Translating EB3 to LNT for verification with CADP

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Verification of EB^3 Specifications using CADP

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Abstract. EB^3 is a specification language for information systems. The core of the EB^3 language consists of process algebraic specifications describing the behaviour of the entities in a system, and attribute function definitions describing the entity attributes. The verification of EB^3 specifications against temporal properties is of great interest to users of EB^3. In this paper, we propose a translation from EB^3 to LOTOS NT (LNT for short), a value-passing concurrent language with classical process algebra features. Our translation ensures the one-to-one correspondence between states and transitions of the labelled transition systems corresponding to the EB^3 and LNT specifications. We automated this translation with the EB^{3}2LNT tool, thus equipping the EB^3 method with the functional verification features available in the CADP toolbox.

1 Introduction

The EB^3 method [10] is an event-based paradigm tailored for information systems (ISs). A typical EB^3 specification defines entities, associations, and their respective attributes. The process algebraic nature of EB^3 enables the explicit definition of intra-entity constraints, making them easy for the IS designer to review and understand. Yet its specificity compared to classical process algebras, such as CSP [15], lies in the use of *attribute functions*, a special kind of recursive functions evaluated on the system execution trace. Combined with guards, attribute functions facilitate the definition of complex inter-entity constraints involving the history of events. The use of attribute functions simplifies system understanding, enhances code modularity, and streamlines maintenance. However, given that ISs are complex systems involving data management and concurrency, a rigorous design process based on formal specification using EB^3 must be completed with effective formal verification features.

Existing attempts for verifying EB^3 specifications are based on translations from EB^3 to other formal methods equipped with verification capabilities. A first line of work [13, 14] focused on devising translations from EB^3 attribute functions and processes to the B method [2], which opened the way for proving invariant properties of EB^3 specifications using tools like Atelier B [6]. Another line of

work concerned the verification of temporal logic properties of EB^3 specifications by means of model checking techniques. For this purpose, the formal description and verification of an IS case-study using six model checkers was undertaken in [9, 5]. This study revealed the necessity of branching-time logics for accurately characterizing properties of ISs, and also the fact that process algebraic languages are suitable for describing the behaviour and synchronization of IS entities. However, no attempt of providing a systematic translation from EB^3 to a target language accepted as input by a model checker was made so far.

In this paper, we aim at filling this gap by proposing a translation from EB^3 to LNT [7], a process algebraic specification language inspired from E-LOTOS [16]. As far as we know, this is the first tentative to provide a general translation from EB^3 to a classical value-passing process algebra. It is worth noticing that CSP and LNT were already considered in [9] for describing ISs, and identified as candidate target languages for translating EB^3. Since our primary objective was to provide temporal property verification features for EB^3, we focused our attention on LNT, which is one of the input languages accepted by the CADP verification toolbox [11], and hence is equipped with on-the-fly model checking for action-based, branching-time logics involving data.

At first sight, given that EB^3 has a structured operational semantics underlied by a labelled transition system (LTS) model, its translation to a process algebra may seem straightforward. However, this exercise proved to be rather involved, the main difficulty being to translate a history-based language to a process algebra with standard LTS semantics. To overcome this difficulty, we considered an alternative memory-based semantics of EB^3 [18], which was shown to be equivalent to the original trace-based semantics defined for finite-state systems in [10]. Another important ingredient of the translation was the multiway value-passing rendezvous of LNT, which enabled to obtain a one-to-one correspondence between the transitions of the two LTSs underlying the EB^3 and LNT descriptions, and hence to preserve strong bisimulation. The presence of array types and of usual programming language constructs (e.g., loops and conditionals) in LNT was also helpful for specifying the memory, the Kleene star-closure operators, and the EB^3 guarded expressions containing attribute function calls. At last, the constructed data types and pattern-matching mechanisms of LNT enabled a natural description of EB^3 data types and attribute functions.

We implemented our translation in the EB^{3}2LNT tool, thus making possible the analysis of EB^3 specifications using all the state-of-the-art features of the CADP toolbox, in particular the verification of data-based temporal properties expressed in MCL [17] using the on-the-fly model checker EVALUATOR 4.0.

The paper is organized as follows. Sections 2 and 3 give an overview of the EB^3 and LNT languages, respectively. Section 4 presents in detail our translation from EB^3 to LNT, implemented by the EB^{3}2LNT translator. Section 5 shows an application of this tool, in conjunction with CADP, for verifying the correctness requirements of an IS. Finally, Section 6 summarizes the results and draws up lines for future work.

$$
\begin{array}{l}
EB^3 ::= A_1; \ldots; A_n; S_1; \ldots; S_m \\
\quad A ::= f\,(\mathsf{T} : \mathcal{T}, \overline{y} : \overline{T}) : T = \textbf{match}\ \mathit{last}\,(\mathsf{T})\ \textbf{with} \\
\qquad\quad \bot : v_0 \mid \alpha_1\,(\overline{x_1}) : v_1 \mid \ \ldots\ \mid \alpha_q\,(\overline{x_q}) : v_q\ [\mid \_ : v_{q+1}] \\
\quad S ::= P\,(\overline{x}) = E \\
\quad E ::= \lambda \mid \alpha\,(\overline{v}) \mid E_1.E_2 \mid E_1 \mid E_2 \mid E_0{}^* \mid E_1 \mid\![\Delta]\!\mid E_2 \mid \mid\! x : V : E_0 \mid \\
\qquad \mid\![\Delta]\!\mid x : V : E_0 \mid C \Rightarrow E \mid P\,(\overline{v})
\end{array}
$$

Fig. 1. EB^3 syntax

2 The Language EB^3

The EB^3 method has been specially designed to specify the functional behaviour of ISs. A standard EB^3 specification comprises (1) a class diagram representing entity types and associations for the IS being specified, (2) a process algebra specification, denoted by *main*, describing the IS, i.e., the valid traces of execution describing its behaviour, (3) a set of attribute function definitions, which are recursive functions on the system execution trace, and (4) input/output rules to specify outputs for input traces, or SQL expressions used to specify queries on the class diagram. We limit the presentation to the process algebra and the set of attribute functions. The EB^3 syntax is presented in Figure 1 and the EB^3 trace semantics Sem_{T} [10] is given in Figure 2 as a set of rules named T_1 to T_{11}. Both figures are commented below.

Process expressions. We write $x, y, z, x_1, x_2, \ldots$ for variables and $v, w, v_1, v_2, \ldots$ for data expressions over user-defined domains, such as integers, Booleans and more complex domains that we do not give formally, for conciseness. Expressions are built over variables, constants, and standard operations.

We also use the overlined notation as a shorthand notation for lists, e.g., $\overline{x}$ denotes a list of variables $x_1, \ldots, x_n$ of arbitrary length. An EB^3 specification consists of a set of attribute function definitions $A_1, \ldots, A_n$, and of a set of process definitions of the form "$P\,(\overline{x}) = E$", where P is a process name and E is a *process expression*.

Let *Act* be a set of *actions* written $\rho, \rho_1, \rho_2, \ldots$ and *Lab* be a set of *labels* written $\alpha, \alpha_1, \alpha_2, \ldots$ Each action ρ is either the *internal action* written λ, or a *visible action* of the form "$\alpha\,(\overline{v})$", where $\alpha \in \mathit{Lab}$. An action ρ is the simplest process expression, whose semantics are given by rule T_1. The symbol $\surd$ (which is not part of the syntax) denotes successful execution. The *trace* T (implicit in the presentation) of an EB^3 specification at a given moment consists of the sequence of visible actions executed since the start of the system. (Note therefore that λ does not appear in the trace.) At system start, the trace is empty. If T denotes the current trace and action ρ can be executed, then $\mathsf{T}.\rho$ denotes the trace just after executing ρ.

EB^3 processes can be combined with classical process algebra operators such as the *sequence* "$E_1.E_2$" ($\mathsf{T}_2, \mathsf{T}_3$), the *choice* "$E_1 \mid E_2$" ($\mathsf{T}_4$) and the *Kleene* closure "$E_0{}^*$" ($\mathsf{T}_5, \mathsf{T}_6$). Rules ($\mathsf{T}_7$ to T_9) define *parallel* composition "$E_1 \mid\![\Delta]\!\mid E_2$"

$$(\mathsf{T}_1)\ \frac{}{\rho \xrightarrow{\rho} \surd} \qquad (\mathsf{T}_7)\ \frac{E_1 \xrightarrow{\rho} E_1' \qquad E_2 \xrightarrow{\rho} E_2'}{E_1 \,|[\Delta]|\, E_2 \xrightarrow{\rho} E_1' \,|[\Delta]|\, E_2'}\ in\,(\rho, \Delta)$$

$$(\mathsf{T}_2)\ \frac{E_1 \xrightarrow{\rho} E_1'}{E_1.E_2 \xrightarrow{\rho} E_1'.E_2} \qquad (\mathsf{T}_8)\ \frac{E_1 \xrightarrow{\rho} E_1'}{E_1 \,|[\Delta]|\, E_2 \xrightarrow{\rho} E_1' \,|[\Delta]|\, E_2}\ \neg in\,(\rho, \Delta)$$

$$(\mathsf{T}_3)\ \frac{E_2 \xrightarrow{\rho} E_2'}{\surd.E_2 \xrightarrow{\rho} E_2'} \qquad (\mathsf{T}_9)\ \frac{}{\surd \,|[\Delta]|\, \surd \xrightarrow{\lambda} \surd}$$

$$(\mathsf{T}_4)\ \frac{E_1 \xrightarrow{\rho} E_1'}{E_1 \mid E_2 \xrightarrow{\rho} E_1'} \qquad (\mathsf{T}_{10})\ \frac{E_0 \xrightarrow{\rho} E_0'}{C \Rightarrow E_0 \xrightarrow{\rho} E_0'}\ \|C\|$$

$$(\mathsf{T}_5)\ \frac{}{E_0{}^* \xrightarrow{\lambda} \surd} \qquad (\mathsf{T}_{11})\ \frac{E[\overline{x} := \overline{v}] \xrightarrow{\rho} E'}{P\,(\overline{v}) \xrightarrow{\rho} E'}\ P\,(\overline{x}) = E$$

$$(\mathsf{T}_6)\ \frac{E_0 \xrightarrow{\rho} E_0'}{E_0{}^* \xrightarrow{\rho} E_0'.E_0{}^*}$$

Fig. 2. EB^3 trace semantics Sem_{T}

of E_1, E_2 with synchronization on $\Delta \subseteq Lab$. The condition "$in\,(\rho, \Delta)$" is true iff the label of ρ belongs to Δ. The symmetric rules for choice and parallel composition have been omitted for brevity. Expressions "$E_1 \,|||\, E_2$" and "$E_1 \,||\, E_2$" are equivalent respectively to "$E_1 \,|[\emptyset]|\, E_2$" and "$E_1 \,|[Lab]|\, E_2$".

The *guarded expression* process "$C \Rightarrow E_0$" (T_{10}) can execute E_0 if the Boolean condition C holds, which is denoted by the side condition "$\|C\|$". Since C may contain calls to attribute functions, its evaluation depends on the trace obtained up to the moment when the condition is evaluated. Note that the evaluation of the guard C and the execution of the first action ρ in E_0 are simultaneous, i.e., no action is allowed in concurrent processes in the meantime. We call this property the *guard-action atomicity*. This property is essential for consistency as, by side effects, the occurrence of actions in concurrent processes could implicitly change the value of C before the guarded action has been executed.

Quantification is permitted for *choice* and *parallel* composition. If V is a set of expressions $\{v_1, \ldots, v_n\}$, "$\mid x : V : E_0$" and "$|[\Delta]| x : V : E_0$" stand respectively for "$E_0[x := v_1] \mid \ldots \mid E_0[x := v_n]$" and "$E_0[x := v_1] \,|[\Delta]|\, \ldots \,|[\Delta]|\, E_0[x := v_n]$", where "$E[x := v]$" denotes the replacement of all occurrences of x by v in E. For instance, "$||\, x : \{1, 2, 3\} : a\,(x)$" stands for "$a\,(1) \,||\, a\,(2) \,||\, a\,(3)$". At last, named processes can be instantiated as usual (T_{11}). Given an EB^3 process expression E, we write $vars\,(E)$ for the set of variables occurring free in E.

Attribute functions. Attribute functions definitions are denoted by the symbol A in the grammar of Figure 1. Attribute functions are defined recursively on the current trace T representing the history of actions executed, with the aid of functions $last\,(\mathsf{T})$ which denotes the last action of the trace, and $front\,(\mathsf{T})$

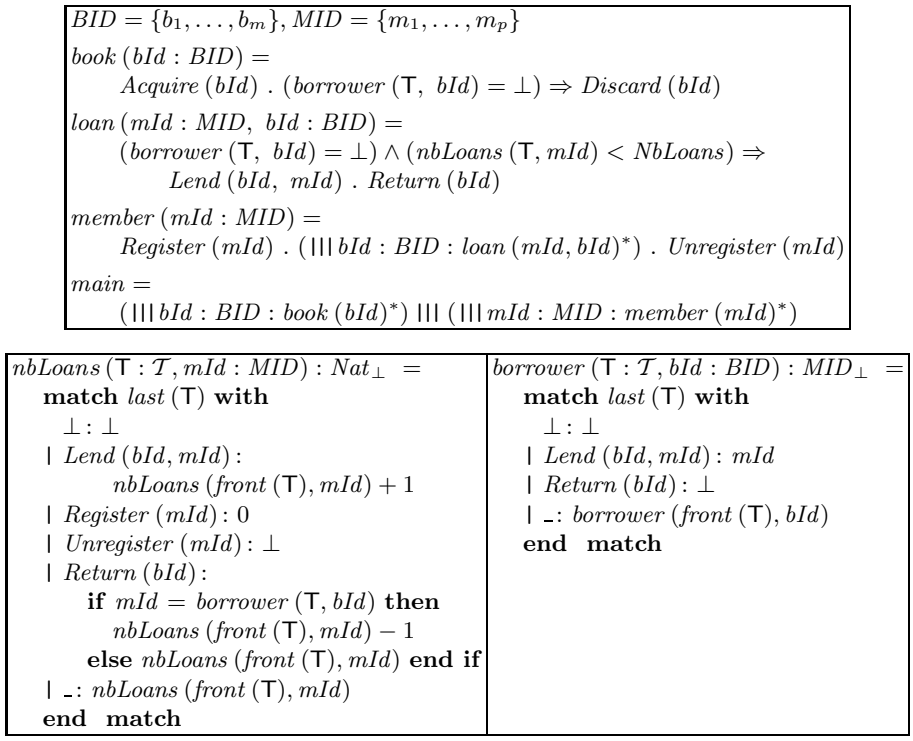

Fig. 3. EB^3 specification of a library management system

which denotes the trace without its last action. The symbol $\bot$ represents the undefined value. In particular, both $last\,(\mathsf{T})$ and $front\,(\mathsf{T})$ match $\bot$ when the trace is empty. The symbol _ (wildcard) matches all actions not matched by any of the preceding action patterns $\alpha_1\,(\overline{x_1}), \ldots, \alpha_q\,(\overline{x_q})$. Each v_i $(i \in 0..n)$ is an expression of the same type as f's return type built over the variables $\overline{y} \cup \overline{x_i}$.

For defining a formal semantics for attribute functions, the semantics of Figure 1 has to be expanded with trace and memory contexts for each process, representing the sequence of actions executed since the process was initiated, and the value of attribute functions for the current trace and any value for the rest of their arguments, stored into process memory M. Due to space limitations, we do not present the formal semantics here, but show how attribute functions are evaluated on a concrete example. The formal trace-memory semantics for attribute functions can be found in the companion paper [18].

Example. We give an example of how the Trace/Memory Semantics works for a simplified library management system, whose specification (processes and attribute functions) in EB^3 is given in Figure 3. Process *main* is the parallel interleaving between m instances of process *book* and p instances of process *member*. Process *book* stands for a book acquisition followed by its eventual

discard. The attribute function "*borrower* $(\mathsf{T},\ bId)$" looks for actions of the form "*Lend* (mId, bId)" or "*Return* (bId)" in the trace and returns the current borrower of book *bId* or $\perp$ if the book is not lent. In process book, action "*Discard* (bId)" is thus guarded to guarantee that book *bId* cannot be discarded if it is currently lent.

We illustrate how the EB^3 specification describing the library management system is evaluated. The idea lies in the observation that attribute functions can be turned into state variables (the memory M) carrying the effect of the system trace on their corresponding values. This avoids keeping the (ever-growing) trace leading to a finite state model. If $f\,(\mathsf{T}, x_1{:}T_1, \ldots, x_l{:}T_l)$ is an attribute function, we construct $|T_1| \times \ldots \times |T_l|$ state variables, where $|T_i|$ $(i \in 1..l)$ stands for T_i's cardinality.

As an example, we set $m = p = NbLoans = 2$, i.e. we consider two books b_1 and b_2, and two members m_1 and m_2. The memory has four cells: $\mathsf{M} = (borrower\,[b_1]\,, borrower\,[b_2]\,, nbLoans\,[m_1]\,, nbLoans\,[m_2]\,)$, the first two cells keep the two values of the attribute function $(borrower)(\mathsf{T}, \bullet)$ for a given trace T, and the two last keeping the values of $nbLoans(\mathsf{T}, \bullet)$. After every step, the new value of each cell can be calculated from the previous memory and the action that has just been executed. The memory is initially set to $(\perp, \perp, \perp, \perp)$. After the trace "*Acquire* (b_1).*Acquire* (b_2).*Register* (m_1).*Register* (m_2)" the memory contains $(\perp, \perp, 0, 0)$. If action "*Lend*(b_1, m_1)" is then executed, the new memory is $(m_1, \perp, 1, 0)$. For instance, the new value m_1 for $borrower\,[b_1]$ is obtained from the rule "*Lend*(bId, mId) : *mId*" in the definition of the attribute function *borrower* (see Fig. 3), and the new value 1 for $nbLoans\,[m_1]$ by the rule "*Lend*(bId, mId) : *nbLoans* $(front\,(\mathsf{T}), mId) + 1$" of the attribute function *nbLoans*, where the value of *nbLoans* $(front\,(\mathsf{T}), m_1)$ corresponds to the value of $nbLoans\,[m_1]$ in the previous memory state (value 0).

3 The Language LNT

LNT aims at providing the best features of imperative and functional programming languages and value-passing process algebras. It has a user friendly syntax and formal operational semantics defined in terms of labeled transition systems (LTSs). LNT is supported by the LNT.OPEN tool of CADP, which allows the on-the-fly exploration of the LTS corresponding to an LNT specification.

We present the fragment of LNT that serves as the target of our translation. Its syntax is given in Figure 4. LNT terms denoted by B are built from actions, choice (**select**), conditional (**if**), sequential composition (**;**), breakable loop (**loop** and **break**) and parallel composition (**par**). Communication is carried out by rendezvous on gates, written G, G_1, ..., G_n, and may be guarded using Boolean conditions on the received values (**where** clause). LNT allows multiway rendezvous with bidirectional (send/receive) value exchange on the same gate occurrence, each offer O being either a send offer (**!**) or a receive offer (**?**), independently of the other offers. Expressions E are built from variables, type constructors, function applications and constants. Labels L identify loops,

$$
\begin{array}{l}
B ::= \textbf{stop} \mid \textbf{null} \mid G\,(O_1, \ldots, O_n)\ \textbf{where}\ E \mid B_1; B_2 \\
\quad \mid\ \textbf{if}\ E\ \textbf{then}\ B_1\ \textbf{else}\ B_2\ \textbf{end if} \mid \textbf{var}\ x{:}T\ \textbf{in}\ B\ \textbf{end var} \mid x := E \mid \\
\quad \mid\ \textbf{loop}\ L\ \textbf{in}\ B\ \textbf{end loop} \mid \textbf{break}\ L \mid \textbf{select}\ B_1\ \texttt{[]}\ \ldots\ \texttt{[]}\ B_n\ \textbf{end select} \\
\quad \mid\ \textbf{par}\ G_1, \ldots, G_n\ \textbf{in}\ B_1\ \texttt{||}\ \ldots\ \texttt{||}\ B_n\ \textbf{end par} \mid P\,\texttt{[}G_1, \ldots, G_n\texttt{]}\,(E_1, \ldots, E_n) \\
O ::= \texttt{!}\,E \mid\ \texttt{?}x
\end{array}
$$

Fig. 4. LNT syntax (limited to the fragment used in this paper)

which can be escaped using "**break** L" from inside the loop body. Processes are parameterized by gates and data variables. LNT semantics are formally defined in SOS style in [7].

4 Translation from EB^3 to LNT

Principles. Our translation of EB^3 relies on semantics Sem_{M}. Thus, we explicitly model in LNT a memory, which stores the state variables corresponding to attribute functions (we call these variables *attribute variables*) and is modified each time an action is executed.

Assuming n attribute functions $f_1, \ldots, f_n$, we model the memory as a process M placed in parallel with the rest of the system (a common approach for modeling global variables in process algebras), which manages for each attribute function f_i an attribute variable (also named f_i) that encodes the function. To read the values of these attribute variables (i.e., to evaluate the attribute functions), processes need to communicate with the memory M, and every action must have an immediate effect on the memory (so as to reflect the immediate effect on the execution trace). To achieve this, the memory process synchronizes with the rest of the system on every possible action of the system (including λ, to which we associate an LNT gate also written λ for convenience), and updates its attribute variables accordingly. The list of attribute variables $\overline{f} = (f_1, \ldots, f_n)$ is added as a supplementary offer on each EB^3 action $\alpha\,(\overline{v})$, so that attribute variables can be directly accessed to evaluate the guard associated to the action, wherever needed, while guaranteeing the guard-action atomicity. Therefore, every action $\alpha\,(\overline{v})$ will be encoded in LNT as $\alpha\,(\texttt{!}\,\overline{v}, \texttt{?}\,\overline{f})$, and synchronized with an action of the form $\alpha\,(\texttt{?}\,\overline{x}, \texttt{!}\,\overline{f})$ in the memory process M, thus taking benefit of bidirectional value exchange during the rendezvous.

Translation of attribute functions. To formalize the translation, we assume $Lab = \{\alpha_1, \ldots, \alpha_q\}$ (not including λ), each α_j has formal parameters $\overline{x_j}$, $\{f_1, \ldots, f_n\}$ is the set of attribute functions, and each f_i is uniquely defined by the set of formal parameters $\overline{y_i}$ and the set of data expressions $w_i^0, \ldots, w_i^q$, such that:

$$f_i\,(\mathsf{T}, \overline{y_i}) = \textbf{match}\ \mathit{last}\,(\mathsf{T})\ \textbf{with}\ \bot : w_i^0 \mid \alpha_1\,(\overline{x_1}) : w_i^1 \mid \ \ldots\ \mid \alpha_q\,(\overline{x_q}) : w_i^q$$

We also assume that the attribute functions are ordered, so that for all $h \in 1..n, i \in 1..n, j \in 1..q$, every function call of the form $f_h\,(\mathsf{T}, \ldots)$ occurring in w_i^j

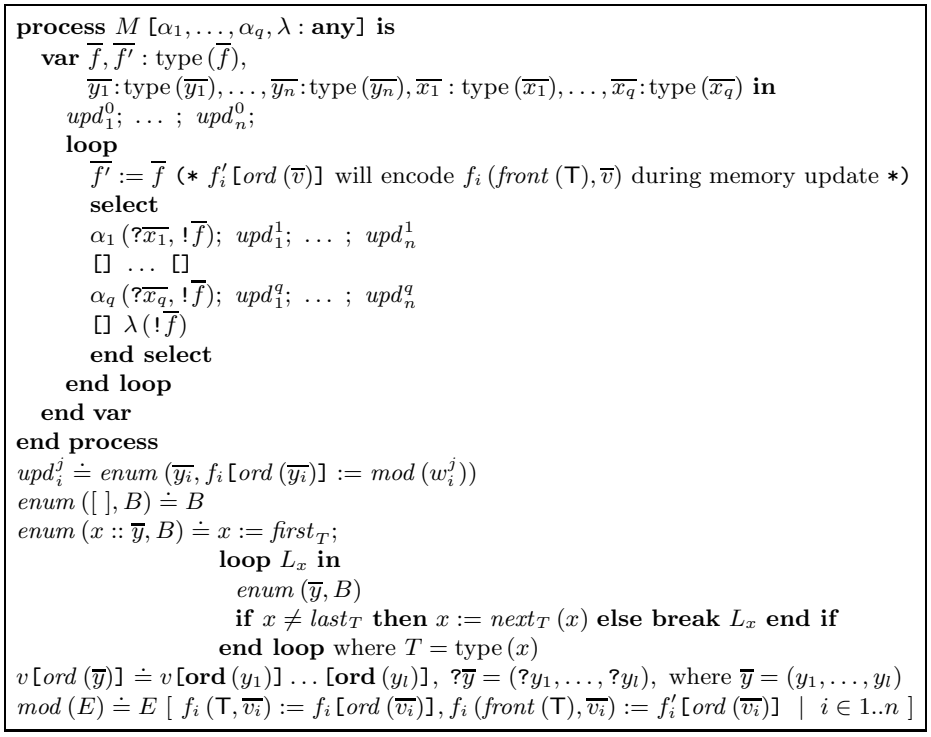

Fig. 5. LNT code for the memory process implementing attribute functions

satisfies $h < i$ and every call of the form $f_h\ (front\ (\mathsf{T}), \ldots)$ satisfies $h \geq i$. Such an ordering can be constructed if the EB^3 specification does not contain circular dependencies between function calls, which would potentially lead to infinite attribute function evaluation. In particular, the definition of an attribute function f_i cannot contain recursive calls of the form "$f_i\ (\mathsf{T}, \ldots)$", but only recursive calls of the form "$f_i\ (front\ (\mathsf{T}), \ldots)$". Note that this does not limit the expressiveness of EB^3 attribute functions, because every recursive computation on data expressions only (which keeps the trace unchanged) can be described using standard functions and not attribute functions.

Ordering attribute functions in this way allows the memory to be updated consistently, from f_1 to f_n in turn. At every instant, already-updated values correspond to calls of the form $f_h\ (\mathsf{T}, \ldots)$ (the value of f_h on the current trace), whereas calls of the form $f_h\ (front\ (\mathsf{T}), \ldots)$ are replaced by accesses to a copy $\overline{f'}$ of the memory $\overline{f}$, which was made before starting the update. This encoding thus enables the trace parameter to be discharged from function calls, ensuring that while updating f_i, accesses to f_h with $h < i$ necessarily correspond to calls with parameter T.

Process M is defined in Figure 5. It runs an infinite loop, which "listens" to all possible actions α_j of the system. Each attribute variable f_i is an array with l_i dimensions, where l_i is the arity of the attribute function f_i minus 1 (because

the trace parameter is now discharged). Each dimension of the array f_i thus corresponds to one formal parameter in $\overline{y_i}$, so that $f_i\,[\mathbf{ord}\,(v_1)]\,\ldots\,[\mathbf{ord}\,(v_{l_i})]$ encodes the current value of $f_i\,(\mathsf{T}, v_1, \ldots, v_{l_i})$, where $\mathbf{ord}\,(v)$ is a predefined LNT function that denotes the *ordinate* of value v, i.e., a unique number between 1 and the cardinal of v's type. For each type T we assume the existence of functions first_T that returns the first element of type T, last_T that returns the last element of type T, and $\mathit{next}_T\,(x)$ that returns the successor of x in type T (following the total order induced by **ord**). Such functions are available in LNT for all finite types. Function *mod* transforms an expression E by syntactically replacing function calls by array accesses, while discharging the trace parameter as explained above.

Upon synchronisation on action $\alpha_j\,(?\overline{x_j}, !\,\overline{f})$ with the LNT process corresponding to EB^3's *main* process (see translation of processes below), the values of all attribute variables f_i $(i \in 1..n)$ are updated using function upd_i^j.

Translation of processes. We define a translation function t from an EB^3 process expression to an LNT process. Most EB^3 constructs are process algebra constructs with a direct correspondence in LNT. The main difficulty arises in the translation of guarded process expressions of the form "$C \Rightarrow E_0$" in a way that guarantees the guard-action atomicity. This led us to consider a second parameter for the translation function t, namely the condition C, whose evaluation is delayed until the first action occurring in the process expression E_0. The definition of $t\,(E, C)$ is given in Figure 6. An EB^3 specification E_0 will then be translated into "**par** $\alpha_1, \ldots, \alpha_q, \lambda$ **in** $t\,(E_0, \mathrm{true})$ || M [$\alpha_1, \ldots, \alpha_q, \lambda$] **end par**" and every process definition of the form "$P\,(\overline{x}) = E$" will be translated into the process "**process** P [$\alpha_1, \ldots, \alpha_q, \lambda$: **any**] $(\overline{x} : \mathrm{type}\,(\overline{x}))$ **is** $t\,(E, \mathrm{true})$ **end process**", where $\{\alpha_1, \ldots, \alpha_q\} = \mathit{Lab}$.

The rules of Figure 6 can be commented as follows:

- Rule (1) translates the λ action. Note that λ cannot be translated to the empty LNT statement **null**, because execution of λ may depend on a guard C, whose evaluation requires the memory to be read, so as to get attribute variable values. This is done by the LNT communication action $\lambda\,(?\overline{f})$. The guard C is evaluated after replacing calls to attribute functions (all of which have the form $f_i\,(\mathsf{T}, \overline{v_i})$) by the appropriate attribute variables, using function *mod* defined in Figure 5. Rule (2) is similar but handles visible actions.
- Rule (3) translates EB^3 sequential composition into LNT sequential composition. By doing so, the evaluation of C is passed to the first process expression.
- Rule (4) makes a conjunction between the guard of the current process expression with the guard already accumulated from the context.
- Rules (5) and (6) translate the choice and quantified choice operators of EB^3 into their direct LNT counterpart.
- Rule (7) translates the Kleene closure into a combination of LNT loop and select, following the identity ${E_0}^* = \lambda \mid E_0.{E_0}^*$.
- Rule (8) translates EB^3 parallel composition into LNT parallel composition.

$$t(\lambda, C) = \lambda(?\overline{f}) \textbf{ where } mod(C) \quad (1)$$

$$t(\alpha(\overline{v}), C) = \alpha(\overline{v}, ?\overline{f}) \textbf{ where } mod(C) \quad (2)$$

$$t(E_1.E_2, C) = t(E_1, C);\ t(E_2, \text{true}) \quad (3)$$

$$t(C' \Rightarrow E_0, C) = t(E_0, C \textbf{ and } C') \quad (4)$$

$$t(E_1 \mid E_2, C) = \textbf{select } t(E_1, C) \text{ [] } t(E_2, C) \textbf{ end select} \quad (5)$$

$$t(|x : V : E_0, C) = \textbf{var } x := \textbf{any } V;\ t(E_0, C) \textbf{ end var} \quad (6)$$

$$t(E_0{}^*, \text{true}) = \textbf{loop } L_{E_0} \textbf{ in } \textbf{select } \lambda(?\overline{f});\ \textbf{break } L_{E_0} \text{ [] } t(E_0, \text{true}) \textbf{ end select end loop} \quad (7)$$

$$t(E_1 \ |[\Delta]|\ E_2, \text{true}) = \textbf{par } \Delta \textbf{ in } t(E_1, \text{true}) \ ||\ t(E_2, \text{true}) \textbf{ end par} \quad (8)$$

$$t(|[\Delta]| x : V : E_0, \text{true}) = \textbf{par } \Delta \textbf{ in } E_0[x := v_1] \ ||\ \ldots \ ||\ E_0[x := v_n] \textbf{ end par} \quad \text{where } V = \{v_1, \ldots, v_n\} \quad (9)$$

$$t(P(\overline{v}), \text{true}) = P\ [\alpha_1, \ldots, \alpha_q, \lambda]\ (\overline{v}) \quad (10)$$

In all other cases:

$$t(E_0, C) = \begin{cases} \textbf{if } mod(C) \textbf{ then } t(E_0, \text{true}) \textbf{ else stop end if} \\ \quad \text{if } C \text{ does not use attribute functions} \\ \textbf{par } \alpha_1, \ldots, \alpha_q, \lambda \textbf{ in} \\ \quad t(E_0, \text{true}) \\ \ ||\ pr_C\ [\alpha_1, \ldots, \alpha_q, \lambda]\ (vars(C)) \\ \textbf{end par} \qquad \text{otherwise} \end{cases} \quad (11)$$

Fig. 6. Translation from EB^3 process to LNT process

- Rule (9) translates EB^3 quantified parallel composition into LNT parallel composition by expanding the type V of the quantification variable, since LNT does not have a quantified parallel composition operator.
- Rule (10) translates an EB^3 process call into the corresponding LNT process call, which requires gates to be passed as parameters.
- Rules (7) to (10) only apply when the guard C is trivially true. In the other cases, we must apply rule (11), which generates code implementing the guard. If C does not use attribute functions, i.e., does not depend on the trace, then it can be evaluated immediately without communicating with the memory process (first case). Otherwise, the guard evaluation must be delayed until the first action of the process expression E_0. When E_0 is either a Kleene closure, a parallel composition, or a process call, identifying its first action syntactically is not obvious. One solution would consist in expanding E_0 into a choice in which every branch has a fixed initial action[3], to which the guard would be added. We preferred an alternative solution that avoids the potential combinatorial explosion of code due to static expansion. A process

[3] Such a form, commonly called *head normal form* [3], is used principally in the context of the process algebra ACP [4] to analyse the behaviour of recursive processes.

```
process pr_C [α_1, ..., α_q, λ : any] (vars (C) : type (vars (C))) is
var b : bool, x_1 : type (x_1), ..., x_q : type (x_q) in
  b := true;
  loop L in select
    if b then
      b := false;
      select
        α_1 (?x_1, ?f) where mod (C)
        [] ... []
        α_q (?x_q, ?f) where mod (C)
        []
        λ (?f) where mod (C)
      end select
    else
      select
        α_1 (?x_1, ?f)
        [] ... []
        α_q (?x_q, ?f)
        []
        λ (?f)
      end select
    end if
  [] break L end select end loop
end var
end process
```

Fig. 7. Process pr_C

pr_C (defined in Fig. 7) is placed in parallel to $t\,(E_0, \text{true})$ and both processes synchronize on all actions. Process pr_C imposes on $t\,(E_0, \text{true})$ the constraint that the first executed action must satisfy the condition C (**then** branch). For subsequent actions, the condition is relaxed (**else** branch).

Theorem 1. *Let E, E' be* EB^3 *process expressions, T be the current trace, $\overline{f}$ be the set of attribute functions, and $\rho \in Act$. Then:*

$$E \xrightarrow{\rho\,(\overline{x})} E' \text{ if and only if}$$
$$t\,(E, true) \xrightarrow{\rho\,(\overline{x},\overline{f})} t\,(E', true) \wedge (\forall f_i \in \overline{f})\ (\forall \overline{v})\ f_i\,(\mathsf{T}, \overline{v}) = f_i\,[ord(\overline{v})]\,.$$

The proof strategy for Theorem 1 relies on the existence of a bisimulation between each EB^3 specification and its corresponding LNT translation. It works by providing a match between the reduction rules of EB^3 [18] and the corresponding LNT rules [7]. The proof will be available in the extended version of the paper.

We developed an automatic translator tool from EB^3 specifications to LNT, named EB^{3}2LNT, implemented using the Ocaml Lex/Yacc compiler construction technology. It consists of about 900 lines of OCaml code. We applied EB^{3}2LNT

on a benchmark of EB^3 specifications, which includes variations of the library management system (examined in its simplest version in Section 2) and a bank account management system.

We noticed that for each EB^3 specification the equivalent LNT specification is twice as big. Part of this expansion is caused by the fact that LNT is more structured than EB^3: LNT requires more keywords and gates have to be declared and passed as parameters to each process call. By looking at the rules of Figure 6, we can see that the other causes of expansion are rule (5), which duplicates the condition C, and rule (9), which duplicates the body E_0 of the quantified parallel composition operator "$|[\Delta]|\, x : V : E_0$" as many times as there are elements in the set V. Both expansions are linear in the size of the source EB^3 code. However, in the case of a nested parallel composition "$|[\Delta_1]|\, x_1 : V_1 : \ldots\ |[\Delta_n]|\, x_n : V_n : E_0$", the expansion factor is as high as the product of the number of elements in the respective sets $V_1, \ldots, V_n$, which may be large. If E_0 is a big process expression, the expansion can be limited by encapsulating E_0 in a parameterized process "$P_{E_0}\,(x_1, \ldots, x_n)$" and replacing duplicated occurrences of E_0 by appropriate instances of P_{E_0}.

5 Case Study

We illustrate below the application of the EB^{3}2LNT translator in conjunction with CADP for analyzing an extended version of the IS library management system, whose description in EB^3 can be found in Annex C of [12]. With respect to the simplified version presented in Section 2, the IS enables e.g., members to renew their loans and to reserve books, and their reservations to be cancelled or transferred to other members on demand. The desired behaviour of this IS was characterized in [9] as a set of 15 requirements expressed informally as follows:

R1. A book can always be acquired by the library when it is not currently acquired.
R2. A book cannot be acquired by the library if it is already acquired.
R3. An acquired book can be discarded only if it is neither borrowed nor reserved.
R4. A person must be a member of the library in order to borrow a book.
R5. A book can be reserved only if it has been borrowed or already reserved by some member.
R6. A book cannot be reserved by the member who is borrowing it.
R7. A book cannot be reserved by a member who is reserving it.
R8. A book cannot be lent to a member if it is reserved.
R9. A member cannot renew a loan or give the book to another member if the book is reserved.
R10. A member is allowed to take a reserved book only if he owns the oldest reservation.
R11. A book can be taken only if it is not borrowed.
R12. A member who has reserved a book can cancel the reservation at anytime before he takes it.
R13. A member can relinquish library membership only when all his loans have been returned and all his reservations have either been used or cancelled.
R14. Ultimately, there is always a procedure that enables a member to leave the library.
R15. A member cannot borrow more than the loan limit defined at the system level for all users.

We expressed all the above requirements using the property specification language MCL [17]. MCL is an extension of the alternation-free modal μ-calculus [8] with action predicates enabling value extraction, modalities containing extended regular expressions on transition sequences, quantified variables and parameterized fixed point operators, programming language constructs, and fairness operators encoding generalized Büchi automata. These features make possible a concise and intuitive description of safety, liveness, and fairness properties involving data, without sacrificing the efficiency of on-the-fly model checking, which has a linear-time complexity for the dataless MCL formulas [17].

We show below the MCL formulation of two requirements from the list above, which denote typical safety and liveness properties. Requirement R2 is expressed in MCL as follows[4]:

$$[\,\mathbf{true}^*.\{\texttt{ACQUIRE ?}B : \mathbf{string}\}.(\mathbf{not}\ \{\texttt{DISCARD !}B\})^*.\{\texttt{ACQUIRE !}B\}\,]\ \mathbf{false}$$

This formula uses the standard *safety* pattern "$[\beta]$ **false**", which forbids the existence of transition sequences matching the regular formula β. Here the undesirable sequences are those containing two *Acquire* operations for the same book B without a *Discard* operation for B in the meantime. The regular formula $\mathbf{true}^*$ matches a subsequence of (zero or more) transitions labeled by arbitrary actions. Note the use of the construct "$\texttt{?}B : \mathbf{string}$", which matches any string and extracts its value in the variable B used later in the formula. Therefore, the above formula captures all occurrences of books carried by *Acquire* operations in the model. Requirement R12 is formulated in MCL as follows:

$$\begin{array}{l}[\,\mathbf{true}^*.\{\texttt{RESERVE ?}M : \mathbf{string}\ \texttt{?}B : \mathbf{string}\}.\\ \ (\mathbf{not}\ (\{\texttt{TAKE !}M\ \texttt{!}B\}\ \mathbf{or}\ \{\texttt{TRANSFER !}M\ \texttt{!}B\}))^*\,]\\ \quad \langle\,(\mathbf{not}\ (\{\texttt{TAKE !}M\ \texttt{!}B\}\ \mathbf{or}\ \{\texttt{TRANSFER !}M\ \texttt{!}B\}))^*.\ \{\texttt{CANCEL !}M\ \texttt{!}B\}\,\rangle\ \mathbf{true}\end{array}$$

This formula denotes a *liveness* property of the form "$[\beta_1]\ \langle\beta_2\rangle$ **true**", which states that every transition sequence matching the regular formula β_1 (in this case, book B has been reserved by member M and subsequently neither taken nor transferred) ends in a state from which there exists a transition sequence matching the regular formula β_2 (in this case, the reservation can be cancelled before being taken or transferred).

Using EB^{3}2LNT, we translated the EB^3 specification of the library management system to LNT. The resulting specification was checked against all the 15 requirements, formulated in MCL, using the EVALUATOR 4.0 model checker of CADP. The experiments were performed on an Intel(R) Core(TM) i7 CPU 880 at 3.07GHz. Table 1 shows the results for several configurations of the IS, obtained by instantiating the number of books (m) and members (p) in the IS.

[4] Note that MCL requires actions to have the form $G\ \texttt{!}E_1\ \ldots\ \texttt{!}E_n$ instead of $G\,(E_1, \ldots, E_n)$. This is a minor drawback for the user that will not be difficult to fix in future versions of the tools. Note also that attribute variables $\overline{f}$ do not have to occur on action formulas. Instead, those internal details are hidden in the LTS using action renaming. This can easily be done on-the-fly while evaluating the formula using the `-rename` option of the EVALUATOR 4.0 model checker of CADP.

All requirements were shown to be valid on the IS specification. The second and third line of the table indicate the number of states and transitions of the LTS corresponding to the LNT specification. The fourth line gives the time needed to generate the LTS and the other lines give the verification time for each requirement.

Table 1. Model checking results for the library management system

(m, p)	(3,2)	(3,3)	(3,4)	(4,3)
states	1,002	182,266	8,269,754	27,204,016
trans.	5,732	1,782,348	105,481,364	330,988,232
time	1.9s	14.4s	31'39s	140'22s
R1	0.3s	1.8s	5'19s	20'13s
R2	0.2s	2.9s	9'26s	36'7s
R3	0.2s	9.4s	97'46s	26'47s
R4	0.2s	1.7s	5'15s	18'40s
R5	0.2s	2.2s	6'46s	21'52s
R6	0.2s	4.1s	38'30s	10'19s
R7	0.2s	7.4s	65'22s	24'33s
R8	0.2s	2.2s	6'52s	22'27s
R9	0.2s	2.3s	6'38s	22'29s
R10	0.3s	13.3s	43'59s	62'07s
R11	0.3s	2.5s	6'36s	22'14s
R12	0.3s	4.0s	10'47s	45'09s
R13	0.4s	4.3s	11'46s	1'07s
R14	0.3s	3.6s	10'41s	37'33s
R15	0.2s	2.8s	7'53s	28'56s

6 Conclusion

We proposed an approach for equipping the EB^3 method with formal verification capabilities by reusing already available model checking technology. Our approach relies upon a new translation from EB^3 to LNT, which provides a direct connection to all the state-of-the-art verification features of the CADP toolbox. The translation, based on an alternative memory semantics of EB^3 [18] instead of the original trace semantics [10], was automated by the EB^{3}2LNT translator and validated on several examples of typical ISs. So far, we experimented only the model checking of MCL data-based temporal properties on EB^3 specifications. However, CADP also provides extensive support for equivalence checking and compositional LTS construction, which can be of interest to IS designers.

As future work, we plan to provide a formal proof of the translation from EB^3 to LNT, which could serve as reference for translating EB^3 to other process algebras as well. We also plan to study abstraction techniques for verifying

properties regardless of the number of entity instances that participate in the IS, following the approaches for parameterized model checking [1]. In particular, we will observe how the insertion of new functionalities into an IS affects this issue, and we will formalize this in the context of EB^3 specifications.

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A LNT Code for the Simplified Library Management System (for referees only)

We give the LNT code for the simplified Library Management System of Section 2, with 2 members, 1 book, and *NbLoans* set to 1.

```
module library is

type MEMBERID is
   m1, m2, m_bot
   with "eq", "ne", "ord"
end type

type BOOKID is
   b1, b_bot
   with "eq", "ne", "ord"
end type

type NB is
   array [0..2] of NAT
end type

type BOR is
   array [0..2] of MEMBERID
end type

process memory [ACQUIRE, DISCARD, REGISTER, UNREGISTER,
                LEND, RETURN: ANY] is
   var mId : MEMBERID, bid : BOOKID, borrower : BOR, nbLoans : NB in
      mId := m_bot; borrower := BOR (m_bot); nbLoans := NB (0);
      loop
         select
            ACQUIRE (?bid)
         []
            DISCARD (?bid, ?borrower)
         []
            REGISTER (?mid)
         []
            UNREGISTER (?mid)
         []
            LEND (?bid, ?mid, !nbLoans, !borrower);
            borrower[ord (bid)] := mid;
            nbLoans[ord (mid)] := nbLoans[ord (mid)] + 1
         []
            RETURN (?bid);
            mId := borrower[ord (bid)];
            borrower[ord (bid)] := m_bot;
            nbLoans[ord (mid)] := nbLoans[ord (mid)] - 1
         end select
      end loop
```

```
   end var
end process

process loan [LEND, RETURN : ANY] (mid: MEMBERID, bid : BOOKID) is
   var borrower: BOR, nbLoans: NB in (* NbLoans is set to 1 *)
      LEND (bid, mid, ?nbLoans, ?borrower) where
         ((borrower[ord (bid)] eq m_bot) and
         (nbLoans[ord (mid)] eq 1));
      RETURN (bid)
   end var
end process

process book [ACQUIRE, DISCARD : ANY] (bid: BOOKID) is
   var borrower: BOR in
      ACQUIRE (bid);
      DISCARD (bid, ?borrower) where (borrower[ord (bid)] eq m_bot)
   end var
end process

process member [REGISTER, UNREGISTER, LEND, RETURN: ANY]
               (mid: MEMBERID) is
   REGISTER (mid);
   loop L in
      select
         break L
      []
         loan [LEND, RETURN] (mid, b1)
      end select
   end loop;
   UNREGISTER (mid)
end process

process MAIN [ACQUIRE, DISCARD, REGISTER, UNREGISTER,
              LEND, RETURN: ANY] () is
   par ACQUIRE, DISCARD, REGISTER, UNREGISTER, LEND, RETURN in
      par
         loop L in
            select
               break L
            []
               book [ACQUIRE, DISCARD] (b1)
            end select
         end loop
      ||
         par
            loop L in
               select
                  break L
               []
                  member [REGISTER, UNREGISTER, LEND, RETURN] (m1)
```

```
            end select
         end loop
      ||
         loop L in
            select
               break L
            []
               member [REGISTER, UNREGISTER, LEND, RETURN] (m2)
            end select
         end loop
      end par
   end par
||
   memory [ACQUIRE, DISCARD, REGISTER, UNREGISTER, LEND, RETURN]
end par
end process

end module
```

B EB^3 Code for the Extended Library Management System (for referees only)

We give the EB^3 code for the extended Library Management System, mentioned in Section 5, with 2 members, 3 books, and *NbLoans* set to 2. Functions "add_reservation","cancel_reservation", "oldest_reservation", "nil_reservation" and "is_reserved" are standard functions on lists. They are not attribute functions.

```
Acq (bid : BOOKID)
Dis (bid : BOOKID)
Join (mid : MEMBERID)
Leave (mid : MEMBERID)
Lend (mid : MEMBERID, bid : BOOKID)
Res (mid : MEMBERID, bid : BOOKID)
Take (mid : MEMBERID, bid : BOOKID)
Cancel (mid : MEMBERID, bid : BOOKID)
Ret (bid : BOOKID)
Transfer (mid : MEMBERID, bid : BOOKID)
Renew (bid : BOOKID)

;

BOOKID = [b1, b2, b3]
MEMBERID = [m1, m2]

;

(* Adds a member to the reservation queue *)
function add_reservation (m : MEMBERID, l : list MEMBERID) : list MEMBERID =
```

```
match l with
| NIL : CONS(m, NIL)
| CONS(temp_mem, temp_list) :
       CONS(temp_mem, add_reservation (m, temp_list))
end match
end function

(* Removes all possible occurence of member m in the list *)
function cancel_reservation (m : MEMBERID, l : list MEMBERID)
     : list MEMBERID =
match l with
| NIL : return NIL
| CONS (m, temp_list) : temp_list
| CONS (temp_mem, temp_list) :
       CONS (temp_mem, cancel_reservation(m, temp_list))
end match
end function

(* Returns true if the member is in the reservation queue,
returns false if the member is not in the queue *)
function is_reserved (m : MEMBERID, l : list MEMBERID) : BOOL =
match l with
| NIL : false
| CONS (m, temp_list) : true
| _ : is_reserved (m, temp_list)
end match
end function

(* Returns true if the member is the oldest in the reservation queue,
returns false if the member is not in the queue *)
function oldest_reservation (m: MEMBERID, l: list MEMBERID) : BOOL =
match l with
| NIL : false
| CONS (m, temp_list) : true
| _ : false
end match
end function

function nil_reservation (l : list MEMBERID) : BOOL =
match l with
| NIL : true
| _ : false
end match
end function

;

Borrower (T : Trace, bid : BOOKID) : MEMBERID =
match last (T) with
| _|_ : _|_
```

```
| Lend (mid, bid) : mid
| Take (mid, bid) : mid
| Ret (bid) : _|_
| Transfer (mid, bid) : mid
| _ : Borrower (front(T), bid)
end match

Nbloans (T : Trace, mid : MEMBER) : NAT =
match last (T) with
| _|_ : _|_
| Join (mid) : 0
| Lend (mid, bid) : Nbloans (front(T), mid) + 1
| Take (mid, bid) : Nbloans (front(T), mid) + 1
| Ret (bid) AND mid = Borrower (T, bid)
       : Nbloans (front(T), mid) - 1
| Transfer (mid2, bid) AND mid = Borrower (T, bid)
       : Nbloans (front(T), mid) - 1
| Transfer (mid, bid) : Nbloans (front(T), mid) + 1
| Leave (mid) : _|_
end match

Acquired (T : Trace, bid) : BOOL =
match last (T) with
| _|_ : false
| Acq (bid) : true
| Dis (bid) : false
| _ : Acquired (front(T), bid)
end match

Reservation (T : Trace, bid : BOOKID) : list MEMBERID =
match last (T) with
| _|_ : NIL
| Res (mid, bid)
       : add_reservation (mid, Reservation (front(T), bid))
| Take (mid, mid)
       : cancel_reservation (mid, Reservation (front(T), bid))
| Cancel (mid, bid)
       : cancel_reservation (mid, Reservation (front(T), bid))
| _ : Reservation (front(T), bid)
end match

;

book(bid : BOOKID) =
Acq (bid).
( Borrower (T, bid) = _|_ AND
  null_reservation (Reservation (T, bid)) = true )
=> Dis(bid)

member (mid : MEMBERID, bid : BOOKID) =
```

```
(
  (
    ( Acquired (T, bid) = true AND
      Borrower (T, bid) = _|_ AND
      nil_reservation (Reservation(T, bid)) = true AND
      NbLoans (T, bid) < 2 )
    => Lend (mid, bid)
  )
  |
  (
    ( Acquired (T, bid) = true AND
      Borrower (T, bid) = _|_ AND
      oldest_reservation (mid, Reservation (T, bid)) = true AND
      NbLoans (T, bid) < 2 ) => Take (mid, bid)
  ).

  ( ( Acquired (T, bid) = true AND
      Borrower (T, bid) = _|_ AND
      nil_reservation (Reservation(T, bid)) = true AND
      NbLoans (T, bid) < 2 )
    => Renew (bid)
  ) *.

  (
    ( Acquired (T, bid) = true AND
      Borrower (T, bid) = mid )
    => Ret (bid)
  )
  |
  (
    | mid2 : MEMBERID :
        ( nil_reservation (Reservation (T, bid)) = true AND
          Acquired (T, bid) = true AND
          Borrower (T, bid) <> mid2 AND
          NbLoans (T, bid) > 0 AND
          NbLoans (T, bid) < 2 )
        => Transfer (mid2, bid)
   )
)
|
(
  ( Borrower (T, bid) <> _|_ AND
    Borrower (T, bid) <> mid AND
    Acquired (T, bid) = true AND
    is_reserved (mid, Reservation(T, bid)) = false )
  => Res (mid, bid).

  (
    ( Borrower (T, bid) = _|_ AND
      Acquired (T, bid) = true AND
```

```
      oldest_reservation_list (mid, Reservation (T, bid)) = false AND
      NbLoans (T, bid) < 2 )
    => Take(mid, bid)
  )
  |
  (
    ( Borrower (T, bid) != mid AND
      Acquired (T, bid) = true
    => Cancel (mid, bid)
  )
)
|
(
  (
    ( Acquired (T, bid) = true
      Borrower (T, bid) = mid )
    => Ret (bid)
  )
  |
  (
    | mid2 : MEMBERID :
        ( nil_reservation (Reservation (T, bid)) = true AND
          Acquired (T, bid) = true AND
          Borrower (T, bid) = mid AND
          NbLoans (T, bid) > 0 AND
          NbLoans (T, bid) < 2 )
        => Transfer (mid2, bid)
  )
)

;
main =
( |[]| bid : BOOKID : book (bid) * )
|[]|
( |[]| mid : MEMBERID :
( ( Join (mid). ( |[]| bid : BOOKID : member (mid, bid) * ).
    ( NbLoans (T, mid) AND
              is_reserved (mid, Reservation (T, b1)) = false AND
              is_reserved (mid, Reservation (T, b2)) = false AND
              is_reserved (mid, Reservation (T, b3)) = false )
      => Leave (mid) ) ) )
```

C LNT Code for the Extended Library Management System (for referees only)

We give the LNT code for the extended Library Management System. This code is generated by EB^{3}2LNT except the functions "add_reservation","cancel_reservation",

"oldest_reservation", "nil_reservation" and "is_reserved", which are coded by hand, since our compiler does not support user-defined EB^3 types and (non-attribute) functions for the time being. We also define type "RESERV" to simplify the coding. By convention, for every type T we have $ord(\perp) = 0$, $ord(first_T) = 1$, etc.

```
module library is

type BOOKID is
   b1, b2, b3, b_bot
   with "eq", "ne", "ord"
end type

type MEMBERID is
   m1, m2, m_bot
   with "eq", "ne", "ord"
end type

type MEMBERLIST is
   NIL, CONS (HD: MEMBERID, TL: MEMBERLIST)
   with "eq", "ne"
end type

type ACQUIR is
   array [0..3] of BOOL
end type

type BOR is
   array [0..3] of MEMBERID
end type

type NB is
   array [0..2] of NAT
end type

type RESERV is
   array [0..2] of MEMBERLIST
end type

function add_reservation (m : MEMBERID, l : MEMBERLIST ) : MEMBERLIST is
case l in
var temp_mem : MEMBERID, temp_list : MEMBERLIST in
   NIL -> return CONS (m, NIL)
 | CONS (temp_mem, temp_list) ->
      return CONS (temp_mem, add_reservation (m, temp_list))
end case
end function

function cancel_reservation (m : MEMBERID, l : MEMBERLIST) : MEMBERLIST is
case l in
```

```
var temp_mem : MEMBERID, temp_list : MEMBERLIST in
    NIL -> return NIL
 | CONS (temp_mem, temp_list ) where (temp_mem eq m) ->
     return temp_list
 | CONS (temp_mem, temp_list ) ->
     return CONS (temp_mem, cancel_reservation (m, temp_list))
end case
end function

function is_reserved(m : MEMBERID, l : MEMBERLIST) : BOOL is
case l in
var temp_mem: MEMBERID, temp_list : MEMBERLIST in
   NIL -> return false
 | CONS (temp_mem, temp_list) where (temp_mem eq m) -> return true
 | CONS (temp_mem, temp_list) -> return is_reserved(m, temp_list)
end case
end function

function oldest_reservation (m : MEMBERID, l : MEMBERLIST) : BOOL is
case l in
var temp_mem: MEMBERID, temp_list : MEMBERLIST in
   NIL -> return false
 | CONS (temp_mem, temp_list) where (temp_mem eq m) -> return true
 | CONS (temp_mem, temp_list) -> return false
end case
end function

function nil_reservation(l: MEMBERLIST): BOOL is
case l in
var temp_list : MEMBERLIST in
   NIL -> return true
 | ANY MEMBERLIST -> return false
end case
end function

process memory[ACQ, DIS, JOIN, LEND, TAKE, RENEW, RET, RES, CANCEL,
               LEAVE, TRANSFER : ANY] is
var mid : MEMBERID, bid : BOOKID, acquired : ACQUIR,
   borrower : BOR, nbloans : NB, reservation : RESERV in
   acquired := ACQUIR (false); borrower := BOR (m_bot);
   nbloans := NB (0); reservation := RESERV (NIL);
   loop
      select
         ACQ (?bid);
         acquired[ord (bid)] := true
      []
         DIS (?bid, !borrower, !reservation);
         acquired[ord (bid)] := false
      []
         JOIN (?mid);
```

```
         nbloans[ord (mid)] := 1
      []
         LEAVE (?mid, !nbloans, !reservation);
         nbloans[ord (mid)] := 0
      []
         LEND (?mid, ?bid, !acquired, !borrower, !reservation, !nbloans);
         borrower[ord (bid)] := mid;
         nbloans[ord (mid)] := nbloans[ord (mid)] + 1
      []
         RES (?mid, ?bid, !acquired, !borrower, !reservation);
         reservation[ord (bid)] :=
            add_reservation (mid, reservation[ord (bid)])
      []
         TAKE (?mid, ?bid, !acquired, !borrower, !reservation, !nbloans);
         borrower[ord (bid)] := mid;
         nbloans[ord (mid)] := nbloans[ord (mid)] + 1;
         reservation[ord (bid)] :=
            cancel_reservation (mid, reservation[ord (bid)])
      []
         CANCEL (?mid, ?bid, !acquired, !borrower);
         reservation[ ord(bid)]:=
            cancel_reservation (mid, reservation[ord (bid)])
      []
         TRANSFER (?mid, ?bid, !acquired, !borrower, !reservation, !nbloans);
         nbloans[ord (borrower[ord(bid)])]:=
            nbloans[ord (borrower[ord (bid)])] - 1;
         borrower[ord (bid)]:= mid;
         nbloans[ord (mid)]:= nbloans[ord (mid)] + 1
      []
         RENEW (?bid, !acquired, !borrower, !reservation)
      []
         RET (?bid, !acquired, !borrower);
         nbloans[ord (borrower[ord (bid)])] :=
            nbloans[ord (borrower[ord (bid)])] - 1;
         borrower[ord (bid)] := m_bot
      end select
   end loop
end var
end process

process book[ACQ, DIS : ANY](bid : BOOKID) is
var acquired : ACQUIR, borrower : BOR, reservation: RESERV in
   ACQ(bid);
   DIS(bid, ?borrower, ?reservation) where
      ( (borrower[ord (bid)] eq m_bot) AND
        (nil_reservation (reservation[ord (bid)]) eq true) )
end var
end process

process member[LEND, TAKE, RENEW, RET, RES, CANCEL, TRANSFER : ANY]
```

```
          (mid : MEMBERID, bid : BOOKID) is
var acquired : ACQUIR, borrower : BOR, reservation : RESERV,
    nbloans : NB in
   select
      select
         LEND(!mid, !bid,
              ?acquired, ?borrower, ?reservation, ?nbloans) where
              ( (acquired[ord (bid)] eq true) AND
                (borrower[ord (bid)] eq m_bot) AND
                (nil_reservation (reservation[ord(bid)]) eq true) AND
                (nbloans[ord (mid)] lt 2) )
      []
         TAKE(!mid, !bid,
              ?acquired, ?borrower, ?reservation, ?nbloans) where
              ( (acquired[ord (bid)] eq true) AND
                (borrower[ord (bid)] eq m_bot) AND
                (oldest_reservation (mid, reservation[ord(bid)]) eq true) AND
                (nbloans[ord (mid)] lt 2) )
      end select;
      loop L in select break L []
         RENEW(!bid,
               ?acquired, ?borrower, ?reservation) where
               ( (acquired[ord (bid)] eq true) AND
                 (nil_reservation (reservation[ord (bid)]) eq true) AND
                 (borrower[ord (bid)] eq mid) )
      end select end loop;
      select
         RET(!bid, ?acquired, ?borrower) where
             ( (acquired[ord(bid)] eq true) AND
               (borrower[ord(bid)] eq mid) )
      []
         var mid2 : MEMBERID in
            mid2 := ANY MEMBERID where ( (mid2 ne m_bot) AND (mid2 ne mid) );
            TRANSFER (!mid2, !bid,
                      ?acquired, ?borrower, ?reservation, ?nbloans) where
                    ( (nil_reservation (reservation[ord (bid)]) eq true) AND
                      (acquired[ord(bid)] eq true) AND
                      (borrower[ord(bid)] ne mid2) AND
                      (nbloans[ord(mid2)] gt 0) AND
                      (nbloans[ord(mid2)] lt 2) )
         end var
      end select
   []
      RES(!mid, !bid, ?acquired, ?borrower, ?reservation) where
          ( (borrower[ord(bid)] ne m_bot) AND
            (borrower[ord(bid)] ne mid) AND
            (acquired[ord(bid)] eq true) AND
            (is_reserved(mid, reservation[ord(bid)]) eq false) );
      select
         TAKE(!mid, !bid, ?acquired, ?borrower, ?reservation, ?nbloans) where
```

```
      ( (borrower[ord(bid)] eq m_bot) AND
        (acquired[ord(bid)] eq true) AND
        (oldest_reservation(mid, reservation[ord(bid)]) eq true) AND
        (nbloans[ord(mid)] lt 2) )
   []
       CANCEL(!mid, !bid, ?acquired, ?borrower) where
          ( (borrower[ord(bid)] ne mid) AND
            (acquired[ord(bid)] eq true) )
   end select
[]
   RET(!bid, ?acquired, ?borrower) where
       ( (acquired[ord(bid)] eq true) AND
         (borrower[ord(bid)] eq mid) )
[]
   var mid2: MEMBERID in
      mid2:= ANY MEMBERID where ( (mid2 ne m_bot) AND (mid2 ne mid) );
      TRANSFER(!mid2, !bid,
               ?acquired, ?borrower, ?reservation, ?nbloans) where
             ( (nil_reservation(reservation[ord(bid)]) eq true) AND
               (acquired[ord(bid)] eq true) AND
               (borrower[ord(bid)] eq mid) AND
               (nbloans[ord(mid2)] gt 0) AND
               (nbloans[ord(mid2)] lt 2) )
   end var
end select
end var
end process

process MAIN[ACQ, DIS, JOIN, LEND, TAKE, RENEW, RET, RES,
             CANCEL, LEAVE, TRANSFER: ANY] () is

par ACQ, DIS, JOIN, LEND, TAKE, RENEW, RET,
    RES, CANCEL, LEAVE, TRANSFER in
par
   par
     loop L in select break L []
       book[ACQ, DIS](b1)
     end select end loop
   ||
     loop L in select break L []
       book[ACQ, DIS](b2)
     end select end loop
   ||
     loop L in select break L []
       book[ACQ, DIS](b3)
     end select end loop
   end par
||
   par
     loop L in select break L []
```

```
      JOIN(m1);
      par
        loop L2 in select break L2 []
          member[LEND, TAKE, RENEW, RET, RES, CANCEL, TRANSFER](m1, b1)
        end select end loop
      ||
        loop L2 in select break L2 []
          member[LEND, TAKE, RENEW, RET, RES, CANCEL, TRANSFER](m1, b2)
        end select end loop
      ||
         loop L2 in select break L2 []
           member[LEND, TAKE, RENEW, RET, RES, CANCEL, TRANSFER](m1, b3)
         end select end loop
      end par;
      var nbloans: NB, bid: BOOKID, reservation: RESERV in
        LEAVE(m1, ?nbloans, ?reservation) where
           ( (nbloans[ord(m1)] eq 1) AND
             (is_reserved(m1, reservation[ord(b1)]) eq false) AND
             (is_reserved(m1, reservation[ord(b2)]) eq false) AND
             (is_reserved(m1, reservation[ord(b3)]) eq false) )
      end var
    end select end loop
  ||
    loop L in select break L []
      JOIN(m2);
      par
        loop L2 in select break L2 []
           member[LEND, TAKE, RENEW, RET, RES, CANCEL, TRANSFER](m2, b1)
        end select end loop
      ||
        loop L2 in select break L2 []
           member[LEND, TAKE, RENEW, RET, RES, CANCEL, TRANSFER](m2, b2)
        end select end loop
      ||
        loop L2 in select break L2 []
           member[LEND, TAKE, RENEW, RET, RES, CANCEL, TRANSFER](m2, b3)
        end select end loop
      end par;
      var nbloans: NB, bid: BOOKID, reservation: RESERV in
         LEAVE(m2, ?nbloans, ?reservation) where
           ( (nbloans[ord(m2)] eq 1) AND
             (is_reserved(m2, reservation[ord(b1)]) eq false) AND
             (is_reserved(m2, reservation[ord(b2)]) eq false) AND
             (is_reserved(m2, reservation[ord(b3)]) eq false) )
      end var
    end select end loop
  end par
end par
||
  memory[ACQ, DIS, JOIN, LEND, TAKE, RENEW, RET, RES, CANCEL, LEAVE, TRANSFER]
```

```
end par
end process

end module
```

D MCL Formulas for Requirements R1 to R15 (for referees only)

Requirement R1

"*A book can always be acquired by the library when it is not currently acquired*"

macro $R_1\,(B) =$
  (
    $[\,(\textbf{not}\ \{\texttt{ACQUIRE !}B\})^*\,]\ \langle\,\{\texttt{ACQUIRE !}B\}\,\rangle\ \textbf{true}$
    and
    $[\,\textbf{true}^*\,.\,\{\texttt{DISCARD !}B\}\,.\,(\textbf{not}\ \{\texttt{ACQUIRE !}B\})^*\,]\ \langle\,\{\texttt{ACQUIRE !}B\}\,\rangle\ \textbf{true}$
)
end_macro
$R_1\,(\texttt{"B1"})$ **and** $R_1\,(\texttt{"B2"})$ **and** $R_1\,(\texttt{"B3"})$

This is a classical liveness property. The second conjunct of "$R_1\,(B)$" expresses the eventuality that a book be withdrawn from the library before it is reacquired.

Requirement R2

"*A book cannot be acquired by the library if it is already acquired*"

$$[\,\textbf{true}^*\,.\,\{\texttt{ACQUIRE ?}B : \textbf{string}\}\,.\,(\textbf{not}\ \{\texttt{DISCARD !}B\})^*\,.\,\{\texttt{ACQUIRE !}B\}\,]\ \textbf{false}$$

This is a classical safety property.

Requirement R3

"*An acquired book can be discarded only if it is neither borrowed nor reserved*"

$[\,\textbf{true}^*\,.\,\{\texttt{?}G : \textbf{string}\ \texttt{?any} : \textbf{string}\ \texttt{?}B : \textbf{string}\ \textbf{where}\ (G = \texttt{"LEND"})\ \textbf{or}\ (G = \texttt{"TAKE"})\}\,.$
  $(\textbf{not}\ \{\texttt{RETURN !}B\})^*\,.\,\{\texttt{DISCARD !}B\}\,]\ \textbf{false}$
and
$[\,\textbf{true}^*\,.\{\texttt{RESERVE ?any} : \textbf{string}\ \texttt{?}B : \textbf{string}\}\,.$
  $(\textbf{not}\ (\{\texttt{CANCEL ?any} : \textbf{string}\ \texttt{!}B\}\ \textbf{or}\ \{\texttt{RETURN !}B\}))^*\,.\,\{\texttt{DISCARD !}B\}\,]\ \textbf{false}$

Requirement R4

"*A person must be a member of the library in order to borrow a book*"

```
macro R4 (M) =
  (
    [ (not {JOIN !M})* . ({LEND !M ?any : string} or {TAKE !M ?any : string}) ] false
    and
    [ true* .{LEAVE !M} . (not {JOIN !M})* .
      ({LEND !M ?any : string} or {TAKE !M ?any : string}) ] false
  )
end_macro
R4 ("M1") and R4 ("M2") and R4 ("M3")
```

The first conjunct or "$R_4\,(M)$" expresses the fact that a member cannot borrow a book if (s)he has not registered to the library. The second conjunct expresses that if a member relinquishes his/her membership, (s)he may not lend a book neither via the regular loan action `LEND` nor the reservation action `RESERVE`.

Requirement R5

"*A book can be reserved only if it has been borrowed or already reserved by some member*"

```
macro R5 (B) =
  (
    [ (not ({LEND ?any : string !B} or {TAKE ?any : string !B}))* .
      {RESERVE ?any : string !B} ] false
    and
    [ true* . {RETURN !B} .
      (not ({LEND ?any : string !B} or {TAKE ?any : string !B}))* . {RESERVE !B} ] false
    and
    [ (not ({LEND ?any : string !B} or {TAKE ?any : string !B} or
      {TRANSFER ?any : string !B} or {RESERVE ?any : string !B}))* .
        {RESERVE ?any : string !B} ] false
  )
end_macro
R5 ("B1") and R5 ("B2") and R5 ("B3")
```

The first conjunct expresses the obligation for a book not to be lent in order to be added to the reservation list. The second conjunct complements the first in the sense that at least one loan cycle is completed in the beginning of the transition sequence via "`{ RETURN !B }`" thus making the book available for loan again. The third conjunct denies any reservation history for the book in question. All possible loan operations should be excluded as well.

Requirement R6

"*A book cannot be reserved by the member who is borrowing it*"

```
[ true* . {LEND ?M : string ?B : string} .
  (not ({RETURN !B} or {TRANSFER ?M2 : string !B}))* . {RESERVE !M !B} ] false
```

The difficulty here lies in the fact that the borrower may transfer the book to another member. For this reason, the following formula is false.

```
[ true* . {LEND ?M : string ?B : string} . (not ({RETURN !B}))* . {RESERVE !M !B} ] false
```

Requirement R7

"*A book cannot be reserved by a member who is reserving it*"

```
[ true* . {RESERVE ?M : string ?B : string} . (not ({TAKE !M !B} or {CANCEL !M !B}))* .
  {RESERVE !M !B} ] false
```

Requirement R8

"*A book cannot be lent to a member if it is reserved*"

```
macro R8 (B, M1, M2) =
  (
    [ true* . {RESERVE !M1 !B} . (not ({TAKE !M1 !B} or {CANCEL !M1 !B}))* .
      {LEND !M2 !B} ] false
  )
end_macro
R8 ("B1", "M1", "M2")
```

In this case (as well as for the subsequent requirements R9, R11, R13, R14, and R15), we only check the property for a specific book (`B1`) and members (`M1`, `M2`). So doing, we exploit the symmetry of the specification (all books and members have similar behaviour), which is crucial to avoid the exponential state space explosion.

Requirement R9

"*A member cannot renew a loan or give the book to another member if the book is reserved*"

```
macro R9 (B, M) =
  (
    [ true* . {RESERVE !M !B} . (not ({TAKE !M !B} or {CANCEL !M !B}))* . {RENEW !B} ] false
  )
end_macro
R9 ("B1", "M1")
```

Requirement R10

"*A member is allowed to take a reserved book only if he owns the oldest reservation*"

```
[
  true* .
  {RESERVE ?M1 : string ?B : string} .
  (not ({TAKE !M1 !B} or {CANCEL !M1 !B} or {TRANSFER !M1 !B}))* .
  {RESERVE ?M2 : string !B where M2 ≠ M1} .
  (not ({TAKE !M1 !B} or {CANCEL !M1 !B} or {TRANSFER !M1 !B}))* .
  {TAKE !M2 !B}
] false
```

This property has been rephrased in the following way: If two members reserve a book, the first member to get it, is the first to have ordered it.

Requirement R11

"*A book can be taken only if it is not borrowed*"

```
macro R11 (B, M) =
  (
    [ true* . ({LEND !M !B} or {TAKE !M !B}) . (not ({RETURN !B}))* .
      ({LEND !M !B} or {TAKE !M !B}) . (not ({RETURN !B}))* . {RETURN !B} ] false
  )
end_macro
R11 ("B1", "M1")
```

This property corresponds to the pattern "α_1 does not occur between α_2 and α_3", which is expressed by the following scheme, easily recognizable in this formula:

$$[\,\mathbf{true}^*\,.\,\alpha_2\,.\,(\mathbf{not}\ \alpha_3)^*\,.\,\alpha_1\,.\,(\mathbf{not}\ \alpha_3)^*\,.\,\alpha_3\,]\ \mathbf{false}$$

Requirement R12

"*A member who has reserved a book can cancel the reservation at anytime before he takes it*"

```
[ true* . {RESERVE ?M : string ?B : string} . (not ({TAKE !M !B} or {TRANSFER !M !B}))* ]
    ⟨ (not ({TAKE !M !B} or {TRANSFER !M !B}))* . {CANCEL !M !B} ⟩ true
```

Requirement R13

"*A member can relinquish library membership only when all his loans have been returned and all his reservations have either been used or cancelled*"

```
macro R13 (B, M) =
  (
    [ true* .
      ({LEND !M !B} or {TAKE !M !B}) .
      (not ({RETURN !B} or {TRANSFER !"M2" !B} or {TRANSFER !"M3" !B}))* .
      {LEAVE !M} . (not ({RETURN !B} or {TRANSFER !"M2" !B} or {TRANSFER !"M3" !B}))* .
      ({RETURN !B} or {TRANSFER !"M2" !B} or {TRANSFER !"M3" !B}) ] false
    and
    [ true* . {RESERVE !M !B} . (not ({TAKE !M !B} or {CANCEL !M !B}))* .
      {LEAVE !M} . (not ({TAKE !M !B} or {CANCEL !M !B}))* .
      ({TAKE !M !B} or {CANCEL !M !B}) ] false
  )
end_macro
R13 ("B1", "M1")
```

Requirement R14

"*Ultimately, there is always a procedure that enables a member to leave the library*"

```
macro R14 (M) =
  (
    [ true* . {JOIN !M} . (not {LEAVE !M})* ] ⟨ (not {LEAVE !M})* . {LEAVE !M} ⟩ true
  )
end_macro
R14 ("M1")
```

Requirement R15

"*A member cannot borrow more than the loan limit defined at the system level for all users*"

```
macro R15 (M) =
  (
    [ true* . let B1 : string := "B1", B2 : string := "B2" in
      ({LEND !M !B1} or {TAKE !M !B1}) .
      (not ({TRANSFER ?M2 : string !B1} or {RETURN !B1}))* .
      ({LEND !M !B2} or {TAKE !M !B2}) end let ] false
  )
end_macro
R15 ("M1")
```

This property is dependent on the maximum number *NbLoans* of books a member can have at any time in his/her possession. In the above, *NbLoans* was set to two.