firstly, they define the class of temporalized automata, which can be proved to be the automata-theoretic counterpart of temporalized logics, and they show that relevant properties, such as closure under Boolean operations, decidability, and expressive equivalence with respect to temporal logics, transfer from component automata to temporalized ones. Then, on the basis of the established correspondence between temporalized logics and automata, they reduce the task of finding a temporal logic counterpart of the MSO theories of the DULS and the UULS to the easier one of finding temporalized automata counterparts of them. The mapping of MSO formulas into automata (the difficult direction) can indeed greatly benefit from automata closure properties.

As a by-product, the alternative characterization of temporalized logics for time gran-

ularity as temporalized automata allows one to reduce logical problems to automata ones. As it is well-known in the area of automated system specification and verification, such a reduction presents several advantages, including the possibility of using automata for both system modeling and specification, and the possibility of checking the system on-the-fly (a detailed account of these advantages can be found in [Franceschet and Montanari, 2001b]).

3.4.4 Coda: time granularity and interval temporal logics

As pointed out in [Montanari, 1996], there exists a natural link between structures and theories of time granularity and those developed for representing and reasoning about time intervals. Differently-grained temporal domains can indeed be interpreted as different ways of partitioning a given discrete/dense time axis into consecutive disjoint intervals. According to this interpretation, every time point can be viewed as a suitable interval over the time axis and projection implements an intervals-subintervals mapping. More precisely, let us define *direct constituents* of a time point x , belonging to a given domain, the time points of the immediately finer domain into which x can be refined, if any, and *indirect constituents* the time points into which the direct constituents of x can be directly or indirectly refined, if any. The mapping of a given time point into its direct or indirect constituents can be viewed as a mapping of a given time interval into (a specific subset of) its subintervals.

The existence of such a natural correspondence between interval and granularity structures hints at the possibility of defining a similar connection at the level of the corresponding theories. For instance, according to such a connection, temporal logics over DULSs allow one to constrain a given property to hold true densely over a given time interval, where P densely holds over a time interval w if P holds over w and there exists a direct constituent of w over which P densely holds. In particular, establishing a connection between structures and logics for time granularity and those for time intervals would allow one to transfer decidability results from the granularity setting to the interval one. As a matter of fact, most interval temporal logics, including Moszkowski's Interval Temporal Logic (ITL) [Moszkowski, 1983], Halpern and Shoham's Modal Logic of Time Intervals (HS) [Halpern and Shoham, 1991], Venema's CDT Logic [Venema, 1991a], and Chaochen and Hansen's Neighborhood Logic (NL) [Chaochen and Hansen, 1998], are highly undecidable. Decidable fragments of these logics have been obtained by imposing severe restrictions on their expressive power, e.g., the *locality* constraint in [Moszkowski, 1983].

Preliminary results can be found in [Montanari *et al.*, 2002b], where the authors propose a new interval temporal logic, called Split Logic (SL for short), which is equipped with operators borrowed from HS and CDT, but is interpreted over specific interval structures, called *split-frames*. The distinctive feature of a split-frame is that there is at most one way to chop an interval into two adjacent subintervals, and consequently it does not possess *all* the intervals. They prove the decidability of SL with respect to particular classes of split-frames which can be put in correspondence with the first-order fragments of the monadic theories of time granularity. In particular, *discrete* split-frames with maximal intervals correspond to the n -layered structure, discrete split-frames (with unbounded intervals) can be mapped into the upward unbounded layered structure, and *dense* split-frames with maximal intervals can be encoded into the downward unbounded layered structure.

3.5 Qualitative time granularity

Granularity operators for qualitative time representation have been first provided in [Euzenat, 1993; Euzenat, 1995a]. These operators are defined in the context of relational algebras and they apply to both point and interval algebras. They have the advantage of being applicable to fully qualitative and widespread relational representations. They account for granularity phenomena occurring in actual applications using only qualitative descriptions.

After a short recall of relation algebras (Section 3.5.1), a set of six constraints applying to the granularity operators is defined (Section 3.5.2). These constraints are applied to the well-known temporal representation of point and interval algebras (Section 3.5.3). Some general results of existence and relation of these operators with composition are also given (Section 3.5.4).

3.5.1 Qualitative time representation and granularity

The qualitative time representation considered here is a well-known one:

1. it is based on an algebra of binary relations $\langle 2^T, \cup, \circ, ^{-1} \rangle$ (see Chapter 1); we focus our attention on the point and interval algebras [Vilain and Kautz, 1986; Allen, 1983];
2. this algebra is augmented with a neighborhood structure (in which $N(r, r')$ means that the relationships r and r' are neighbors) [Freksa, 1992];
3. last, the construction of an interval algebra [Hirsh, 1996] is considered (the conversion of a quadruple of base relationships R into an interval relation is given by $\Rightarrow R$ and the converse operation by $\Leftarrow r$ when it is defined).

In such an algebra of relations, the situations are described by a set of possible relationships holding between entities (here points or intervals).

As an example, imagine several witnesses of an air flight incident with the witness from the ground (g) saying that “the engine stopped working (W) and the plane went [immediately] down”, the pilot (p) saying that “the plane worked correctly (W) until there has been a misfiring period (M) and, after that, the plane lost altitude”, and the (unfortunately out of reach) “blackbox” flight data recorder (b) revealing that the plane had a short misfiring period (M) and a short laps of correct behavior before the plane lost altitude (D).

If these descriptions are rephrased in the interval algebra (see Figure 3.9), this would correspond to three different descriptions: $g = \{WmD\}$, $p = \{WmM, MmD\}$ and $b = \{WmM, MbD\}$. Obviously, if any two of these descriptions are merged, the result is an inconsistent description. However, such inconsistencies arise because the various sources of information do not share the same precision and not because of intrinsically contradictory descriptions. It is thus useful to find in which way the situations described by g and p can be coarse views of that expressed by b .

The qualitative granularity is defined through a couple of operators for converting the representation of a situation into a finer or coarser representation of the same situation. These operators apply to the relationships holding between the entities and transform these relationship into other plausible relationships at a coarser (with upward conversion denoted by \uparrow) or finer (with downward conversion denoted by \downarrow) granularity. When the conversion is not oriented, i.e., when we talk about a granularity change between two layers, but it is not necessary to know which one is the coarser, a neutral operator is used (denoted by \rightarrow).

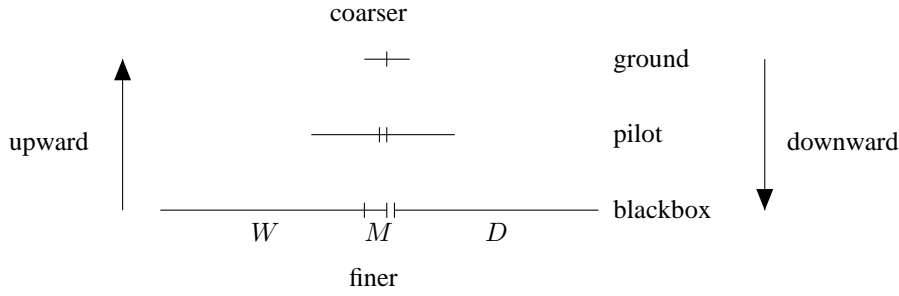


Figure 3.9: The air flight incident example.

Before turning to precisely define the granularity conversion, the assumptions underlying them must be clear. First of all, the considered language is qualitative and relational. Each layer represents a situation in the unaltered language of the relational algebra. This has the advantage of considering any description of a situation as being done under a particular granularity. Thus the layers are external to the language. The descriptions considered here are homogeneous (i.e., the language is the same for all the layers). The temporal structure is given by the algebra itself. The layers are organised as a partial order $\langle T, \prec \rangle$ (sometimes it is known that a layer is coarser than another). In the example of Figure 3.9, it seems clear that $b \prec p \prec g$. It is not assumed that they are aligned or decomposed into homogeneous units, but the constraints below can enforce contiguity. The only operators considered here are the projection operators. The contextualisation operator is not explicit since (by opposition to logical systems) it cannot be composed with other operators. However, sometimes the notation $g \rightarrow_{g'}$ is used, providing a kind of contextualisation (by specifying the concerned granularities). The displacement operator is useless since the relational language is not situated (or absolute, i.e., it does not evaluate the truth of a formula at a particular moment, but rather evaluates the truth of a temporal relationship between two entities).

3.5.2 Generic constraints on granularity change

Anyone can think about a particular set of projection operators by imagining the effects of coarseness. But here we provide a set of properties which should be satisfied by any system of granularity conversion operators. In fact, the set of properties is very small. Next section shows that they are sufficient for restricting the number of operators to only one (plus the expected operators corresponding to identity and conversion to everything).

Constraints below are given for unit relations (singletons of the set of relations). The operators on general relations are defined by:

$$\rightarrow R = \cup_{r \in R} \rightarrow r \quad (3.2)$$

Self-conservation

Self-conservation states that whatever be the conversion, a relationship must belong to its own conversion (this corresponds to the property named reflexivity when the conversion is a

relation).

$$r \in \rightarrow r \quad (\text{self-conservation}) \quad (3.3)$$

It is quite a sensible and minimal property: the knowledge about the relationship can be less precise, but it must have a chance to be correct. Moreover, in a qualitative system, it is possible that nothing changes through granularity if the (quantitative) granularity step is small enough. Not requiring this property would disable the possibility that the same situation looks the same under different granularity. Self-conservation accounts for this.

Neighborhood compatibility

A property considered earlier is the *order preservation* property — stated in [Hobbs, 1985] as an equivalence: $\forall x, y, x < y \equiv (\rightarrow x) < (\rightarrow y)$. This property takes for granted the availability of an order relation ($<$) structuring the set of relationships. It states that

$$\text{if } x > y \text{ then } \neg(\rightarrow x < \rightarrow y) \quad (\text{order preservation})$$

However, order preservation has the shortcoming of requiring the order relation. Its algebraic generalization could be reciprocal avoidance:

$$\text{if } xry \text{ then } \neg(\rightarrow xr^{-1} \rightarrow y) \quad (\text{reciprocal avoidance})$$

Reciprocal avoidance is over-generalized and conflicts with self-conservation in case of auto-reciprocal relationships (i.e. such that $r = r^{-1}$). The neighborhood compatibility, while not expressed in [Euzenat, 1993], has been taken into account informally: it constrains the conversion of a relation to form a conceptual neighborhood (and hence the conversion of a conceptual neighborhood to form a conceptual neighborhood).

$$\begin{aligned} \forall r, \forall r', r'' \in \rightarrow r, \exists r_1, \dots, r_n \in \rightarrow r : \\ r_1 = r', r_n = r'' \text{ and } \forall i \in [1, n - 1] N(r_i, r_{i+1}) \end{aligned} \quad (\text{neighborhood compatibility}) \quad (3.4)$$

This property has already been reported by Freksa [Freksa, 1992] who considers that a set of relationships must be a conceptual neighborhood in order to be seen as a coarse representation of the actual relationship. It is weaker than the two former proposals because it does not prevent the opposite to be part of the conversion. But in such a case, it constrains a path between the relation and its converse to be in the conversion too. Neighborhood compatibility seems to be the right property, partly because, instead of the former ones, it does not forbid a very coarse granularity under which any relationship is converted in the whole set of relations. It also seems natural because granularity can hardly be imagined as discontinuous (at least in continuous spaces).

Conversion-reciprocity distributivity

An obvious property for conversion is symmetry. It states that the conversion of the relation between a first object and a second one must be the reciprocal of the conversion of the

relation between the second one and the first one. It is clear that the relationships between two temporal occurrences are symmetric and thus granularity conversion must respect this.

$$\rightarrow r^{-1} = (\rightarrow r)^{-1} \quad (\text{distributivity of } \rightarrow \text{ on } ^{-1}) \quad (3.5)$$

Inverse compatibility

Inverse compatibility states that the conversion operators are consistent with each other, i.e., that if the relationship between two occurrences can be seen as another relationship under some granularity, then the inverse operation from the latter to the former can be achieved through the inverse operator. Stated otherwise, this property corresponds to symmetry when the operator is described as a relation.

$$r \in \bigcap_{r' \in \uparrow r} \downarrow r' \text{ and } r \in \bigcap_{r' \in \downarrow r} \uparrow r' \quad (\text{inverse compatibility}) \quad (3.6)$$

For instance, if someone in situation (p) of Figure 3.9 is able to imagine that, under a finer granularity (say situation b), there is some time between the misfiring period and the loss of altitude, then (s)he must be ready to accept that if (s)he were in situation (b), (s)he could imagine that there is no time between them under a coarser granularity (as in situation p).

Idempotency

A property which is usually considered first (especially in quantitative systems) is the full transitivity:

$$g \rightarrow_{g'} g' \rightarrow_{g''} r =_g \rightarrow_{g''} r \quad (\text{transitivity})$$

This property is too strong; it would for instance imply that:

$$g \uparrow^{g'} g' \downarrow_g r = r$$

Of course, it cannot be achieved because this would mean that there is no loss of information through granularity conversion: this is obviously false. If it were true anyway, there would be no need for granularity operators: everything would be the same under any layer. On the other hand, other transitivity such as the oriented transitivity (previously known as cumulated transitivity) can be expected:

$$g \uparrow_{g'}^{g'} \uparrow_{g''}^{g''} r =_g \uparrow_{g''}^{g''} r \text{ and } g \downarrow_{g'}^{g'} \downarrow_{g''}^{g''} r =_g \downarrow_{g''}^{g''} r \quad (\text{oriented transitivity})$$

However, in a purely qualitative calculus, the precise granularity (g) is not relevant and this property becomes a property of idempotency of operators:

$$\uparrow \uparrow r = \uparrow r \text{ and } \downarrow \downarrow r = \downarrow r \quad (\text{idempotency}) \quad (3.7)$$

At first sight, it could be clever to have non idempotent operators which are less and less precise with granularity conversion. However, if this applies very well to quantitative data, it does not apply for qualitative: the qualitative conversion applies equally for a large granularity conversion and for a small one which is ten times less. If, for instance, in a particular situation, a relationship between two entities is r , in a coarser representation it is r' and in an even coarser representation it is r'' , then r'' must be a member of the upward conversion of r .

This is because r'' is indeed the result of a qualitative conversion from the first representation to the third. Thus, qualitatively, $\uparrow\uparrow=\uparrow$.

If there were no idempotency, converting a relationship directly would give a different result than when doing it through ten successive conversions.

Representation independence

Since the operation allowing one to go from a relational space to an interval relational space has been provided (by \Leftarrow and \Rightarrow), the property constraining the conversion operators can also be given at that stage: representation independence states that the conversion must not be dependent upon the representation of the temporal entity (as an interval or as a set of bounding points). Again, this property must be required:

$$\rightarrow r = \Leftarrow \rightarrow \Rightarrow r \text{ and } \rightarrow r = \Rightarrow \rightarrow \Leftarrow r \quad (\text{representation independence}) \quad (3.8)$$

It can be thought of as a distributivity:

$$\Rightarrow \rightarrow r = \Rightarrow \rightarrow r \text{ and } \Leftarrow \rightarrow r = \Rightarrow \Leftarrow r$$

Note that, since \Leftarrow requires that the relationship between bounding points allows the result to be an interval, there could be some restrictions on the results (however, these restrictions correspond exactly to the vanishing of an interval which is out of scope here).

The constraints (3.3, self-conservation) and (3.7, idempotence), together with the definition of the operators for full relations (3.2), characterise granularity operators as closure operators.

Nothing ensures that these constraints lead to a unique couple of operators for a given relational system.

Definition 3.5.1. *Given a relational system, a couple of operators up-down satisfying 3.3-3.7 is a coherent granularity conversion operator for that system.*

For any relation algebra there are two operators which always satisfy these requirements: the identity function (Id) which maps any relation into itself (or a singleton containing itself) and the non-informative function (Ni) which maps any relation into the base set of the algebra. It is noteworthy that these functions must then be their own inverse (i.e., they are candidates for both \uparrow and \downarrow at once). These solutions are not considered anymore below.

The framework provided so far concerns two operators related by the constraints, but there is no specificity of the upward or downward operator (this is why constraints are symmetric). By convention, if the system contains an equivalence relation (defined as e such that $e = e \circ e = e^{-1}$ [Hirsh, 1996]), the operators which maps this element to a strictly broader set is denoted as the downward operator. This meets the intuition because the coarser the view the more indistinguishable the entities (and they are then subject to the equivalence relation).

3.5.3 Results on point and interval algebras

From these constraints, it is possible to generate the possible operators for a particular relation algebra. This is first performed for the point algebra and the interval algebra in which

it turns out that only one couple of non-trivial operators exists. Moreover, these operators satisfy the relationship between base and interval algebra.

Granularity for the point algebra

Proposition 3.5.1. *Table 3.1 defines the only possible non auto-inverse upward/downward operators for the point algebra.*

relation: r	$\uparrow r$	$\downarrow r$
$<$	$<=$	$<$
$=$	$=$	$<=>$
$>$	$>=$	$>$

Table 3.1: Upward and downward granularity conversions for the point algebra.

These operators fit intuition very well. For instance, if the example of Figure 3.9 is modeled through bounding points (x^- for the left endpoint and x^+ for the right endpoint) of intervals W^+ , M^- , M^+ and D^- , it is represented in (b) by $W^+ = M^-$ (the engine stops working when it starts misfiring), $M^- < M^+$ (the beginning of the misfire is before its end), $M^+ < D^-$ (the end of the misfiring period is before the beginning of the loss of altitude) in (p) by $M^+ = D^-$ (the misfiring period ends when the loss of altitude begins) and in (g) by $M^- = M^+$ (the misfiring period does not exist anymore). This is possible by converting $M^+ < D^-$ into $M^+ = D^-$ ($=\in\uparrow<$) and $M^- = M^+$ into $M^- < M^+$ ($<\in\downarrow=$).

Granularity for the interval algebra

Since the temporal interval algebra is a plain interval algebra, the constraint 3.8 can be applied for deducing its granularity operators. This provides the only possible operators for the interval algebra. Table 3.2 shows the automatic translation from points to intervals:

r	$\uparrow r$				$\uparrow r$	$\downarrow r$				$\downarrow r$
b	$<=$	$<=$	$<=$	$<=$	bm	$<$	$<$	$<$	$<$	b
d	$>=$	$<=$	$>=$	$<=$	$dsfe$	$>$	$<$	$>$	$<$	d
o	$<=$	$<=$	$>=$	$<=$	$osmef^{-1}$	$<$	$>$	$>$	$<$	o
s	$=$	$<=$	$>=$	$=$	se	$<=>$	$<$	$>$	$<$	osd
f	$>=$	$<=$	$>=$	$=$	fe	$>$	$<$	$>$	$<=>$	$o^{-1}fd$
m	$<=$	$<=$	$=$	$<=$	m	$<$	$<$	$<=>$	$<$	bmo
e	$=$	$<=$	$>=$	$=$	e	$<=>$	$<$	$>$	$<=>$	$of^{-1}d^{-1}s$ $es^{-1}dfo^{-1}$

Table 3.2: Transformation of upward and downward operators between points into interval relation quadruples.

The conversion table for the interval algebra is given below. The corresponding operators enjoy the same properties as the operators for the point algebra.

Proposition 3.5.2. *The upward/downward operators for the interval algebra of Table 3.3 satisfy the properties 3.3 through 3.7.*

r	$\uparrow r$	$\downarrow r$	r^{-1}	$\uparrow r^{-1}$	$\downarrow r^{-1}$
b	bm	b	b^{-1}	$b^{-1}m^{-1}$	b^{-1}
d	$dfse$	d	d^{-1}	$d^{-1}s^{-1}f^{-1}e$	d^{-1}
o	$of^{-1}sme$	o	o^{-1}	$o^{-1}s^{-1}fem^{-1}$	o^{-1}
s	se	osd	s^{-1}	$s^{-1}e$	$d^{-1}s^{-1}o^{-1}$
f	fe	$df o^{-1}$	f^{-1}	$f^{-1}e$	$d^{-1}f^{-1}o$
m	m	bmo	m^{-1}	m^{-1}	$o^{-1}m^{-1}b^{-1}$
e	e	$of^{-1}d^{-1}ses^{-1}df o^{-1}$			

Table 3.3: Upward and downward granularity conversion for the interval algebra.

Proposition 3.5.3. *The upward/downward operators for the interval algebra of Table 3.3 are the only ones that satisfy the property 3.8 with regard to the operators for the point algebra of Table 3.1.*

If one wants to generate possible operators for the interval algebra, many of them can be found. But the constraint that this algebra must be the interval algebra (in the sense of [Hirsh, 1996]) of the point algebra restricts drastically the number of solutions.

The reader is invited to check on the example of Figure 3.9, that what has been said about point operators is still valid: the situation (b) is described by $W\{m\}M$ (the working period meets the misfiring one), $M\{b\}D$ (the misfiring period is anterior to the loss of altitude), in (p) by $M\{m\}D$ (the misfiring period meets the loss of altitude) and in (g) where the misfiring period does not appear anymore by $W\{m\}D$ (the working period meets the loss of altitude). This is compatible with the idea that, under a coarser granularity, b can become m ($m \in \uparrow b$) and that under a finer granularity m can become b ($b \in \downarrow m$).

The upward operator does not satisfy the condition 3.4 for B-neighborhood (in which objects are translated continuously [Freksa, 1992]) as it is violated by d , s , and f and C-neighborhood (in which the objects are continuously expanded or contracted by preserving their center of gravity [Freksa, 1992]) as it is violated by o , s , and f . This is because the corresponding neighborhoods are not based upon independent limit translations while this independence has been used for translating the results from the point algebra to the interval algebra.

It is noteworthy that the downward operator corresponds exactly to the closure of relationships that Ligozat [Ligozat, 1990] introduced in his own formalism. This seems natural since this closure, just like the conversion operators, provides all the adjacents relationships of a higher dimension.

3.5.4 General results of existence and composition

We provide here general results about the existence of granularity operators in algebra of binary relations. Then, the relationships between granularity conversion and composition, i.e., the impact of granularity changes on inference results, are considered.

Existence results for algebras of binary relations

The question of the general existence of granularity conversion operators corresponding to the above constraints can be raised. Concerning granularity conversion operators different from Id and Ni , two partial results have been established [Euzenat, 2001]. The first one shows that there are small algebras with no non-trivial operators:

Proposition 3.5.4. *The algebra based on two elements a and a^{-1} such that $N(a, a^{-1})$ has no granularity conversion operators other than identity and non-informative map.*

A more interesting result is that of the existence of operators for a large class of algebras. In the case of two auto-inverse operators (e.g., $=$ and \neq), there must exist conversion operators as shown by proposition 3.5.5. Proposition 3.5.5 exhibits a systematic way of generating operators from minimal requirements (but does not provide a way to generate all the operators). It only provides a sufficient, but not necessary, condition for having operators.

Proposition 3.5.5. *Given a relation algebra containing two relationships a and b such that $N(a, b)$ (it is assumed that neighborhood is converse independent, i.e., $N(a^{-1}, b^{-1})$), there exists a couple of upward/downward granularity operators defined by :*

if a and b are auto-inverse $\downarrow a = \{a, b\}$, $\uparrow b = \{a, b\}$, the remainder being identity;

if a only is auto-inverse $\downarrow a = \{a, b, b^{-1}\}$, $\uparrow b = \{a, b\}$, $\uparrow b^{-1} = \{a, b^{-1}\}$, the remainder being identity;

if a and b are not auto-inverse $\downarrow a = \{a, b\}$, $\uparrow b = \{a, b\}$, $\downarrow a^{-1} = \{a^{-1}, b^{-1}\}$, $\uparrow b^{-1} = \{a^{-1}, b^{-1}\}$, the remainder being identity.

There can be, in general, many possible operators for a given algebra. Proposition 3.5.5 shows that the five core properties of Section 3.5.2 are consistent. Another general question about them concerns their independence. It can be answered affirmatively:

Proposition 3.5.6. *The core properties of granularity operators are independent.*

This is proven by providing five systems satisfying all properties but one [Euzenat, 2001].

Granularity and composition

The composition of symbolic relationships is a favored inference means for symbolic representation systems. One of the properties which would be interesting to obtain is the independence of the results of the inferences from the granularity level (equation 3.9). The distributivity of \rightarrow on \circ denotes the independence of the inferences from the granularity under which they are performed.

$$\rightarrow (r \circ r') = (\rightarrow r) \circ (\rightarrow r') \quad (\text{distributivity of } \rightarrow \text{ over } \circ) \quad (3.9)$$

This property is only satisfied for upward conversion in the point algebra.

Proposition 3.5.7. *The upward operator for the point algebra satisfies property 3.9.*

It does not hold true for the interval algebra. Let three intervals x , y and z be such that xy and yz . The application of composition of relations gives $x\{b o m d s\}z$ which, once upwardly converted, gives $x\{b m e d f s o f^{-1}\}z$. By opposition, if the conversion is first applied, it returns $x\{b m\}y$ and $y\{d f s e\}z$ which, once composed, yields $x\{b o m d s\}z$. The interpretation of this result is the following: by first converting, the information that there exists an interval y forbidding x to finish z is lost; however, if the relationships linking y to x and z are preserved, then the propagation will take them into account and recover the lost precision: $\{b m e d f s o^{-1}\} \circ \{b o m d s\} = \{b o m d s\}$. In any case, this cannot be enforced since, if the length of y is so small that the conversion makes it vanish, the correct information at that granularity is the one provided by applying first the composition: x can meet the end of z under such a granularity. However, if equation 3.9 cannot be achieved for upward conversion in the interval algebra, upward conversion is super-distributive over composition.

Proposition 3.5.8. *The upward operator for the interval algebra satisfies the following property:*

$$(\uparrow r) \circ (\uparrow r') \subseteq \uparrow (r \circ r') \quad (\text{super-distributivity of } \uparrow \text{ over } \circ)$$

A similar phenomenon appears with the downward conversion operators (it appears both for points and intervals). Let x , y and z be three points such that $x > y$ and $y = z$. On the one hand, the composition of relations gives $x > z$, which is converted to $x > z$ under the finer granularity. On the other hand, the conversion gives $x > y$ and $y \leq z$ because, under a more precise granularity, y could be close but not really equal to z . The composition then provides no more information about the relationship between x and z ($x \leq z$). This is the reverse situation as before: it takes into account the fact that the non-distinguishability of two points cannot be ensured under a finer grain. Of course, if everything is converted first, then the result is as precise as possible: downward conversion is sub-distributive over composition.

Proposition 3.5.9. *The downward operators for the interval and point algebras satisfy the following property:*

$$\downarrow (r \circ r') \subseteq (\downarrow r) \circ (\downarrow r') \quad (\text{sub-distributivity of } \downarrow \text{ over } \circ)$$

These two latter properties can be useful for propagating constraints in order to get out of them the maximum of information quickly. For instance, in the case of upward conversion, if no interval vanishes, every relationship must be first converted and then composed.

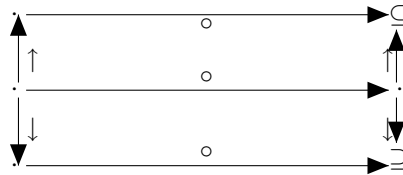


Figure 3.10: A diagrammatic summary of Propositions 3.5.9 and 3.5.8.

These properties have been discovered independently in the qualitative case [Euzenat, 1993] and in the set-theoretic granularity area through an approximation algorithm for quantitative constraints [Bettini *et al.*, 1996].

3.5.5 Granularity through discrete approximation

The algebra of relations can be directly given or derived as an interval algebra. It can also be provided by axiomatizing properties of objects or generated from properties of artefacts. Bittner [Bittner, 2002] has taken such an approach for generating sets of relations depending on the join of related objects. He has adapted a framework for qualitatively approximating spatial position to temporal representation. This framework can be used in turn for finding approximate relations between temporal entities which can be seen as relations under a coarser granularity.

Qualitative temporal relations

This work is based on a new analysis of the generation of relations between two spatial areas. These relations are characterized through the "intersection" (or meet) between the two regions. More precisely, the relation is characterized by the triple:

$$\langle x \wedge y \not\approx \perp, x \wedge y \approx x, x \wedge y \approx y \rangle$$

The items in these triples characterize the non emptiness of $x \wedge y$ (1st item) and its relation to x and y (2nd and 3rd items). So the values of this triple are relations (this approach is inspired from [Egenhofer and Franzosa, 1991]). These values are taken out of a set of possible relations Ω . This generates several different sets of relations depending on the kind of relations used:

- boundary insensitive relations (RCC5);
- one-dimensional boundary insensitive relations between intervals (RCC₁⁹);
- one-dimensional boundary insensitive relations between non convex regions (RCC₁⁹);
- boundary sensitive relations (RCC8);
- one-dimensional boundary sensitive relations (RCC₁¹⁵).

Some of these representations are obviously refinement of others. In that sense, we obtain a granular representation of a temporal situation by using more or less precise qualitative relationships. This can also be obtained by using other kinds of temporal representations (RCC8 is less precise than Allen's algebra of relations).

As an example, RCC₁⁹ considers regions x and y corresponding to intervals on the real line. The set Ω is made of FLO, FLI, T, FRI, FRO. FLO indicates that no argument is included in the other (O) and there is some part of the first argument left (L) of the second one, FLI indicates that the second argument is included in the first one and there is some part of the first argument left (L) of the second one, T corresponds to the equality of the intersection with the interval, and FRI and FRO are the same for the right hand bound. This provides the relations of Table 3.4.

$x \wedge y \not\sim \perp$	$x \wedge y \sim x$	$x \wedge y \sim y$	Allen
FLO	FLO	FLO	b m
FRO	FRO	FRO	$b^{-1} m^{-1}$
T	FLO	FLO	o
T	FRO	FRO	o^{-1}
T	T	FLI	d s
T	T	FRI	d f
T	FLI	T	$d^{-1} f^{-1}$
T	FRI	T	$d^{-1} s^{-1}$
T	T	T	e

Table 3.4: The relations of RCC_1^9 .

The relations in these sets are not always jointly exhaustive and pairwise disjoint. For instance, RCC_1^9 is exhaustive but not pairwise disjoint, simply because d and d^{-1} appear in two lines of the table.

Qualitative temporal locations

The framework as it is developed in [Bittner and Steel, 1998] considers a space, here a temporal domain, as a set of places T_0 . Any spatial or temporal occurrence will be a subset of T_0 . So, with regard to what has been considered in Section 3.3, the underlying space is aligned and structured.

An approximation is based on the partition of T_0 into a set of cells K (i.e., $\forall k, k' \in K, k \subseteq T_0, k \cap k' = \emptyset$ and $\cup_{k \in K} k = T_0$). The localization of any temporal occurrence is then approximated by providing its relation to each cell. The location of $x \subseteq T_0$ is a function $\rho_x : K \rightarrow \Omega'$ from the set of cells to a set of relations Ω' (which may but have not to correspond to Ω or a RCC_q^p defined above). The resulting approximation is thus dependent on the partition K and the set of relations Ω' .

From this, we can state that two occurrences x and y are indistinguishable under granularity $\langle K, \Omega' \rangle$ if and only if $\rho_x = \rho_y$. This formulation is typical from the set-theoretic approach to temporal granularity used in a strictly qualitative domain.

We can also define the interpretation of an area of the set of cells ($X : K \rightarrow \Omega$) as the set of places it approximates:

$$[X] = \{x \subseteq T_0 \mid \rho_x = X\}$$

Relations between approximations and granularity

It is clear that the approximation of a region x can be considered as its representation $\uparrow x$ under the granularity $\langle K, \Omega' \rangle$ (i.e., ρ_x). In the same vein, the interpretation of approximation $[X]$ corresponds to the conversion of this region to the finer granularity $\downarrow X$. In that respect we are faced with two discrete and aligned granularities.

The following question can be raised: given a relation $r \in RCC_q^p$ between x and y , the approximations $\uparrow x$ and $\uparrow y$, and $\uparrow r$ holding between $\uparrow x$ and $\uparrow y$, what can be said of the

relationship between r and $\uparrow r$? The approximate relation $\uparrow r$ holding between X and Y is characterized as $SEM(X, Y)$ and defined as:

$$SEM(X, Y) = \{r \in RCC_q^p \mid x \in [X], y \in [Y], xRy, \text{ and } r \in R\}$$

The author goes on to define a syntactic operator ($SYN(X, Y)$) for determining the relationships between approximate regions. This operator must be as close as possible to $SEM(X, Y)$. It is defined by replacing in the equations defining the relations of the considered set, the region variables (x and y) by approximation variables (X and Y) and the meet operation by upper or lower bounds for the meet operation. This provides a pair of values for the relations between X and Y depending on whether they have been computed with the upper and lower meet.

It is now possible to obtain the relations between granular representations of the entities by considering that $x \uparrow r y$ can be obtained in the usual way (but for obtaining $\uparrow r$ we need to consider all the possible granularities, i.e., all the possible K and all the possible Ω'). $X \downarrow r Y$ is what should be obtained by $SEM(X, Y)$ and approximated by $SYN(X, Y)$.

Hence, a full parallel can be made between the above-described work on qualitative granularity and this work on discrete approximation in general. Unfortunately, the systems developed in [Bittner, 2002] do not include Allen's algebra. The satisfaction of the axioms by this scheme has not been formally established. However, one can say that self-conservation and idempotence are satisfied. Neighborhood compatibility depends on a neighborhood structure, but $SYN(X, Y)$ is very often an interval in the graph of relations (which is not very far from a neighborhood structure). It could also be interesting to show that when $RCC_1^{1.5}$ relations correspond to Allen's ones, the granularity operators correspond.

In summary, this approximation framework has the merit of providing an approximated representation of temporal places interpreted on the real line. The approximation operation itself relies on aligned granularities. This approach is entirely qualitative in its definition but can account for orientation and boundaries.

3.6 Applications of time granularity

Time granularity come into play in many classes of applications with different constraints. Thus, the contributions presented below not only offer an application perspective, but generally provide their own granular formalism. The fact that there are no applications to multi-agent communication means that the agents currently developed communicate with agents of the same kind. With the development of communicating programs, it will become necessary to consider the compatibility of two differently grained descriptions of what they perceive.

3.6.1 Natural language processing, planning, and reasoning

The very idea of granularity in artificial intelligence comes from the field of natural language understanding [Hobbs, 1985]. In [Gayral, 1992] Gayral and Grandemange take into account the same temporal unit under a durative or instantaneous aspect. Their work is motivated by problems in text understanding. A mechanism of upward/downward conversion is introduced and modeled in a logical framework. It only manages symbolic constraints and it converts the entities instead of their relationships. The representation they propose is based

on a notion of composition and it allows the recursive decomposition of beginning and ending bounds of intervals into new intervals. The level of granularity is determined during text understanding by the election of a distinguished individual (which could be compared with a focus of attention) among the set of entities and the aspect (durative vs. instantaneous) of that individual. Unlike most of the previously-described approaches, where granularity is considered orthogonal to a knowledge base, in Gayral and Grandemange's work the current granularity is given relatively to the aspect of a particular event. A link between the two notions can be established by means of the decomposition relation between entities (or history [Euzenat, 1993]). Time granularity in natural language processing and its relation with the durative/instantaneous aspects have been also studied by other authors. As an example, Becher et al. model granularity by means of time units and two basic relations over them: precedence and containment (alike the set-theoretic approach, Section 3.3) [Becher *et al.*, 1998]. From a model of time units consisting of a finite sequence of rational numbers, the authors build an algebra of relations between these units, obtaining an algebraic account of granularity.

In [Badaloni and Berati, 1994], Badaloni and Berati use different time scales in an attempt to reduce the complexity of planning problems. The system is purely quantitative and it relies on the work presented in Section 3.3. The NatureTime [Mota *et al.*, 1997] system is used for integrating several ecological models in which the objects are modeled under different time scales. The model is quantitative and it explicitly defines (in Prolog) the conversions from a layer to another. This is basically used during unification when the system unifies the temporal extensions of the atoms. Combi et al. [Combi *et al.*, 1995] applied their multi-granular temporal database to clinical medicine. The system is used for the follow-up of therapies in which data originate from various physicians and the patient itself. It allows one to answer (with possibility of undefined answers) to various questions about the history of the patient. In this system (like in many other) granularity usually means "converting units with alignment problems".

3.6.2 Program specification and verification

In [Ciapessoni *et al.*, 1993], Ciapessoni et al. apply the logics of time granularity to the specification and verification of real-time systems. The addition of time granularity makes it possible to associate coarse granularities with high-level modules and fine granularities with the lower level modules that compose them. In [Fiadeiro and Maibaum, 1994], Fiadeiro and Maibaum achieve the same practical goal by considering a system in which granularity is defined a posteriori (it corresponds to the granularity of actions performed by modules, while in the work by Ciapessoni et al. the granularity framework is based on a metric time) and the refinement (granularity change) takes place between classical logic theories instead of inside a specialized logical framework (as in Section 3.4.1). It is worth pointing out that both contributions deal with refinement, in a quite different way, but they do not take into account upward granularity change. Finally, in [Broy, 1997], Broy introduces the notion of temporal refinement into the description of software components in such a way that the behavior of these components is temporally described under a hierarchy of temporal models.

3.6.3 Temporal Databases

Time granularity is a long-standing issue in the area of temporal databases (see Chapter 14). As an evidence of the relevance of the notion of time granularity, the database community has released a “glossary of time granularity concepts” [Bettini *et al.*, 1998a]. As we already pointed out, the set-theoretic formalization of granularity (see Section 3.3) has been settled in the database context. Moreover, besides theoretical advances, the database community contributed some meaningful applications of time granularity. As an example, in [Bettini *et al.*, 1998b] Bettini *et al.* design an architecture for dealing with granularity in federated databases involving various granularities. This work takes advantage of extra information about the database design assumptions in order to characterize the required transformations. The resulting framework is certainly less general than the set-theoretic formalization of time granularity reported in Section 3.3, but it brings granularity to concrete databases applications. Time granularity has also been applied to data mining procedures, namely, to procedures that look for repeating collection of events in federated databases [Bettini *et al.*, 1998d] by solving simple temporal reasoning problems involving time granularities (see Section 3.3). An up-to-date account of the system is given in [Bettini *et al.*, 2003].

3.6.4 Granularity in space

(Spatial) granularity plays a major role in geographic information systems. In particular, the granularity for the Region Connection Calculus [Randell *et al.*, 1992; Egenhofer and Franzosa, 1991] has been presented in that context [Euzenat, 1995b]. Moreover, the problem of generalization is heavily related to granularity [Muller *et al.*, 1995]. Generalization consists in converting a terrain representation into a coarser map. This is the work of cartographers, but due to the development of computer representation of the geographic information, the problem is now tackled in a more formal, and automated, way.

In [Topaloglou, 1996], Topaloglou *et al.* have designed a spatial data model based on points and rectangles. It supports aligned granularities and it is based on numeric constraints. The treatment of granularity consists in tolerant predicates for comparing objects of different granularities which allow two objects to be considered as equals if they only deviate from the granularity ratio.

In [Puppo and Dettori, 1995; Dettori and Puppo, 1996], Puppo and Dettori outline a general approach to the problem of spatial granularity. They represent space as a cell complex (a set of elements with a relation of containment and the notion of dimension as a map to integers) and generalization as a surjective mapping from one complex cell into another. One can consider the elements as simplexes (points of dimension 1, segments of dimension 2 bounded by two points, and triangles of dimension 3 bounded by three segments). This notion of generalization takes into account the possible actions on an object: preservation, if it persists with the same dimension under the coarser granularity, reduction, if it persists at a lower dimension, and immersion, if it disappears (it is then considered as immersed in another object). The impact of these actions on the connected objects is also taken into account through a set of constraints, exactly like it has been done in Section 3.5.2. This should be totally compatible with the two presentations of granularity given here. Other transformations, such as exaggeration (when a road appears larger than it is under the map scale) and displacement, have been taken into account in combination with generalization, but they do not fit well in the granularity framework given in Section 3.2. Last, it must be noted that

these definitions are only algebraic and that no analytical definitions of the transformations have been given.

Other authors have investigated multi-scale spatial databases, where a simplified version of the alignment problem occurs [Rigaux and Scholl, 1995]. It basically consists in the requirement that each partition of the space is a sub-partition of those it is compared with (a sort of spatial alignment).

Finally, some implementations of multi-resolution spatial databases have been developed with encouraging results [Devogele *et al.*, 1996]. As a matter of fact, the addressed problem is simpler than that of generalization, since it consists in matching the elements of two representations of the same space under different resolutions. While generalization requires the application of a (very complex) granularity change operator, this problem only requires to look for compatibility of representations. Tools from databases and generalization can be used here.

3.7 Related work

We would like to briefly summarize the links to time granularity coming from a variety of research fields and to provide some additional pointers to less-directly related contributions which have not been fully considered here due to the lack of space. Relationships with research in databases have been discussed in Sections 3.3 and 3.6.3. Granularity as a phenomenon that affects space has been considered in Section 3.6.4. The integration of a notion of granularity into logic programming is dealt with in [Mota *et al.*, 1997; Liu and Orgun, 1997] (see Section 3.6.1 and see also Chapter 13). Work in qualitative reasoning can also be considered as relevant to granularity [Kuipers, 1994] (see Chapter 20).

The relationships between (time) granularity and formal tools for abstraction have been explored in various papers. As an example, Giunchiglia *et al.* propose a framework for abstraction which applies to a structure $\langle L, A, R \rangle$, where L is a language, A is a set of axioms, and R is a set of inference rules [Giunchiglia *et al.*, 1997]. They restrict abstraction to A , because the granularity transformations are constrained to remain within the same language and the same rules apply to any abstraction. One distinctive feature of this work is that it is oriented towards an active abstraction (change of granularity) in order to increase the performance of a system. As a matter of fact, using a coarse representation reduces the problem size by getting rid of details. The approaches to time granularity we presented in this chapter are more oriented towards accounting for the observed effects of granularity changes instead of creating granularity change operators which preserve certain properties.

Concluding remarks

We would like to conclude this chapter by underlining the relevance and complexity of the notion of time granularity. On the one hand, when some situations can be seen from different viewpoints (of designers, observers, or agents), it is natural to express them under different granularities. On the other hand, problems immediately arise from using multiple granularity, because it is difficult to assign a proper (or, at least, a consistent) meaning to these granular representations.

As it can be seen from above, a lot of work has already been devoted to granularity. This

research work has been developed in various domains (e.g., artificial intelligence, databases, and formal specification) with various tools (e.g., temporal logic, set theory, and algebra of relations). It must be clear that the different approaches share many concepts and results, but they have usually considered different restrictions. The formal models have provided constraints on the interpretations of the temporal statements under a particular granularity, but they did not provide an univocal way to interpret them in a specific application context.

On the theoretical side, further work is required to formally compare and/or integrate the various proposals. On the application side, if the need for granularity handling is acknowledged, it is not very developed in the solutions. There are reasons to think that this will change in the near future, drained by applications such as federated databases and agent systems, providing new problems to theoretical research.

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