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Model Based Testing for Concurrent Systems with Labeled Event Structures

Hernán Ponce de León
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December 6, 2013

Abstract

We propose a theoretical testing framework and a test generation algorithm for concurrent systems specified with true concurrency models, such as Petri nets or networks of automata. The semantic model of computation of such formalisms are labeled event structures, which allow to represent concurrency explicitly. We introduce the notions of strong and weak concurrency: strongly concurrent events must be concurrent in the implementation, while weakly concurrent ones may eventually be ordered. The **io** type conformance relations for sequential systems rely on the observation of sequences of actions and blockings, thus they are not capable of capturing and exploiting concurrency of non sequential behaviors. We propose an extension of **io** for labeled event structures, named **co-io**, allowing to deal with strong and weak concurrency. We extend the notions of test cases and test execution to labeled event structures, and give a test generation algorithm building a complete test suite for **co-io**.

1 Introduction

Model-based Testing. One of the most popular formalisms studied in conformance testing is that of *labeled transition systems* (LTS). A labeled transition system is a structure consisting of states and transitions labeled with actions from one state to another. This formalism is usually used for modeling the behavior of sequential processes and as a semantical model for various formal languages such as CCS [1], CSP [2], SDL [3] and LOTOS [4].

Several testing theories have been defined for labeled transition systems [5, 6, 7, 8, 9, 10, 11]. A formal testing framework relies on the definition of a conformance relation which formalizes the relation that the system under test (SUT) and its specification must verify. Depending on the nature of the possible observations of the system under test, several conformance relations have been defined for labeled transition systems. The relation of *trace preorder* (trace inclusion) is based on the observation of possible sequences of actions only. It

was refined into the *testing preorder*, that requires not only the inclusion of the implementation traces in those of the specification, but also that any action refused by the implementation should be refused by the specification [5, 12]. A practical modification of the testing preorder was presented in [7], which proposed to base the observations on the traces of the specification only, leading to a weaker relation called **conf**. A further refinement concerns the inclusion of quiescent traces as a conformance relation (e.g. [10]). Moreover, Tretmans [11] proposed the **ioco** relation, which refines **conf** with the observation of blockings (quiescence).

The **ioco** conformance relation is defined for input-output labeled transition systems which are LTS where stimuli received from the environment (inputs) are distinguished from answers given by the system (outputs). It relies on two kinds of observation: traces, that are sequences of inputs and outputs, and quiescence, which is the observation of a blocking of the system (the system will not produce outputs anymore or is waiting for an input from the environment to produce some). A system under test conforms to its specification with respect to **ioco** if after any trace of the specification that can be executed on the system, the observable outputs and blockings of the system are possible outputs and blockings in the specification.

The testing theory based on the **ioco** conformance relation has now become a standard and is used as a basis in several testing theories for extended state-based models. Let us mention here the works on restrictive transition systems [13, 14], symbolic transition systems [15, 16], timed automata [17, 18], and multi-port finite state machines [19].

Model-based Testing of Concurrent Systems. Systems composed of concurrent components are naturally modeled as a *network of finite automata*, a formal class of models that can be captured equivalently by *safe Petri nets*. Concurrency in a specification can arise for different reasons. First, two events may be physically located on different components, and thus be “naturally” independent of one another; this distribution is then part of the system construction. Second, the specification may not care about the order in which two actions are performed *on the same component*, and thus leave the choice of their ordering to the implementation. Depending on the nature of the concurrency specified in a given case, and thus on the intention of the specification, the *implementation relations* have to allow or disallow ordering of concurrent events.

Model-based testing of concurrent systems has been studied for a long time [20, 21, 22], however it is most of the time studied in the context of interleaving semantics, or trace semantics, which is known to suffer the state space explosion problem. While the passage to concurrent models has been successfully performed in other fields of formal analysis such as model checking or diagnosis, *testing* has embraced concurrent models somewhat more recently.

Already in [23], Ulrich and König propose a framework for testing concurrent systems specified by communicating labeled transition systems. They define a concurrency model called behavior machines that is an interleaving-free and

finite description of concurrent and recursive behavior, which is a sound model of the original specification. Their testing framework relies on a conformance relation defined by labeled partial order equivalence, and allows to design tests for each component from a labeled partial order representing an execution of the behavior machine.

In another direction, Haar et al [24, 25] generalized the basic notions and techniques of I/O-sequence based conformance testing on a generalized I/O-automaton model where partially ordered patterns of input/output events were admitted as transition labels. An important practical benefit of true-concurrency models here is an overall complexity reduction, despite the fact that checking partial orders requires in general multiple passes through the same labelled transition, so as to check for presence/absence of specified order relations between input and output events. In fact, if the system has n parallel and interacting processes, the length of checking sequences increases by a factor that is polynomial in n . At the same time, the overall size of the automaton model (in terms of the number of its states and transitions) shrinks exponentially if the concurrency between the processes is explicitly modeled. This feature indicates that with increasing size and distribution of SUTs in practice, it is computationally wise to seek alternatives for the direct sequential modeling approach. However, the models of [24, 25] still force us to maintain a sequential automaton as the system’s skeleton, and to include synchronization constraints (typically: that all events specified in the pattern of a transition must be completed before any other transition can start), which limit both the application domain and the benefits from concurrency modeling.

The approach that we follow here, continuing the work started in [26, 27], proposes a formal framework for testing concurrent systems from true concurrency models in which no synchronization on global states is required.

Our Framework and Contributions. We use a canonical semantic model for concurrent behavior, *labeled event structures*, providing a unifying semantic framework for system models such as Petri nets, networks of automata, communicating automata, or process algebras; we abstract away from the particularities of system specification models, to focus entirely on behavioral relations.

The underlying mathematical structure for the system semantics is given by *event structures* in the sense of Winskel et al [28]. Mathematically speaking, they are particular partially ordered sets, in which order between two events e and e' indicates precedence, and where any two events e and e' that are *not* ordered may be either

- in *conflict*, meaning that in any evolution of the system in which e occurs, e' *cannot* occur; or
- *concurrent*, in which case they may occur in the same system run, without a temporal ordering, i.e. e may occur before e' , after e' , or simultaneously.

Event structures arise naturally under the partial order unfolding semantics for Petri nets [28], and also as a natural semantics for process algebras (see e.g. [29]).

The state reached after some execution is represented by a *configuration* of the event structure, that is a conflict-free, history-closed set. The use of partial order semantics provides richer information and finer system comparisons than the interleaved view.

In [26], we proposed an extension of the **ioco** conformance relation to labeled event structures, named **co-ioco**, which takes concurrency explicitly into account. In particular, it forces events that are specified as concurrent to remain concurrent in the implementation when partial order semantics is chosen. In [27] we additionally dropped the input enabledness assumption and enlarged the conformance relation with the observation of refusals. In this paper, we refine these conformance relations introducing the notions of strong and weak concurrency. Events specified as strongly concurrent must remain concurrent in a correct implementation while weakly concurrent events may be ordered. These two notions reflect the two usual interpretations of concurrency in a specification, that are true-concurrency semantics and interleaving semantics. These refinements lead to a new definition of the **co-ioco** conformance relation.

The contributions of this paper are twofold. First, we define the notions of strong and weak concurrency along with a new semantics for labeled event structures based on a notion of relaxed executions. Second, we define a whole framework for testing concurrent systems from labeled event structures. Besides the definition of a **co-ioco** conformance relation handling strong and weak concurrency, we define the notion of test case, we give sufficient properties for a test suite to be sound (not reject correct systems) and exhaustive (not accept incorrect systems), and we provide a test case generation algorithm that builds a complete (i.e. sound and exhaustive) test suite. The paper is presented according to the following structure.

Structure of the Paper. In the next section, we will introduce several basic notions such as input output labeled event structures (*IOLES*) and the new notions of strong and weak concurrency, along with a novel partial order semantics for IOLES, that allows to “relax” concurrency. In Section 3, we develop the *observational* framework for IOLES, introducing in particular the notions of quiescence and refusals for partial order semantics. Section 4 is dedicated to the definition, discussion and characterization of the input-output conformance relation **co-ioco**, refining the **co-ioco** relations of our previous papers [26, 27]. Section 5 develops the definitions of test cases and test suites, characterizing soundness, exhaustiveness and completeness of test suites, while Section 6 proposes an algorithm that builds a complete test suite, thus completing the contributions of the paper before Section 7 concludes.

2 Input/Output Labeled Event Structures

2.1 Syntax

We shall be using event structures following Winskel et al [28] to describe the dynamic behavior of a concurrent system. In this paper we will consider only prime event structures [30], a subset of the original model which is sufficient to describe concurrent models (therefore we will simply call them event structures), and we label their events with actions over a fixed alphabet L . As it is usual with reactive systems, we want to distinguish between the controllable actions (inputs proposed by the environment) and the observable ones (outputs produced by the system), leading to *input-output labeled event structures*.

Definition 1 (Input/Output Labeled Event Structure) *An input/output labeled event structure (IOLES) over an alphabet $L = L_{\mathcal{I}} \uplus L_{\mathcal{O}}$ is a 4-tuple $\mathcal{E} = (E, \leq, \#, \lambda)$ where*

- E is a set of events,
- $\leq \subseteq E \times E$ is a partial order (called causality) satisfying the property of finite causes, i.e. $\forall e \in E : |\{e' \in E \mid e' \leq e\}| < \infty$,
- $\# \subseteq E \times E$ is an irreflexive symmetric relation (called conflict) satisfying the property of conflict heredity, i.e. $\forall e, e', e'' \in E : e \# e' \wedge e' \leq e'' \Rightarrow e \# e''$,
- $\lambda : E \rightarrow L \cup \{\tau\}$ is a labeling mapping.

We denote the class of all input/output labeled event structures over L by $\text{IOLES}(L)$.

We assume that there exists an unique minimal element denoted and labeled by \perp which is unobservable. The special label $\tau \notin L$ represents an unobservable (also said internal or silent) action. Given an event e , its past is defined as $[e] \triangleq \{e' \in E \mid e' \leq e\}$. The sets of input, output and silent events are defined by $E^{\mathcal{I}} \triangleq \{e \in E \mid \lambda(e) \in L_{\mathcal{I}}\}$, $E^{\mathcal{O}} \triangleq \{e \in E \mid \lambda(e) \in L_{\mathcal{O}}\}$ and $E^{\tau} \triangleq \{e \in E \mid \lambda(e) = \tau\}$. When it is clear from the context, we will refer to an event by its label.

Concurrency. Two given events $e, e' \in E$ are said to be *concurrent* ($e \text{ co } e'$) iff neither $e \leq e'$ nor $e' \leq e$ nor $e \# e'$ hold. As it is shown in Figure 1, concurrency can be implemented in two different ways. In a distributed architecture, two actions specified as concurrent belong to different components and therefore should be implemented as such: this situation corresponds to the notion of *strong concurrency*. In Figure 1, actions a and b belong to different processes (are strongly concurrent) in Spe and are implemented as such in both Impl_1 and Impl_2 . In [27], concurrency is interpreted as strong concurrency, therefore the conformance relation forces concurrent actions to be implemented as such.

However, in an early stage of specification, concurrency between events may be used as underspecification. Actions belonging to the same component may be implemented in any order (as it is the case of a and c in Impl_1) or the specification may still be refined and this component implemented as several ones as it is the case of P_1 from Impl_2 . We capture this kind of underspecification with *weak concurrency*. In this paper we allow both kinds of concurrency in an

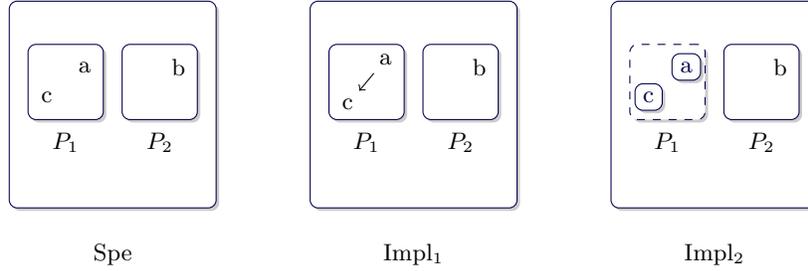


Figure 1: How to implement concurrency?

IOLES and split the **co** relation into two relations **sco** (strong concurrency) and **wco** (weak concurrency), such that $\mathbf{co} = \mathbf{sco} \uplus \mathbf{wco}$.

We illustrate the need to make these two notions of concurrency live in the same model by an example coming from the field of microcontroller design. We consider a *ParSeq controller* which manages two handshakes $A = (req_a, ack_a)$ and $B = (req_b, ack_b)$ on its right side according to the *operation code* (*opcode*) provided on its left side as shown in Figure 2. Depending on the *opcode* signals the handshakes are to be initiated either in parallel (concurrent events $A \mathbf{co} B$) or in sequence (in two possible orders $A < B$ or $B < A$), hence the name of the controller. As soon as both handshakes are completed the controller issues signal *done*. The reset phase is similar but the handshakes are always reset concurrently regardless of the *opcode*. In this example events A and B would be specified as weakly concurrent, but their actual order would depend on the *opcode* rather than on an implementation choice.

The kind of concurrent systems that we consider are distributed. The architecture of such systems allows to distinguish different components and there is a way to distinguish to which component each concurrent action belongs.

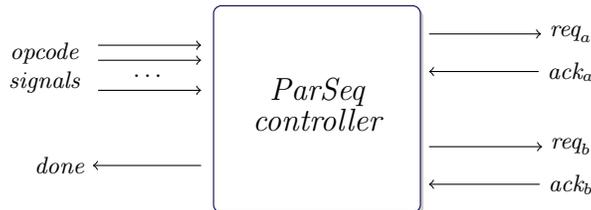


Figure 2: ParSeq controller interface.

Therefore, we make the following assumption.

Assumption 1 We will only consider systems where concurrent events are labeled by different actions, i.e. $\forall e, e' \in E : e \text{ co } e' \Rightarrow \lambda(e) \neq \lambda(e')$.

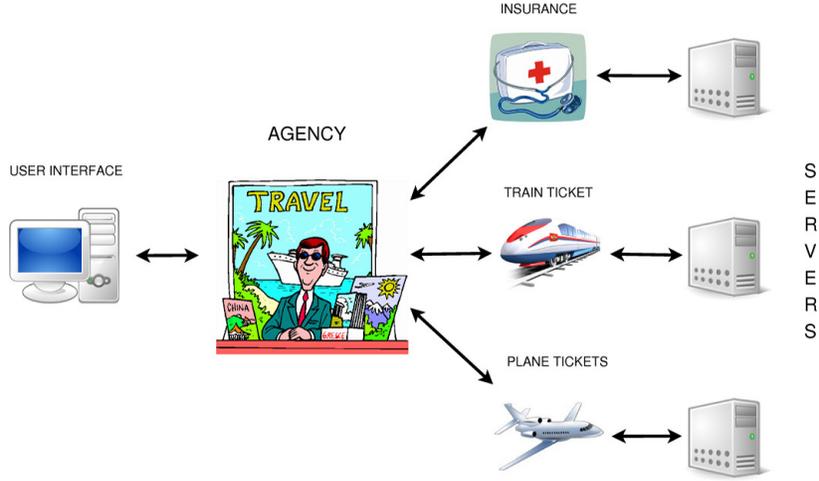
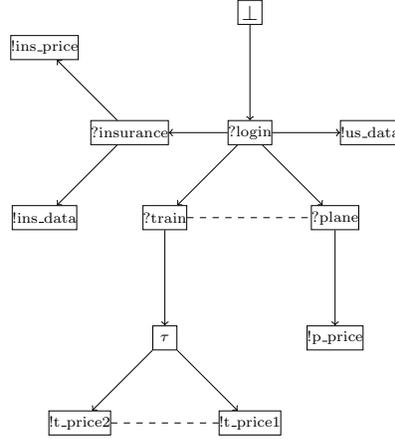


Figure 3: A travel agency example.

Example 1 Figure 3 shows a schematic travel agency whose behavior can be formally specified by the IOLESs presented in Figure 4, where causality and conflict are represented by \rightarrow and $- - -$ respectively, $?$ denotes input actions and $!$ output ones. In this system, once the user has logged in ($?login$), some data is sent to the server ($!us_data$) and he can choose an insurance ($?insurance$) and a train ticket ($?train$) or a plane ticket ($?plane$). If a plane ticket is chosen, its price is sent to the user ($!p_price$). If a train ticket is selected, the agency can internally decide (τ) what price to propose: a first class ($!t_price1$) or a second class one ($!t_price2$). The insurance choice is followed by its price ($!ins_price$) and some extra data that is sent to the user ($!ins_data$).

Data cannot be sent before the user logged in ($?login \leq !us_data$), selections for a ticket and an insurance can be done concurrently ($?train \text{ co } ?insurance$), but only one ticket can be chosen ($?train \# ?plane$). From the conflict heredity property, we have that only one ticket price can be produced ($!t_price1 \# !p_price$ and $!t_price2 \# !p_price$).

Strong concurrency only holds between actions of the insurance and those belonging to the ticket selection, i.e. $\text{sco} = \{?insurance, !ins_price, !ins_data\} \times \{?train, \tau, !t_price1, !t_price2, ?plane, !p_price\}$. All the actions belonging to each procedure (ticket and insurance selection) are weakly concurrent with the $!us_data$ action. In addition the actions $!ins_price$ and $!ins_data$ are also weakly concurrent and we finally have $\text{wco} = \{(!ins_data, !ins_price)\} \cup (\{!us_data\} \times \{?insurance, !ins_price, !ins_data, ?train, \tau, !t_price1, !t_price2, ?plane, !p_price\})$.



s

Figure 4: Input/output labeled event structure of a travel agency.

Immediate Conflict. Most of the specification languages allow some way of modeling choice. As conflict is inherited w.r.t causal dependency, a pair of events in conflict need not represent a choice between these events. We can see that $!t_price1$ and $!p_price$ are in conflict (by hierarchy), but any computation that continues by $!t_price1$, cannot continue by $!p_price$: the conflict was solved by the choice of $?train$ instead of $?plane$, and this makes $!p_price$ impossible. When the system makes a choice, we have a case of the *immediate conflict* relation in the following sense.

Definition 2 (Immediate Conflict) *Consider $\mathcal{E} = (E, \leq, \#, \lambda) \in \mathcal{IOLES}(L)$ and $e_1, e_2 \in E$. Events e_1 and e_2 are said in immediate conflict, written $e_1 \# e_2$, iff*

$$[e_1] \times [e_2] \cap \# = \{(e_1, e_2)\}$$

Prefix of an IOLES. Another important feature in the modeling of a system's behavior is the modeling of a subpart of it. The behavior of a subsystem is given by a *prefix* of the original system. As causality represents the events that should occur before a given event, the past of an event e that belongs to the prefix should also be part of the prefix.

Definition 3 (Prefix) *Let $\mathcal{E} = (E, \leq, \#, \lambda) \in \mathcal{IOLES}(L)$. A prefix of \mathcal{E} is an IOLES $\mathcal{E}' = (E', \leq', \#, \lambda')$ where*

- $E' \subseteq E$ such that $\forall e \in E' : [e] \subseteq E'$,
- $\leq' = \leq \cap (E' \times E')$,
- $\# = \# \cap (E' \times E')$, and

- $\lambda' = \lambda|_{E'}$

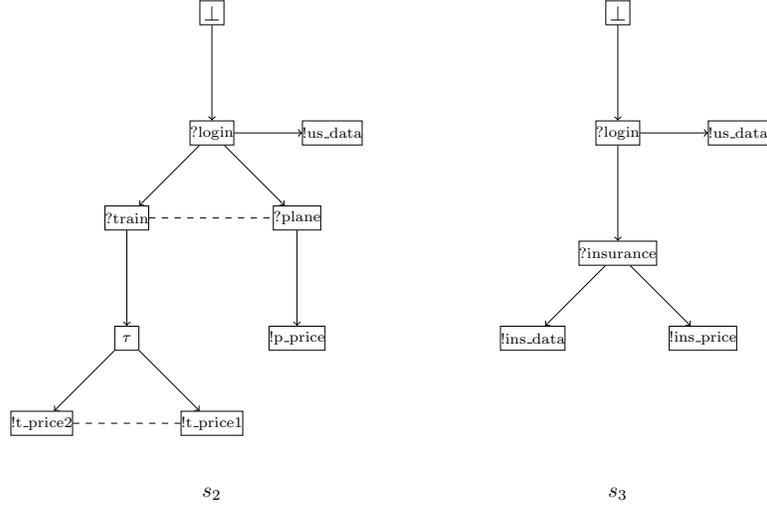


Figure 5: Two prefixes of the travel agency.

Example 2 In Figure 5, s_2 specifies the behavior of a travel agency that sells tickets, but not insurances, while the agency in s_3 only sells insurances. We can see that s_2 and s_3 are prefixes of s .

2.2 Semantics

In order to give semantics to event structures, we have to define the notion of execution, which relies on the notion of state, named configuration in labeled event structures. A computation state of an event structure is called a *configuration* and is represented by the set of events that have occurred in the computation. If an event is present in a configuration, then so are all the events on which this event causally depends (causal closure). Moreover, a configuration obviously does not contain conflicting events (conflict freedom). This is captured by the following standard definition [30].

Definition 4 (Configuration) Let $\mathcal{E} = (E, \leq, \#, \lambda) \in \text{IOLES}(L)$. A configuration of \mathcal{E} is a non-empty set of events $C \subseteq E$ where

- C is causally closed: $e \in C \Rightarrow \forall e' \leq e : e' \in C$, and
- C is conflict-free: $\forall e, e' \in C : \neg(e \# e')$.

A configuration C , equipped with the restriction of \leq , yields a partially ordered set, whose totally ordered extensions, or interleavings, describe possible sequential executions. Conversely, every sequential execution of the system is

an interleaving of a unique configuration of the system; a configuration gives an equivalence class of possible interleavings. In this sense, configurations represent non-sequential executions.

Note that we define, for technical convenience, all configurations to be non-empty; the initial configuration of \mathcal{E} , containing only \perp and denoted by $\perp_{\mathcal{E}}$, is contained in every configuration of \mathcal{E} . We denote the set of all the configurations of \mathcal{E} by $\mathcal{C}(\mathcal{E})$.

Example 3 In the IOLES of the travel agency of Figure 4, after the user has logged in, the selections can be made while his information is sent to the server, i.e. $\{\perp, ?login, !us_data, ?insurance, ?train\} \in \mathcal{C}(s)$, but a train and a plane cannot be in the same execution, i.e. $?plane, ?train \in C \Rightarrow C \notin \mathcal{C}(s)$. Configuration $\{\perp, ?login, !us_data, ?insurance, !ins_price, !ins_data, ?train, \tau, !t_price1\}$ is maximal (w.r.t \subseteq) as the remaining events are in conflict with the ones in the configuration.

Executions. The definition of the notion of execution for an event structure is not straightforward since it relies on the chosen semantics for concurrency [31]. Here, we have two notions of concurrency, which impose partial orders and allow interleavings. We are interested in testing both kinds of concurrency and therefore we want to keep concurrency explicit in the executions. *Labeled partial orders* can then be used to represent executions of such systems.

Definition 5 (Labeled partial order) *A labeled partial order over an alphabet L is a tuple $lpo = (E, \leq, \lambda)$, where*

- E is a set of events,
- \leq is a reflexive, antisymmetric, and transitive relation, and
- $\lambda : E \rightarrow L \cup \{\tau\}$ is a labeling mapping.

We denote the class of all labeled partial orders over L by $\mathcal{LPO}(L)$.

As we can only observe the ordering between the labels and not between the events, we should consider partial orders respecting such an order as equivalent. Two labeled partial orders are *isomorphic* iff there exists a bijective function that preserves ordering and labeling.

Definition 6 (Isomorphic LPOs) *Let $lpo_1 = (E_1, \leq_1, \lambda_1)$, $lpo_2 = (E_2, \leq_2, \lambda_2) \in \mathcal{LPO}(L)$. A bijective function $f : E_1 \rightarrow E_2$ is an isomorphism between lpo_1 and lpo_2 iff*

- $\forall e, e' \in E_1 : e \leq_1 e' \Leftrightarrow f(e) \leq_2 f(e')$
- $\forall e \in E_1 : \lambda_1(e) = \lambda_2(f(e))$

Two labeled partial orders lpo_1 and lpo_2 are isomorphic if there exists an isomorphism between them.

Definition 7 (Partially ordered multisets) A partially ordered multiset (*pomset*) is the isomorphic class of some LPO. We will represent such class by one of its objects. We denote the class of all pomsets by $\mathcal{POMSET}(L)$.

When it is clear from the context, we will use “.” to express causality between pomsets and “**co**” to represent the pomset whose elements are unordered. The pomset μ_4 of Figure 6 can be represented by $\perp \cdot ?login \cdot !us_data \cdot ?insurance \cdot (!ins_price \text{ co } !ins_data)$.

As weak concurrency is not necessarily preserved, the selection of a ticket in the travel agency can be done after sending the data and therefore μ_1 and μ_2 from Figure 6 should be treated as equal (it is also the case with μ_3, μ_4, μ_5 and μ_6). For this reason, an execution of this specification has to preserve the partial order semantics of the IOLES, up to adding order between weakly concurrent events (while strongly concurrent events must remain concurrent).

Definition 8 (Relaxed concurrency) Let $\mu_1, \mu_2 \in \mathcal{POMSET}(L)$, we have that $\mu_1 \sqsubseteq \mu_2$ iff there exist $lpo_1 = (E, \leq_{\mu_1}, \lambda) \in \mu_1$ and $lpo_2 = (E, \leq_{\mu_2}, \lambda) \in \mu_2$ such that

- $\leq_{\mu_1} \subseteq \leq_{\mu_2}$
- $sco_1 = sco_2$

In other words, $\mu_1 \sqsubseteq \mu_2$ if strong concurrency is preserved and some weakly concurrent events from μ_1 are ordered by \leq_{μ_2} .

Example 4 We see in Figure 6 that μ_2 adds some ordering between weakly concurrent events $!us_data$ and $?train$ from μ_1 , but strong concurrency is preserved, and therefore $\mu_1 \sqsubseteq \mu_2$. The same order is added from μ_3 in μ_4 , and μ_5 adds an ordering between the weakly concurrent events $!ins_price$ and $!ins_data$. Therefore $\mu_3 \sqsubseteq \mu_4$ and $\mu_4 \sqsubseteq \mu_5$. As \sqsubseteq is transitive, we have $\mu_3 \sqsubseteq \mu_5$. In μ_6 , $!us_data$ is preceded by $?insurance$ and then $\mu_3 \sqsubseteq \mu_6$.

As explained above, an execution of an event structure can be represented by a pomset, where the same pomset can reflect different executions in which concurrency can be relaxed, leading to the following notion of *relaxed executions*.

Definition 9 (Relaxed execution) Let $\mathcal{E} = (E, \leq, \#, \lambda) \in \mathcal{IOLES}(L)$, $\mu, \mu'' \in \mathcal{POMSET}(L)$ and $C, C', C'' \in \mathcal{C}(\mathcal{E})$, we define

$$\begin{aligned}
C \xrightarrow{\mu} C' &\triangleq \exists \mu' \sqsubseteq \mu, lpo = (E_{\mu'}, \leq_{\mu'}, \lambda_{\mu'}) \in \mu', A \subseteq E \setminus C : \\
&C' = C \cup A, A = E_{\mu'}, \leq \cap (A \times A) = \leq_{\mu'} \text{ and } \lambda|_A = \lambda_{\mu'} \\
C \xrightarrow{\mu \cdot \mu''} C'' &\triangleq \exists C' : C \xrightarrow{\mu} C' \text{ and } C' \xrightarrow{\mu''} C'' \\
C \xrightarrow{\mu} &\triangleq \exists C' : C \xrightarrow{\mu} C'
\end{aligned}$$

We say that μ is a relaxed execution of C if $C \xrightarrow{\mu}$.

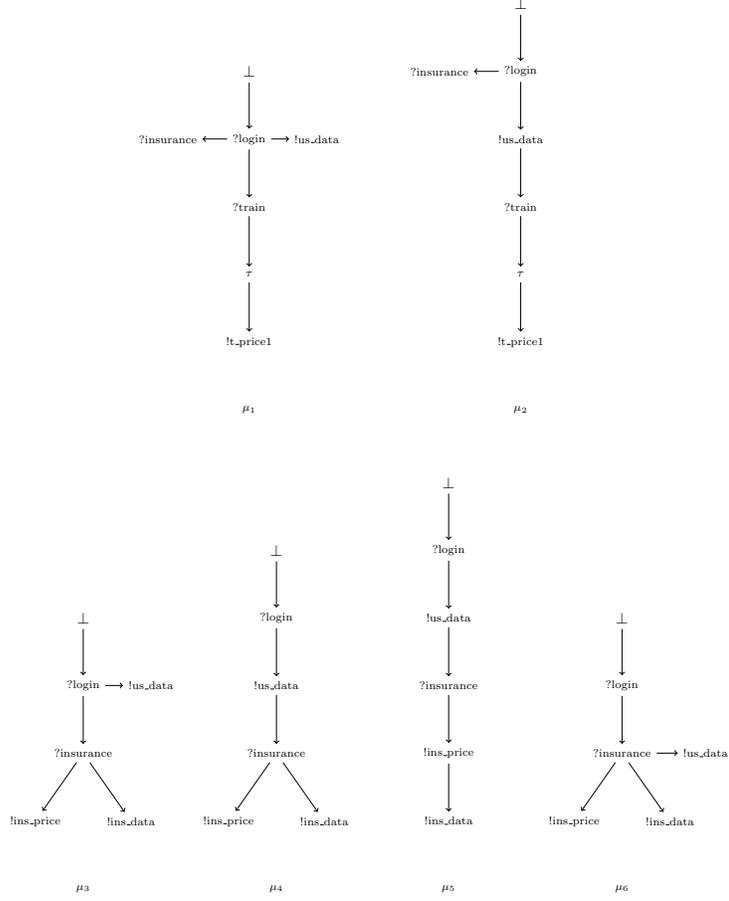


Figure 6: Relaxed executions of the travel agency

Example 5 In Figure 6 we can see that μ_1 and μ_3 respect the structure of s of Figure 4, and therefore both are relaxed executions of it ($\perp_s \xrightarrow{\mu_1}$ and $\perp_s \xrightarrow{\mu_3}$). However, as seen earlier, $\mu_1 \sqsubseteq \mu_2$, $\mu_3 \sqsubseteq \mu_4$, $\mu_3 \sqsubseteq \mu_5$ and $\mu_3 \sqsubseteq \mu_6$; therefore μ_2, μ_4, μ_5 and μ_6 are also relaxed executions of s ($\perp_s \xrightarrow{\mu_2}$, $\perp_s \xrightarrow{\mu_4}$, $\perp_s \xrightarrow{\mu_5}$ and $\perp_s \xrightarrow{\mu_6}$). In the case of μ_6 , we see that our semantics allows an execution where an output (!us_data) depends on an extra input (?insurance). However, we will see later that our conformance relation prevents an output from depending on an extra input, even if these events are specified as a weakly concurrent pair. We can conclude that the same structure can have several relaxed executions where weakly concurrent events are ordered.

3 Observing Event Structures

The notion of conformance in a testing framework is based on the chosen notion of observation of the system behavior. One of the most popular ways of defining the behavior of a system is in terms of its *traces* (observable sequences of actions of the system). Phillips [8], Heerink and Tretmans [13] and Lestiennes and Gaudel [14] propose conformance relations that in addition considers the actions that the system *refuses*. Finally, when there is a distinction between inputs and output actions, one can differentiate between situations where the system is still processing some information from those where the system cannot evolve without the interaction of the environment (usually called *quiescence*). This notion was introduced by Segala in [10]. In this section, we define these three notions in the context of labeled event structures, since the **co-ioco** conformance relation that we present in Section 4 relies on these observations.

3.1 Traces

The labels in L represent the observable actions of a system; they model the interactions of the system with its environment while internal actions are denoted by the special label $\tau \notin L$. The observable behavior can be captured by abstracting the internal actions from the executions of the system (which are pomset in our setting).

Definition 10 (τ -abstraction of a pomset) *Let $\mu, \omega \in \mathcal{POMSET}(L)$, we have that $abs(\mu) = \omega$ iff there exist $lpo_\mu = (E_\mu, \leq_\mu, \lambda_\mu) \in \mu$ and $lpo_\omega = (E_\omega, \leq_\omega, \lambda_\omega) \in \omega$ such that*

- $E_\omega = \{e \in E_\mu \mid \lambda_\mu(e) \neq \tau\}$
- $\leq_\omega = \leq_\mu \cap (E_\omega \times E_\omega)$
- $\lambda_\omega = \lambda_\mu|_{E_\omega}$

Finally, an *observation* of a configuration is the τ -abstraction of one of its execution.

Definition 11 (Observation) *Consider $\mathcal{E} = (E, \leq, \#, \lambda) \in \mathcal{IOLES}(L)$, $\omega \in \mathcal{POMSET}(L)$ and $C, C' \in \mathcal{C}(\mathcal{E})$, we define*

$$\begin{aligned} C \xrightarrow{\omega} C' &\triangleq \exists \mu : C \xrightarrow{\mu} C' \text{ and } abs(\mu) = \omega \\ C \xrightarrow{\omega} &\triangleq \exists C' : C \xrightarrow{\omega} C' \end{aligned}$$

We say that ω is an observation of C if $C \xrightarrow{\omega}$.

In the **ioco** theory, $?$ and $!$ are used to denote input and output actions respectively. We extend this notation and denote by $?\omega$ and $!\omega$ observations composed only of input and output actions respectively.

We can now define the notion of traces and reachable configurations from a given configuration by an observation. Our notion of trace is similar to the one of Ulrich and König [23] where a trace is considered as a sequence of partial orders. The reachable configurations that we consider are those that can be reached by abstracting the silent actions of an execution and only considering observable ones. This notion is similar to the one of unobservable reach proposed by Genc and Lafortune [32].

Definition 12 (Traces and reachable configurations) *Let $\mathcal{E} \in \mathcal{IOLES}(L)$, $\omega \in \mathcal{POMSET}(L)$ and $C, C' \in \mathcal{C}(\mathcal{E})$, we define*

- $traces(\mathcal{E}) \triangleq \{\omega \in \mathcal{POMSET}(L) \mid \perp_{\mathcal{E}} \xRightarrow{\omega}\}$
- $C \text{ after } \omega \triangleq \{C' \mid C \xRightarrow{\omega} C'\}$

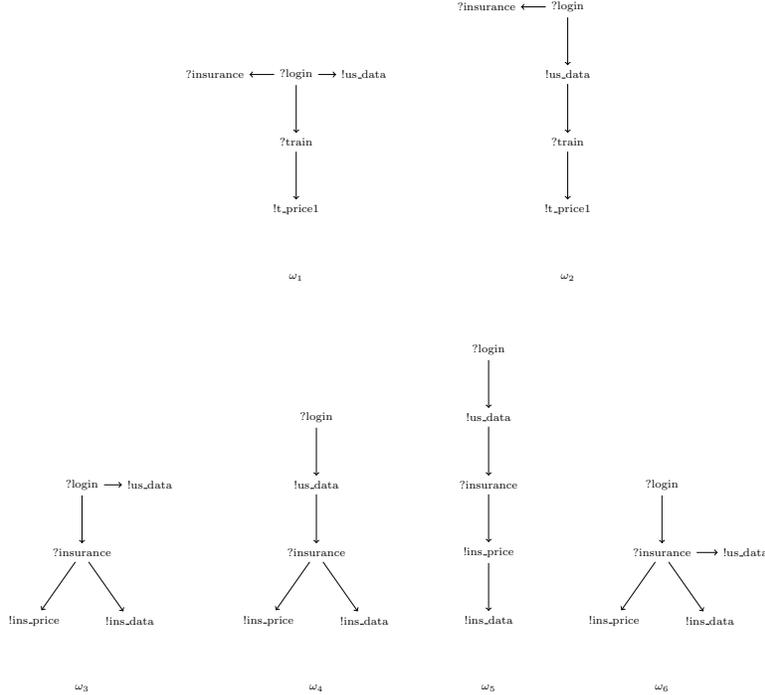


Figure 7: Traces of the travel agency

Example 6 *Consider the pomsets of Figures 6 and 7. Clearly, $abs(\mu_i) = \omega_i$, and we saw in Example 5 that $\perp_s \xrightarrow{\mu_i}$; therefore, $\perp_s \xRightarrow{\omega_i}$ and $\omega_i \in traces(s)$ for $i = 1, \dots, 6$. From the initial configuration in s , the configuration reached after the observations $\omega_3, \omega_4, \omega_5$ and ω_6 is the same, i.e. $(\perp_s \text{ after } \omega_i) = \{\perp, ?login, !us_data, ?insurance, !ins_price, !ins_data\}$ for $i = 3, 4, 5, 6$. This*

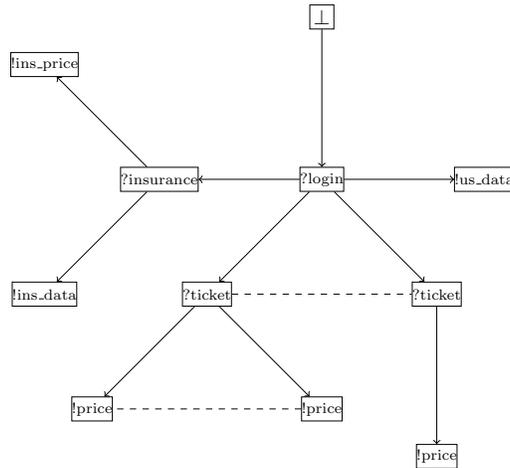
example shows that even if the way of observing executions are different (due to weak concurrency), they all come from the same structure and lead to the same configuration.

Our definition of **after** is general enough to handle nondeterminism in the computation, however in this paper we will only consider specifications where one configuration can be reached after some observation. Such systems are called *deterministic*.

Definition 13 (Deterministic IOLES) *Let $\mathcal{E} \in \text{IOLES}(L)$, we have*

$$\mathcal{E} \text{ is deterministic} \Leftrightarrow \forall \omega \in \text{traces}(\mathcal{E}), (\perp_{\mathcal{E}} \text{ after } \omega) \text{ is a singleton}$$

When the set of reachable configurations is a singleton $\{C\}$ we will simply denote it by C .



s_4

Figure 8: A nondeterministic IOLES.

Example 7 *We can see in Figure 8 that there is no distinction between the ticket choice, i.e. two configurations can be reached from the initial configuration after observing $?login \cdot ?ticket$, and then s_4 is nondeterministic.*

In the **ioco** framework, the specification is determined before the construction of test cases. Our notion of determinism is similar to that of *denotational determinism* presented in [33]. Since we assume concurrent events to have different labels, the problem arises if conflicting events have the same label. Such conflicting events can be merged to obtain a deterministic IOLES as it is explained in [33] allowing us to make the following assumption.

Assumption 2 *The specification of the system is deterministic, i.e. $\forall \omega \in \text{traces}(s) : (\perp_s \text{ after } \omega)$ is a singleton.*

3.2 Quiescence and Produced Outputs

Since the testing activity depends on the interaction between the tester and the system, such interaction becomes impossible if we allow the system to have infinitely many occurrences of silent or output actions without input ones. Therefore we make the following assumption.

Assumption 3 *We will only consider systems that cannot diverge by infinitely many occurrences of silent or output actions, i.e. $\forall C \in \mathcal{C}(\mathcal{E}) : \text{if } C \cap (E^o \cup E^\tau)$ is infinite then so is $C \cap E^\perp$.*

This assumption is classical in model-based testing frameworks, as it is necessary to be able to identify the blockings of the system under test.

With reactive systems, we need to differentiate configurations where the system can still produce some outputs, and those where the system cannot evolve without an input from the environment. Such situations are captured by the notion of quiescence [10]. The observation of quiescence in such configurations is usually implemented by timers. Jard and Jérón [34] present three different kinds of quiescence: *output quiescence*: the system is waiting for an input from the environment, *deadlock*: the system cannot evolve, and *livelock*: the system diverges by an infinite sequence of silent actions. The observation of quiescence is usually made explicit by adding self loops labeled by a δ action on quiescent states, where δ is considered as a new output action. But since event structures are acyclic, we define the δ action semantically and not syntactically: the δ action does not represent an event, and thus no new configuration is reached after observing it.

Definition 14 (Quiescence) *Let $\mathcal{E} \in \text{IOLES}(L)$ and $C \in \mathcal{C}(\mathcal{E})$, we have*

$$C \text{ is quiescent} \Leftrightarrow \forall !\omega \in \text{POMSET}(L_o) : C \not\stackrel{!}{\Rightarrow} \omega$$

Quiescence is observable by a δ action, i.e. C is quiescent iff $C \stackrel{\delta}{\Rightarrow}$.

Both output quiescence and deadlock are captured by the definition above, while livelock is not possible by Assumption 3.

Example 8 *In the travel agency example, the configuration reached after logging in is not quiescent as there is an execution where the user's data can be sent, i.e. $(\perp_s \text{ after } ?login) = \{\perp, ?login\}$ and $\{\perp, ?login\} \stackrel{!us_data}{\Rightarrow}$, but the configuration reached after sending the user's data is quiescent because only input actions are enabled in all the possible executions, i.e. $(\perp_s \text{ after } (?login \cdot !us_data)) = \{\perp, ?login, !us_data\}$ and for every ω such that $\{\perp, ?login, !us_data\} \stackrel{\omega}{\Rightarrow}$, we have $E_\omega^\perp \neq \emptyset$.*

In the LTS framework, the *produced outputs* of the systems are single elements of the alphabet of outputs rather than sequences of them [11]. Consider a system s that produced $!a$ followed by $!b$ after σ , then $\text{out}(s \textbf{ after } \sigma) = \{!a\}$ and $\text{out}(s \textbf{ after } (\sigma \cdot !a)) = \{!b\}$ rather than $\text{out}(s \textbf{ after } \sigma) = \{!a \cdot !b\}$. A first extension proposed in [26] considers that the outputs produced by the system in response to stimuli could be elementary actions as well as sets of concurrent ones. However, here we need any set of outputs to be entirely produced by the system under test before we send a new input; this is necessary to detect outputs depending on extra inputs. In fact, suppose one has two concurrent outputs out_1 and out_2 depending on input in_1 and another input in_2 depending on both outputs. Clearly, an implementation that accepts in_2 before out_2 should not be considered as correct, but if in_2 is sent too early to the system, we may not know if the occurrence of out_2 depends or not on in_2 . For this reason, Definition 15 defines the expected outputs from a configuration as the pomset of outputs leading to a quiescent configuration. Such a configuration always exists, and is finite by Assumption 3.

However, conformance of output pomset is not always captured by isomorphism. Consider again the example presented in the paragraph above and consider out_1 and out_2 as weakly concurrent. After in_1 the system produces outputs out_1 and out_2 which can be observed concurrently or in any order (due to the relaxed executions). We want to compare the produced outputs of the implementation with those of the specification but here, both $out_1 \cdot out_2$ and $out_2 \cdot out_1$ can be inferred from $out_1 \textbf{ wco } out_2$. Therefore, to facilitate the comparison, we will only consider $out_1 \textbf{ wco } out_2$, which is the “most abstract” pomset representing both orders, i.e. the minimal pomset w.r.t. \sqsubseteq .

Definition 15 (Produced outputs) *Let $\mathcal{E} \in \mathcal{IOLES}(L)$ and $C \in \mathcal{C}(\mathcal{E})$, we define*

$$\text{out}(C) \triangleq \min_{\sqsubseteq} \{ \omega \in \mathcal{POMSET}(L_o) \mid C \xrightarrow{! \omega} C' \wedge C' \xrightarrow{\delta} \} \cup \{ \delta \mid C \xrightarrow{\delta} \}$$

Example 9 *The only output produced by the system of Figure 4 after logging in is the user’s data, i.e. $\text{out}(\perp_s \textbf{ after } ?login) = \{!us_data\}$ and after this output, a quiescent configuration is reached, then $\text{out}(\perp_s \textbf{ after } (?login \cdot !us_data)) = \{\delta\}$. If a train ticket is chosen, different prices may be produced, i.e. $\text{out}(\perp_s \textbf{ after } (?login \cdot !us_data \cdot ?train)) = \{!t_price1, !t_price2\}$. The outputs after selecting the insurance are weakly concurrent and can be observed in different ways (concurrently or in order), however we only consider the \sqsubseteq -minimal one, i.e. $\text{out}(\perp_s \textbf{ after } (?login \cdot !us_data \cdot ?insurance)) = \{!ins_price \textbf{ co } !ins_data\}$.*

3.3 Refusals

The **io**co theory assumes the input enabledness of the implementation, i.e. in any state of the implementation, every input action is enabled. This assumption is made to avoid computation interference [35] in the parallel composition between the implementation and the test cases. However, as explained by

Heerink [36] and Lestiennes and Gaudel [14] even if many realistic systems can be modeled with such an assumption, there remains a significant portion of realistic systems that cannot be modeled as such. An example of such a system is an automatic cash dispenser where the action of introducing a card becomes (physically) unavailable after inserting a card, as the automatic cash dispenser is not able to swallow more than one card at a time. Furthermore, this theory proposes test cases that are always capable of observing every output produced by the system, a not very realistic situation in a concurrent environment.

In order to overcome these difficulties, Heerink [36] distributes the points of control and observation, and the input enabledness assumption is weakened by the following assumption: “if an input action can be performed in a control point, all the inputs actions of that control point can be performed”. Refused inputs in the implementation are made observable by a special ξ -action (as quiescence is observable by a δ action). In [14], Lestiennes and Gaudel enrich the system model by *refused* transitions and a set of *possible* actions is defined in each state. Any possible input in a given state of the specification should be possible in a correct implementation.

Our approach is closer to [14]; any *possible input* in a configuration of the specification should also be possible in the implementation (or any input refused by the implementation should be refused by the specification). This implies that we assume that there exists a way to observe the refusal of an input by the implementation during testing. This assumption is quite natural, for instance in the case of the cash dispenser which cannot accept more than one card. One can consider that the system under test would display an error message or a warning in case it cannot handle an input the test sends.

In an observation, an input action may be preceded by an output that was specified to be weakly concurrent as it is the case with $!us_data$ and $?train$ in ω_2 . Therefore $?train$ should still be considered as possible even if the $!us_data$ output has not been produced yet. This is similar in remote testing [37] where communication between test cases and the SUT is asynchronous and a new input can be send even if an outputs that precedes it was not still produced.

The possible inputs of a configuration are those that are enabled or those that will be enabled after producing some outputs. As in the case of produced outputs, we just consider the set of \sqsubseteq -minimal inputs.

Definition 16 (Possible inputs) *Let $\mathcal{E} \in IOLES(L)$ and $C \in \mathcal{C}(\mathcal{E})$, we define*

$$poss(C) \triangleq \min_{\sqsubseteq} \{ ?\omega \in \mathcal{POMSET}(L_i) \mid C \xrightarrow{?\omega} \vee \exists !\omega \in \mathcal{POMSET}(L_o) : C \xrightarrow{!\omega} C' \wedge C' \xrightarrow{?\omega} \}$$

Example 10 *Consider the IOLES s of Figure 3, the first possible input is the logging in followed by the selections of tickets and insurance. Selections are possible either alone or concurrently, i.e. $poss(\perp_{i_1}) = \{ ?login, ?login \cdot ?insurance, ?login \cdot ?train, ?login \cdot ?plane, ?login \cdot (?insurance \mathbf{co} ?train), ?login \cdot (?insurance \mathbf{co} ?plane) \}$.*

In order to allow for the observation of the possible inputs of the system under test, a configuration where inputs are possible should not alternatively allow for the production of outputs. As a matter of fact, if an input and an output are in conflict in a given configuration, once the output is produced, the input is not enabled anymore. Such configurations prevent from observing the possible inputs of the system under test. For this reason, we restrict the form of labeled event structures we consider with the following assumption.

Assumption 4 *We will only consider IOLES such that there is no immediate conflict between input and output events, i.e. $\forall e \in E^I, e' \in E^O : \neg(e \# e')$.*

Note that a similar assumption was also made by Gaudel et al in [14], where such specifications are called IO-exclusive. Under assumption 4, no enabled input can be *disabled* by the production of outputs: to disable an input, some *conflicting input* must be made.

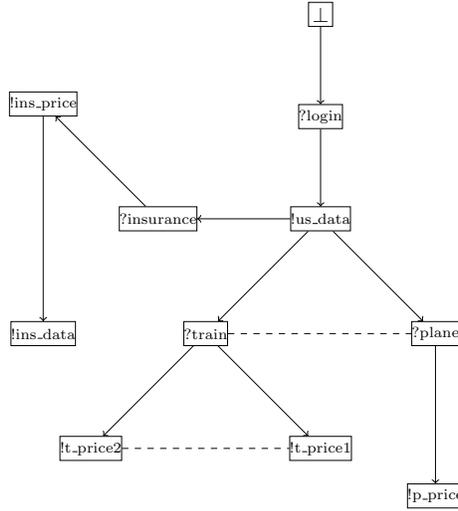
Proposition 1 *Let $\mathcal{E} \in \text{IOLES}(L)$ such that \mathcal{E} satisfies Assumption 4. Let $C, C' \in \mathcal{C}(\mathcal{E})$ such that there exists $!\omega \in \text{POMSET}(L_o)$, $C \xrightarrow{!\omega} C'$ and C' is quiescent. Then any possible input in C is a possible input in C' , i.e. $\text{poss}(C) = \text{poss}(C')$.*

Proof 1 *Let assume that $?\omega \in \text{poss}(C)$ for a non quiescent configuration C . We have then that $C \xrightarrow{?\omega}$, or we can reach from C a quiescent configuration C' such that $C' \xrightarrow{?\omega}$. The result is immediate for the second case. If it is the case that $C \xrightarrow{?\omega}$, let C'' be the quiescent configuration reachable from it by some $!\omega$, i.e. $C \xrightarrow{!\omega} C''$ and C'' is quiescent. We have two possible observations $?\omega$ and $!\omega$ at the same configuration C and then its events should be in immediate conflict or concurrent. By the hypothesis, we know they are concurrent (they are not in immediate conflict) and then they remain observable after some of them have been observed, i.e. $C \xrightarrow{!\omega} C''$ and $C'' \xrightarrow{?\omega}$. Finally $?\omega \in \text{poss}(C'')$.*

We now have all the elements to define a conformance relation for IOLES based in the observation notions of traces, refusals and quiescence.

4 The Conformance Relation: **co-ioco**

The activity of testing relies crucially on the definition of a *conformance* relation that specifies which observed behaviors must be considered conforming, or *not* conforming, to the specification. Aceto et al [31] propose several testing equivalences depending in the chosen semantics for event structures. In [26], we propose two extensions for the **ioco** conformance relation proposed by Tretmans [38], one for the interleaving semantics and another for the partial order one. In [27] we dropped the input enabledness assumption and enlarged the conformance relation in order to observe refusals. Actions specified as concurrent must occur independently (on different processes) in any conformant implementation.



i_1

Figure 9: A correct implementation w.r.t **co-ioco** of the travel agency of Figure 4.

Here, since we refine the semantics of IOLES with strong and weak concurrency, we need to refine the conformance relation **co-ioco** in order to take these two interpretations of concurrency into account.

Our conformance relation for labeled event structures can be informally described as follows. The behavior of a correct **co-ioco** implementation after some observations (obtained from the specification) should respect the following restrictions:

1. any output produced by the implementation should be produced by the specification;
2. if a quiescent configuration is reached in the implementation, this should also be the case in the specification;
3. any time an input is possible in the specification, this should also be the case in the implementation;
4. strongly concurrent events are implemented concurrently while weakly concurrent events may be ordered.

Before the definition of the conformance relation itself, we need a few more technical definitions in order to be able to compare the inputs and outputs of the system under test to those of its specification.

Concurrent Completeness. As two inputs may be weakly concurrent in the specification, we want to accept an implementation where they are only implemented in one order. Suppose there exists two weakly concurrent inputs in_1, in_2 such that $\perp_s \xrightarrow{in_1 \text{ co } in_2}$, then $\text{poss}(\perp_s) = \{in_1, in_2, in_1 \text{ co } in_2\}$. Now consider an implementation that orders them, e.g. $\text{poss}(\perp_i) = \{in_1, in_1 \cdot in_2\}$. We can not compare the possible inputs of both systems w.r.t set inclusion because we want inputs to be implemented in at least one of the allowed orders.

We expect any pomset of possible inputs in the specification to be implemented either as such or as one of its refinements. However, this is not enough. In the example presented in the paragraph above there is not a possible input of the implementation (in its initial configuration) that refines in_2 . In addition, our definition of possible inputs accepts partial orders with some causality as in the case of s where we have $?login \cdot (?insurance \text{ co } ?train) \in \text{poss}(\perp_s)$. However, we may add some order for a weakly concurrent output (as is the case of $!us_data$ in i_1) and therefore we can not find a possible input in the implementation that refines one of the specification. For this reason, we restrict to *concurrent complete sets* of inputs.

Definition 17 (Concurrent Complete Set) *Let $\omega \in \mathcal{POMSET}(L)$ and $C \in \mathcal{C}(\mathcal{E})$, we say that ω is a concurrent complete set in C iff any other execution from C (without causality) does not contain events that are concurrent to those of ω*

$$cc(\omega, C) \Leftrightarrow \omega = \max_{\sqsubseteq} \{w \mid C \xrightarrow{\omega} \wedge \leq_{\omega} = \emptyset\}$$

Example 11 *Consider i_1 from Figure 9, we have that $?insurance$ is possible after logging in and sending the data, i.e. $(\perp_{i_1} \text{ after } (?login \cdot !us_data)) \xrightarrow{?insurance}$. However this input is not a concurrent complete set as it can be “extended” by concurrent events, i.e. $(\perp_{i_1} \text{ after } (?login \cdot !us_data)) \xrightarrow{?insurance \text{ co } ?train}$.*

Possible inputs are checked in several steps: we first find a refinement for $?login$ from the initial configuration, and later another for $?insurance \text{ co } ?train$ from $\{?login\}$.

As explained above, the possible inputs of the specification can not be directly compared with those of the implementation. We want any concurrent complete input of the specification without causality to be implemented by one of its refinements (as \sqsubseteq is reflexive, the input can be implemented as it is specified).

Definition 18 (Input refinement) *Let $C, C' \in \mathcal{POMSET}(L)$ we define*

$$\text{poss}(C) \ggg^+ \text{poss}(C') \Leftrightarrow \forall ?\omega \in \text{poss}(C) : (cc(?\omega, C) \Rightarrow \exists ?\omega' \in \text{poss}(C') : \omega \sqsubseteq \omega')$$

Analogously, outputs can not be compared directly by set inclusion and we need every output produced by the implementation to refine some output of the specification.

Definition 19 (Output abstraction) *Let $C, C' \in \mathcal{POMSET}(L)$ we define*

$$out(C) \gg^- out(C') \Leftrightarrow \forall x \in out(C) : \exists x' \in out(C') : x' \sqsubseteq x$$

Notice that δ only refines itself and therefore if $\delta \in out(C)$ and $C \gg^- out(C')$ then $\delta \in out(C')$.

The co-ioco Conformance Relation. Now requirements 1, 2, 3 and 4 can be formalized by the following conformance relation.

Definition 20 (co-ioco) *Let $i, s \in \mathcal{IOLES}(L)$, then*

$$\begin{aligned} i \text{ co-ioco } s &\Leftrightarrow \forall \omega \in traces(s) : \\ & \quad poss(\perp_s \text{ after } \omega) \gg^+ poss(\perp_i \text{ after } \omega) \\ & \quad out(\perp_i \text{ after } \omega) \gg^- out(\perp_s \text{ after } \omega) \end{aligned}$$

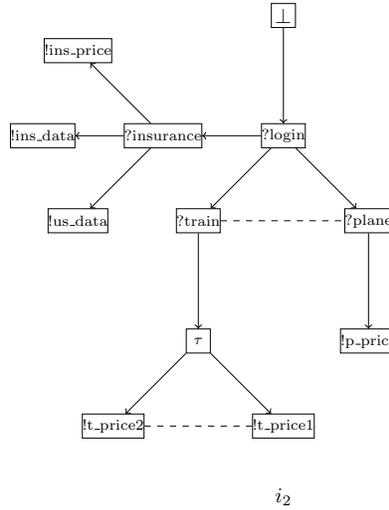
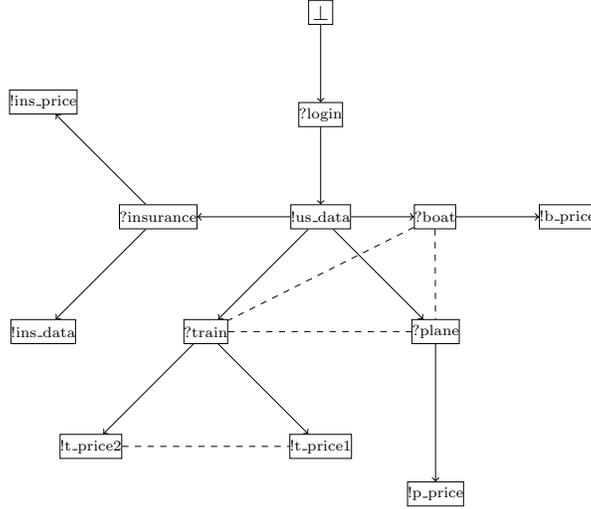


Figure 10: Output depending on extra input.

Example 12 (Order of Weakly Concurrent Events) *The implementation i_1 of the travel agency proposed in Figure 9 order some weakly concurrent events. The outputs $!ins_price$ and $!ins_data$ are implemented sequentially instead of concurrently, but the output produced ($!ins_price \cdot !ins_data$) refines an output produced by the specification ($!ins_price \text{ co } !ins_data$). Some order is also added between inputs $?insurance$, $?train$, $?plane$ and output $!us_data$. However these inputs depend on the output and therefore the produced outputs in the implementation are those specified. Even if some order is added, by Proposition 1, every possible input of the specification is implemented. We can conclude that $i_1 \text{ co-ioco } s$.*



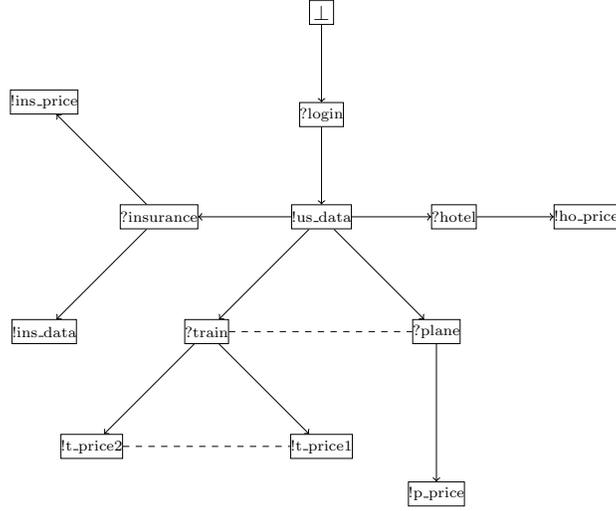
i_3

Figure 11: Extra conflicting inputs.

Events $?insurance$ and $!us_data$ are ordered in the opposite way in implementation i_2 of Figure 10 ($?insurance \leq !us_data$). A quiescent configuration is reached after logging in, i.e. $out(\perp_{i_2} \text{ after } ?login) = \{\delta\}$ while $out(\perp_s \text{ after } ?login) = \{!us_data\}$ and then $\neg(i_2 \text{ co-ioco } s)$. We can conclude that whenever an input and an output are weakly concurrent, then if ordering is added in a conformant implementation, the output should precede the input.

Example 13 (Extra Inputs) The behaviors of the implementation and the specification are compared after some observations are made. These observations are taken from the specification (they are traces of s in Figure 4), therefore, there is no restriction for the implementation about how to react to unspecified inputs. Figure 11 shows a possible implementation i_3 that also allows the user to choose a boat ticket. Even if this implementation may produce an extra output ($!b_price$), this output is only produced after the boat ticket has been chosen, but the behavior of the system after choosing a boat ticket is not specified. Finally, we have $i_3 \text{ co-ioco } s$. Figure 12 presents implementation i_4 that allows the user to concurrently chose for a hotel. We consider concurrent complete possible inputs only in the specification and then the $?hotel$ action and its corresponding output are never tested. As every concurrent complete possible input of the specification is refined by one of the implementation, we can conclude that $i_4 \text{ co-ioco } s$.

Example 14 (Refused Inputs) The conformance relation considers the input actions that the implementation may refuse. Figure 13 presents two possible



i_4

Figure 12: Extra concurrent inputs.

implementations i_5 and i_6 of the travel agency. The one on the left removes the possibility to choose an insurance, while the one on the right removes the choice for a train ticket. In the specification, we have that $\text{poss}(\perp_s \text{ after } ?\text{login}) = \{?\text{insurance}, ?\text{train}, ?\text{plane}, ?\text{insurance co } ?\text{train}, ?\text{insurance co } ?\text{plane}\}$, but $?\text{insurance}$ is not part of any possible input in i_5 , i.e. $\text{poss}(\perp_{i_5} \text{ after } ?\text{login}) = \{?\text{train}, ?\text{plane}\}$ and finally $\neg(i_5 \text{ co-ioco } s)$. The $?\text{train}$ action is neither part of any possible input in i_6 , i.e. $\text{poss}(\perp_{i_6} \text{ after } ?\text{login}) = \{?\text{insurance}, ?\text{plane}, ?\text{insurance co } ?\text{plane}\}$ and then $\neg(i_6 \text{ co-ioco } s)$.

Example 15 (Extra/incomplete Outputs) The second condition of the conformance relation establishes that all the outputs produced by the implementation should be specified. Consider the implementation i_7 presented in Figure 14: after choosing the plane ticket, the implementation can produce an output with the ticket price or an error message due to the fact that there are no tickets available, i.e. $\text{out}(\perp_{i_7} \text{ after } (?\text{login} \cdot !\text{us_data} \cdot ?\text{plane})) = \{!p_price, !p_full\}$, but $!p_full$ is not a possible output in the specification, i.e. $!p_full \notin \text{out}(\perp_s \text{ after } (?\text{login} \cdot !\text{us_data} \cdot ?\text{plane})) = \{!p_price\}$, therefore $\neg(i_7 \text{ co-ioco } s)$. The conformance relation only considers “complete” outputs (those that lead to a quiescent configuration), while incomplete outputs lead to non conformance. Implementation i_7 also shows an example of this: after choosing the insurance, only its price is produced, i.e. $\text{out}(\perp_{i_7} \text{ after } (?\text{login} \cdot !\text{us_data} \cdot ?\text{insurance})) = \{!ins_price\}$. This output does not refine any produced output of the specification, as some insurance data should also be produced (either concurrently

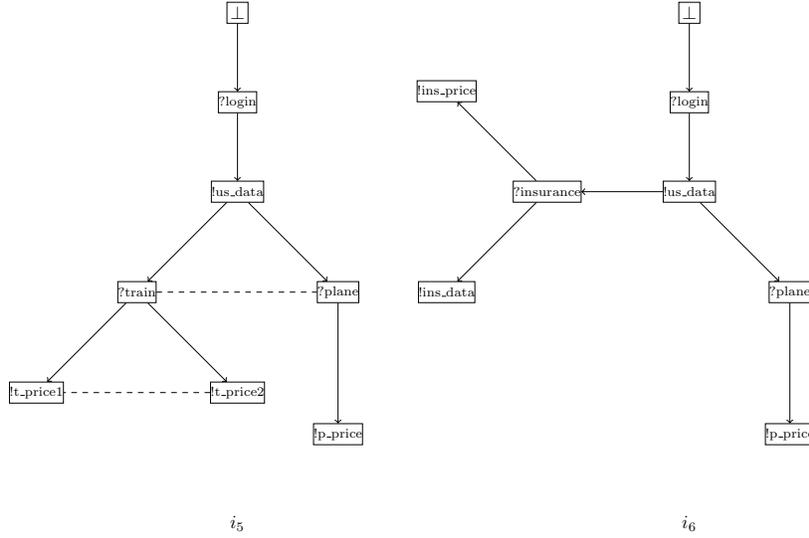


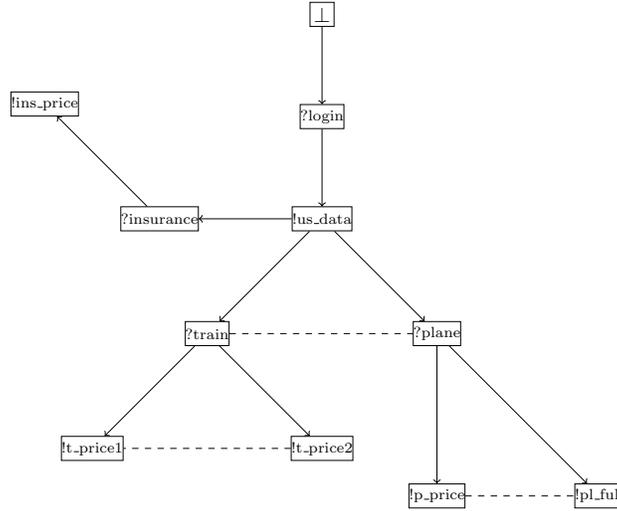
Figure 13: Refused inputs.

or in some order), i.e. $out(\perp_s \text{ after } (?login \cdot !us_data \cdot ?insurance)) = \{!ins_price \text{ co } !ins_data\}$, and again $\neg(i_7 \text{ co-ioco } s)$.

Example 16 (Extra Quiescence) *The second condition of the conformance relation stipulates that absence of outputs can only occur when it is specified. Figure 15 shows an implementation i_8 that does not send the user's data after logging in, thus a quiescent configuration is reached after logging in, i.e. $out(\perp_{i_8} \text{ after } ?login) = \{\delta\}$, but this quiescence is not specified, i.e. $\delta \notin out(\perp_s \text{ after } ?login) = \{!us_data\}$, and $\neg(i_8 \text{ co-ioco } s)$.*

Comparing the Conformance Relations. We present now a comparison between the previous conformance relations presented in [26, 27] and the one presented in this paper. The **co-ioco** conformance relation was introduced in [26] with two different semantics. Under interleaving semantics this relation boils down to **ioco** while partial order semantics allows to distinguish true concurrency from interleavings. Conformance in [27] only considers partial order semantics: events specified as concurrent should be implemented as such. In addition, in [27] we drop the input enabledness assumption of the implementation and we allow to test for refusals. Finally, as explained above, under the definition of **co-ioco** we give in this paper, implementations where events specified as weakly concurrent are ordered are considered as correct.

When every pair of concurrent event is specified as strongly concurrent (there are not weakly concurrent events), the **co-ioco** relation presented in this paper boils down to the conformance relation presented in [27]. In addition, if we



i_7

Figure 14: Extra/Incomplete Outputs.

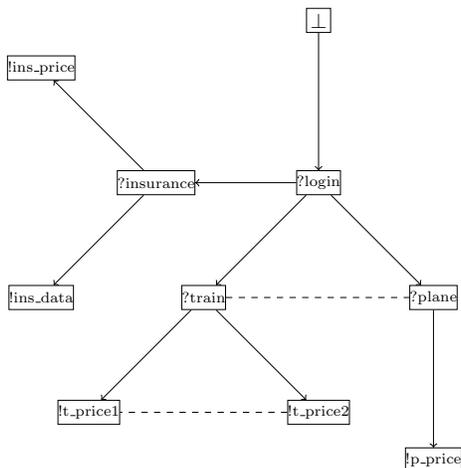
assume that the implementation is input enabled, then the relations from [26] and [27] (with partial order semantics) are equivalent. Finally, when there is no concurrency at all (the system is sequential), the relations from [26] boil down to **ioco**. These results are summarized in the following table.

| Assumptions | Results |
|---|--|
| $\mathbf{co} = \mathbf{sco}$ | $\mathbf{co-ioco} = [27]$ |
| $\mathbf{co} = \mathbf{sco} \wedge$ input enabledness of the SUT | $\mathbf{co-ioco} = [27] = [26]$ |
| $\mathbf{co} = \mathbf{sco} \wedge$ input enabledness of the SUT $\wedge \mathbf{co} = \emptyset$ | $\mathbf{co-ioco} = [27] = [26] = \mathbf{ioco}$ |

5 A Testing Framework for Labeled Event Structures

In section 4 we have formally defined what it means for an implementation to conform to its specification, and we have seen several examples of conforming and non conforming implementations. Now, we need a way to test this notion of conformance. In this section we define the notions of test cases and test suites, as well as their interaction with the implementations and we give sufficient conditions for detecting all and only incorrect implementations.

In order to formally reason about implementations, we make the usual testing assumption that the implementation under test can be modeled by an IOLES.



i_8

Figure 15: Extra Quiescence.

5.1 Test Cases and Test Suites

A *test case* is a specification of the tester’s behavior during an experiment carried out on the system under test. In such an experiment, the tester serves as a kind of artificial environment of the implementation. The output¹ actions are observed, but not controlled by the tester; however, the tester does control the input ones. It follows that there should be no choices between them, i.e. the next (set of concurrent) input(s) to be proposed should be unique, therefore no *immediate conflict between inputs* should exist in a test case.

This property is not enough to avoid all choices in a test case: if we allow the tester to reach more than one configuration after some observation and each of them enables different inputs, there is still some (nondeterministic) choice for the tester about the next input to propose even if those inputs are not in immediate conflict. We require thus determinism: the reached configuration after some observation should be unique.

Finally, we require the experiment to finish, therefore the event structure should be finite.

We model the behavior of the tester by a deterministic event structure with a finite set of events and without immediate conflicts between its inputs.

Definition 21 (Test Case / Test Suite) *A test case is a deterministic i/o labeled event structure $t = (E_t, \leq_t, \#_t, \lambda_t)$ where*

¹When we refer to inputs/outputs, we refer to input or output from the point of view of the implementation. We do not assume, as it is usual, that the test case is a “mirror” of the specification

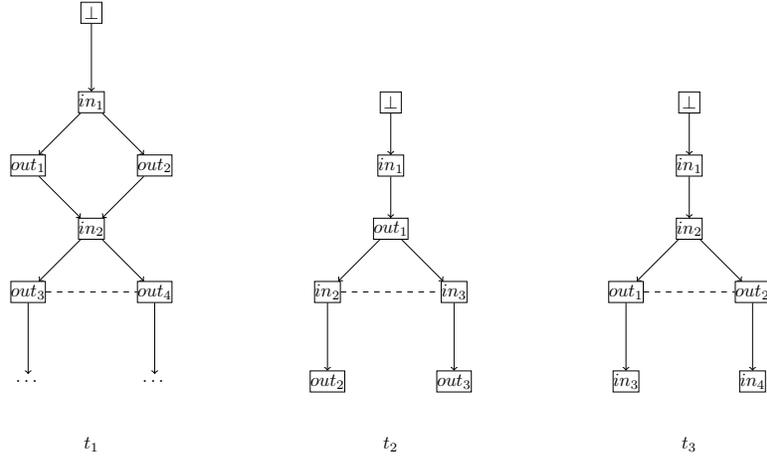


Figure 16: **Left:** an infinite event structure, **Center:** immediate conflict between inputs, **Right:** a test case

1. $(E_t^I \times E_t^I) \cap \overline{\#}_t = \emptyset$,
2. E_t is finite

A test suite is a set of test cases.

Example 17 Figure 16 presents three event structures. The behavior of t_1 is infinite which prevents it from being a test case; t_2 is not a test case either since there is an immediate conflict between in_2 and in_3 . The inputs in_3 and in_4 are in conflict in t_3 , but this conflict is not immediate. In addition E_{t_3} is finite and t_3 is deterministic, therefore t_3 is a test case.

We are interested in the interaction between the test case and the implementation (called *test execution*) in order to give a *verdict* about the success or failure of the test w.r.t. the conformance relation. Verdicts are usually modeled via a labeling function from the states of the test case to the set $\{\mathbf{pass}, \mathbf{fail}\}$. Only leaves are labeled, and a **pass** verdict can only be reached after observing some output of the implementation (in this framework, δ is considered an output). One possibility would be to label configurations with verdicts, but as there is no event labeled by δ , i.e. observing δ does not lead to a new configuration, we need to model verdicts differently. As in the case of quiescence, we do not define verdicts syntactically, but rather semantically.

5.2 Test Execution and Verdicts

The interaction between two systems is usually formalized by their parallel composition. This composition assumes that both systems are always prepared to accept an output that the other may produce. In the sequential setting, it is

assumed that the implementation accepts any input the tester can propose (input enabledness of the implementation). Analogously, the tester should be able to synchronize with any output the implementation may produce. Constructing an event structure having such a property is almost impossible due to the fact that it should not only accept any output, but also all the possible ways such an output could happen (concurrently/sequentially with other outputs). We propose another approach to formalize the interaction between the implementation and a test case.

Deadlocks of the parallel composition are used to give verdicts about the test run in the **ioco** framework. Such deadlocks are produced in the following situations:

1. the implementation proposes an output or a δ action that the test case cannot accept,
2. the test case proposes an input that the implementation cannot accept, or
3. the test case has nothing else to propose (it deadlocks).

The first two situations lead to a *fail* verdict, and the last to a *pass* one. For having such verdicts, we will define the notion of blocking in the test execution.

After observing a trace, the test execution can block because of an output the implementation produces for three reasons. First, if after such an observation the test case cannot accept that output. Second, the test case can accept such output, but this is not the maximal output it can accept (the reached configuration is not quiescent). Finally the test execution blocks if the implementation reaches a quiescent configuration and the test case does not.

Such situations can be simplified to the observation of an element in the set of outputs produced by the implementation that does not refine any output of the test case, i.e. $\exists x \in \text{out}(\perp_i \text{ after } \omega) : \forall x' \in \text{out}(\perp_t \text{ after } \omega) : x' \not\sqsubseteq x$ where $x \in \text{POMSET}(L_o) \cup \{\delta\}$.

Definition 22 (Blocking because of an output) *Let $i, t \in \text{IOLES}(L)$ and $\omega \in \text{POMSET}(L)$, we have*

$$\mathbf{blocks}_{\mathcal{O}}(i, t, \omega) \Leftrightarrow \text{out}(\perp_i \text{ after } \omega) \not\gg^- \text{out}(\perp_t \text{ after } \omega)$$

Example 18 *Consider the implementation i_7 , the test case t_4 presented in Figure 17 and let $\omega'_1 = (?login \cdot !us_data \cdot ?plane)$. We have that the test execution blocks after ω'_1 because the implementation produces a $!p_full$ action (which leads to a quiescent configuration) and the test case is not able to accept it, i.e. $!p_full \in \text{out}(\perp_{i_7} \text{ after } \omega'_1)$, but $\forall x \in \text{out}(\perp_{t_4} \text{ after } \omega'_1) : x \not\sqsubseteq !p_full$, and finally $\mathbf{blocks}_{\mathcal{O}}(i_7, t_4, \omega'_1)$. If we consider $\omega'_2 = (?login \cdot !us_data \cdot ?insurance)$, the test execution also blocks, because the $!ins_price$ action proposed by the implementation (leading to a quiescent configuration) is enabled in the test case. However, the reached configuration is not quiescent because $!ins_data$ is still enabled, i.e. $!ins_price \in \text{out}(\perp_{i_7} \text{ after } \omega'_2)$, but $\text{out}(\perp_{t_4} \text{ after } \omega'_2) =$*

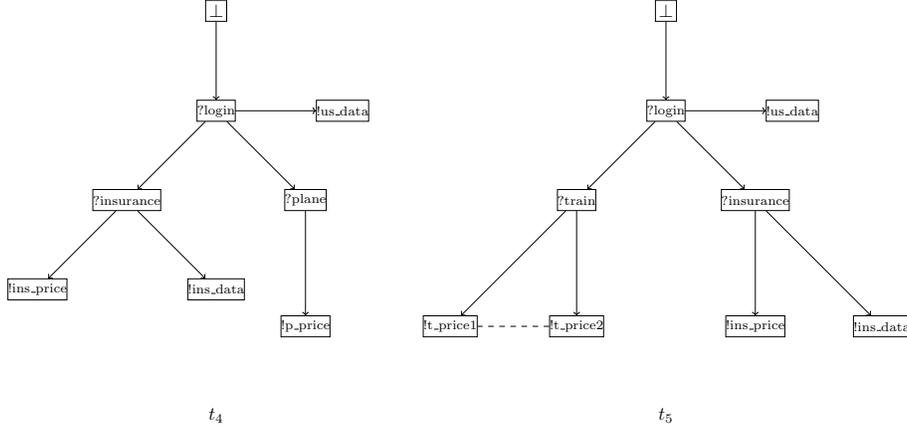


Figure 17: Two test cases for the travel agency in Figure 4

$\{!ins_price \text{ co } !ins_data\}$ and $!ins_price \not\sqsubseteq !ins_price \text{ co } !ins_data$. Finally $\mathbf{blocks}_{\mathcal{O}}(i_7, t_4, \omega'_2)$.

Blocking because of an output can be also be caused by extra quiescence. Consider the implementation i_2 and the test case t_4 . We have that the test execution blocks after $?login$ because the implementation reaches a quiescent configuration, i.e. $\delta \in out(\perp_{i_2} \text{ after } ?login)$, but δ is not observable in the test case, i.e. $\delta \notin out(\perp_{t_4} \text{ after } ?login)$, and $\mathbf{blocks}_{\mathcal{O}}(i_2, t_4, ?login)$. The same holds for i_8 and we have $\mathbf{blocks}_{\mathcal{O}}(i_8, t_4, ?login)$.

The second blocking situation occurs when the test case proposes a concurrent complete set of inputs that the implementation is not prepared to accept, but as the implementation can add some causality, we should also consider the inputs that will become enabled after producing some outputs, i.e. $\exists ?\omega \in poss(\perp_t \text{ after } \omega) : cc(?\omega, \perp_t \text{ after } \omega) \wedge \forall ?\omega' \in poss(\perp_i \text{ after } \omega) : ?\omega \not\sqsubseteq ?\omega'$.

Definition 23 (Blocking because of an input) *Let $i, t \in \mathcal{IOLES}(L)$ and $\omega \in \mathcal{POMSET}(L)$, we have*

$$\mathbf{blocks}_{\mathcal{I}}(i, t, \omega) \Leftrightarrow poss(\perp_t \text{ after } \omega) \not\gg^+ poss(\perp_i \text{ after } \omega)$$

Example 19 *Consider implementation i_5 and test case t_5 of Figure 17, the test execution blocks after logging in because $?insurance \text{ co } ?train \in poss(\perp_{t_5} \text{ after } ?login)$, but the implementation is not able to accept it (neither one of its refinements), i.e. $\forall ?\omega \in poss(\perp_{i_5} \text{ after } ?login) : ?insurance \text{ co } ?train \not\sqsubseteq ?\omega$, and $\mathbf{blocks}_{\mathcal{I}}(i_5, t_5, ?login)$. If we consider i_6 as the implementation, the test execution also blocks because neither the $?insurance \text{ co } ?train$ input action nor its refinements are possible in the implementation and $\mathbf{blocks}_{\mathcal{I}}(i_6, t_5, ?login)$.*

We can now define the verdict of the executions of a set of test cases with an implementation.

Definition 24 (Failure of a test suite) *Let i be an implementation, and T a test suite, we have:*

$$i \text{ fails } T \Leftrightarrow \exists t \in T, \omega \in \text{traces}(t) : \mathbf{blocks}_{\mathcal{O}}(i, t, \omega) \vee \mathbf{blocks}_{\mathcal{I}}(i, t, \omega)$$

If the implementation does not fail the test suite, it passes it, denoted by i passes T .

Example 20 *Let $T = \{t_4, t_5\}$ from Figure 17. We have seen in section 4 several situations that lead to the non conformance of an implementation. As seen in Example 18, the execution of the test case t_4 with the (non conforming) implementations i_2, i_7, i_8 leads to a blocking, so we have i_2, i_7, i_8 **fails** T . We saw in Example 19 that the test executions between the implementations i_5, i_6 and the test case t_5 block after logging in, therefore we also have i_5, i_6 **fails** T . We can conclude that T is capable of detecting the non conforming implementations presented in the last section. We can easily check that the (correct) implementations i_1, i_3, i_4 pass T .*

5.3 Completeness of the Test Suite

We saw in Example 20 that all the possible situations seen in Section 4 that may lead to the non conformance of the implementation are detected by the test suite $\{t_4, t_5\}$. When testing implementations, we intend to reject all, and nothing but, non conformant implementations. A test suite which rejects only non conformant implementations is called *sound*, while a test suite that accepts only conformant implementations is called *exhaustive*. A test suite may not be sound if it contains a test case which is too strict: for instance, a test case containing two weakly concurrent events which would accept only implementations where these events are concurrent, thus rejecting those ordering the events, even though they are correct w.r.t **co-ioco**. In other words, a sound test suite does not produce false negatives. Conversely, a test suite will not be exhaustive if it is too loose and accepts incorrect implementations. A sound and exhaustive test suite is called *complete*.

Definition 25 (Properties of test suites) *Let s be a specification and T a test suite, then*

$$\begin{aligned} T \text{ is sound} &\triangleq \forall i : i \text{ fails } T \text{ implies } \neg(i \text{ co-ioco } s) \\ T \text{ is exhaustive} &\triangleq \forall i : i \text{ fails } T \text{ if } \neg(i \text{ co-ioco } s) \\ T \text{ is complete} &\triangleq \forall i : i \text{ fails } T \text{ iff } \neg(i \text{ co-ioco } s) \end{aligned}$$

The following theorem gives sufficient conditions for having a sound test suite.

Theorem 1 *Let $s \in \mathcal{IOLES}(L)$ and T a test suite such that*

$$a) \forall t \in T : \text{traces}(t) \subseteq \text{traces}(s)$$

- b) $\forall t \in T, \omega \in \text{traces}(t) : \text{out}(\perp_s \text{ after } \omega) \subseteq \text{out}(\perp_t \text{ after } \omega)$
c) $\forall t \in T, \omega \in \text{traces}(t) : \text{cc}(\omega, \perp_t \text{ after } \omega) \Rightarrow \text{cc}(\omega, \perp_s \text{ after } \omega)$

then T is sound for s w.r.t **co-ioco**.

Notice that the trace inclusion required in a) ensures that any possible input in the test case is also possible in the specification.

Proof 2 T is sound for s w.r.t. **co-ioco** iff for every implementation i that fails the test suite, we have that it does not conform to the specification. We assume i fails T and by Definition 24 we have:

$$\exists t \in T, \omega \in \text{traces}(t) : \mathbf{blocks}_{\mathcal{O}}(i, t, \omega) \vee \mathbf{blocks}_{\mathcal{I}}(i, t, \omega)$$

and at least one of the following cases holds:

1. the test execution blocks after ω because of an output produced by the implementation:

$$\begin{aligned} & \exists \omega \in \text{traces}(t) : \mathbf{blocks}_{\mathcal{O}}(i, t, \omega) \\ \text{implies} & \quad \{ * \text{ Definition 22 } * \} \\ & \exists \omega \in \text{traces}(t) : \text{out}(\perp_i \text{ after } \omega) \not\gg^- \text{out}(\perp_t \text{ after } \omega) \\ \text{implies} & \quad \{ * \text{ Definition 19 } * \} \\ & \exists \omega \in \text{traces}(s) : \exists x \in \text{out}(\perp_i \text{ after } \omega) : \\ & \forall x' \in \text{out}(\perp_t \text{ after } \omega) : x' \not\sqsubseteq x \\ \text{implies} & \quad \{ * \text{ Assumptions a) and b) } * \} \\ & \exists t \in T, \omega \in \text{traces}(t) : \exists x \in \text{out}(\perp_i \text{ after } \omega) : \\ & \forall x' \in \text{out}(\perp_s \text{ after } \omega) : x' \not\sqsubseteq x \\ \text{implies} & \quad \{ * \text{ Definition 19 } * \} \\ & \exists \omega \in \text{traces}(s) : \text{out}(\perp_i \text{ after } \omega) \not\gg^- \text{out}(\perp_s \text{ after } \omega) \\ \text{implies} & \quad \{ * \text{ Definition 20 } * \} \\ & \neg(i \text{ co-ioco } s) \end{aligned}$$

2. the test execution blocks after ω because of an input proposed by the test case:

$$\begin{aligned} & \exists \omega \in \text{traces}(t) : \mathbf{blocks}_{\mathcal{I}}(i, t, \omega) \\ \text{implies} & \quad \{ * \text{ Definition 23 } * \} \\ & \exists \omega \in \text{traces}(t) : \text{poss}(\perp_t \text{ after } \omega) \not\gg^+ \text{poss}(\perp_i \text{ after } \omega) \\ \text{implies} & \quad \{ * \text{ Definition 18 } * \} \\ & \exists \omega \in \text{traces}(t) : \exists ?\omega \in \text{poss}(\perp_t \text{ after } \omega) : \\ & \text{cc}(\omega, \perp_t \text{ after } \omega) \wedge \forall ?\omega' \in \text{poss}(\perp_i \text{ after } \omega) : !\omega \not\sqsubseteq !\omega' \\ \text{implies} & \quad \{ * \text{ Assumptions a) and c) } * \} \\ & \exists \omega \in \text{traces}(s) : \exists ?\omega \in \text{poss}(\perp_s \text{ after } \omega) : \\ & \text{cc}(\omega, \perp_s \text{ after } \omega) \wedge \forall ?\omega' \in \text{poss}(\perp_i \text{ after } \omega) : !\omega \not\sqsubseteq !\omega' \\ \text{implies} & \quad \{ * \text{ Definition 18 } * \} \\ & \exists \omega \in \text{traces}(s) : \text{poss}(\perp_s \text{ after } \omega) \not\gg^+ \text{poss}(\perp_i \text{ after } \omega) \\ \text{implies} & \quad \{ * \text{ Definition 20 } * \} \\ & \neg(i \text{ co-ioco } s) \end{aligned}$$

We can easily see that the test suite $\{t_4, t_5\}$ proposed in Figure 17 fulfills the three properties of Theorem 1 and thus is sound w.r.t the specification s .

The following theorem gives the sufficient conditions for the exhaustiveness of a test suite.

Theorem 2 *Let $s \in \text{IOLES}(L)$ and T a test suite such that*

- a) $\forall \omega \in \text{traces}(s) : \exists t \in T : \omega \in \text{traces}(t)$
- b) $\forall t \in T, \omega \in \text{traces}(t) : \text{out}(\perp_t \text{ after } \omega) \subseteq \text{out}(\perp_s \text{ after } \omega)$
- c) $\forall t \in T, \omega \in \text{traces}(t) : \text{cc}(\omega, \perp_s \text{ after } \omega) \Rightarrow \text{cc}(\omega, \perp_t \text{ after } \omega)$

*then T is exhaustive for s w.r.t **co-ioco**.*

Proof 3 *We need to prove that if i does not conform to s then i **fails** T . We assume $\neg(i \text{ co-ioco } s)$, then at least one of the following two cases holds:*

1. *The implementation does not conform to the specification because an output produced by the implementation does not refine any specified output:*

$$\begin{aligned}
& \exists \omega \in \text{traces}(s) : \text{out}(\perp_i \text{ after } \omega) \not\gg^- \text{out}(\perp_s \text{ after } \omega) \\
\text{implies } & \{ * \text{ Definition 19 } * \} \\
& \exists \omega \in \text{traces}(s) : \exists x \in \text{out}(\perp_i \text{ after } \omega) : \\
& \forall x' \in \text{out}(\perp_s \text{ after } \omega) : x' \not\sqsubseteq x \\
\text{implies } & \{ * \text{ Assumptions a) and b) } * \} \\
& \exists t \in T, \omega \in \text{traces}(t) : \exists x \in \text{out}(\perp_i \text{ after } \omega) : \\
& \forall x' \in \text{out}(\perp_t \text{ after } \omega) : x' \not\sqsubseteq x \\
\text{implies } & \{ * \text{ Definition 19 } * \} \\
& \exists t \in T, \omega \in \text{traces}(t) : \text{out}(\perp_i \text{ after } \omega) \not\gg^- \text{out}(\perp_t \text{ after } \omega) \\
\text{implies } & \{ * \text{ Definition 22 } * \} \\
& \exists t \in T, \omega \in \text{traces}(t) : \text{blocks}_{\mathcal{O}}(i, t, \omega) \\
\text{implies } & \{ * \text{ Definition 24 } * \} \\
& i \text{ fails } T
\end{aligned}$$

2. *The implementation does not conform to the specification because an input from the specification is not possible in the implementation (neither its*

refinements):

$$\begin{array}{l}
\exists \omega \in \text{traces}(s) : \text{poss}(\perp_s \text{ after } \omega) \ggg^+ \text{poss}(\perp_i \text{ after } \omega) \\
\text{implies } \{ * \text{ Definition 18 } * \} \\
\exists \omega \in \text{traces}(s) : \exists ?\omega \in \text{poss}(\perp_s \text{ after } \omega) : \\
cc(?\omega, \perp_s \text{ after } \omega) \wedge \forall ?\omega' \in \text{poss}(\perp_i \text{ after } \omega) : !\omega \not\sqsubseteq !\omega' \\
\text{implies } \{ * \text{ by Assumption b) we can find } t \text{ such that } cc(?\omega, \perp_t \text{ after } \omega) \\
\text{ and by Assumption a) } ?\omega \in \text{poss}(\perp_t \text{ after } \omega) * \} \\
\exists t \in T, \omega \in \text{traces}(t) : \exists ?\omega \in \text{poss}(\perp_t \text{ after } \omega) : \\
cc(?\omega, \perp_t \text{ after } \omega) \wedge \forall ?\omega' \in \text{poss}(\perp_i \text{ after } \omega) : !\omega \not\sqsubseteq !\omega' \\
\text{implies } \{ * \text{ Definition 18 } * \} \\
\exists t \in T, \omega \in \text{traces}(t) : \text{poss}(\perp_t \text{ after } \omega) \ggg^+ \text{poss}(\perp_i \text{ after } \omega) \\
\text{implies } \{ * \text{ Definition 23 } * \} \\
\exists t \in T, \omega \in \text{traces}(t) : \mathbf{blocks}_{\mathcal{I}}(i, t, \omega) \\
\text{implies } \{ * \text{ Definition 24 } * \} \\
i \text{ fails } T
\end{array}$$

We can see that the test suite $\{t_4, t_5\}$ from Figure 17 also fulfills the conditions of Theorem 2, therefore it is exhaustive and thus complete.

While sufficient conditions for soundness and exhaustiveness of test suites have been given, we need more: in practice, only a finite number of test cases can be executed; hence we need a method to select a finite set of relevant test cases covering as many behaviors as possible (thus finding as many anomalies as possible). The behavior of the system described by the specification consists usually of infinite traces. However, in practice, these long traces can be considered as a sequence of (finite) “basic” behaviors. Any “complex” behavior is built from such basic behaviors. A criterion allowing to cover each basic behavior described by the specification once is presented in [27] using a proper notion of complete prefixes [39].

6 Test Derivation

We have seen sufficient conditions to ensure the completeness of a test suite. In this section we will explain how to construct a test suite that fulfills such conditions.

6.1 An Algorithm to Construct a Complete Test Suite

We know recall the algorithm to build a test suite in the **ioco** setting and explain the main differences with our test derivation algorithm. In addition we prove that the test suite obtained is complete w.r.t **co-ioco** and analyze the complexity of our approach.

Test Derivation for LTS [38]. In the **ioco** theory, the behavior of a test case is described by a (finite) tree with verdicts (**pass/fail**) in the leaves where

in each internal node either one specific input action can occur (also any possible output is accepted), or all outputs together with the special action θ can occur. The special label $\theta \notin L \cup \{\delta\}$ is used in a test case to detect quiescent states of an implementation, so it can be thought of as the communicating counterpart of a δ -action.

The test cases are denoted using a process-algebraic notation: “;” denotes action prefix and “+” denotes choice. Moreover, for S a set of states, S **after** a denotes the set of states which can be reached from any state in S via action a . Let S be a non-empty set of states, with initially $S = \{s_0\}$. Then a test case t is obtained from S by a finite number of recursive applications of one of the following three nondeterministic choices:

1. (* terminate the test case *)

$$t := \mathbf{pass}$$

2. (* give a next input to the implementation *)

$$\begin{aligned} t := & a; t_a \\ & + \{x; \mathbf{fail} \mid x \in L_{\mathcal{O}}, x \notin \text{out}(S)\} \\ & + \{x; t_x \mid x \in L_{\mathcal{O}}, x \in \text{out}(S)\} \end{aligned}$$

where $a \in L_{\mathcal{I}}$ such that S **after** $a \neq \emptyset$, t_a is obtained recursively by applying the algorithm for S **after** a , and for each $x \in \text{out}(S)$, t_x is obtained by recursively applying the algorithm for the set of states S **after** x .

3. (* check the next output of the implementation *)

$$\begin{aligned} t := & \{x; \mathbf{fail} \mid x \in L_{\mathcal{O}}, x \notin \text{out}(S)\} \\ & + \{\theta; \mathbf{fail} \mid \delta \notin \text{out}(S)\} \\ & + \{x; t_x \mid x \in L_{\mathcal{O}}, x \in \text{out}(S)\} \\ & + \{\theta; t_\theta \mid \delta \in \text{out}(S)\} \end{aligned}$$

where t_x and t_θ are obtained by recursively applying the algorithm for S **after** x and S **after** δ respectively.

Test Derivation for IOLES. The basic idea of our algorithm is to divide the specification into behaviors triggered by incompatible inputs, that are prefixes of the specification (with a particular property that we call input choice free, to be defined below), and then to build test cases from finite prefixes of these event structures.

We explained in the last section the reason to avoid immediate conflict between input events in a test case. Hence we start by dividing the specification in prefixes in a way that any choice between inputs is represented by one of those prefixes. We call such prefixes *input choice free*.

Definition 26 (Input choice free IOLES) *Let $\mathcal{E} = (E, \leq, \#, \lambda) \in \mathcal{IOLES}(L)$, we have*

$$\mathcal{E} \text{ is input choice free} \Leftrightarrow (E^{\mathcal{I}} \times E^{\mathcal{I}}) \cap \overline{\#} = \emptyset$$

The algorithm below builds an input choice free IOLES by removing silent actions and resolving immediate conflicts between inputs, while accepting several branches in case of conflict between outputs (note that “mixed” immediate conflicts between inputs and outputs have been ruled out by Assumption 4) and conserving concurrency. At the end of the algorithm, all input conflicts have been resolved in one way, following one fixed strategy of resolution of immediate input conflicts. Such a strategy can be represented as a linearization of the causality relation that specifies in which order the events are selected by the algorithm. In order to cover the other branches, the algorithm must be run several times with *different* conflict resolution schemes, i.e. different linearizations, to obtain a test suite that represents every possible event in at least one test case.

Definition 27 (Linearization of a partial order) *Consider $\mathcal{E} = (E, \leq, \#, \lambda) \in \mathcal{IOLES}(L)$. A total order \mathcal{R} over E is a linearization of \leq if for all $e, e' \in E$ we have that $e \leq e'$ implies $e\mathcal{R}e'$.*

The choice of such linearization is analogous to the non deterministic choice of the next input to give to the implementation in the algorithm above (point 2.). Such algorithm builds the test case in a way it accepts any output the implementation may produce (points 2. and 3.) returning a **pass** verdict if the output was specified and a **fail** one if not. Contrary to this, we build a test case that only allow to accept those outputs that were specified. Finally, this algorithm allows to chose for termination (point 1.) while the termination of our algorithm is given by the finiteness of the IOLES that is given as an input to the algorithm (see Theorem 3).

Given a deterministic specification that satisfies Assumption 4 and a linearization of its causality relation, Algorithm 1 constructs an input choice free prefix of the specification as can be seen in Example 21. It is worthy to notice that the algorithm does not terminate if the event structure is infinite. However, as it can be seen in Theorem 3, the algorithm is only applied to finite IOLES. A parameter can be added to stop the algorithm at a given depth of the specification, customized by the user as it is done in [27].

As it is explained above, we need to be sure that the collection of linearizations that we use considers all resolutions of immediate input conflicts, i.e. is rich enough to provide, for any given immediate input conflict, a pair of linearizations that reverses the order on that pair.

Definition 28 *Fix $\mathcal{E} \in \mathcal{IOLES}(L)$, and let \mathcal{L} be a set of linearizations of \leq . Then \mathcal{L} is an immediate input conflict saturated set (or iics set) for \mathcal{E} iff for all $e_1, e_2 \in E^{\mathcal{I}}$ such that $e_1 \overline{\#} e_2$, there exist $\mathcal{R}_1, \mathcal{R}_2 \in \mathcal{L}$ such that $e_1 \mathcal{R}_1 e_2$ and $e_2 \mathcal{R}_2 e_1$.*

Algorithm 1 Calculate an input choice free prefix of a given event structure

Require: $s = (E, \leq, \#, \lambda) \in \text{IOLES}(L) : \forall e \in E_s^{\mathcal{I}}, e' \in E_s^{\mathcal{O}} : \neg(e \overline{\#}_s e')$, a linearization \mathcal{R} of \leq

Ensure: An input choice free prefix of s

```

1:  $E_p := \emptyset$ 
2:  $E_{temp} := E$ 
3: while  $E_{temp} \neq \emptyset$  do
4:    $e_m := \min_{\mathcal{R}}(E_{temp})$  /* the minimum always exists as  $\mathcal{R}$  is total and finite */
5:    $E_{temp} := E_{temp} \setminus \{e_m\}$ 
6:   if  $(\{e_m\} \times E_p^{\mathcal{I}}) \cap \# = \emptyset \wedge ([e_m] \setminus E^\tau) \subseteq E_p \wedge \lambda(e_m) \neq \tau$  then
7:     /* the current event  $e_m$  is not in conflict with any event of the prefix, it is not a
       silent event and its past (not considering silent events) is already in the prefix */
8:      $E_p := E_p \cup \{e_m\}$ 
9:   end if
10: end while
11:  $\leq_p := \leq \cap (E_p \times E_p)$ 
12:  $\#_p := \# \cap (E_p \times E_p)$ 
13:  $\lambda_p := \lambda|_{E_p}$ 
14: return  $p = (E_p, \leq_p, \#_p, \lambda_p)$ 

```

Proposition 2 Let \mathcal{L} be an iics set for \mathcal{E} and $e \in E$ with $\lambda(e) \neq \tau$. There exists $\mathcal{R} \in \mathcal{L}$ such that e belongs to the set of events of an IOLES p constructed by Algorithm 1 and \mathcal{R} .

Proof 4 Let p be the IOLES constructed by a fix linearization \mathcal{R}_1 . Suppose e is not in p ; then either (i) $e \in E^{\mathcal{I}}$ and $\{e\} \times E_p^{\mathcal{I}} \cap \# \neq \emptyset$ or (ii) $[e \setminus E^\tau] \not\subseteq E_p$. In case (i), there exists $e' \in E_p^{\mathcal{I}}$ such that $e \overline{\#} e'$ and $e' \mathcal{R}_1 e$. As \mathcal{L} is an iics set, we know there exist $\mathcal{R}_2 \in \mathcal{L}$ such that $e \mathcal{R}_2 e'$ and then we can use \mathcal{R}_2 to construct p' with e belonging to its events. If (ii) holds, then there exists $e' \in [e]$ such that $\{e'\} \times E_p^{\mathcal{I}} \cap \# \neq \emptyset$, and the analysis is analogous to the one in (i).

The following result shows how to construct a test case for the specification from an input choice free prefix of it.

Proposition 3 Let p be any input choice free prefix of s . If t is a finite prefix of p , then t is a test case.

Proof 5 Let t be a finite prefix of p . We need to prove that t is deterministic, that there is no immediate conflict between its input events and that it is finite.

1. As p is input choice free, there is no immediate conflict between its input actions. This is also the case in t as it is its prefix.
2. Its finiteness is immediate from the hypothesis.
3. As the specification is deterministic, so it is p and therefore t .

Let $\mathcal{PREFIX}(s)$ be the set of all finite prefixes of s , we show now that Algorithm 1 is general enough to produce a complete test suite from it.

Theorem 3 *From $\mathcal{PREFIX}(s)$ and an iics set \mathcal{L} for s , Algorithm 1 yields a complete test suite T .*

Proof 6 Soundness: *By Theorem 1 we need to prove: (1) the traces of every test case are traces of the specification; (2) the outputs following a trace of the test are at least those specified; (3) any concurrent complete set of possible input in the case case is concurrent complete in the specification. (1) Trace inclusion is immediate since the algorithm only removes silent actions and resolves conflicts. (2) For a test t and a trace $\omega \in \text{traces}(t)$, if an output in $\text{out}(\perp_s \text{ after } \omega)$ is not in $\text{out}(\perp_t \text{ after } \omega)$, it means either that it is in conflict with an input in t , which is impossible by Assumption 4, or that its past is not already in t , which is impossible since ω is a trace of t . (3) As inputs are considered as concurrent complete, if the test case has a concurrent complete possible input that is not concurrent complete in the specification, then either a new input event was introduced (which is not possible as the test case is a prefix of the specification) or because some concurrency had been removed; but this is not possible as only conflicting inputs are removed.*

Exhaustiveness: *By Theorem 2 we need to prove: (1) every trace is represented in at least one test case; (2) the test case do not produce outputs that are not specified; (3) concurrent complete set of inputs of the specification remain as concurrent complete sets in the test case. (1) Clearly, for all $\omega \in \text{traces}(s)$ there exists at least one prefix $c \in \mathcal{PREFIX}(s)$ such that $\omega \in \text{traces}(c)$. By Proposition 2 we can find $\mathcal{R} \in \mathcal{L}$ such that this trace remains in the test case obtain by the algorithm. (2-3) The inclusion of outputs and preservation of concurrent complete sets in immediate since the algorithm do not add events.*

Example 21 *Let $\mathcal{R}_1 = ?login \rightarrow !us_data \rightarrow ?insurance \rightarrow !ins_price \rightarrow !ins_data \rightarrow ?plane \rightarrow !p_price \rightarrow ?train \rightarrow \tau \rightarrow !t_price2 \rightarrow !t_price1$ and $\mathcal{R}_2 = ?login \rightarrow !us_data \rightarrow ?insurance \rightarrow !ins_price \rightarrow !ins_data \rightarrow ?train \rightarrow \tau \rightarrow !t_price2 \rightarrow !t_price1 \rightarrow ?plane \rightarrow !p_price$ two total orders of the events of s . Both \mathcal{R}_1 and \mathcal{R}_2 are linearizations of \leq_s and form an iics set of s . The input choice free prefix t_4 can be obtained by the Algorithm 1 using \mathcal{R}_1 while t_5 is obtain with \mathcal{R}_2 . As s is finite, by Theorem 3 we have that $\{t_4, t_5\}$ is a complete test suite.*

6.2 Constructing an iics Set

The complexity of constructing a complete test suite depends on finding an iics set \mathcal{L} : for a finite prefix of the system, we need one test case for each linearization in \mathcal{L} . We present an upper bound for the size of \mathcal{L} and discuss informally how to improve it.

Consider linearizations \mathcal{R}_1 and $\mathcal{R}_3 = ?login \rightarrow ?plane \rightarrow !p_price \rightarrow ?train \rightarrow \tau \rightarrow !t_price2 \rightarrow !t_price1 \rightarrow ?insurance \rightarrow !ins_price \rightarrow !ins_data \rightarrow$

!us_data. We can easily see that some events of them commute, however, Algorithm 1 constructs t_4 whichever of them we use. We have seen that some commutations produce differences test cases (as it is the case of \mathcal{R}_2 and t_5). The concept of partial commutation was introduced by Mazurkiewicz [40] where he defines a *trace* as a congruence of a word (or sequence) modulo identities of the form $ab = ba$ for some pairs of letters.

Let Σ be a finite alphabet (its elements are called letters) and $I \subseteq \Sigma \times \Sigma$ a symmetric and irreflexive relation called *independence* or *commutation*. The complement of I is called the *dependance* relation D . The relation I induces an equivalence relation \equiv_I over Σ^* . Two words x and y are equivalent ($x \equiv_I y$) if there exists a sequence z_1, \dots, z_k of words such that $x = z_1, y = z_k$ and for all $1 \leq i \leq k$ there exists words z'_i, z''_i and letters a_i, b_i satisfying

$$z_i = z'_i a_i b_i z''_i, \quad z_{i+1} = z'_i b_i a_i z''_i, \quad \text{and } (a_i, b_i) \in I$$

Thus, two words are equivalent by \equiv_I if one can be obtained from the other by successive commutation of neighboring independent letters.

For a word $x \in \Sigma^*$ the equivalence class of x under \equiv_I is defined as $[x]_I \triangleq \{y \in \Sigma^* \mid x \equiv_I y\}$.

Example 22 Consider $\Sigma = \{a, b, c, d\}$ and $I = \{(a, d)(d, a)(b, c)(c, d)\}$, we have:

$$[baadcb]_I = \{baadcb, baadbc, badacb, badabc, bdaacb, bdaabc\}$$

As explained above, several linearizations of the causality relation build the same test case, therefore they can be seen as equivalents under some relation and we only need one representative for each class. It is shown in [41] that every (Mazurkiewicz's) trace has an unique normal form (every trace in the equivalence class has the same one) and an algorithm is given to construct it.

We have seen than the order between concurrent events or output events in immediate conflict do not change the test cases constructed by Algorithm 1, but immediate conflict between inputs and causality do. We propose the following independence relation:

$$I_s \triangleq (E \times E) \setminus (\leq \cup (\overline{\#} \cap E^{\mathcal{I}} \times E^{\mathcal{I}}))$$

Example 23 Consider system s_5 from Figure 18 and $e_2, e_3, e_4 \in E^{\mathcal{I}}$. The dependance relation contains all the pairs of events that are related either by causality or input immediate conflict. Now consider $\mathcal{R} = \perp e_1 e_2 e_8 e_3 e_6 e_4 e_5 e_7$ and $\mathcal{R}' = \perp e_1 e_8 e_2 e_5 e_3 e_6 e_4 e_7$ two linearizations of \leq_s . The Foata normal form of both \mathcal{R}_1 and \mathcal{R}_2 is $(\perp)(e_1)(e_2)(e_3)(e_4)(e_5 e_6 e_7 e_8)$, meaning that the order of e_5, e_6, e_7, e_8 is not really important for the constructing of the test case. For any linearization of \leq_{s_5} , its normal form is one of the followings:

$$\begin{aligned} \mathcal{R}_1 &= (\perp)(e_1)(e_2)(e_3)(e_4)(e_5 e_6 e_7 e_8) & \mathcal{R}_2 &= (\perp)(e_1)(e_2)(e_4)(e_3)(e_5 e_6 e_7 e_8) \\ \mathcal{R}_3 &= (\perp)(e_1)(e_3)(e_2)(e_4)(e_5 e_6 e_7 e_8) & \mathcal{R}_4 &= (\perp)(e_1)(e_3)(e_4)(e_2)(e_5 e_6 e_7 e_8) \\ \mathcal{R}_5 &= (\perp)(e_1)(e_4)(e_2)(e_3)(e_5 e_6 e_7 e_8) & \mathcal{R}_6 &= (\perp)(e_1)(e_4)(e_3)(e_2)(e_5 e_6 e_7 e_8) \end{aligned}$$

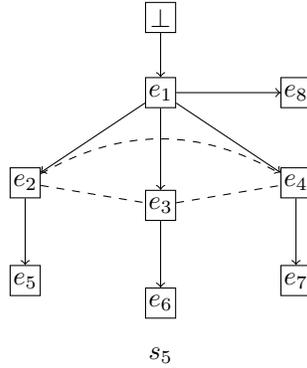


Figure 18: An IOLES with three inputs in immediate conflict

For constructing a test case, we can consider only the normal form of all the possible linearizations (one representative per equivalence class) and therefore the cardinality of the test suite is bounded by the number of equivalence classes under \equiv_{I_s} which is $2^{\mathcal{K}}$, where $\mathcal{K} = |\# \cap (E^{\mathcal{I}} \times E^{\mathcal{I}})|$.

However, linearizations \mathcal{R}_1 and \mathcal{R}_2 lead to the same test case (the same happens for $\mathcal{R}_3, \mathcal{R}_4$ and $\mathcal{R}_5, \mathcal{R}_6$). This is due to the fact that once we add an input event to the test case, all the other inputs that are in immediate conflict with it will not be added, and their order is irrelevant. In the example above, linearizations $\mathcal{R}_1, \mathcal{R}_3$ and \mathcal{R}_5 construct a complete test suite.

7 Conclusion and Future Work

We have presented a formal framework for conformance testing over *concurrent* systems whose behavior is given in the form of labeled event structures. Two possible interpretations for concurrency are presented, weak and strong concurrency, which can both be present in the same IOLES specification. Along with the definition of the conformance relation **co-ioco** designed for such specifications, we have defined test cases and test executions, and proposed a test case generation algorithm able to produce a complete test suite. This continues the work of [26, 27].

Future technical studies include the questions whether it is possible to handle the non-determinism of the specification, and to drop Assumption 4 that avoids conflicts between inputs and outputs. One way to avoid making such assumptions would be to assume a fair scheduler. Otherwise, controllability of test cases must be ensured during their construction [34], and the linearizations that are needed to build the test cases should not only reverse the order between conflicting inputs, but also between conflicting inputs and outputs.

All notions of this article are defined in terms of events structures, which is the semantic model for several formalisms. However, real specifications are usually given in one of these *generator* formalisms, such as Petri nets or net-

works of automata, rather than as event structures. Our approach therefore needs to come on top of an *unfolding* mechanism that generates event structure semantics. Already in [27], an algorithm for building test cases is given based on an unfolding algorithm. An implementation of this algorithm and the one presented in this article is planned based on the MOLE tool [42], which builds a complete finite prefix of the unfolding of a net.

Another important dimension to be explored is *distribution* of observation and of testing. The **dioco** and associated relations studied by Hierons et al. [19, 43] allow to link the conformance of *local* observations to the *global* conformance of the SUT. There, the underlying specification is a multi-port IOTS; by contrast, we shall be studying multi-component, concurrent systems with local observation, and distributed test suites to be developed. As another line of work, [44] studies different ways of globally and locally testing a distributed system specified with Message Sequence Charts, by defining global and local conformance relations, for which exhaustive test sets are built. Moreover, conditions under which local testing is equivalent to global testing are set. However, this work considers trace semantics. We are currently working on a generalization of those ideas.

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