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Optimizing microalgal production in raceway systems

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Abstract

The industrial exploitation of microalgae is characterized by the production of high value compounds. Optimization of the performance of microalgae culture systems is essential to render the process economically viable. For raceway systems, the task of optimization is rather challenging since the process is by essence periodically forced and, as a consequence, optimization must be carried out in a periodic framework. In this paper, we propose a simple operational criterion for raceway systems that when integrated in a strategy of closed-loop control allows to attain biomass productivities very near to the maximal producitivities. The strategy developed was tested numerically by using a mathematical model of microalgae growth in raceways. The model takes into account the dynamics of environmental variables temperature and light intensity and their influence on microalgae growth.

Keywords: control, microalgae, modeling, optimization, photobioreactors, raceway

1 1. Introduction

Microalgae assimilate inorganic carbon through photosynthesis, a process that takes place in two phases, namely light-dependent stage (light reactions) and light-independent stage (dark reactions). The second phase comprises a series of reactions catalyzed by the enzyme ribulose bisphosphate carboxylase oxygenase (RuBisCO). In this phase, CO₂ is incorporated into organic material, leading to the formation of the carbon building blocks that are further synthesized into carbohydrates, proteins, lipids and nucleic acids [38].

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Due to its biochemical properties, microalgae have been raised as promising feed-8 stocks for the production of high value compounds. The commercial use of microalgae 9 includes applications in food industry and cosmetics [35]. Moreover, microalgae have been 10 identified as a renewable source for biodiesel production [5, 18]. However, despite these 11 favorable characteristics, microalgae production in a sustained and large scale basis is 12 probably carried out far from an optimal working mode. Here, we mainly refer to the 13 technology of raceways (high rate open ponds), which are nowadays the systems generally 14 used for large microalgae production. 15

The difficulty of achieving optimal productivities of microalgae in outdoor systems 16 results from the high interaction of phenomena that take place during growth and the low 17 level of control that we have on them. This factor makes the whole process inefficient under 18 an environment that is fluctuating by nature. The challenge of optimizing microalgal 19 culture systems is a broad endeavour that includes reactor design [24, 32] and strain 20 selection [33]. Furthermore, once the reactor configuration and the microalgal strain have 21 been chosen, optimal performances can be achieved by acting on operational variables, 22 such as temperature, pH and nutrient feeding rate. In this aspect, mathematical models 23 offer a powerful tool to be exploited. Indeed, optimization can be model driven. Since 24 microalgal metabolism is mainly influenced by nutrient availability, light intensity and 25 temperature, several models have been developed to account for these factors [8, 14, 15, 26 29, 26, 3]. A work of synthesis has been performed to provide a mathematical model that 27 incorporates the main factors that influences microalgal dynamics by keeping a relative 28 simple structure [2] that might be suitable for control processes. 29

The task of bringing a process close to optimality by acting on the inputs of the system 30 is the realm of optimal control. The optimal control problem that we are considering 31 consists in finding the time evolution of the manipulated variables maximizing a given 32 criterion on a finite time horizon. This problem can be solved by indirect methods such 33 as the Pontryagin's maximum principle or by direct methods (numerical optimization). 34 The advantage of using Pontryagin's maximum principle is that of providing an analytic 35 solution. In this respect, a theoretical study on a simplified model of microalgae growth 36 provided guidelines on the form of the controller to reach an optimal productivity [16]. 37

This study was the first dedicated to optimal control of microalgae in a periodically varying environment. A series of simplifications were needed to provide a very simple model suitable for applying the Pontryagin's maximum principle. The distance between the proposed optimal strategy and the optimal strategy for a more realistic model is therefore difficult to assess.

When a mathematical model is complex, the application of the Pontryagin's maxi-43 mum principle is not straightforward. Hence, methods based on numerical optimization 44 are, in practice, the most used. In the standard form, the numerical approach takes 45 place in open loop fashion, without taking into account the real state of the system. For 46 a real implementation, however, available measurements (either online or offline) must 47 be used to compensate for disturbances and to correct model mismatches (see, e.g., [4] 48 for a survey of methods). An example of this type of strategy is the predictive con-49 trol approach, in which the optimal control problem is solved online. This strategy was 50 developed for the optimization of biomass and oil productivities for the heterotrophic 51 microalgae Auxenochlorella protothecoides [11]. This approach, however, is computation-52 ally expensive and requires sophisticated algorithms of adaptation and proof of process 53 stability is lacking. 54

A practical alternative for optimizing system performance is to translate the optimiza-55 tion problem into a regulatory (tracking) problem. The objective then consists in finding 56 a variable (or a combination of variables) that when regulated maintains the system close 57 to optimality [34]. In the case of photobioreactors, the phenomenon of light transfer 58 to the culture governs the performance of the system [28]. Based on this principle, it 59 has been proposed that under constant light, maximal productivities can be attained by 60 maintaining the light intensity at the bottom of the reactor at a constant value. This 61 value corresponds to the compensation irradiance (G_c) , defined as the minimum value 62 of light intensity required to guarantee a positive net growth rate (strict compensation 63 condition) [7, 6, 37]. By defining the working illuminated fraction χ as the fraction of 64 the reactor volume with light intensities higher than the compensation irradiance, it has 65 been demonstrated mathematically that an optimal biomass productivity requires the 66 condition $\chi = 1$. 67

For outdoor raceways, the definition of a strategy to guarantee maximal productivities 68 is not trivial due to the diurnal light cycle. It has been conjectured that the compensation 69 point should also be reached for natural light in order to maximize productivity [25]. 70 Inspired on this premise, an experimental study with *Chlorella sorokiniana* was carried 71 out on an artificial lightened photobioreactor with planar geometry mimicking the daily 72 cycle of light [9]. The experimental set-up was conceived to maintain the photon flux 73 density leaving the reactor at a constant value. The luminostat operation did not exhibit 74 significant improvements of productivity compared to an operation at constant dilution 75 rate. From these results it can be drawn that keeping a constant light intensity at the rear 76 of the reactor might not be an optimal strategy for varying light conditions. Accordingly, 77 an imminent question is thus how to attain maximal productivities when light is varying. 78 In the present work, we proposed a simple operational criterion which when regulated 79 to an adequate set point maintains the system near to optimal operation. The proposed 80 strategy has the advantage to be straightforward to implement in a classical closed loop 81 control. 82

As a basis, we use the model proposed by [2] for a planar culturing device in combination to a model describing lipid production under nitrogen limitation [19, 20]. These models have shown to reproduce experimental data of lab scale systems. Here, we extend such models to account for characteristics of raceway systems. Our *in silico* case study takes the configuration of a pilot-scale open raceway (Algotron) located at INRA-LBE, France.

⁸⁹ 2. Modeling

⁹⁰ Under the assumption that nitrogen and light are the limiting factors for the growth ⁹¹ of microalgae, we combined the biomass model from [2] to the lipid production model ⁹² proposed in [19, 20]. It results in the following mass balance equations for a completely ⁹³ mixed reactor at constant volume V

$$\dot{s} = f_i s_{in} / V - f_o s / V - \rho x, \tag{1}$$

$$\dot{q_n} = \rho - (\mu - R)q_n,\tag{2}$$

$$\dot{x} = (\mu - f_o/V - R)x,\tag{3}$$

$$\dot{x}_l = \beta q_n \mu x - \gamma \rho x - r_0 \phi_T x_l - f_o x_l / V, \tag{4}$$

$$\dot{x_f} = (\alpha + \gamma)\rho x - r_0 \phi_T x_f - f_o x_f / V, \tag{5}$$

where s is the extracellular nitrogen concentration and q_n is the internal nitrogen quota. The concentration of the total carbon biomass x is the sum of three carbon pools, namely storage lipids (x_l) , carbohydrates (x_g) and a functional pool (x_f) , mainly formed by proteins and phospholipids. Note that the dynamics of x_g can be easily deduced since $x_g = x - (x_l + x_f)$. The influent nitrogen concentration is s_{in} .

The temperature exerts a strong influence on the behaviour of microalgae systems, in particular in outdoor raceways [27]. This effect is included in the model in two manners. Firstly, it is assumed, in line with [14], that temperature has an homogeneous effect on uptake, growth and respiration rates. Secondly, following the work of [13], the Chl a:N ratio was set to be dependent on the temperature and light. The equations are detailed later on.

¹⁰⁵ To model the growth rate, the following is assumed:

(i) Microalgal growth is uncoupled dynamically to nutrient uptake. Growth kinetics
 follows the cell quota model of Droop [12].

(*ii*) Light intensity is distributed spatially in the raceway. The absorption of light in the raceway follows the Lambert-Beer law. Thus, for a given depth z, the corresponding light intensity I_z satisfies

$$I_z = I_0 \exp(-\xi z),\tag{6}$$

where I_0 is the incident light and ξ is the light attenuation factor, expressed as

$$\xi = a \mathrm{Chl} + b. \tag{7}$$

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At the bottom of the reactor z = L. The term ξL is known as optical depth (λ) .

It should be noted that I_0 varies in time in an oscillatory fashion. Its amplitude depends on the season and the geographical location. For a given day, I_0 follows an increasing behaviour until noon, then decreases until midnight.

(*iii*) Light intensity affects the growth rate. This effect is described by a Monod type kinetics. For a given depth z ($0 \le z \le L$) with intensity I_z , the growth rate at hypothetical infinite nitrogen quota is

$$\mu_z = \tilde{\mu} \frac{I_z}{I_z + K_{sI}}.$$
(8)

Finally, the growth rate is represented by an average growth rate obtained by integration of (8) along the raceway depth. The resulting equation for the growth rate reads

$$\mu = \bar{\bar{\mu}}\phi_T \left(1 - \frac{Q_0}{q_n}\right),\tag{9}$$

with

$$\bar{\bar{\mu}} = \frac{\bar{\mu}}{\xi L} \ln \frac{I_0 + K_{sI}}{I_0 e^{-\xi L} + K_{sI}},$$

$$\phi_T = \frac{(T - T_{\max})(T - T_{\min})^2}{(T_{\text{opt}} - T_{\min}) \left[(T_{\text{opt}} - T_{\min})(T - T_{\text{opt}}) - (T_{\text{opt}} - T_{\max})(T_{\text{opt}} + T_{\min} - 2T) \right]}$$

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¹²³ The term ϕ_T represents the temperature effect. It is described by the model developed ¹²⁴ for bacteria by [30] and validated for microalgae by [3].

Nitrogen uptake rate (ρ) is modeled by a modified Michaelis-Menten kinetics [19].

$$\rho = \bar{\rho}\phi_T \frac{s}{s+K_s} \left(\nu + (1-\nu)\frac{\bar{I}^m}{\bar{I}^m + \epsilon_I^m}\right) \left(1 - \frac{q_n}{Q_l}\right). \tag{10}$$

The nitrogen uptake rate is expressed as a function of the average irradiance in the raceway \bar{I}_{27} \bar{I} . Here, it is considered that nutrient uptake is regulated by the internal nitrogen quota, *i.e.*, when the cells are nutrient saturated, uptake rate stops. Additionally, the equation includes a light regulating factor (in the form of a Hill-type function). Therefore, when the cells enter to the dark period, the nutrient uptake rate exhibits a slowdown. The model includes an overall respiration rate R, that gathers maintenance respiration and biosynthesis cost (assumed to be proportional to nitrogen uptake rate):

$$R = r_0 \phi_T + \varphi \rho, \tag{11}$$

where r_0 is the maintenance respiration and φ is a biosynthesis cost coefficient. Model notation is given in Table 1.

Additionally, it is assumed that chlorophyll concentration (Chl) is correlated to particulate nitrogen (xq_n) [2]. The Chl:N ratio (θ_N) is influenced by light and temperature following [13]

$$\theta_N^{-1} = (g_1 - g_2 T) + g_3 \bar{I} \exp(-g_4 T).$$
(12)

In this equation, it is implicitly assumed that the cells are photoacclimated at the average light intensity \bar{I} .

Environmental variables, notably light intensity (solar irradiance) and temperature govern reactor performance. These two variables incorporated in the kinetics of growth and nitrogen uptake can be accessible from online sensors or meteorological stations. In addition, mathematical models have been developed to predict light intensity [23] and raceway temperature [1] for a given location. In the present study, mathematical modeling supported by meteorological data was used for the location of Narbonne, France (see Fig. 1).

¹⁴⁷ Model parameters were taken from studies on the microalgae *Isochrysis* aff. *galbana*, ¹⁴⁸ when available. The parameters describing ϕ_T are those obtained for *Nannochloropsis* ¹⁴⁹ oceanica [3].

¹⁵⁰ 3. Driving raceway operation to optimal performance

151 3.1. Optimal problem statement

In this study, we are interested in designing a control law on the input flow rate (f_i) that allows to bring either the biomass productivity (P_x) or the lipid productivity (P_l) very close to the maximal productivities that can be attained in the raceway. For a given time horizon t_f , the maximal productivities can be obtained by solving an optimal control problem that can be formulated as follows

$$\max_{f_i(t)} \int_{t_0}^{t_f} \psi(t, \mathbf{x}(t), f_i(t)) dt.$$

s.t.
$$0 \le f_i(t) \le f_{\max}$$

$$\dot{\mathbf{x}} = \mathbf{g}(\mathbf{x}, f_i, t), \ \mathbf{x}(0) = \mathbf{x}_0.$$
 (13)

With **x** the state vector and f_{max} the upper bound of the input flow rate. If the purpose of the controller is to optimize biomass productivity P_x , then

$$\psi(t, \mathbf{x}(t), f_i(t)) = f_o(t) \ x(t). \tag{14}$$

If the objective is to optimize lipid productivity P_l , then

$$\psi(t, \mathbf{x}(t), f_i(t)) = f_o(t) \ x_l(t).$$
(15)

For the sake of clarity, we will call CP_x the optimal controller that maximizes biomass productivity and CP_l the optimal controller that maximizes lipid productivity.

The model equations (1)-(5) were used for the optimization study. The influent nitrogen concentration s_{in} was set to 50 g N m⁻³. This value is an operational concentration used in Algotron. The volume was assumed to be constant, so $f_o = f_i$.

The Matlab toolbox DOTcvpSB [17] was used for solving the optimal control problens numerically. DOTcvpSB uses the approach of sequential discretization (control vector parametrization) to solve the non-linear programming (NLP) problem. In the optimization stage, the stochatisc algorithms developed by [31] and [36] were used.

170 3.2. Quasi optimal closed loop control

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As it was mentioned in the Introduction section, solving the optimal control problem (13) (with the functional objective defined by (14) or (15)) might be computationally expensive and difficult to implement in practice. For a real implementation, it will be desirable to identify a controlled variable that when regulated towards a set point will ensure that the system operates close to optimality. In this respect and since light transfer is a crucial phenomenon of the process of microalgal growth, we propose the efficiency of light absorption (η_L) to be such a controlled variable.

$$\eta_L = \frac{I_0 - I_L}{I_0} = 1 - \exp(-\xi L).$$
(16)

As it will be shown hereafter, this simple controller has a very good ability to maintain the system close to the optimal solution. In fact, several strategies where tested based on preliminary studies, and η_L turned out to present the best trade-off between simplicity and efficiency.

For a given microalgae, there exists a set point η_L^* that maintains the system near to 182 optimal productivities. The value η_L^* depends on the characteristics of the microalgae, 183 namely optical properties and light affinity. In this study a set point $\eta_L^* = 0.95$ was 184 selected. Note that regulating η_L implies the regulation of the optical depth λ . Given the 185 form of the attenuation factor (7), regulating the optical depth is equivalent to regulating 186 the Chlorophyll concentration. For $\eta_L^* = 0.95$, the set point for Chlorophyll concentration 187 is $Chl^* = 4.95$ g Chl m⁻³. This result is very convenient because during darkness the 188 efficiency of light absorption can not be defined but we can still regulate the Chlorophyll 189 concentration to Chl^{*} in such a way that when $I_0 > 0$ the efficiency of light absorption 190 will be close to η_L^* . 191

In the following, we show by means of numerical simulation, the performance of the raceway by regulating η_L to the set point η_L^* . This regulation can be achieved by any adequate feedback controller. In this work, we use a standard PI controller. Since our premise is that this controller brings the system to work almost optimally, we call it a quasi optimal (QO) controller.

197 4. Results

198 4.1. Comparison of the QO controller to optimal strategy

Figure 2 displays the responses of the state variables and the lipid and biomass productivities (P_l, P_x) when applying the QO controller and the optimal CP_x controller for a time period of 30 days. To calculate the productivities, it was assumed that carbon contributes to the 56% of ash-free dry weight [38]. The productivities are divided by the

surface of the raceway and the time. The QO control controller brings the efficiency of 203 light absorption very close to the defined set point. At t = 6.5 d, η_L is 95% of η_L^* . The 204 maximal biomass productivity obtained with the optimal controller CP_x is 168 tons dry 205 weight $ha^{-1} a^{-1}$. This value is consistent with productivities reported in the literature 206 [5, 38]. Importantly, the biomass and lipid productivity provided by the QO controller 207 were both 98% of those given by the controller CP_x (Table 2). After 25 d, the final lipid 208 quota $(q_l = x_l/x)$ oscillates with a maximal value of 16%. This relative low level of lipids 209 is due to the fact that many of the parameters used in the model were taken from studies 210 with I. galbana, which is known to have a low lipid content. 211

To have an assessment of the maximal lipid productivity that can be attained, the 212 optimal controller CP_l was calculated. For the model parameters used in our case study, 213 it resulted that optimizing lipid productivity was equivalent to optimizing biomass pro-214 ductivity. Thus, the response of the system behaviour when applying the CP_l controller 215 was very similar to the response obtained when applying the CP_x controller. This result 216 is interesting because it is often claimed the conflict between optimizing lipid productivity 217 and optimizing biomass productivity. Indeed, such a conflict occurs when light is con-218 stant. Figure 3 shows the system response for the optimization of the two performance 219 indexes (P_x, P_l) when the system was set to operate at constant temperature (21°C) and 220 constant incident light (250 μ mol photons m⁻²s⁻¹). It is observed that while the optimal 221 strategy for biomass productivity provides a higher biomass concentration, the optimal 222 strategy for lipid productivity drives the microalgae to increase its lipid content, which 223 in turn is detrimental for attaining high concentration of biomass. While the difference 224 between the biomass productivities obtained by the two controllers is very small, the CP_l 225 controller provides a lipid productivity that is 10% higher than that obtained with the 226 CP_x controller. These differences may become more important for microalgae with high 227 potential of lipid accumulation. 228

For a diurnal light cycle, however, our results suggest that there is not discrepancy between optimizing lipid productivity and optimizing biomass productivity. For both performance indexes, the cells should growth as much as they can in the light period to accumulate enough carbon. The higher the biomass the concentration, the higher

the available carbon source that can be potentially directed to the lipid pool. To as-233 sess whether our indication was independent on the properties of lipid accumulation of 234 the microalgae, the coefficients of fatty acid synthesis (β) and fatty acid mobilization 235 (γ) were modified to represent a microalgae with high lipid level ($\approx 40\%$ of the total 236 carbon). The optimal controllers CP_x and CP_l were further calculated with the new pa-237 rameters. The system dynamics were specific to each applied controller CP_x and CP_l , e.g., 238 the biomass concentration for the CP_x exhibited a different dynamics that the biomass 239 concentration provided by the CP_l . However, such differences were not significant and 240 both controllers provided similar biomass and lipid productivities. Hence, we confirm the 241 previous suggestion that optimizing lipid productivity is almost equivalent to optimizing 242 biomass productivity for a photobioreactor with diurnal light cycle. 243

The results presented here are very promising. We show that the QO controller per-244 forms as well as the optimal controllers, confirming our hypothesis that controlling the 245 efficiency of light absorption (η_L) makes it possible to attain high productivities both in 246 lipid and biomass. The response of the QO controller suggests that an optimal strategy 247 consists in driving the biomass concentration to a certain value and to allow it oscillate 248 around this point. This result is consistent with the work developed by |6| and the the-249 oretical results presented by [16], where an optimal controller was developed by forcing 250 the biomass concentration to fulfill a periodicity condition. 25

252 4.2. Comparison of open loop configurations to optimal strategy

We were interested to assess the performance of the raceway in open loop (OL) config-253 uration. To this end, the model was simulated initially with an input flow rate $f_i = 5.13$ 254 $m^3 d^{-1}$ (dilution rate $D = 0.30 d^{-1}$), which is a typical value [5, 22]. The lipid and biomass 255 productivities were, respectively, 54% and 59% of those obtained with the optimal con-256 trollers CP_x and CP_l . This means that for an open loop configuration, a wrong choice 257 of the input flow rate will imply an unsatisfactory performance. To perform a fair com-258 parison, in addition to the optimal controllers previously calculated, the optimal control 259 problem (14) was solved by setting a constant flow rate. The optimal flow rate was found 260 to be $3.22 \text{ m}^3 \text{ d}^{-1}$ (D = 0.19 d⁻¹) and the resulting biomass productivity was 93% of the 261

one obtained with the optimal controller CP_x . Table 2 summarizes the comparison of the performances of different controllers and configurations evaluated (including the QO controller) relative to the optimal productivities. Additionally, Fig. 4 shows the dependency of the biomass and lipid productivities on the dilution rate. The curves are normalized to illustrate that the both productivities reach their maximal value at the same dilution rate.

The relative high productivity obtained with the optimal constant flow rate is not 268 surprising, since experimental studies on artificial photobioreactors [9, 10] have shown 269 that with an adequate constant flow rate it is possible to attain high productivities. This 270 result may suggest that, when the microalgae are not nutrient limited, the environmen-271 tal conditions, namely light intensity and temperature exert such a strong influence on 272 the system behaviour that the improvement of the performance that can be reached by 273 manipulating the dilution rate is only marginal. This finding might, at first sight, dis-274 courages the endeavour of developing any control strategy for raceways systems, since it 275 appears that even with a constant flow rate, a satisfactory performance can be attained. 276 This result, however, must be taken with caution. Indeed, we argue in favor of the QO 277 controller over the other control strategies and, of course, over open loop operation. The 278 arguments supporting our decision are developed in the following. 279

280 4.3. Robustness of optimal strategies and QO controller

The previous results that indicate that an adequate constant flow rate leads to near 281 optimal operation are derived from very well controlled systems (closed photobioreac-282 tors) or from mathematical models that do not take into account model uncertainty and 283 potential disturbances. Since the QO controller operates in closed loop fashion, it has 284 many practical advantages. For instance, it can be easily tuned for a real scenario that is 285 subjected to disturbances and technical failures. The optimal controllers can also be in 286 closed loop fashion. However, its implementation is more demanding than that of the QO 287 controller. If the optimal controllers are used in open loop, the system can be directed to 288 suboptimal operation. Figure 6 displays the productivities given by the QO controller and 289 the optimal controller CP_x considering uncertainty in the model parameters. The value 290

of $\tilde{\mu}$ was decreased 30% of the value used originally to calculate the optimal controller. It is observed that the QO controller provided a biomass productivity that is 17% higher than that provided by the controller CP_x . It should be noted that this result was achieved with a simple PI controller. We expect that by using a nonlinear controller based on the light efficiency, the productivity might be even better. The design of such a nonlinear controller is one of the perspectives of this work.

297 4.4. Is the strict compensation condition relevant for diurnal light cycles?

The strict compensation condition (implying that the working illuminated fraction 298 $\chi = 1$) has been identified as a necessary condition to attain maximal productivities in 299 closed photobioreactors under light constant regime [37]. The light intensity at which the 300 compensation occurs is often expressed as a constant parameter. Indeed, if the incident 301 light intensity is constant, there exists one value of light intensity at the bottom of the 302 reactor at which the productivity is maximal [21]. However, we might notice that for a 303 varying light system, the light of compensation depends on the actual state of the system 304 and thus there is not a fixed value that will bring the system to operate under the strict 305 compensation condition. 306

For outdoor raceways, where microalgae are exposed to long periods of darkness, 307 respiration affects negatively growth. It is clear that in the dark period, the compensation 308 condition do not play any role on the reactor performance. When the incident light is 309 higher than zero, the strict compensation condition is such that $\mu_L = R$. The light of 310 compensation is thus a dynamic operational variable that depends of the state of the 311 system. The optical depth of the reactor must then be adjusted accordingly to reach 312 the light of compensation at the rear of the reactor. Note that if the reactor volume is 313 constant, the regulation acts on the attenuation factor ξ . This strategy, however, may 314 suffer of reachability problems, as experienced in the study of [9], where the light at the 315 bottom of the photobioreactor could not be maintained at the defined set point due to the 316 dynamic boundary imposed by the growth rate. To enlarge the discussion in this point, 317 we assess by means of simulations if the strict compensation condition could be fulfilled 318 in a diurnal light cycle and if it is relevant to attain such a condition to achieve maximal 319

³²⁰ productivities. The following optimal control problem was defined

$$\min_{f_i(t)} \int_{t_0}^{t_f} (\mu_L - R)^2 dt.$$
(17)

³²¹ The controller optimizing (17) is called CP_c .

Figure 5 shows the ratio between the growth rate at the rear of the raceway (μ_L) and the respiration rate (R). The results are given for the optimal controller CP_c. It is observed that, for the light period, the growth rate at the rear of the raceway is higher than the respiration rate and that the compensation condition is not strictly fulfilled all the time $\chi > 1$. The results indicate that attaining the strict compensation throughout the day might be no physically possible due to the dynamic bound imposed by the growth rate.

The optimal controller CP_c resulted in biomass and lipid productivities that were, 329 100% of those obtained with the optimal controllers CP_x and CP_l . Our results suggest that 330 the closest the system is to the compensation condition the closest the system operates 331 optimally. However, the results also indicate that for a photobioreactor subject to the 332 diurnal light cycle, the strict compensation condition is not a necessary condition to be 333 fulfilled for achieving maximal productivities. We have also verified that trying to impose 334 a compensation condition valid around the midday light peak could be inefficient resulting 335 in low productivities. 336

We must note that when the respiration rate is very low, the strict compensation 337 condition became $\mu_L \approx 0$ implying that $I_L \approx 0$. Here, the compensation condition im-338 plies almost full absorption of light which is rather difficult to maintain throughout the 339 day. Due to the limitation of reachability of the strict compensation condition and the 340 difficulty associated to the online determination of μ_L and R, we suggest that the strict 341 compensation condition is not a practical criterion for the design of control strategies. By 342 contrary, the strategy that we proposed of controlling the efficiency of light absorption 343 η_L is technically feasible for real implementation and provides almost optimal productiv-344 ities. In the near future, an optimal framework of harvesting strategies will be proposed 345 complementary to the QO control. 346

347 5. Conclusion

To summarize, controlling the efficiency of light absorption makes it possible to attain maximal productivities. The overall performance of the QO controller developed here and its practical advantages for real implementation makes it a suitable control strategy for optimizing microalgae production in raceways.

352 6. Acknowledgment

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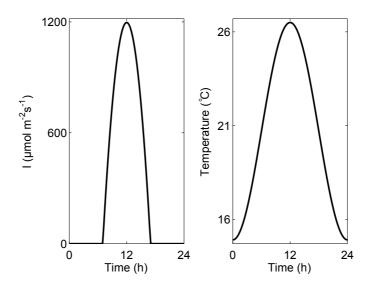


Figure 1: Typical diel variation of light intensity and temperature for the location of Narbonne in June.

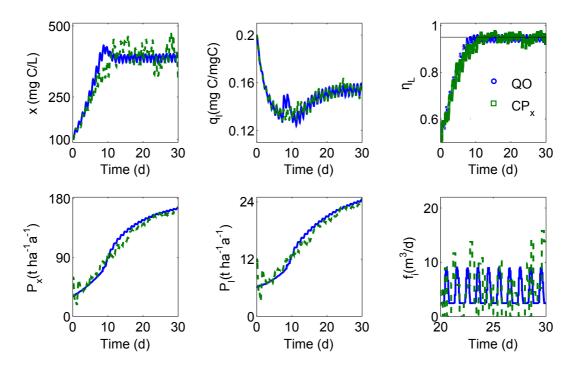


Figure 2: Trajectories of state variables and productivities given by the QO controller (solid blue line) and by the optimal controller CP_x (dashed green line). The productivities are given in dry weight basis. The biomass and lipid productivities given by the QO controller are both 98% of those provided by CP_x . The top right plot shows the evolution η_L during the light period. The horizontal continuous line corresponds to the set point $\eta_L^* = 0.95$.

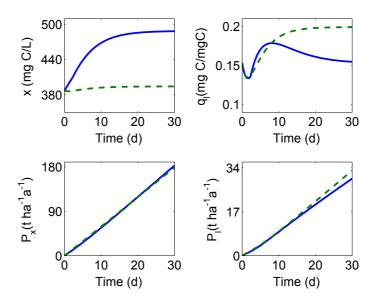


Figure 3: In a photobioreactor with constant incident light, the response of the system when applying a controller to optimize lipid productivity (dashed green line) differs of the response provided by a controller optimizing biomass productivity (solid blue line). Maximizing biomass productivity favors high biomass concentration, while maximizing lipid productivity favors high lipid quota.

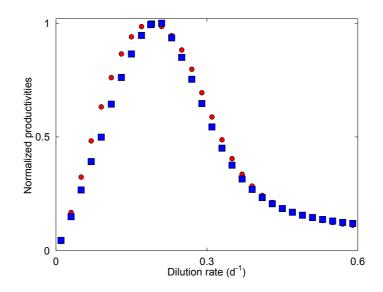


Figure 4: Normalized productivities at different dilution rates. In a raceway reactor, the biomass productivity (circles) and the lipid productivity (squares) reach their maximal value at almost the same dilution rate.

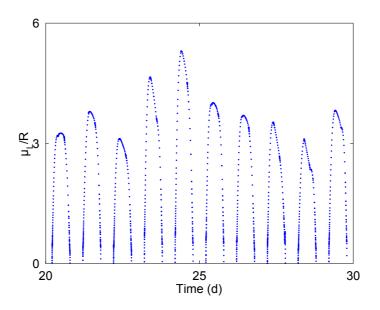


Figure 5: The strict compensation condition ($\mu_L/R=1$) is not attained along the day. Response obtained for the optimal controller CP_c .

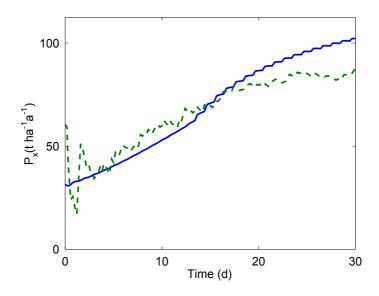


Figure 6: Productivities provided by the QO controller (solid blue line) and the optimal controller CP_x (dashed green line) under parameter uncertainty. The value of $\tilde{\mu}$ was decreased 30%.

	Definition	Units	Value
Variables			
s	Nitrogen concentration	${\rm g~N~m^{-3}}$	
q_l	Neutral lipid quota	g C (g C) ⁻¹	
q_n	Nitrogen quota	g N (g C) $^{-1}$	
x	Carbon biomass concentration	${ m g~C~m^{-3}}$	
x_f	Functional carbon concentration	${ m g~C~m^{-3}}$	
x_g	Carbohydrates carbon concentration	${ m g~C~m^{-3}}$	
x_l	Lipid carbon concentration	${\rm g~C~m^{-3}}$	
Chl	Chlorophyll concentration	g Chl m $^{-3}$	
G_c	Compensation light intensity	$\mu mol photons m^{-2}s^{-1}$	
I_0	Incident light intensity	$\mu mol photons m^{-2}s^{-1}$	
$ar{I}$	Average light intensity	$\mu mol photons m^{-2}s^{-1}$	
I_L	Light intensity at the bottom of the raceway	$\mu \rm mol~photons~m^{-2} s^{-1}$	
I_z	Light intensity at depth z	$\mu \rm mol~photons~m^{-2}s^{-1}$	
T	Raceway temperature	$^{\circ}\mathrm{C}$	
Functions and paramete	rs		
χ	Working illuminated fraction		
η_L	Efficiency of light absoprtion		
ϕ_T	Temperature factor affecting growth kinetics		
λ	Optical depth		
μ	Growth rate	d^{-1}	
$ar{ar{\mu}}$	Average growth rate	d^{-1}	
ρ	Nitrogen uptake rate	g N (g C d) ⁻¹	
$ heta_N$	Chl:N ratio	g Chl (g N) ⁻¹	
ξ	Attenuation factor	m^{-1}	
D	Dilution rate	d^{-1}	
f_{i}	Feeding flow rate	$\mathrm{m}^3~\mathrm{d}^{-1}$	
f_o	Effluent flow rate	$\mathrm{m}^3~\mathrm{d}^{-1}$	
f_r	Rain flow rate	$m^3 d^{-1}$	
f_v	Evaporation flow rate	$m^3 d^{-1}$	
R	Overall respiration rate	d^{-1}	

Table 1: Model notation and parameter values.

α	Protein synthesis coefficient	g C (g N) ⁻¹	3.0
β	Fatty acid synthesis coefficient	${ m g} \ { m C} \ ({ m g} \ { m N})^{-1}$	3.80
ϵ_I	Dissociation light constant.	μ mol photons m ⁻² s ⁻¹	50
φ	Biosynthesis cost coefficient	${ m g} \ { m C} \ ({ m g} \ { m N})^{-1}$	1.30
γ	Fatty acid mobilization coefficient	${ m g} \ { m C} \ ({ m g} \ { m N})^{-1}$	2.90
ν	Reduction factor of nitrogen uptake during night		0.19
$ ilde{\mu}$	Theoretical maximum specific growth rate	d^{-1}	2.11
$\bar{ ho}$	Maximum uptake rate	g N (g C d) ⁻¹	0.10
a	Light attenuation due to chlorophyll	$m^2(g \ Chl)^{-1}$	2.0
b	Light attenuation due to background turbidity	m^{-1}	0.087
g_1	Coefficient Eq. (12)	g N (g Chl) ^{-1}	16.74
g_2	Coefficient Eq. (12)	g N (g Chl °C) ⁻¹	0.39
g_3	Coefficient Eq. (12)	g N (g Chl $\mu \rm{mol}$ photons $\rm{m}^{-2}\rm{s}^{-1})^{-1}$	0.0014
g_4	Coefficient Eq. (12)	$(^{\circ}\mathrm{C})^{-1}$	0.0015
K_s	Nitrogen saturation constant	${ m g~N~m^{-3}}$	0.018
K_{sI}	Light saturation constant	μ mol photons m ⁻² s ⁻¹	150
L	Pond depth	m	0.30
m	Hill coefficient		3.0
Q_l	Saturation cell quota	$g N (g C)^{-1}$	0.20
Q_0	Minimal nitrogen cell quota	$g N (g C)^{-1}$	0.05
r_0	Maintenance respiration rate	d^{-1}	0.01
s_{in}	Influent nitrogen concentration	${ m g~N~m^{-3}}$	50
S	Pond surface	m^2	57
T_{\min}	Lower temperature for microalgae growth	$^{\circ}\mathrm{C}$	-0.20
T_{\max}	Upper temperature for microalgae growth	$^{\circ}\mathrm{C}$	33.30
$T_{\rm opt}$	Temperature at which growth rate is maximal	$^{\circ}\mathrm{C}$	26.70
V	Raceway volume	m^3	17.10

	$100 \mathbf{P}_x/\mathbf{P}_x^*$	$100\mathrm{P}_l/\mathrm{P}_l^*$
QO	98%	98%
CP_c	100%	100%
OL: $f_i^{\star} = 3.22 \text{ m}^3 \text{ d}^{-1}$	93%	91%
OL: $f_i = 5.13 \text{ m}^3 \text{ d}^{-1}$	54%	59%

Table 2: Productivity performance of open loop (OL) configuration and closed loop controller. The resulting performance is presented relative to the optimal strategy.

* stands for the productivities obtained by the optimal controllers CP_x and CP_l . \star optimal constant flow rate.