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# Delta: Scalable Data Dissemination under Capacity Constraints

Konstantinos Karanasos, Asterios Katsifodimos, Ioana Manolescu

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## Delta: Scalable Data Dissemination under Capacity Constraints

Konstantinos Karanasos\*, Asterios Katsifodimos†, Ioana Manolescu†

Project-Team Oak

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**Abstract:** In content-based publish-subscribe (pub/sub) systems, users express their interests as queries over a stream of publications. Scaling up content-based pub/sub to very large numbers of subscriptions is challenging: users are interested in low *latency*, that is, getting subscription results fast, while the pub/sub system provider is mostly interested in *scaling*, i.e., being able to serve large numbers of subscribers, with low *computational resources utilization*.

We present a novel approach for scalable content-based pub/sub in the presence of constraints on the available CPU and network resources, implemented within our pub/sub system Delta. We achieve scalability by off-loading some subscriptions from the pub/sub server, and leveraging view-based query rewriting to feed these subscriptions from the data accumulated in others. Our main contribution is a novel algorithm for organizing views in a multi-level dissemination network, exploiting view-based rewriting and powerful linear programming capabilities to scale to many views, respect capacity constraints, and minimize latency. The efficiency and effectiveness of our algorithm are confirmed through extensive experiments and a large deployment in a WAN.

**Key-words:** Web data, publish/subscribe, materialized views, query optimization, data management.

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## **Delta: Dissémination de Données en Présence de Contraintes**

**Résumé :** Dans des systèmes d'abonnements basés sur le contenu, les utilisateurs expriment leurs intérêts par des requêtes sur les flux de publications. Le passage à l'échelle des systèmes d'abonnements pose de nombreux problèmes de performance: les utilisateurs sont intéressés par la fraîcheur des données, c'est à dire, obtenir les résultats de leurs abonnements le plus vite possible, tandis que les fournisseurs du système sont surtout intéressés par le passage à l'échelle, c'est à dire, être capable de répondre à de grands nombres d'utilisateurs tout en utilisant peu de ressources système.

Nous décrivons une nouvelle approche de dissémination de données dans un système d'abonnements, en présence de contraintes sur les ressources CPU et réseau disponibles; cette approche est mise en oeuvre dans le cadre de notre plateforme Delta. Le passage à l'échelle est obtenu en déchargeant le fournisseur de données de l'effort de répondre à une partie des abonnements; en échange, nous tirons profit de techniques de re-écriture de requêtes à l'aide de vues afin de propager les données de ces abonnements à partir d'autres abonnements. Notre contribution principale est un nouvel algorithme qui organise les vues dans un réseau de dissémination d'information sur plusieurs niveaux, qui s'appuie sur la re-écriture à base de vues ainsi que sur des techniques puissantes de programmation linéaire afin de passer à l'échelle pour de grands nombres de vues, respecter les contraintes de capacité du système, et minimiser les délais de propagation des informations. L'efficacité et la performance de notre algorithme est confirmée par notre évaluation expérimentale, qui inclut l'étude d'un déploiement réel dans un réseau WAN.

**Mots-clés :** Données du web, systèmes d'abonnements, vues matérialisées, optimisation des requêtes, gestion des données.

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## 1 Motivation and Outline

Publish/subscribe (*pub/sub*, in short) is a popular model for disseminating content to large numbers of distributed subscribers. The literature distinguishes *topic-based* pub/sub, where users subscribe to a set of predefined topics, from *content-based* pub/sub, where users express their subscriptions as custom complex-structured queries on the published data. Topic-based pub/sub offer better scalability at the expense of subscription expressiveness, while in more complex systems, the increased expressive power of content-based pub/sub makes it preferable. For instance, within a large company ACME, “*senior positions representing ACME in Singapore*” should be pushed to the senior staff which may be interested, while “*sales seminar in Singapore*” interests the sales department plus the administrative staff that must make the travel arrangements.

Pub/sub subscribers are interested in *low latency*, that is, getting all the results to their subscriptions, as soon as possible after the data is published. The *publisher* of a pub/sub system faces several performance challenges in order to meet subscriber requirements. The first is matching published items against the set of subscriptions, a CPU-intensive task. Then, the publisher’s outgoing bandwidth is another physical limitation, as more and more updates must be sent to the interested subscribers. Third, the speed of the network connecting the publisher to the subscribers imposes a lower bound on the dissemination latency.

Both centralized and distributed approaches have been proposed to address the above issues, while aiming at latency minimization. The centralized ones [6, 9] mostly rely on efficient filtering algorithms for matching the data against subscriptions. However, for more expressive and numerous subscriptions, subscription matching remains an onerous task. To this end, distributed pub/sub systems have been proposed [10, 15, 25, 31], providing solutions for serving thousands or millions of subscribers with minimum resources utilization and low latency. In most cases, they focus on distributed filtering and design overlay networks in the form of logical multicast trees. Those trees are formed by specialized nodes, called *brokers*, able to efficiently filter and move the data from the publisher to the subscribers, or by the subscribers themselves. Nevertheless, as the amount of subscribers and data increases, the publisher’s (or broker’s) resource capacity becomes insufficient.

**Problem Statement** To overcome the above resource constraints, we allow the subscribers to *take part in the dissemination of data* (i.e. serve other subscribers that have similar interests) in order to offload the data publisher. Due to their similarity of interests, the subscribers can form a logical overlay network, over which subscription results can flow from the data publisher to the subscribers. Since subscribers have to use their resources to serve others, the problem we consider is how to (i) minimize the total resource utilization (e.g., CPU and bandwidth), while (ii) keeping the subscription latency as low as possible, and (iii) respecting the given resource capacity constraints.

The key idea on which we build our approach is that subscriptions often overlap, completely or partially, when user interests are close. In such a case, results of several subscriptions can be combined to compute the results of other subscriptions. For instance, from the subscriptions  $s_1$ : “*open positions in Asia*” and  $s_2$ : “*open positions in Sales*”, one can compute  $s_3$ : “*open Sales positions in Asia*” by joining  $s_1$  and  $s_2$ .

**Rewriting Subscriptions** More formally, a subscription can be *rewritten based on other subscriptions*, by filtering their results, e.g., through classic database selections and projections, combining them through joins, etc. For instance, rewriting and serving  $s_3$  based on  $s_1$  and  $s_2$  instead of the publisher, relieves the publisher from the effort of computing  $s_3$  against the published data, and saves bandwidth between the publisher and the site of  $s_3$ . At the same time, rewriting  $s_3$  from  $s_1$  and  $s_2$  incurs computations to the sites of  $s_1$ ,  $s_2$  and/or  $s_3$  to evaluate the rewriting, and also bandwidth consumption from the sites of  $s_1$  and  $s_2$ , to the site of  $s_3$ . Notice that if we consider subscriptions as queries (or views), deciding how to serve a subscription based on others, can be turned to a problem of *view-based query rewriting*, which has been extensively studied in the database literature (e.g. [26, 23]).

**Multi-level Subscriptions** Moving a subscription from being served directly by the publisher (we



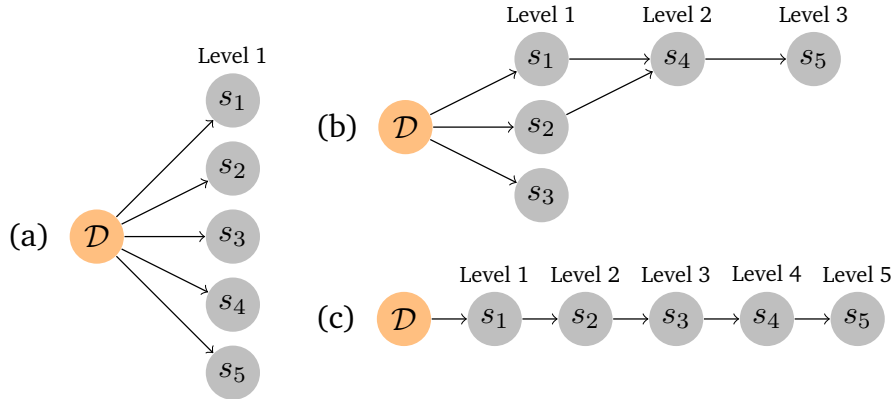


Figure 1: Sample dissemination networks.

call this a *level 1* subscription), to being served from other subscriptions by rewriting (we call this a *level 2*, *level 3* subscription, etc.), changes the data transfer and processing paths, with many possible consequences on subscription latency and resources utilization for data dissemination.

For illustration, Figure 1 shows three possible dissemination networks. At left (a), there is only one level and all subscriptions are filled from the publisher  $\mathcal{D}$ . The data paths from  $\mathcal{D}$  to all subscriptions are as short as possible, however all the load is on  $\mathcal{D}$ . At (b), the subscription  $s_5$  gets its data from  $s_4$  instead of the publisher, while  $s_4$  results are computed based on  $s_1$  and  $s_2$ . At (c), only  $s_1$  is filled from  $\mathcal{D}$ , while  $s_2$  gets data from  $s_1$ ,  $s_3$  from  $s_2$ , etc. The load on the publisher is minimal, but the four hops from  $\mathcal{D}$  to  $s_5$ , increase the latency of this subscription

More generally, dissemination effort decreases at the publisher, at the expense of subscribers joining this effort. A less-loaded publisher will likely match data against the rest of the subscriptions faster, which may reduce the total latency for all the subscriptions. However, moving a subscription to a higher level lengthens the data path from the publisher to that subscription, which may increase its latency. Finally, pushing some processing at the subscribers require taking into account a new set of capacity constraints, since subscriber resources should be sparingly used, to keep the respective sites willing to participate in the system.

**Contributions and Outline** Given a set  $S$  of subscriptions and a data publisher  $\mathcal{D}$ , we term *configuration* a choice for each subscription  $s \in S$  of filling  $s$  either (i) directly from  $\mathcal{D}$  or (ii) by rewriting  $s$  over some other  $S$  subscriptions and thus computing  $s$  results from these other subscriptions' results. The *cost* of a configuration is a weighted sum of the resource utilization and subscription latencies incurred by the configuration. This work makes the following contributions:

- We show how to model the problem of finding a minimum-cost configuration under some resource capacity constraints as a graph problem, related to the known Degree-bounded Arborescence problem [1], but departing from it through our interest in minimizing both resource utilization and latency. As we will explain, resource utilization and latency differ in fundamental ways, making existing solutions inapplicable in our setting.
- Based on this insight, we provide a novel two-step algorithm for selecting a configuration. First, we employ an Integer Linear Programming (ILP) approach to find a resource utilization-optimal solution (ignoring latency); second, we provide a latency optimization algorithm which starts from the configuration found by the ILP solver and modifies it to reduce latency.
- We have implemented all our algorithms and performed extensive experiments, including a deployment of Delta on a significant-size pub/sub scenario on a WAN. Our experiments demonstrate the efficiency and effectiveness of our algorithms and the practical interest of multi-level subscriptions in large data dissemination networks.

This report is organized as follows. Section 2 introduces our problem and presents its graph-based formalization. Section 3 describes our algorithms for selecting an efficient configuration, based on the graph models previously introduced. Section 4 details our view-based approach for rewriting subscriptions based on other subscriptions, given the large number of subscribers. Section 5 describes our experiments, we then discuss related works and conclude.

## 2 Problem Model

We now describe our multi-level subscription problem model.

Let  $\mathcal{D}$  denote a data source publishing a set of data items  $i_1, i_2, \dots$  and  $S = \{s_1, s_2, \dots, s_n\}$  be a finite set of subscriptions, each defined by a query and established on some network site. The semantics of a subscription  $s$  defined by query  $q_s$  and issued at site  $n_s$  is that  $s$  must receive the results of  $q_s(i)$  for any data item  $i$  published by the data source  $\mathcal{D}$  after  $s$  was created. From now on, for simplicity, whenever possible we will simply use  $s$  to denote both a subscription and the query defining it.

At the core of our work is the observation that it may be possible to compute results of a subscription out of the results of others. We say subscription  $s$  can be *rewritten* based on subscriptions  $s_1, s_2, \dots, s_k$ , if there exists a query  $r$ , which, evaluated over the results of  $s_1, s_2, \dots, s_k$ , produces exactly the results of subscription  $s$ , regardless of the actual data items published by  $\mathcal{D}$ :  $r(s_1(\mathcal{D}), s_2(\mathcal{D}), \dots, s_k(\mathcal{D})) = s(\mathcal{D})$  for any  $\mathcal{D}$ , or more simply,  $r(s_1, s_2, \dots, s_k) \equiv s$ , where  $\equiv$  denotes query equivalence.

**Subscriptions = Views** Observe that we are interested in complete rewritings, that is, we assume that  $r$  can either rely completely on the data source, or on the results of other subscriptions  $s_1, s_2, \dots, s_k$ . This is because our goal is to off-load subscriptions from the data source and serve them solely from other subscriptions instead. In turn, a subscription  $s$  rewritten based on  $s_1, \dots, s_k$  as above, may be used to rewrite another subscription  $s'$ . This shows that every subscription may be considered as a (materialized) view, based on which to rewrite the others. Thus, from now on, for conciseness, we will simply use *view* to designate a subscription.

In the sequel, we introduce the central concepts and data structures of our work. We define rewritability graphs (RGs) and configurations in Section 2.1. Section 2.2 presents the basic metrics we use to gauge the interest of a configuration, namely utilization and latency, and shows how to incorporate load balancing in the discussion under the form of constraints over the configurations. Based on these notions, Section 2.3 formalizes our problem statement.

### 2.1 Rewritability Graph (RG)

A rewritability graph (RG) indicates which views can be rewritten based on other views. Its simplest representation is an AND-OR rewritability graph as in, e.g., [16]. For each view  $v$  at site  $s$ , there is a corresponding node in the AND-OR graph (if the same  $v$  is declared at  $n$  distinct sites  $s_1, s_2, \dots, s_n$ , there are  $n$  corresponding nodes in the graph). Moreover, for every view set  $v_1, v_2, \dots, v_k$ , based on which  $v$  can be equivalently rewritten, there exists a  $\wedge$  (AND) node  $a_v$  such that: (i) each of the nodes corresponding to  $v_1, v_2, \dots, v_k$  points to  $a_v$ , and (ii)  $a_v$  points to the  $v$  node. If  $v$  can be rewritten based on several view sets, there will be one  $\wedge$  node pointing to  $v$  for each such rewriting possibility<sup>1</sup>.

A sample RG over seven views is depicted in Figure 2. Each view can always be evaluated directly from the data source  $\mathcal{D}$ , thus, for each view  $v$ , there is a  $\wedge$  node through which  $\mathcal{D}$  is connected to  $v$ . Further, in Figure 2,  $v_2$  and  $v_3$  can be used to rewrite  $v_5$ , as shown by the lower  $\wedge$  node pointing to  $v_5$ ;  $v_3$  and  $v_4$  can be used to rewrite  $v_6$ , etc. Observe that there may be cycles in the RG:  $v_6$  can be used to rewrite  $v_7$  and vice versa. This entails that  $v_6$  and  $v_7$  are equivalent.

Formally, given a view set  $S$ , an RG is a directed graph, defined by the pair  $(V \cup \{\mathcal{D}\} \cup A, E)$ , such that:

- $V \cup \{\mathcal{D}\} \cup A$  is the set of nodes:
  - For each view  $s_i \in S$ , there exists a corresponding node  $v_i \in V$ .
  - $\mathcal{D}$  is the node corresponding to the data source.

<sup>1</sup>To keep the AND-OR graph shape, one would have needed to use a  $\vee$  node pointing to  $v$  and have the  $\wedge$  nodes pointing to that  $\vee$  node instead of  $v$  directly. We omit the  $\vee$  nodes for simplicity.

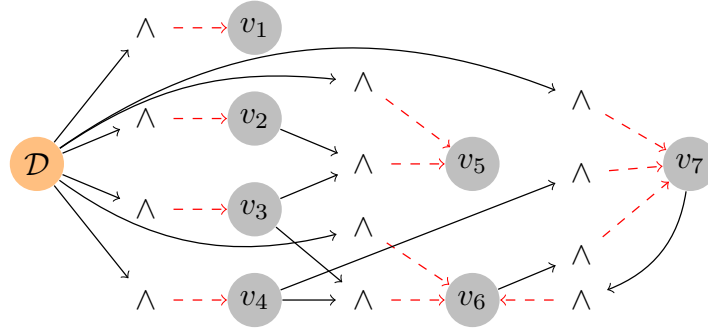


Figure 2: Rewritability Graph (RG).

- $A$  is the set of  $\wedge$  nodes, each of which represents a rewriting of a view  $s \in S$  based on a set of other views  $\{s_1, s_2, \dots, s_k\} \subseteq S \setminus \{s\}$ .
- $E \subseteq ((V \cup \{\mathcal{D}\}) \times A) \cup (A \times V)$  is the set of directed edges that connect the graph's nodes as follows:
  - $V$  nodes (as well as  $\mathcal{D}$ ) can only point to  $A$  nodes, while  $A$  nodes can only point to  $V$  nodes.
  - Each node  $a \in A$  has an indegree of at least one, and an outdegree equal to one.
  - For each view  $v \in V$ , there exists a  $\wedge$  node  $a_v \in A$  such that (i)  $\mathcal{D} \rightarrow a_v \rightarrow v$  and (ii)  $\mathcal{D}$  is the only node pointing to  $a_v$ .
  - For each view set  $\{s_1, s_2, \dots, s_k\}$  based on which another view  $s$  can be rewritten, there exists a  $\wedge$  node  $a_v \in A$  such that the edges  $(v_1, a_v), (v_2, a_v), \dots, (v_k, a_v), (a_v, v) \in E$ .

**Size of RG** The number of nodes in an RG is  $|V| + |A| + 1$  (where 1 corresponds to  $\mathcal{D}$ ). We have  $|V| = |S|$ , which is the number of views (subscriptions). As for the  $A$  nodes, there is one for every  $V$  node  $v$ , connecting  $\mathcal{D}$  to  $v$  (thus,  $|S|$  such  $A$  nodes). Moreover, we have one  $A$  node for every view set that can rewrite a view  $v$ . Since there are  $|S| - 1$  views that can be used to rewrite  $v$  (we exclude  $v$  itself), we can have at most  $2^{|S|-1}$  such  $A$  nodes for  $v$ . Thus, we have  $|A| \leq |S| \times (2^{|S|-1} + 1)$ .

We now turn to the number of edges. Since by definition the outdegree of each  $A$  node is one, there are  $|A|$  edges from  $A$  to  $V$  nodes. Furthermore, an  $A$  node has at most  $|S| - 1$  incoming edges (a rewriting can involve at most that many views), leading to at most  $|A| \times (|S| - 1)$  edges from  $V$  to  $A$  nodes. Hence, we have  $|E| \leq |S|^2 \times (2^{|S|-1} + 1) \approx |S|^2 \times 2^{|S|}$ .

Clearly, an RG may be very large when there are many views. Therefore, it is also of interest to develop *partial rewritability graphs*, each of which can be seen as the RG from which some  $\wedge$  nodes (and their corresponding input and output edges) have been erased.

**Configuration (CFG)** Given an RG, a configuration (CFG) is a subgraph of RG encapsulating a concrete choice of how to rewrite every view  $v \in V$ . Specifically, in a configuration, only a single  $\wedge$  node points to each view. Moreover, there exists a directed path from  $\mathcal{D}$  to each view of the RG<sup>2</sup>.

Formally, given an RG  $rg = (V \cup \{\mathcal{D}\} \cup A, E)$ , a CFG  $cfg = (V \cup \{\mathcal{D}\} \cup A', E')$  is a subgraph of  $rg$  such that:

- $A' \subseteq A$  and  $E' \subseteq E$ ;
- for any  $v \in V$ , there exists exactly one  $a \in A'$  such that  $a \rightarrow v$ ;
- there exists a path from  $\mathcal{D}$  to any view  $v \in V$ ;

<sup>2</sup>This also guarantees that a configuration is acyclic.

- for each node  $a \in A'$ , if edge  $(v_i, a) \in E$  (for each  $v_i \in V$ ), then  $(v_i, a) \in E'$ .

The last point in the above definition guarantees that when we select an  $A$  node to be included in  $cfg$ , we also select all its incoming edges that constitute the rewriting. Observe that a CFG completely specifies the paths along which data is disseminated to all the subscribers. Moreover, multiple data dissemination paths starting from the source  $\mathcal{D}$  may meet, for instance, when two views  $v_1$  and  $v_2$ , together, rewrite another view  $v_3$ .

The number of CFGs which may be derived from an RG is  $\prod_{v \in V} (in(v))$  where  $in$  denotes the indegree of a view node. It follows from the RG size estimations that the upper bound for the number of CFGs is  $|S|^{2|S|}$ , which is extremely high.

## 2.2 Characteristics of a Configuration

We now discuss how to quantify the cost of a CFG.

For each rewriting ( $\wedge$ ) node in a CFG, there can be several ways of distributing the effort entailed by the rewriting (typically selections and joins) across the network nodes in which the views reside. For example, consider the views  $v_2, v_3$  and  $v_5$  of Figure 2. Assume that  $v_2$  resides on site  $n_2$ ,  $v_3$  on  $n_3$  and  $v_5$  on  $n_5$ . To join  $v_2$  and  $v_3$ , they could both be shipped to the site  $n_5$  and joined there. Alternatively,  $v_3$  could be shipped to  $n_2$ , the join could be evaluated at  $n_2$  and the results shipped to  $n_5$ , at a different resources utilization. More generally, the utilization incurred by the operations of a  $\wedge$  node depend on the operations' types and ordering, where each operation runs etc.

**Distributed Resources Utilization** To estimate the resources *utilization* of a given  $\wedge$  node, we quantify the resources (e.g., I/O, CPU, bandwidth) needed for its execution over the various sites.

Let  $N$  be the set of network sites on which work can be distributed (we assume for simplicity  $N$  is the set of all the sites having subscriptions), and  $k$  be the number of distinct resources considered for each site, such as: I/O at that site, CPU, incoming and outgoing bandwidth, etc. Let  $P_\wedge$  be the set of all physical plans for a given  $\wedge$  node. We define the utilization function  $u : P_\wedge \rightarrow \mathbb{R}^{|N| \times k}$ , assigning to each plan  $p \in P_\wedge$ , the estimated resources utilization, along different resource dimensions, entailed by the evaluation of  $p$ . Observe that each result of  $u$  is a matrix stating the consumption along each dimension and at each site.

To enable comparing utilizations, we rely on a single *utilization aggregator*  $\mathcal{U} : \mathbb{R}^{|N| \times k} \rightarrow \mathbb{R}$ , which combines the utilization of all the different resource components of the sites involved in the execution of a plan, and returns a single (real) number. The aggregator may for instance sums up all the utilization components, possibly assigning them various weights depending on the metric and/or the site involved. In the sequel, for a plan  $p \in P_\wedge$ , we will simply write  $\mathcal{U}(p)$  to denote the scalar aggregation  $\mathcal{U}(u(p))$  of  $p$ 's multidimensional utilization.

Finally, for a given  $\wedge$  node  $a \in A$ , we denote by  $\mathcal{U}(a)$  the smallest value of  $\mathcal{U}(p)$ , over all the plans  $p \in P_\wedge$ . Moreover, the utilization of a CFG  $cfg = (V \cup \{\mathcal{D}\} \cup A', E')$  is:

$$\mathcal{U}(cfg) = \sum_{a \in A'} \mathcal{U}(a).$$

**Latency** In a CFG, given a data item  $i$  and subscription  $v$  such that  $v(i) \neq \emptyset$ , the data dissemination *latency* of  $v$  with respect to  $i$ , denoted  $\lambda(v, i)$ , is the time interval between the publication of  $i$  and the moment when  $v(i)$  reaches the site of  $v$ . In the sequel, we may simply use  $\lambda(v)$  to denote  $v$ 's latency.

Clearly,  $\lambda(v)$  is determined by the paths in CFG followed by the data that is moving from  $\mathcal{D}$  to  $v$ . Each  $\wedge$  node  $a$  encountered along these paths adds to the latency its contribution, which we term *local latency* of  $a$ . That reflects the delays introduced on the propagation of data in the rewriting graph, by evaluating that rewriting. For instance, if the best physical plan for a  $\wedge$  node requires shipping data across the network from  $n_1$  to  $n_2$  and performing a join at  $n_2$ , the local latency of this node will reflect the data transfer and the processing time in the join. We assume available a *local latency estimation function*  $l$ , which estimates the local latency introduced by  $a$ . We stress

that  $l(a)$  characterizes only the operations at the rewriting node  $a$ , and not the behaviour of its input(s).

Given that for every subscription  $v$  there is a single  $\wedge$  node  $a_v$  pointing to  $v$  (see RG definition, Section 2.1),  $v$ 's latency is equal to the *total latency* of  $a_v$  (denoted  $\lambda(a_v)$ ), thus  $\lambda(v) = \lambda(a_v)$ . This latency can be computed by adding  $a_v$ 's local latency  $l(a_v)$  to the maximum latency of the subscriptions  $\{v_i\}$  that are inputs to  $a_v$ . Denoting by  $v_i \rightarrow a_v$  the fact that node  $v_i$  points to  $a_v$  in the RG, we have:

$$\lambda(a_v) = \lambda(v) = \max_{v_i \rightarrow a_v} (\{\lambda(v_i)\}) + l(a_v)$$

Note that the latency of  $\mathcal{D}$  is defined as 0. We also define the latency of a CFG  $cfg = (V \cup \{\mathcal{D}\} \cup A', E')$  as follows:

$$\lambda(cfg) = \sum_{v \in V} \lambda(v).$$

**Cost** We define the cost of a  $\wedge$  node  $a$  in a CFG as a linear combination of its utilization and latency:

$$\mathcal{C}(a) = \alpha \times \mathcal{U}(a) + \beta \times \lambda(a)$$

where  $\alpha$  and  $\beta$  are coefficients controlling the importance given to the utilization and latency. A high  $\alpha$  prioritizes solutions of low utilization, incurring a low consumption of resources across the network, while a high  $\beta$  prefers solutions having a low latency, favoring quick dissemination of data to the subscribers. Finally, we define the cost of a CFG  $cfg = (V \cup \{\mathcal{D}\} \cup A', E')$ :

$$\mathcal{C}(cfg) = \sum_{a \in A'} \mathcal{C}(a).$$

**Constraints** In practice, resources such as CPU, memory, incoming and outgoing network bandwidth, are limited on each site. This has to be taken into account when deciding whether to use a view  $v_1$  to feed another view  $v_2$  with data, since doing so incurs some consumption of resources on the site of  $v_1$ : such resource consumption should be kept within the capacity limits. Each site may have different such *capacity constraints*, according, for instance, to its specific infrastructure or available bandwidth.

We make the simplifying assumption that there is a single view published in each network site. We model capacity constraints by a single integer  $B_v^{out}$ , which is the maximum number of views that can be served by  $v$  (and which coincides with the maximum number of views served by a network site, since there is one view per site), and design our algorithms to operate within these constraints. This can be easily extended to more (and more complex) constraints. For more complex cases where more than one view can reside at a network site, we refer the reader to the Appendix.

### 2.3 Problem Statement

Given an RG  $rg = (V \cup \{\mathcal{D}\} \cup A, E)$ , a cost function  $\mathcal{C}$ , a limit  $B_v^{out}$  for each  $v \in V$ , as well as a limit  $B_{\mathcal{D}}^{out}$  for the data source, the problem we address is to find a CFG  $cfg = (V \cup \{\mathcal{D}\} \cup A', E')$ , such that:

1. Capacity constraints are respected:

$$\forall v \in V \cup \{\mathcal{D}\}, \text{out}(v) \leq B_v^{out}$$

where  $\text{out}(v)$  denotes the outdegree of node  $v$  in the CFG;

2. The cost of CFG  $\mathcal{C}(cfg)$  is minimized.

### 3 Configuration Selection

We now describe our approach for selecting a low-cost configuration. We start by discussing RG construction in Section 3.1. Section 3.2 provides an overview of the CFG selection, a two-step process described in detail in Section 3.3 and 3.4, respectively. Section 3.5 shows how we treat with CFG updates (view addition/removal).

#### 3.1 Rewritability Graph Generation

Given a set of views, we show how to construct the corresponding RG, modelling the ways to rewrite views based on other views.

**Naive RG Generation** Assume we initially create a graph that contains the nodes ( $V \cup \{\mathcal{D}\}$ ), as well as the  $\wedge$  nodes that are needed to connect  $\mathcal{D}$  with each view  $v \in V$  (along with the corresponding edges). Based on this graph, the most direct way of building the RG is by calling the view-based rewriting algorithm exhaustively, and adding, each time a rewriting is found, the corresponding  $\wedge$  nodes and edges. This simple method requires calling the rewriting algorithm  $|V|$  times, using each time  $|V| - 1$  views. Given the typically high complexity of view-based query rewriting algorithms, this method is unlikely to scale to large problems. Moreover, even if we optimize the calls to the rewriting algorithm (e.g., by reducing the number of views we use as input each time, as discussed in Section 4), the resulting *complete* RG is usually too dense, hampering in turn the process of choosing a CFG from RG.

**Partial RG Generation** In the interest of efficiency, one can limit the search performed during each call to the rewriting algorithm to at most  $k$  rewritings. In other words, we only consider the first (at most)  $k$  alternative ways we find to rewrite a given query. Clearly, the internals of the rewriting algorithm affect the order in which rewritings are explored and, thus, the first  $k$  rewritings found; we will revisit this issue in Section 4. Algorithm 1 outlines the construction of the partial RG, obtained through this limited exploration of rewritings. When a view cannot be rewritten based on the others, Algorithm 1 connects it directly to the data source  $\mathcal{D}$ .

#### 3.2 Configuration Selection Overview

We now turn to the problem of selecting out of a (possibly partial) RG, a CFG that minimizes the cost as a weighted sum of *utilization* and *latency*, under *capacity constraints* (as per our problem

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##### Algorithm 1: Partial RG Generation

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```

Input : View set  $V$ , maximum number  $k$  of rewritings per view
Output: RG of  $V$  with at most  $k$  rewritings per view
// RG initially contains only  $V$  and  $\mathcal{D}$ 
1  $A \leftarrow \emptyset, E \leftarrow \emptyset, G \leftarrow (V \cup \{\mathcal{D}\} \cup A, E)$ 
2 foreach  $v \in V$  do
3    $rewrNo \leftarrow 0$ 
4   while  $hasNextRewriting(v, V \setminus \{v\})$  and  $(rewrNo < k)$  do
5     // Get next rewriting
6      $rw \leftarrow nextRewriting(v, V \setminus \{v\})$ 
7      $A \leftarrow A \cup \{rw\}$  // Add rewriting ( $\wedge$ ) node  $rw$ 
8      $E \leftarrow E \cup \{(u_i, rw)\}, \forall u_i \in rw$  // Add edges to  $rw$ 
9      $E \leftarrow E \cup \{(rw, v)\}$  // Add edges to  $v$ 
10     $rewrNo++$ 
// All views are also fed by  $\mathcal{D}$ 
11  $E \leftarrow E \cup \{(\mathcal{D}, u)\}, \forall u \in V$ 
12 return  $G$ 

```

---

statement in Section 2.3).

**Complexity and Relationship with Known Problems** We now discuss how our problem relates to already studied graph problems.

First, consider *resources utilization optimization alone*, that is, ignore the latency and capacity constraints. This simplified problem can be solved in linear time, by selecting for each view  $v$  in an RG, the lowest resources utilization  $\wedge$  node pointing to  $v$ , together with the corresponding edge and the  $\wedge$  node's incoming edges.

Now assume given bounds on the number of views that can be fed (i) from  $\mathcal{D}$  and (ii) from each view, and consider the problem of finding a CFG that respects these *capacity constraints*, *without considering the cost*. This version of the problem is more complex than the previous one, as choosing  $\wedge$  nodes is no longer a local decision for each view  $v$  in the RG: selecting an  $\wedge$  node can break the capacity constraints of any of the nodes that are serving it.

This last problem of selecting a CFG under capacity constraints is largely connected to the problem of finding a *Degree-bounded Arborescence* (DBA, for short) in a given graph. An arborescence is a spanning tree of a directed graph rooted at a given root node. Although efficient, polynomial-time algorithms have been proposed for solving the *Minimum Cost Arborescence* problem [12], finding a DBA is NP-hard [1]; the NP-hardness is due to the fact that, in order to respect the degree bounds, the edge-selection decisions cannot be local. We have shown that the DBA problem can be reduced in polynomial time to finding a capacity-constrained CFG, which is already a specialization of the general problem we consider (Section 2.3), since it does not take into account the cost. This gives the following proposition:

**Proposition 3.1.** *Finding a minimum-cost CFG under capacity constraints is NP-hard.*

*Proof.* To show that a problem  $\Pi$  is NP-hard, it suffices to show that there exists another NP-hard problem  $\Pi'$  that can be reduced in polynomial time to problem  $\Pi$ . This can be done with the *proof by restriction* [13]: to show that  $\Pi$  is NP-hard, we can simply show that the NP-hard problem  $\Pi'$  is a special case of  $\Pi$ .

We first recall the definition of the Degree-bounded Arborescence (DBA) problem (which is known to be NP-hard [1]), then introduce a specialization of the general problem we consider (we term this specialization *SCFG*). Finally, we show that finding a DBA can be reduced to the problem of finding an SCFG.

*The Degree-bounded Arborescence Problem (DBA).* Let  $G = (V \cup \{\mathcal{D}\}, E)$  be a directed graph with root  $\mathcal{D}$ , and let  $B_v^{out}$  be the bounds on the out-degree of each vertex  $v \in V$ . The DBA problem consists of finding an (out-)arborescence starting from  $\mathcal{D}$  that satisfies the degree bounds, or declare that no such arborescence exists (if that is the case). Since in an arborescence each vertex except the root has an in-degree of exactly one, the DBA problem does not consider bounds on the in-degree.

We now show that we can specialize the problem of finding a capacity-constrained CFG so that it coincides with the Degree-bounded Arborescence Problem. This can be done by restricting  $\wedge$  nodes in an RG to have *only one incoming node* and by *ignoring the resources utilization and latency of the selected CFGs*. We formalize this specialization of our problem below.

*The Specialized CFG Problem (SCFG).* Let  $G = (V \cup A \cup \{\mathcal{D}\}, E)$  be an RG with root  $\mathcal{D}$ , and let  $B_v^{out}$  be the bounds on the out-degree of each vertex  $v \in V \cup \{\mathcal{D}\}$ . Each  $a \in A$  is allowed to have only one input edge. The goal of the SCFG problem is to find a feasible SCFG rooted at  $\mathcal{D}$  that respects the bounds  $B_v^{out}$ , or declare that it is unfeasible.

First, it is easy to see that the SCFG problem is a specialization of the original problem presented in Section 2.3, since: (i) it ignores the cost of the CFGs (resource utilization and latency), and (ii) it restricts all  $\wedge$  nodes  $a \in A$  to have exactly one input edge. Interestingly, this last restriction allows only for CFGs in which each subscription is fed by another single subscription, as opposed to the more general problem we are tackling (Section 2.3), in which subscriptions can be combined (joined) in order to feed other subscriptions.

Second, an SCFG is an arborescence, since:



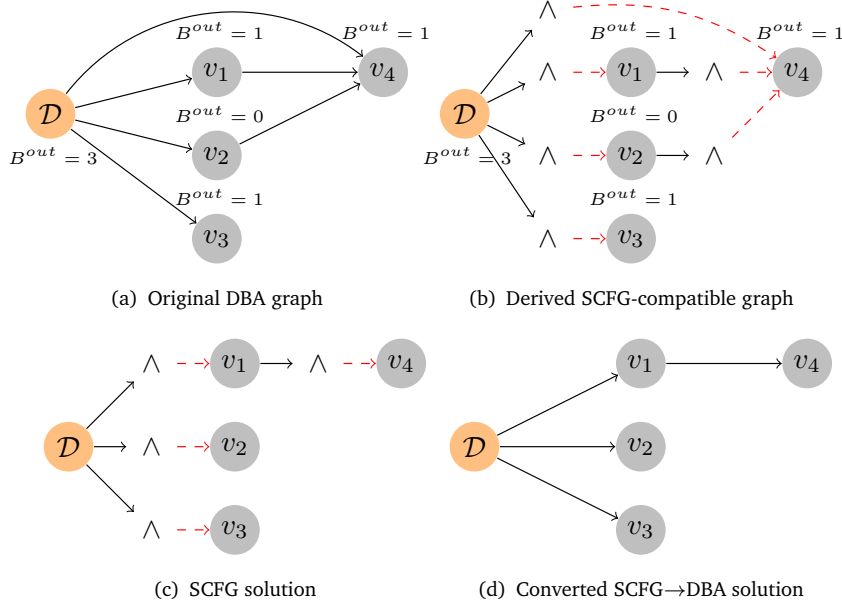


Figure 3: Solving a DBA instance by converting it into an SCFG.

- all views are reachable from the publisher (or root)  $\mathcal{D}$ ;
- there is exactly one  $\wedge$  node that points to each view node  $v \in V$ ;
- each  $\wedge$  node has exactly one input and one output edge.

Since an SCFG is an arborescence, the next question is whether the DBA problem can be solved with an SCFG solver. If this is possible, and transformations between DBA and SCFG graphs can be done in polynomial time, then the SCFG problem is at least as hard as the DBA problem (thus, NP-hard). To answer this question, we will show how to polynomially transform a graph from the DBA format into an SCFG solver-compatible graph (SCFG-compatible graphs contain  $\wedge$  nodes), and polynomially convert the solution that the SCFG solver has produced back to a DBA graph (with no  $\wedge$  nodes).

In order to transform a DBA input into an SCFG solver-compatible input, one has to simply replace each edge of the form  $n_1 \rightarrow n_2$  of the DBA input graph by one edge  $n_1 \rightarrow \wedge$  pointing to a new  $\wedge$  node and a second edge  $\wedge \rightarrow n_2$ . In order to transform an SCFG solution into a DBA solution, one needs to remove the  $\wedge$  nodes from the resulting SCFG and connect the input/output edges of all  $\wedge$  nodes. Since the transformations are straightforward, we omit their formal description and instead illustrate through an example.

Figure 3a shows a graph for which we want to solve the DBA problem. Figure 3b shows a derived SCFG solver-compatible graph. Note that, since all  $\wedge$  nodes in an SCFG graph have only one input and one output, converting simple edges from a DBA graph into edge-node-edge triplets ( $\rightarrow \wedge \rightarrow$ ) and vice versa is straightforward. Figure 3c shows the (only) feasible solution to the SCFG problem that respects the bounds  $B^{out}$  for all views. Finally, Figure 3d shows the conversion of the SCFG solution into a DBA solution, i.e., a Degree-bounded Arborescence. Clearly, both conversions DBA  $\rightarrow$  SCFG and SCFG  $\rightarrow$  DBA can be done in linear time.

Finally, the problem of finding an SCFG  $\in NP$  since a non-deterministic algorithm only needs to guess a solution for a given graph  $G$  and then check in polynomial time whether this solution is indeed an SCFG. To do this, a traversal of the graph is sufficient (linear time).

In this proof we have reduced the NP-hard DBA problem to the SCFG problem, and therefore the SCFG problem is NP-hard. Since the SCFG problem is a specialization of our original problem (Section 2.3), we have shown that our original problem is also NP-hard.  $\square$

Importantly, the latest effective techniques for solving DBA and even more general network design problems, rely on solving linear relaxations of *Integer Linear Programs* [22]. The idea is to use one boolean variable  $x_i$  to encode whether a node (or edge) is part of the solution, and to formulate the total utilization (objective function) as a weighted sum of all the variables, with the weights being the respective node (or edge) utilizations. Such an ILP formulation can be handed to an ILP solver, which takes advantage of advanced techniques that enable it to solve large-size problems corresponding in our context to many views and many rewritings.

**Two-step Optimization Approach** Although our problem (Section 2.3) is naturally expressed as a linear program when one considers capacity constraints and optimizes for utilization (ignoring latency), and can thus be delegated to an ILP solver, it turns out that one cannot rely on an ILP solver to also reduce *latency* (as explained in Section 3.3). Thus, our approach for addressing the problem is organized in two steps:

1. Formulate our optimization problem *considering utilization and constraints only* as a linear program and delegate it to an efficient ILP solver. We describe this next in Section 3.3.
2. Post-process the utilization-optimal configuration returned by the solver (if one exists under the given constraints) to reduce latency in a heuristic fashion, as described in Section 3.4.

### 3.3 CFG Utilization Optimization Through ILP

Integer Linear programming (ILP) is a well-explored branch of mathematical optimizations. A wide class of problems can be expressed as: given a set of linear inequality constraints over a set of variables, find value assignments for the variables, such that a target expression on these variables is minimized. Such problems can be tackled by dedicated *ILP solvers*, some of which are by now extremely efficient, benefiting from many years of research and development efforts. Following the model for directed graphs of [22] (with some changes), we formulate our problem as an integer linear program as follows.

**Variables** For each node  $n \in V \cup \{D\} \cup A$ , we denote by  $E_n^{in}$  and  $E_n^{out}$  the sets of its incoming and respectively outgoing edges. Selecting a CFG amounts to selecting *one way to compute each view*, which is equivalent to selecting for each view  $v$ , one of the  $\wedge$  nodes pointing to  $v$ , or, equivalently, one edge from  $E_v^{in}$ . Thus, for each  $v \in V$  and  $e \in E_v^{in}$ , we introduce a variable  $x_e$ , taking values in the set  $\{0, 1\}$ , denoting whether or not  $e$  is part of the CFG.

**Coefficients** Our problem model attached rewriting evaluation utilization to the rewriting nodes, through the utilization function  $\mathcal{U}$  returning for each  $\wedge$  node  $a \in A$ , the associated utilization  $\mathcal{U}(a)$  which aggregates various types of utilizations (CPU, I/O, network, etc.) Further, as explained in Section 2.2,  $\mathcal{U}(a)$  is the smallest over the utilizations of all physical plans that could be used for this rewriting. To simplify the presentation, and since there is a bijection between  $A$ , the set of  $\wedge$  node sets, and the set of edges entering view nodes, namely  $\cup_{v \in V} E_v^{in}$ , we *move the utilization of each rewriting, to the edge going from the rewriting  $\wedge$  node, to the corresponding rewritten view*. The other edges, in particular all those entering  $\wedge$  nodes, are assumed to have zero utilization. Thus, for each rewriting node  $a \in A$  and edge  $e \in E_a^{out}$  (recall that  $E_a^{out} = \{e\}$ , that is, each  $a$  node has exactly one outgoing edge), we denote by  $\mathcal{U}_e$  the utilization  $\mathcal{U}(a)$ . Our final ingredient is the  $B_v^{out}$  bounds on the views fan-out, introduced in Section 2.2.

**Putting it All Together** Our problem's ILP statement is given in Table 1. Equation (1) states that each  $x_e$  variable takes values in  $\{0, 1\}$ , (2) ensures that every view is fed exactly by one rewriting, (3) states that if the (only) outgoing edge of a  $\wedge$  node is selected, all of its inputs are selected as well, and finally (4) ensures the respect of the  $B_v^{out}$  constraint.

**LP Example** Consider the RG shown at the top of Figure 4, where for illustration we have added to each  $\wedge$  node leading to the view  $v_i$ , the subscript  $i$  and a superscript  $j$  with  $j = 0, 1, \dots$ . For each edge  $(n, m)$  in the RG, where  $n$  and  $m$  are two RG nodes, we introduce a variable  $x_{n \rightarrow m}$  stating whether that edge is part of the chosen configuration. For simplicity, for each node  $\wedge_i^j$  pointing to

$$\begin{aligned}
& \text{Minimize: } \mathcal{U} = \sum_{e \in E} \mathcal{U}_e x_e \\
& \text{subject to:} \\
& x_e \in \{0, 1\} \quad \forall e \in E \quad (1) \\
& \sum_{e \in E_v^{in}} x_e = 1 \quad \forall v \in V \quad (2) \\
& \sum_{e \in E_a^{in}} x_e = x_{E_a^{out}} \times |E_a^{in}| \quad \forall a \in A \quad (3) \\
& \sum_{e \in E_v^{out}} x_e \leq B_v^{out} \quad \forall v \in V \cup \{\mathcal{D}\} \quad (4)
\end{aligned}$$

Table 1: Utilization optimization problem as a linear program.

the view  $v_i$ , we write  $x_i^j$  instead of  $x_{\wedge_i^j \rightarrow v_i}$ . Thus,  $x_i^j$  is a boolean variable whose value 1 indicates that the view  $v_i$  is filled by its rewriting  $\wedge_i^j$ . Moreover, for each  $\wedge_i^j$ , let  $c_i^j$  be the utilization of the processing incurred by that rewriting.

The linear program whose solution is a minimum-utilization CFG for this graph is shown in the lower part of Figure 4. Equation numbers at the left refer to the generic equations in Table 1.

**Non-linearity of Latency** Still on the RG in Figure 4, we now turn to quantifying the latency of each view. Let  $l_i^j$  be the latency of each rewriting  $\wedge_i^j$ ; for simplicity we include therein the impact of all the transfers and processing incurred by the rewriting.

We consider that  $\mathcal{D}$  implements an efficient algorithm allowing it to match *simultaneously* all the subscriptions it serves, against each newly published document. This is the case in state-of-the-art algorithms such as [9], and also in our simpler implementation. Thus, the latency component that is due to *subscription matching at  $\mathcal{D}$*  (as opposed to latency incurred by shipping data from  $\mathcal{D}$  and possibly further processing and shipping of data) is the same for all views, and we ignore it without loss of generality.

Applying our formulas defining latency, we obtain  $\lambda(v_2) = l_2^0$ ,  $\lambda(v_3) = l_3^0$ , since  $v_2$  and  $v_3$  are fed directly from the publisher. Since  $v_1$  can be fed either through  $\wedge_1^0$  or  $\wedge_1^1$ , its latency is:

$$\lambda(v_1) = x_1^0 l_1^0 + x_1^1 (l_1^1 + \max(\lambda(v_2), \lambda(v_3))) = x_1^0 l_1^0 + x_1^1 (l_1^1 + \max(l_2^0, l_3^0))$$

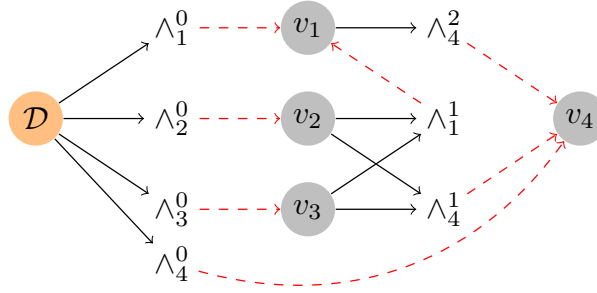
Similarly, given that  $v_3$  can be fed through three different  $\wedge$  nodes, we have:

$$\begin{aligned}
\lambda(v_4) &= x_4^0 l_4^0 + x_4^1 (l_4^1 + \max(\lambda(v_2), \lambda(v_3))) + x_4^2 (l_4^2 + \lambda(v_1)) = \\
& x_4^0 l_4^0 + x_4^1 (l_4^1 + \max(l_2^0, l_3^0)) + x_4^2 (l_4^2 + x_1^0 l_1^0 + x_1^1 (l_1^1 + \max(l_2^0, l_3^0)))
\end{aligned}$$

Observe that the above expression unfolds into a sum having among its terms  $x_4^2 x_1^0 l_1^0$  and  $x_4^2 x_1^1 l_1^1$ , which is *non-linear in the problem's variables  $x_i^j$* ; in contrast, the latencies of  $v_1, v_2$  and  $v_3$  are *linear* combination of these variables. As a consequence, in these examples and in general, *configuration latency cannot be pushed into the ILP objective function*, which only admits linear combinations of variables.

The intuition behind this non-linear behavior is easy to trace on the RG in Figure 4. The variables which end up multiplied correspond to paths of length 2, leading to  $v_4$  through  $v_1$ . If  $x_1^0 = x_4^2 = 1$ ,  $v_1$  is fed from the source and  $v_4$  from  $v_1$ . If  $x_1^1 = x_4^2 = 1$ ,  $v_1$  is fed from  $v_2$  and  $v_3$  and  $v_4$  from  $v_1$ . The multiplication of variables corresponds to the logical conjunction of the edge selection decisions they correspond to.

Concluding this discussion, we will rely on ILP to solve efficiently and exactly the utilization optimization problem, and reduce in a second step the latency of the configuration thus obtained.



Minimize:  $\mathcal{U}_1^0 x_1^0 + \mathcal{U}_1^1 x_1^1 + \mathcal{U}_2^0 x_2^0 + \mathcal{U}_3^0 x_3^0 + \mathcal{U}_4^0 x_4^0 + \mathcal{U}_4^1 x_4^1 + \mathcal{U}_4^2 x_4^2$   
subject to:

eq.(1)	$x_i^j \in \{0, 1\}, \forall i, j$
eq.(2)	$x_1^0 + x_1^1 = 1; x_2^0 = 1; x_3^0 = 1; x_4^0 + x_4^1 + x_4^2 = 1;$
eq.(3)	$x_{\mathcal{D} \rightarrow \wedge_1^0} = x_1^0; x_{\mathcal{D} \rightarrow \wedge_2^0} = x_2^0; x_{\mathcal{D} \rightarrow \wedge_3^0} = x_3^0;$ $x_{\mathcal{D} \rightarrow \wedge_4^0} = x_4^0; x_{v_1 \rightarrow \wedge_4^2} = x_4^2;$ $x_{v_2 \rightarrow \wedge_1^1} + x_{v_3 \rightarrow \wedge_1^1} = 2x_1^1; x_{v_2 \rightarrow \wedge_4^1} + x_{v_3 \rightarrow \wedge_4^1} = 2x_4^1;$
eq.(4)	$x_{v_1 \rightarrow \wedge_4^2} \leq B_{v_1}^{out}; x_{v_2 \rightarrow \wedge_1^1} + x_{v_2 \rightarrow \wedge_4^1} \leq B_{v_2}^{out};$ $x_{v_3 \rightarrow \wedge_1^1} + x_{v_3 \rightarrow \wedge_4^1} \leq B_{v_3}^{out};$ $x_{\mathcal{D} \rightarrow \wedge_1^0} + x_{\mathcal{D} \rightarrow \wedge_2^0} + x_{\mathcal{D} \rightarrow \wedge_3^0} + x_{\mathcal{D} \rightarrow \wedge_4^0} \leq B_{\mathcal{D}}^{out};$

Figure 4: Sample RG and corresponding ILP model.

### 3.4 CFG Latency Optimization

In this second stage, we seek to improve the latency of the CFG obtained by solving the ILP problem (corresponding to the utilization minimization under constraints), by incremental changes on this CFG. We start by introducing a helper notion:

**Impact of a View on CFG Latency** Given a CFG  $cfg$ , we define the *impact* of a view  $v$ , denoted by  $\mathcal{I}(v)$ , as an estimation of  $v$ 's impact on the latency of all of the views that are fed with data by  $v$ , directly or indirectly. Formally:

$$\mathcal{I}(v) = \lambda(v) \times |\text{nodes of } rg \text{ reachable from } v|$$

In the above, we consider that any  $rg$  node reachable from  $v$  is potentially impacted by the latency introduced by  $v$ , and, thus, multiply  $v$ 's latency by the number of such nodes. We also define the impact of a rewriting  $rw_v$  pointing to view  $v$  to be equal to the impact of  $v$ :  $\mathcal{I}(rw_v) = \mathcal{I}(v)$ .

**The LOGA Algorithm** We have devised a Latency Optimization Greedy Algorithm (LOGA, in short), given in Algorithm 2, which incrementally tries to improve the latency of a CFG  $cfg$  obtained from an RG  $rg$ . The algorithm uses the original  $rg$  in order to replace a rewriting in  $cfg$  with another one that leads to a CFG with a globally smaller latency. It initially orders the rewritings of  $cfg$  in descending order of impact, and then tries to replace first the rewritings with the biggest impact. Such replacements are made (i) without violating the  $B^{out}$  bounds, and (ii) without assigning views again to  $\mathcal{D}$ , since the goal of our work is precisely to spread the data dissemination work.

**Incremental Re-computation of Latency** As explained above, a change in the latency of a view  $v$  in a CFG  $cfg$  might affect the latency of every view in  $cfg$  accessible from  $v$ . Therefore, when the latency of  $v$  changes as a consequence of a replacement, LOGA performs a traversal in topological order of the  $cfg$  sub-DAG rooted at  $v$ , to recompute the latency only of the affected views.

**Recomputing Impact of Views** As the CFG changes through rewriting replacements, the number of nodes reachable from any given view node  $v$  must be recomputed. This number is needed in order to update the impact  $\mathcal{I}(v)$ , at line 5 of Algorithm 2. The number of nodes reachable from  $v$

**Algorithm 2:** Latency Optimization Greedy Algorithm (LOGA)

---

```

Input : CFG  $cfg$ , RG  $rg$ 
Output: Latency optimized version of  $cfg$ 
1  $newLat \leftarrow \lambda(cfg)$ 
2 repeat
3    $prevLat \leftarrow \lambda(cfg)$ 
4    $rwList \leftarrow \{rw \in cfg \mid \nexists \text{ edge } (\mathcal{D}, rw)\}$ 
5    $rwList \leftarrow \text{reorder}(rwList)$  in desc. order of interest  $\mathcal{I}(rw)$ 
6   foreach  $rw \in rwList$  do
7      $minLat \leftarrow \lambda(cfg)$ ;  $best_{rw} \leftarrow null$ 
8     // Replace  $rw$  with its latency-optimal alternative (if any)
9     foreach  $rw' \in rg$  s.t.  $rw, rw'$  feed the same view do
10      replace  $rw$  with  $rw'$  in  $cfg$ 
11      if  $(\forall v \in cfg, outdegree(v) \leq B_v^{out})$  and  $(\lambda(cfg) < minLat)$  then
12         $minLat \leftarrow \lambda(cfg)$ 
13         $best_{rw} \leftarrow rw'$ 
14      replace  $rw'$  with  $rw$  in  $cfg$  // leave  $cfg$  intact
15    if  $best_{rw} \neq null$  then
16      replace  $rw$  with  $best_{rw}$  in  $cfg$ 
17       $newLat \leftarrow \lambda(cfg)$ 
17 until  $prevLat = newLat$ 
18 return  $cfg$ 

```

---

is determined by the rewriting opportunities, which in turn depend on the actual views etc. In the worst case this may require a costly traversal of the whole CFG, however, as our experiments show (Section 5), much fewer nodes are traversed and thus this operation is not expensive in practice.

### 3.5 Incremental CFG Computation

Adding a new view  $v$  to an existing configuration  $cfg$ , goes as follows: we compute  $v$ 's rewritings and add them to the existing RG. We then search the RG for a rewriting  $rw$  with the least cost  $\mathcal{C}(rw)$  such that no bounds are violated in  $cfg$ . If such a rewriting  $rw$  exists, we add it to  $cfg$ ; otherwise,  $v$  is assigned to the data source. After a certain number of new subscriptions have been added, or when the data source's are been reached, the solver and LOGA are re-invoked and a full CFG selection takes place.

When a subscription  $v$  is withdrawn or its site fails, the views depending on  $v$ , that is those to whose  $cfg$  rewritings  $v$  contributes, are treated as new and the above incremental process is followed for each of them.

## 4 View-based Rewriting

We now describe the view-based rewriting framework underlying Delta. Section 4.1 presents some preliminary notions on views and rewritings, whereas Section 4.2 describes an auxiliary structure, the embedding graph, which is used for building the RG. Then, Section 4.3 presents our algorithm for efficiently rewriting a subscription (view) based on the others. Its novelty resides in its capability to produce a specified number of solutions, crucial in our setting where not all rewriting opportunities are explored. Finally, Section 4.4 discusses how other view-based rewriting algorithms could substitute ours, to port the Delta architecture in other distributed dissemination contexts.

### 4.1 Views and Rewritings

Since our target applications concern the dissemination of structured text news, and in order to leverage our previous system development [20, 23], we built our system for disseminating XML documents to a network of subscriptions expressed in a rich flavor of XML queries.

Each view is defined by a *tree pattern query* where nodes are labeled with XML element or attribute names, while edges encode parent-child (single) or ancestor-descendant (double) relationships. Unlike XPath 1.0, and close to XPath 2.0 and to simple XQuery for-let-where-return (FLWR) expressions, our tree patterns may return content from multiple nodes.

Node IDs are implemented by virtually all efficient XML engines. Therefore, we include IDs in our views, since, as we have shown in [21], view joins based on such IDs may lead to very efficient rewritings. As a simple example, consider the query  $q$  defined as  $//a[//c]//b$  and the views  $v_1 = //a$ ,  $v_2 = //a_{ID}[//c]$  and  $v_3 = //a_{ID}//b$ , where  $v_2$  and  $v_3$  store IDs for the  $a$  nodes. One can rewrite  $q$  as  $v_2 \bowtie_{a.ID} v_3$ , or alternatively as  $v_1[//c]//b$ . The former is likely to be much more efficient than the latter, because  $v_2$  and  $v_3$  are more selective than  $v_1$ , especially if few  $a$  elements have  $b$  and/or  $c$  descendants.

[23] provides an equivalent view-based rewriting algorithm for this language. Unsurprisingly, this algorithm has high complexity, therefore, it is not applicable in a setting like ours with a very large numbers of views. Therefore, we consider here a sub-language of the one considered in [21, 23] where we assume that *all nodes are annotated with ID*. Moreover, to increase the possibilities of view-based rewriting, we assume *IDs are structural*: by comparing two node IDs one can decide if the node corresponding to the one is a parent/ancestor of the node corresponding to the other. Node IDs are invisible to the user; they are added by the system to the user-issued tree patterns. Storing IDs in subscription data brings a space overhead, but not a very significant one, especially if one relies on space-efficient encodings of such views [35]. Restricting the view language to endow all nodes with *ID* reduces view-based rewriting to a set-cover problem, as we explain shortly below.

**View Embedding** It has been shown [23, 30] that a tree pattern view  $v$  may participate in an equivalent rewriting of another tree pattern view  $q$  only if there exists an embedding  $\phi : v \rightarrow q$  respecting (1) node labels, i.e., for any node  $n \in v$ ,  $label(n) = label(\phi(n))$ , and (2) structural relationships between nodes, that is, for any two nodes  $n, m \in v$ , if  $n$  is a  $/$ -child (resp.,  $//$ -child) of  $m$ , then  $\phi(n)$  is a  $/$ -child (resp., descendant) of  $\phi(m)$ . Finally,  $\phi$  must not contradict value predicates from the query, i.e., for any node  $n \in v$ , such that  $m = \phi(n) \in q$ , if  $m$  is annotated with predicate  $[val = c_1]$  for some constant  $c_1$ , then  $n$  must not be annotated with predicate  $[val = c_2]$  for some constant  $c_2 \neq c_1$ . It follows readily from the above properties of embeddings that:

**Corollary 4.1.** *If a view  $v$  embeds into a query  $q$ , the labels of  $v$  are a subset of the labels of  $q$ .*

**View Coverage** We say that a set of views  $V$  covers a given view  $q$ , iff, for every attribute  $att$  of a node  $n_q \in q$ , there exists a node  $n_v$  belonging to a view  $v \in V$  and an embedding  $\phi : v \rightarrow q$  such that  $\phi(n_v) = n_q$  and  $n_v$  is also annotated with  $att$ . We call such a view set  $V$  an *embedded attribute set cover* (EAC) for  $q$ .

If we restrict the rewriting algorithm [23] to the case when all view nodes are annotated with *ID*, it can be shown that the existence of an EAC  $V$  for  $q$  is a necessary and sufficient condition for

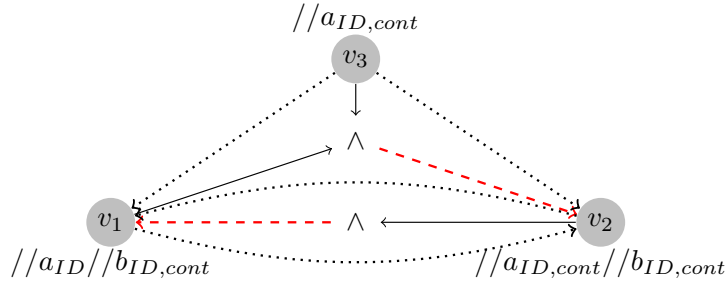


Figure 5: Superposed EG and RG over three views.

an equivalent rewriting of  $q$  based on  $V$  to exist. Indeed, given an EAC  $V$  for  $q$ , the rewriting can be built using structural joins (based on the node IDs) between all the involved views, and adding all required structural predicates (imposing structural relationships present in the query but not in the views), as well as possible value selection predicates still needed. We formalize this as follows:

**Proposition 4.1.** *A query  $q$  can be equivalently rewritten based on a set of views  $V$ , iff  $V$  is an EAC for  $q$ .*

Observe that such a rewriting may be non-minimal; we revisit this issue in Section 4.3.

## 4.2 Embedding Graph (EG)

Given a view set  $V$ , in order to build the corresponding RG, we must solve  $|V|$  view-based rewriting problems, one for each view based on the others. To speed up the rewriting process, we can exploit Proposition 4.1 to attempt to rewrite a given view  $v$ , only using those views that embed into  $v$ . Thus, we are interested in all view pairs  $(v_1, v_2)$  such that  $v_1$  embeds into  $v_2$ . We encode this embedding information in an *embedding graph* (EG, in short), which is a directed graph having a node for each view  $v \in V$  and an edge  $(v_1, v_2)$ , with  $v_1, v_2 \in V$ , iff  $v_1$  embeds in  $v_2$ . Figure 5 depicts a sample EG (view nodes, dotted edges), along with the corresponding RG (view and  $\wedge$  nodes, solid and dashed edges). Next to each view node, we give its view definition. For instance,  $v_3$  embeds in  $v_1$  and  $v_2$  (as shown by the dotted edges).

Testing whether  $v$  embeds into  $v'$  takes at most  $|v| \times |v'|$  operations [23], leading to a total complexity of  $O(|V|^2 \times |v|_{max}^2)$  for creating the EG, where  $|v|_{max}$  is the size of the largest view in  $V$ . Such tests may get quite expensive for large  $V$  sets.

To improve performance, we pre-filter views, based on Corollary 4.1: for  $v$  to embed into  $v'$ , the labels of  $v$  must be among the labels of  $v'$ . We organize the view definitions in a prefix trie specifically designed to support subset queries [18]. Using this trie, given a view  $v$ , we can efficiently identify all the views  $u_i$  such that  $labels(u_i) \subseteq labels(v)$ .

Algorithm 3 shows how to construct an EG given a set of views  $V$ . The algorithm starts by constructing a trie as explained above. Then, it uses the trie as an index to efficiently build the EG: for a given view  $v$ , the trie returns all views whose labels are a subset of  $v$ 's labels. Only the views thus obtained are tested for embedding into  $v$ . Since our pre-filtering has no false negative, Algorithm 3 generates the complete EG.

**EG Cycles and their Consequences** It is possible for two views to embed into each other, as for example  $v_1$  and  $v_2$  in Figure 5, leading to cycles in the EG. In some cases, cycles in the EG lead to cycles in the RG. For instance, in Figure 5, although the EG cycle between  $v_1$  and  $v_2$  does not directly translate to an RG cycle, view  $v_3$  enables some additional rewritings (such as the one represented by the upper  $\wedge$  node), and in turn these lead to an RG cycle (involving  $v_1$ ,  $v_2$  and the two  $\wedge$  edges).

RGs featuring such cycles pose an issue since the ILP solver may return a CFG with cycles, e.g., feeding  $v_1$  from  $v_2$  and  $v_2$  from  $v_1$  in this example, without using the publisher  $\mathcal{D}$  at all. Such

**Algorithm 3:** Trie-based EG Construction Algorithm

---

```

Input : View set  $V$ 
Output: EG of  $V$ 
1  $E \leftarrow \emptyset; EG \leftarrow (V, E)$  // Initially empty edge set
2  $T \leftarrow \text{createTrie}(V)$  // Create the trie for  $V$ 
3 foreach  $v \in V$  do
   | //Retrieve from  $T$  all  $u$  s.t.  $\text{labels}(u) \subseteq \text{labels}(v)$  and add edges corresponding to
   | embeddings
4   foreach  $u \in \{T.\text{lookUp}(v)\}$  do
5   | if  $u$  embeds into  $v$  then  $E \leftarrow E \cup \{(u, v)\}$ 
6 return  $EG$ 

```

---

**Algorithm 4:** Cover-based greedy rewriting (CGR)

---

```

Input : View  $v$ , EG  $eg = (V_{eg}, E_{eg})$ , max. number  $k$  of rewritings
Output: List with at most  $k$  rewritings of  $v$  based on the views of  $eg$ 
// Get from  $eg$  all views embeddable in  $v$ 
1  $V \leftarrow \{u_i \mid (u_i, v) \in E_{eg}\}$ 
2  $rwList \leftarrow \emptyset$  // List with rewritings for  $v$ 
3  $visited \leftarrow \emptyset$  // Set of already visited EACs
4 if  $\exists$  attribute  $att \in v$ , not covered by any  $u \in V$  then return  $\emptyset$ 
5  $crtEAC \leftarrow \emptyset$  // Current EAC view set
6  $\text{backtrackFindEAC}(v, V, crtEAC)$ 
7 return  $rwList$ 
8 Procedure  $\text{backtrackFindEAC}(v, V, crtEAC)$ 
9   if  $crtEAC$  covers all  $v$ 's attributes and  $crtEAC \notin visited$  then
10   |  $visited \leftarrow visited \cup \{crtEAC\}$ 
11   | // Get rewriting from EAC and add to  $rwList$ 
12   |  $rwList.add(\text{EACtoRw}(crtEAC))$ 
13   | if  $(rwList.size = k)$  then return
14   | // Get views not yet used in  $crtEAC$ 
15   |  $remainViews \leftarrow V \setminus crtEAC$ 
16   | if  $remainViews = \emptyset$  then return
17   |  $remainViews \leftarrow \text{sort}(remainViews)$  in desc. order of interest  $i$ 
18   | foreach  $v_{alt} \in remainViews$  do
19   | |  $crtEAC \leftarrow crtEAC \cup \{v_{alt}\}$   $\text{backtrackFindEAC}(v, V, crtEAC)$ 
20   | |  $crtEAC \leftarrow crtEAC \setminus \{v_{alt}\}$ 

```

---

CFGs do not make sense from the application perspective, since the data path feeding each view must start at the publisher  $D$ .

It can be shown that an RG has cycles only if the EG it has been built from had cycles. To avoid RGs (and CFG) cycles, we break EG cycles using the cycle removal algorithm [11].

### 4.3 View-based Rewriting Algorithm

We now describe our rewriting algorithm (Algorithm 4). As stated in Proposition 4.1, to find rewritings of  $v$  it suffices to find all embedded attribute set covers (EACs) of  $v$ , and to build an efficient rewriting from each such EAC.

The novelty of our algorithm is that it generates solutions *incrementally on-demand*, a useful feature given that we only consider  $k$  alternative rewritings for each subscription (recall subsection 3.1). Since all rewritings may never be developed, Algorithm 4 strives to develop the most promising rewritings first, that is those whose evaluation utilization is likely to be low. This is done



by ordering candidate views in decreasing order of their *interest* w.r.t. rewriting (covering) a given view  $v$ : the more  $v$  attributes *currently uncovered* by a partial rewriting are covered by a view  $v'$ , the more interesting it is to add  $v'$  to (join it with) the respective partial rewriting. Clearly, as views are added to the rewriting, view interests have to be recomputed. The algorithm is based on depth-first exploration and backtracks to move from one rewriting to the next one.

First, the algorithm uses the EG to retrieve the view set  $V$  containing only the views embeddable in  $v$ . The EAC exploration starts with an empty EAC, and at each point the highest-interest view not already in the current EAC is added to it. We compute the interest of adding a candidate view  $u$  to the EAC, given that a subset of  $V$  has already been selected, by counting *how many attributes of  $v$  not covered by the EAC views, are covered by the candidate  $u$* .

For example, when rewriting view  $v / a_{ID,cont} / b_{ID,cont}$  and considering a candidate view  $u_1 = / a_{ID} / b_{ID,cont}$ , the interest of  $u_1$  is 3, since  $u_1$  covers the attribute  $ID$  in two nodes of  $v$  as well as  $b.cont$ . Once  $u_1$  is selected, the interest of another candidate view  $u_2 = / a_{ID,cont} / b_{ID}$  is 1, since the only attribute of  $v$  not previously covered by  $u_1$  and covered by  $u_2$  is  $a.cont$ . When several views have the same interest, the tie is broken by picking the one that covers attributes from *the largest number of  $v$  nodes*. Once an EAC for  $v$  is found, we transform it to a rewriting expression and add it to the list of rewriting solutions.

In the worst case, Algorithm 4 will develop all subsets of  $V$ . However, in practice, since we only seek  $k$  rewritings, the number is typically much less, as we verified through our experiments.

**Rewriting Minimization** Algorithm 4 may generate rewritings which include redundant views. These views may be removed from the rewriting while leaving it still equivalent to the target view. Non-minimality is due to the greedy nature of Algorithm 4: after a view  $u$  was included in a rewriting, another set of views  $\{u_1, u_2, \dots, u_k\}$  may be added such that, together, the views in the set cover all attributes that  $u$  was selected for. This makes  $u$  redundant although it was not when initially added. To build efficient (non-redundant) rewritings, we minimize them in a post-processing fashion as in [30]: remove a random view from a non-minimal rewriting, then check if this has compromised the rewriting. If yes, the view is put back in the rewriting, another view is removed, etc.

#### 4.4 Generality of our Approach

The core concepts and framework of Delta, discussed in Section 2, are independent of the concrete underlying data model, query language and query rewriting algorithm. While Delta is currently implemented and deployed for XML subscriptions, it can be easily adapted to another data model and subscription language. We briefly discuss the rewriting-related components needed to do so.

First, an algorithm for equivalent view-based query rewriting is needed, such as proposed in the literature, e.g., for relational [26] or XML data [30, 23]. In particular, the set-cover-based algorithm described above can be used as-is if we model subscriptions simply as *key-value pairs*, e.g., “topic=sport and location=England”, as considered in many publish-subscribe data management settings such as e.g., [6]. We rely on this algorithm to build the RG.

Second, while building the EG is optional, for many-view settings it is likely to significantly improve performance, by limiting the view set input to the rewriting algorithm. The embedding criterium we used to build the EG has natural counterparts in other data models, e.g., the classical containment mappings [5]. If these are not implemented or their computational cost is high, the EG can be approximated using any non-lossy pruning. For instance, if one considers relational queries as subscriptions, we could add an edge  $(v_1, v_2)$  in the EG as soon as the tables in  $v_1$  are a subset of those in  $v_2$ , and for each table, the constants used in selections on that table in  $v_1$  are used in selections over the same tables in  $v_2$ .

## 5 Experimental Evaluation

In this Section we present the experimental evaluation of our system. We describe our setup in Section 5.1, and discuss the construction of EGs and RGs in Section 5.2. Section 5.3 studies the utilization-based selection of CFGs through ILP, while Section 5.4 discusses how to improve the latency of such CFGs. Finally, Section 5.5 presents the deployment of Delta in a wide area network.

### 5.1 Experimental Setup

We implemented all our algorithms in Java, except for the utilization based CFG selection algorithm (Section 3.3), for which we made use of the Gurobi ILP solver [17]. We relied on YFilter [9] to generate our views, based on the XMark DTD [28].

We have generated two view sets,  $V_1$  and  $V_2$  of 100,000 views, the characteristics of which are shown in Table 2. For  $V_1$ , we opted for unique views in order to examine the scalability and efficiency of our algorithms in the absence of trivial rewritings (where equivalent views rewrite one another) and force our utilization and latency optimizations algorithms to consider more complicated CFGs (rather than chains of equivalent views that can be easily optimized).

For  $V_2$  we opted for only 31,925 unique views, whereas the rest are duplicates. This view set is chosen so as to observe the impact of duplicate views in the shape of the RGs and CFGs that are generated by our algorithms.

All our experiments ran on an 8-core server (2 CPUs, Intel Xeon @2.93GHz), with 16GBs of RAM and running CentOS Linux 6.4.

	<b>View Set Metric</b>	<b>Value</b>
	Number of views (unique)	100,000
	Avg. number of predicates per view	0.72
	Avg. number of predicates per node	0.11
	Avg. number of nodes per view	6.13
	Avg. number of return nodes per view	2.52
	<b>EG Metric</b>	<b>Value</b>
$V_1$	Number of edges	10,592,053
	Number of edges deleted to remove cycles	18,665
	% of views in which at least one view is embedded	99.95
	Generation time (sec)	452
$V_2$	Number of edges	2,033,296
	Number of edges deleted to remove cycles	4,692
	% of views embedded by at least another view	100%
	Generation time	56 sec
	<b>RG Metric</b>	<b>Value</b>
$V_1$	Number of rewritings ( $\wedge$ nodes)	2,692,139
	Number of edges	8,589,822
	Generation time (sec)	127
	Views rewritten by other views	94,835
	Avg. number of views used in a rewriting	2.15
	Avg. $ E^{out} $	57.9
$V_2$	Number of rewritings ( $\wedge$ nodes)	2,587,687
	Number of edges	6,527,422
	Generation time	80 sec
	Views rewritten by other views	96,736
	Avg. number of views used in a rewriting	1.48
	Avg. $ \delta^{out} $	38.3

Table 2: Experiment settings and EG/RG statistics.

	$B^{out}$	30	50	100	$\infty$
$V_1$	% rewritten views	94.3	94.7	94.7	94.7
	CFG utilization ( $\times 10^{13}$ )	3.49	3.32	3.31	3.13
	Average views per rewriting	1.77	1.78	1.79	1.8
$V_2$	% rewritten views	-	-	96.7	96.7
	CFG utilization ( $\times 10^{13}$ )	-	-	1.93	1.93
	Average views per rewriting	-	-	1.24	1.24

Table 3: Impact of  $B^{out}$  on the selected CFGs.

## 5.2 EG and RG Generation

We have generated the EG using Algorithm 3, then removed cycles from it, and finally generated the RG using Algorithm 4. Algorithm 4 was instructed to generate no more than  $k = 30$  rewritings for each view. The sizes and generation times for the EG and RG appear respectively in the middle and bottom of Table 2. Every time Algorithm 4 finds a rewriting, we create the corresponding  $\wedge$  node, with an outgoing edge toward the rewritten view, and with an incoming edge from each view used in the rewriting. Table 2 shows that the number of rewritings (and thus, the size of the unrestricted RG) is very high, more than 2.5 millions.

## 5.3 CFG Utilization Optimization Through ILP

In the experiments involving the view set  $V_1$ , we have set the upper bound of the data source as  $B_D^{out} = 6,198$ , that is, the number of views that cannot be rewritten by other views (see Table 2) plus a 20% margin. The respective bound for the view set  $V_2$  was set to  $B_D^{out} = 3,916$ . We did this in order to push to the data source  $\mathcal{D}$  the least possible load, while giving the ILP solver some margin to assign some extra views to  $\mathcal{D}$  if needed. We have also set a common  $B^{out} = \{30, 50, 100, \infty\}$  for all views (to see the effect of bounds on the shape of the resulting CFGs).

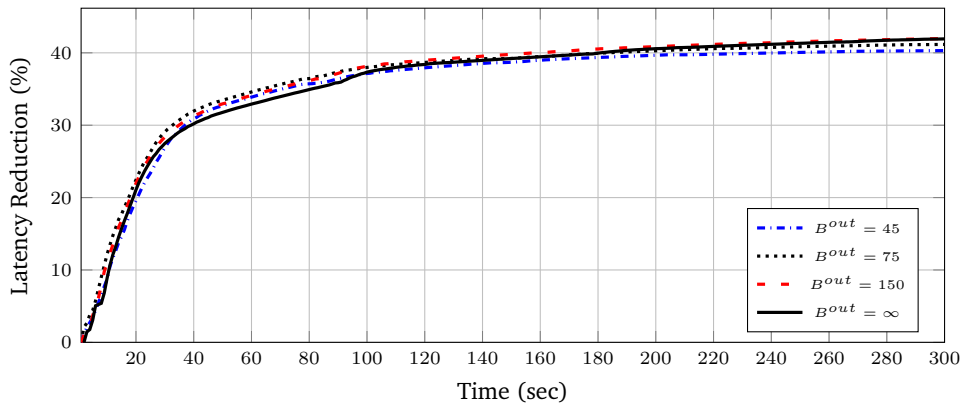
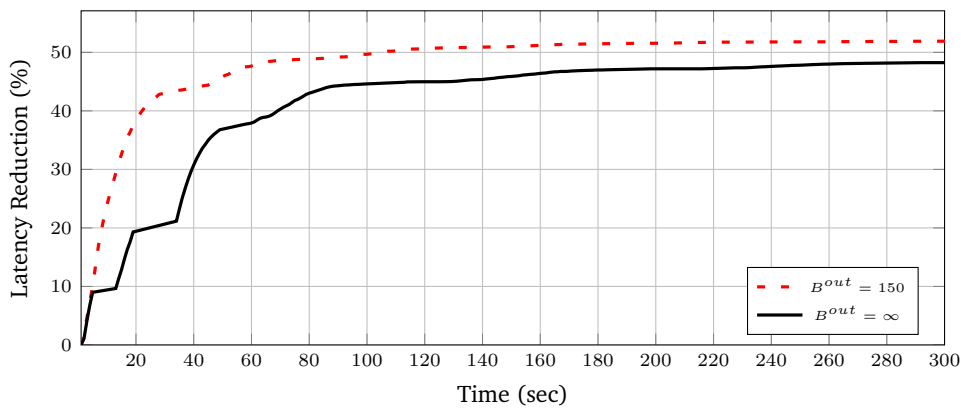
The Gurobi solver was then used to select utilization-optimal CFGs. A first observation was that the running time *decreases* as  $B^{out}$  increases, from about four minutes for  $B^{out} = 30$  to less than two minutes for  $B^{out} = \infty$ . The reason is that a small  $B^{out}$  corresponds to highly restricted settings where the solver must search longer in order to find acceptable solutions.

Table 3 depicts the percentage of views rewritten using other views (and not filled from the data source  $\mathcal{D}$ ) in the CFGs returned by the ILP solver, as well as the utilization of the CFGs and the average number of views that take part in the rewritings. First, notice that even when we keep the load on the views under tight control ( $B^{out} = 30$ ), we achieve a high degree of off-loading (94.3% for  $V_1$  and 96.7% for  $V_2$ ) from the data publisher  $\mathcal{D}$ . Moreover, as can be seen, by decreasing  $B^{out}$  in  $V_1$ , the utilization of the CFG increases (due to tighter constraints), while the number of views participating in a rewriting decreases (since each view is allowed to serve less views).

In Table 3 we can see that the cost of CFGs for  $V_2$  are considerably lower than the ones of  $V_1$ . This is due to the fact that the cost of serving one view from (another) identical view, is very low compared to performing joins that are expensive. Note also the difference in the average views per rewriting: in  $V_1$  almost 1.8 views in average are used to serve another view, while for in  $V_2$ , this number is considerably lower (1.24).

Finally, we observed that the solver could not generate CFGs (i.e. no configuration was feasible) for the duplicate-rich view set  $V_2$  for  $B^{out} < 100$ . This happened because some of the views in  $V_2$  were too popular. Assigning all other views that depended on the popular one could not be done without breaking the bound  $B^{out}$  that was given to the solver and they had to be assigned to the data source. Since there was also a relatively low bound on the data source ( $B_D^{out} = 3,916$ ) that had to also be respected, the ILP was infeasible.

This experiment showed that in case a view set contains some very popular views, one has to

Figure 6: Latency reduction while running LOGA for  $V_1$ .Figure 7: Latency reduction while running LOGA for  $V_2$ .

increase the bound of the data source  $B_D^{out}$ . We have experimented further in that direction and we saw that increasing the bound of the data source to  $B_D^{out} = 6000$  (almost double the previous bound), the solver could finally generate CFGs for  $B^{out} = 50$  but not for  $B^{out} = 30$ .

#### 5.4 Greedy CFG Latency Optimization

We now study the performance of Algorithm 2 (LOGA, Section 3.4), applied on CFGs obtained through ILP optimization. Our initial experiments did not show significant latency improvement, because the ILP-selected CFGs exploited most of the freedom we gave them (almost every view was feeding  $B^{out}$  other views). Hence, there was very little leeway for LOGA to make changes. To circumvent this problem, we allowed LOGA to use as bound 1.5 times the  $B^{out}$  given to the ILP solver. Thus, where the ILP solver had  $B^{out} = 30, 50, 100$ , LOGA used 45, 75, 150, respectively.

**Latency Optimization** Figure 6 depicts the latency improvement as a function of the LOGA running time. We see that LOGA is very effective, achieving a 43% reduction with respect to the latency of the CFG returned by the initial ILP solver. Moreover, such savings are obtained within 150-200 seconds. They stabilize when the data propagation paths to all the high-impact views have been altered and there is not much room for further optimization.

Similarly, Figure 7 depicts the latency improvement for the view set  $V_2$ . We see that in this case LOGA is more effective, achieving a 50% reduction with respect to the latency of the CFG returned by the initial ILP solver. This is explained by the fact that the duplicates in the graph leave a room for further improvement.

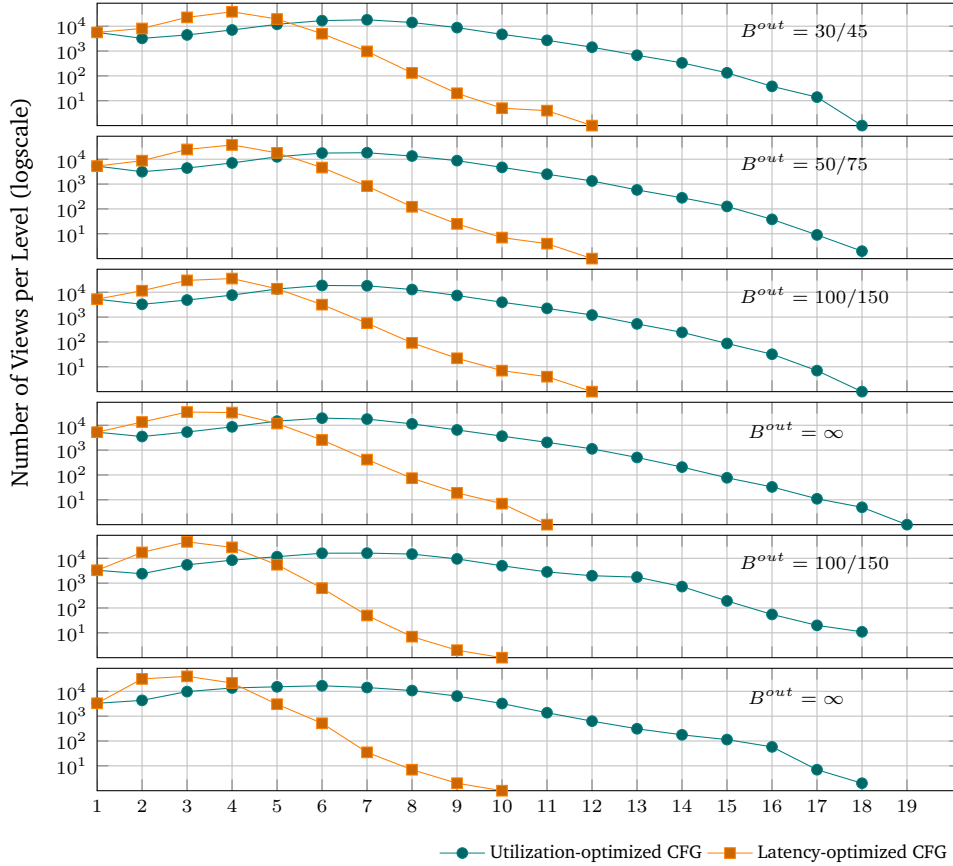


Figure 8: Distribution of views across CFG levels for view sets  $V_1$  (top 4) and  $V_2$  (bottom 2).

**Distribution of Views into Levels** Figure 8 depicts the distribution of views into levels in the CFGs for varying  $B^{out}$ , as produced (i) by the ILP solver, and (ii) after LOGA optimization. Note the logarithmic vertical axis. We see that the latency-optimized CFGs have less than 2/3 of the number of rewriting levels of the CFGs produced by ILP. Moreover, in the latency-optimized CFGs, most of the views lie in levels 1-6, leaving approx. only 1.5% of the views on levels 6-12. Thus, most views are only 4-5 hops away from the data source. This “flattening of rewriting levels” is an expected result of LOGA, since the more levels the data passes through from the publisher to a view, the more latency is added.

**Utilization vs. Latency** Although one may expect latency optimization (that reached 50%) to re-increase utilization, the increase was very moderate (5-7%). LOGA is only making greedy incremental fine-tuning over utilization-optimized CFGs (whose bounds were already attained), and therefore, the changes in the graph could not significantly change utilization.

## 5.5 Experiments in a WAN Deployment

We deployed Delta’s algorithms on top of the distributed query execution engine of ViP2P [20]. We implemented a full set of continuous physical operators (structural joins, selections, buffers etc.) mostly based on the physical operators of ViP2P. We report here on experiments we carried deploying Delta in a WAN.

**Infrastructure** We conducted our experiments in the Grid5000 infrastructure [14], using 300 machines distributed over nine major cities across France and Luxembourg. The hardware of Grid5000 machines varies from dual-core machines with 2GBs of RAM to 16-core machines with

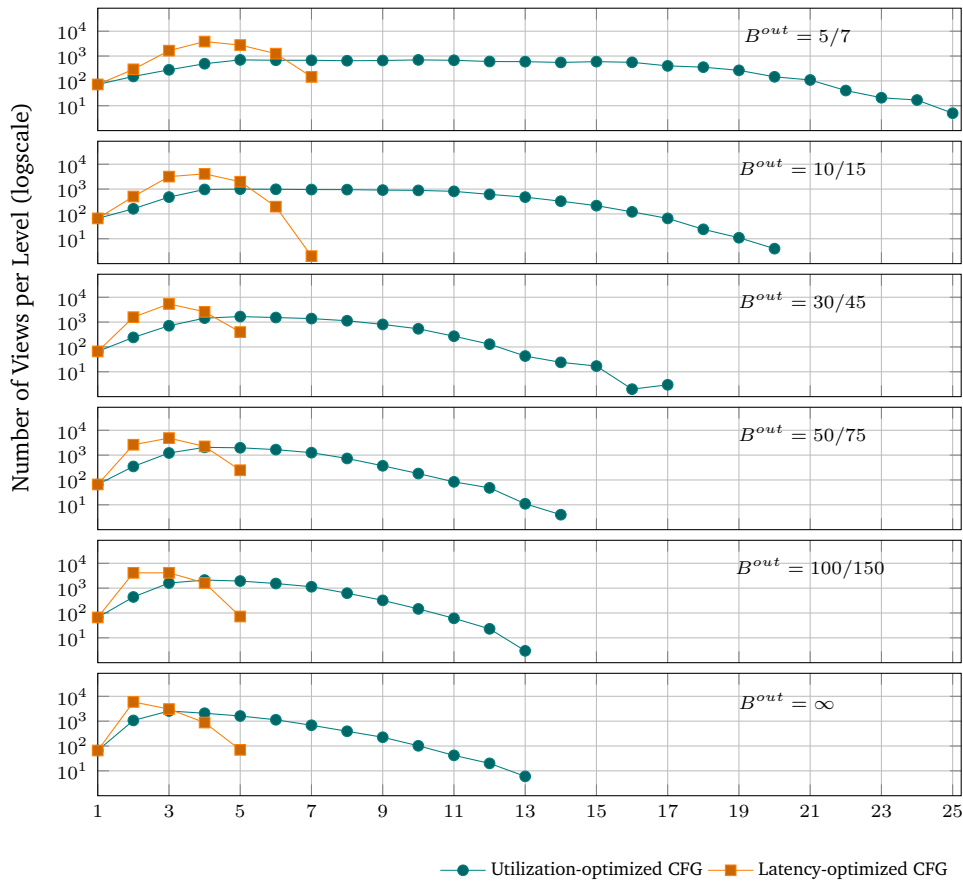


Figure 9: Distribution of views across deployed CFG levels.

32GBs of RAM. This heterogeneous hardware distribution is likely to occur with real settings as subscribers have varied-capacity machines.

**Views and Documents** We have generated a set of 10,000 views, along with a set of 200 small (10-40KB) XMark [28] documents, in a way such that each document matches almost all of the views. Unlike our previous experiment, this view set has only 3,000 unique views, which is more representative of real-life scenarios where some subscription topics are popular.

We have created the corresponding EG and RG and invoked the ILP solver to generate utilization-optimized configurations for  $B^{out} \in \{5, 10, 30, 50, 100, \infty\}$  and  $B_D^{out} = 72$ . The resulting CFGs were optimized for latency with the LOGA Algorithm with bounds  $\{7, 15, 45, 75, 150, \infty\}$ .

The distribution of views into levels is depicted in Figure 9. A first observation is that in the presence of duplicate views, the latency-optimized CFGs can have less than half of the levels of their utilization-optimized counterparts. A CFG with duplicate views is easier to optimize through the LOGA Algorithm since equivalent views may be served from one another.

We now move to presenting our results from deploying the generated CFGs. To characterize the performance of Delta, we have measured two important metrics, namely the *observed latency* and the *document delivery time*.

**Observed View Latency** We measured the latency of a view  $v$  for a document  $d$  as the time elapsed between: (i) the moment when the first tuple of  $d$  leaves the data source, and (ii) the instance when the last tuple of  $d$  reaches the view  $v$ . Note that in the observed view latency we do not include the time needed to extract the level 1 view tuples from a document. We do not include

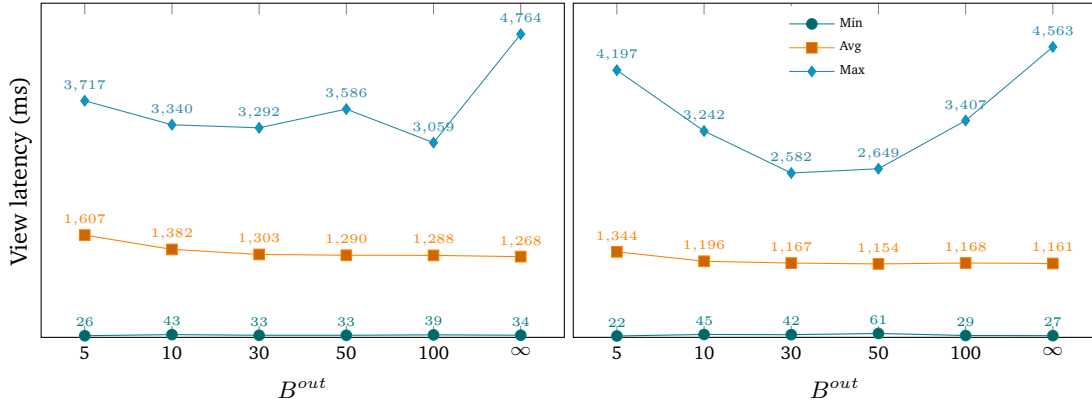


Figure 10: View latency for utilization-optimized CFGs (left) and latency-optimized CFGs (right).

this<sup>3</sup> since this extraction step is not the main scope of the paper and has been studied in other works [9, 19].

Figure 10 depicts the average observed view latency for all pairs of views and documents in our CFGs. A first observation is that on average, views get their results in just 1.6 seconds after a document is published. This translates to a throughput of many thousands of subscriptions served per second, with a data source having to serve only 0.7% (72 out of 10,000) of the views. This demonstrates how Delta makes it possible to serve large numbers of subscribers using very little publisher computing resources.

Our second remark regards the minimum/maximum latencies for  $B^{out} = 5$  in utilization-optimized CFGs. Some views in the network receive their results extremely fast (30ms) while some others considerably slower (3.7s). This is an inherent feature of Delta: views that are close to the data source receive their data faster than the ones that reside in deeper levels.

The LOGA algorithm reduces the observed latency of views up to 20% ( $B^{out} = 5$ ) compared to the utilization-optimized CFGs. This also shows that our latency estimation models (used by our algorithms) are quite accurate.

An interesting phenomenon is the following: in the utilization-optimized CFG where  $B^{out} = \infty$  we notice a very large increase in the maximum latency (4.7s) while the CFG is not too deep (13 levels) compared to other CFGs that showed lower latency. This is explained by the fact that when a view serves a very large number of other views, it can be overloaded and the data processing/transmission throughput is reduced. This shows the importance of the bounds  $B^{out}$  in Delta: for optimal performance,  $B^{out}$  must be set in the “sweet spot” between values too large (to avoid overloading) and too low (to avoid very deep CFGs). In practice, a simple test can be performed at each subscriber machine to tailor its  $B^{out}$  to its observed hardware performance.

**Document Delivery Time** For a view  $v$  and a document  $d$  that matches  $v$ , we term *document delivery time*, or simply DDT, the total time needed for all the matching tuples of document  $d$  to reach the view  $v$ . For a set of views  $V$ , the DDT is measured as the interval between: (i) the moment when the first tuple of the document  $d$  leaves the data source and (ii) the instance when the last tuple of the document  $d$  has reached the slowest view  $v \in V$ . In other words, this metric captures the time it takes for a document to reach its slowest interested view.

Figure 11 shows the average, minimum and maximum DDT over all published documents in our experiment. In general, in all CFGs, a document is delivered to all views in the network, in an average of 2-2.5 seconds. Note that the maximum observed latency coincides with the maximum DDT (see Figures 10 and 11) as the slowest view in the network actually defines the DDT. Thus, we observe the same phenomenon as in the observed latency: DDT slows down for the extreme  $B^{out} = \{5, \infty\}$  values.

<sup>3</sup>For completeness: our view matcher took an average of 100ms to extract from each document the tuples for the 72 first-level views.

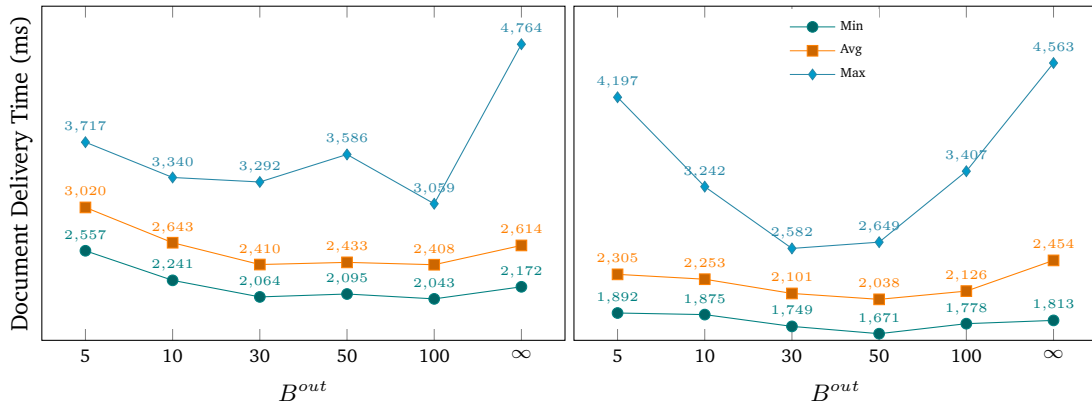


Figure 11: Document delivery time for utilization-optimized CFGs (left) and latency-optimized CFGs (right).

**Note on the LOGA’s Effectiveness Related to the Increase of  $B^{out}$**  In our early experimentations, after a utilization-optimized CFG was obtained, we optimized that CFG for latency with LOGA, without altering the bounds  $B^{out}$ . In that case, the reductions in latency were very small (6-10%). It turned out this was because the bounds of most of the views were already reached and the LOGA algorithm could not significantly change a given CFG in order to optimize it for latency, without breaking the bounds. Increasing the bounds by 50% was the only way to evaluate the effectiveness of the LOGA algorithm; observe that not doing so would prevent LOGA from actually bringing any benefits. One would argue that the latency reductions that LOGA could attain, are due to the 50% increase in  $B^{out}$  and not due to its actual effectiveness. However, this does not hold and our experiments already allow to see the effectiveness of LOGA independently of this “extra leeway” we gave it.

As we can see in Figure 8 in the topmost graph, given a bound  $B^{out} = 45$  the LOGA algorithm managed to reduce the levels of the latency optimized CFG from 18 to 12. However, the same reduction in levels did not happen on the utilization-only optimized CFG for the bound  $B^{out} = 50$  (second graph from the top): the ILP solver generated 18-level deep CFGs. Thus, *the increase of bounds alone is not enough to eliminate levels from a CFG and thus decrease latency*, but has to be credited to LOGA’s effectiveness itself. The same phenomenon can be seen in the observed view latency in Figure 10. Again, we see that an increase in the bounds in utilization-optimized graphs (left graph) does not result in the same latency decrease that LOGA achieves (right graph) for the same bounds.

## 5.6 Experiment Conclusion

Our experiments have demonstrated the efficiency and effectiveness of Delta’s multi-level dissemination approach. With respect to efficiency, for 100,000 distinct subscriptions, the full graph generation, optimization for utilization and then latency took less than 13 minutes. As for effectiveness, the configurations retained have low cost scores. This is confirmed by the WAN deployment of 10,000 subscriptions, which showed a high message delivery throughput and low latency: documents are propagated to 10,000 subscriptions, which are fed with data within 1.5 seconds on average.



## 6 Related Works

Our work belongs to the class of content-based publish subscribe systems, disseminating to users the results of their specified subscriptions over a stream of published data. This work is related to several themes of existing works.

**Filtering Systems** A large part of the literature addresses the problem of optimizing the publisher so that it handles the filtering of incoming data for very large numbers of subscribers.

YFilter [9] stands out as a widely-known system for XML publish-subscribe. It is able to feed many XPath 1.0 subscriptions very efficiently by matching them simultaneously against documents through a single automaton. NiagaraCQ [6] relies on multi-query optimization for continuous queries, taking advantage of the similarity of subscriptions in order to share operators during evaluation. Similarly, [19] addressed the same problem but for a more expressive subscription language, supporting joins over multiple documents while [33, 34] use methods of multi-query optimizations for continuous queries over RSS feeds. Finally, [32] proposes a pub/sub system where the evaluation of subscriptions is done inside a relational database.

The above do not consider distributed data dissemination. Instead, they focus on optimizing the publisher task, to support very large numbers of subscribers. Our work can be seen as complementary since we focus on the design of a logical overlay network (CFG), that exploits the subscribers in order to scale up. Any efficient filtering at the publisher can be adopted in our setting.

**Distributed Publish/Subscribe** Onyx [10] connects multiple publishers and subscribers by employing multiple YFilter instances running on connected brokers. Recently, FoXtrot [24] has distributed YFilter automata on top of a DHT network. Other DHT-based pub/sub systems are, e.g., [7, 15]. Closer to our work, SemCast [25] leverages commonalities between subscriptions and creates logical *channels* between brokers and subscribers to form multicast trees of low utilization and latency. However, the system relies on a network of brokers, and the subscribers do not help in the dissemination of data. Finally, [31] builds one multicast tree per broker aiming at redundancy and fault tolerance.

Contrariwise, in [4], *every peer* can forward messages to its neighbors if the message matches its own interests. Peers are organized in an hierarchy tree based on subscription similarity. However, by design, the peers do not know the subscriptions of their neighbors, and as a result, their routing protocol allows for false positives (peers may receive messages which do not interest them).

In contrast with these works, Delta builds multi-level dissemination networks involving the subscribers, leveraging query rewriting to determine whether some subscriptions can be used to compute results of other subscriptions. One of the consequences unique to Delta is the ability to combine the results of *multiple* subscriptions in order to serve another one.

**View-based Data Management** As explained in Section 4.4, any efficient view-based rewriting algorithm (e.g., [26]) can be used instead of our Algorithm 4. View maintenance has been investigated in the centralized context of data warehousing [29, 27]. In the ViP2P project, incremental algebraic techniques for maintaining materialized views have been described in [2, 3]. Finally in [8], the authors consider “stacked” views, specified as queries over other defined views, study their maintenance and the efficient evaluation of queries using such views; these resemble our multi-level configurations, but in [8] the connections between views are given, whereas we choose them for performance through our algorithms.

## 7 Future Work

Delta, considers complete rewritings, that is, subscriptions are either served from the data publisher or solely from other subscriptions. When the system starts to run and the number of subscribers is limited, subscriptions do not overlap enough to create lots of rewriting opportunities. In that case, Delta will fail to rewrite all subscriptions based solely on other subscriptions and the publisher will have to serve them all individually. In that case, the publisher will be overloaded or even refuse to serve some of the subscriptions.

A possible solution to this overloading would be to use *partial rewritings*. A partial rewriting would allow a subscription to be served partly by other subscriptions and partly by the publisher. This way, the load on the publisher can be reduced since some of the processing effort is pushed to other subscribers.

Supporting partial rewritings in Delta's algorithms is relatively straightforward: given an appropriate rewriting algorithm, the rewritability graph can be easily enriched with partial rewritings. In turn, the enriched rewritability graph can be used by our algorithms without any other change.

In contrast, in order to support partial rewritings a publisher should be slightly modified. Instead of materializing only level 1 views of a given configuration, the publisher would have to also store and serve the extra views for the evaluation of partial rewritings. To sustain the extra effort on the data publisher, one could use a view selection algorithm such as [21]. The possibility of supporting partial rewritings in Delta and selecting custom materialized views for the publisher is left for future work.

## 8 Conclusion

In this report we considered the problem of scaling up content-based publish/subscribe systems under resource constraints (such as finite CPU and network capacity) by off-loading some of the data publisher's effort on the subscriber sites. This is achieved by organizing subscriptions in a rewritability graph which materializes the ways in which one subscription could be served from others, through view-based rewriting. We provide a novel two-step algorithm for organizing the views in a network minimizing a combination of resource utilization and data dissemination latency. First, we express the utilization minimization problem as a linear program and solve it exactly; as we show, latency cannot be included in the ILP formulation due to its non-linear nature. We reduce latency in a second step based on the result obtained from the ILP solver. Our configuration choice algorithm scale well to 100.000 unique subscriptions, whereas in a WAN deployment, Delta succeeds in filling in 10.000 subscriptions with a latency of under 2 seconds.

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## A Appendix

The use of ILP gives our framework the flexibility to support different kinds of constraints with very little changes. The ILP formulation of Section 3.3 can be modified in order to satisfy multiple and more complex constraints. As an example, we show below how to handle the case where multiple views can reside at a network site. In this case, we assume bounds that determine for each site  $n$  the maximum number of subscriptions that belong to different sites and can be served by subscriptions residing at  $n$ .

The changes that need to be done are the following:

- We replace the bound  $B_v^{out}$  with the bound  $B_n^{out}$ , that is *the maximum number of views that can be served by the site  $n$  and which do not reside at  $n$ .*;
- In Section 2.3, replace:

$$\forall v \in V \cup \{\mathcal{D}\}, \text{out}(v) \leq B_v^{out}$$

where  $\text{out}(v)$  denotes the outdegree of node  $v$  in the CFG,  
with:

$$\forall n \in N \cup \{S_{\mathcal{D}}\}, \sum_{v \text{ resides at } n} (|E_{v,n}^{out}|) \leq B_n^{out}$$

where  $E_{v,n}^{out}$  is the set of the outgoing edges of view  $v$ , that do not point to views residing at  $n$  and  $S_{\mathcal{D}}$  denotes the site of the publisher  $\mathcal{D}$ . We assume that a view resides at  $S_{\mathcal{D}}$  in a given configuration if it is served directly from  $\mathcal{D}$ ;

- In our ILP problem formulation (Table 1), replace equation:

$$\sum_{e \in E_v^{out}} x_e \leq B_v^{out} \quad \forall v \in V \cup \{\mathcal{D}\} \quad (4)$$

with:

$$\sum_{v \text{ resides at } n, e \in E_{v,n}^{out}} x_e \leq B_n^{out} \quad \forall n \in N \cup \{S_{\mathcal{D}}\} \quad (4')$$

- In LOGA (Algorithm 2) replace the first “if”-condition of line 10 with:  
 $\forall v \in \text{cfg}, \text{outdegree}(n|v \text{ resides at } n) \leq B_n^{out}$ .

After these modest changes, the complexity study and the rest of our approach would remain unchanged: we would still use ILP to optimize for utilization and then heuristically attempt to improve latency with LOGA.

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