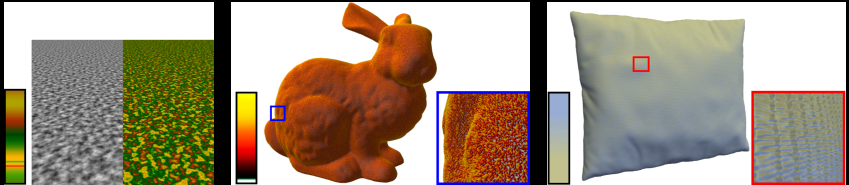


# Filtering Color Mapped Textures and Surfaces

I3D 2013

Eric Heitz Derek Nowrouzezahrai Pierre Poulin Fabrice Neyret

INRIA-LJK (Université de Grenoble and CNRS)  
LIGUM, Dept. I.R.O., Université de Montréal



# Introduction

## NVidia's Endless City Demo

- ▶ real-time
- ▶ amazing content and details

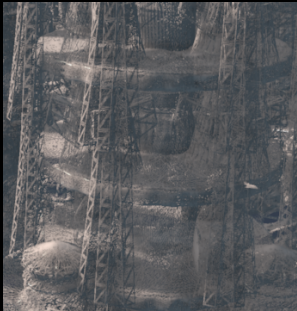


# Introduction

Level of detail transition

## Introduction

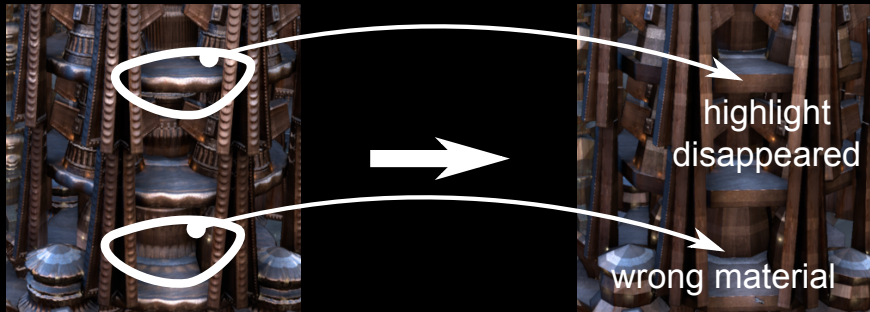
Managing geometry level of detail is important...  
but is not enough



# Introduction

Level of detail should also preserve appearance

- ▶ material
- ▶ BRDF
- ▶ normals
- ▶ visibility

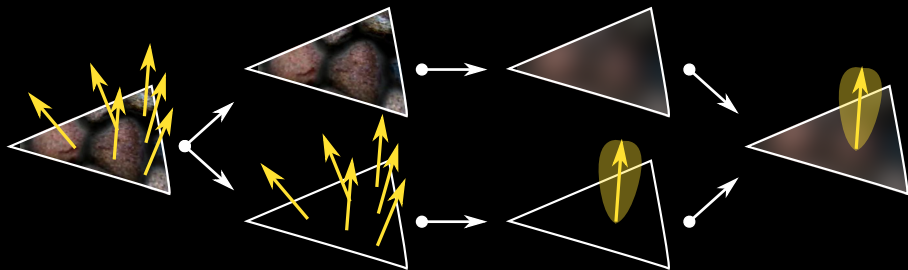


## Introduction

Current CG model: coarse geometry + textures

→ visibility, curvature and orientation are constant within triangles

→ textures can be filtered separately



separate colors and normals filtering

# Introduction

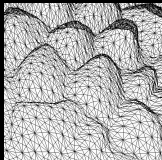
What if geometry matches up texture resolution?

color



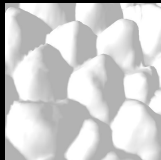
X

geometry



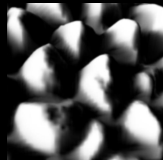
X

shading



X

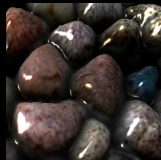
visibility



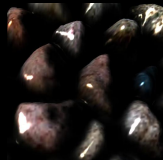
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=



=

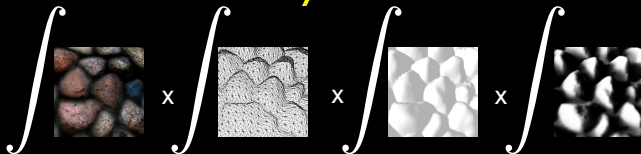


# Introduction

physically correct



$\neq$



physically wrong

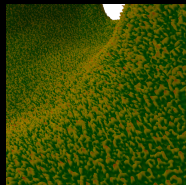
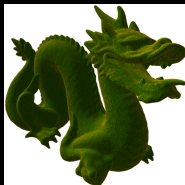
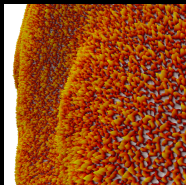
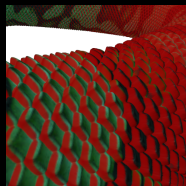
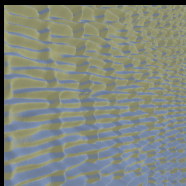
energy conservation violated  
popping, aliasing, and inconsistent appearance



# Introduction

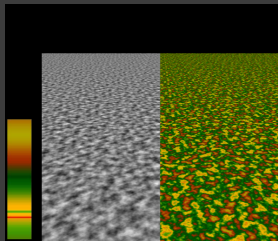
We investigate how to

- ▶ filter correctly procedural surfaces
- ▶ with small-scale geometry, colors, and visibility



# Plan

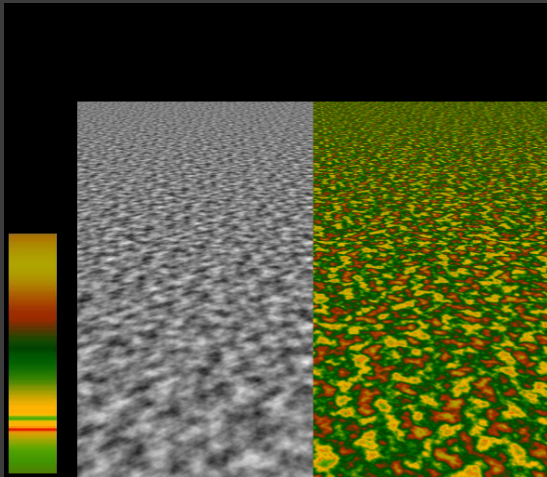
## I. Filtering Procedural Textures (only colors)



## II. Filtering Procedural Surfaces (colors and geometry)



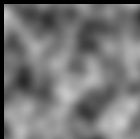
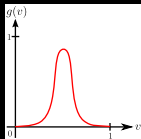
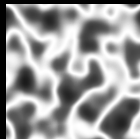
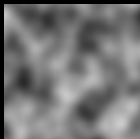
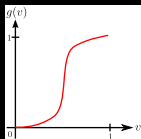
# I. Filtering Procedural Textures



## I.1 Definition

$$\text{texture}(x) = g(f(x))$$

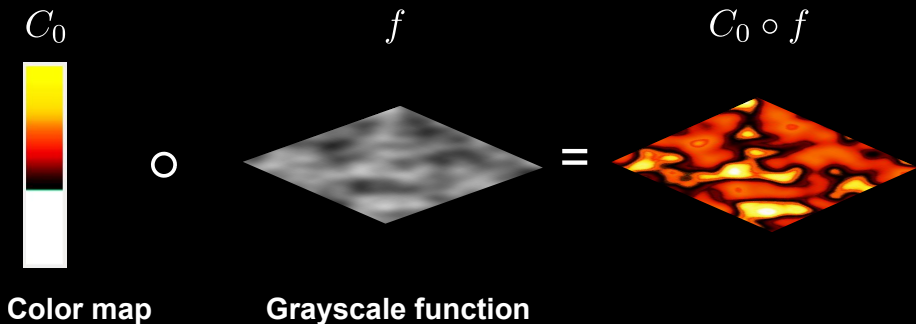
$$g \quad \circ \quad f \quad = \quad g(f)$$



$f$  = noise [Perlin83, Worley96, LLDD09]  
 $g$  = nonlinear transfer function

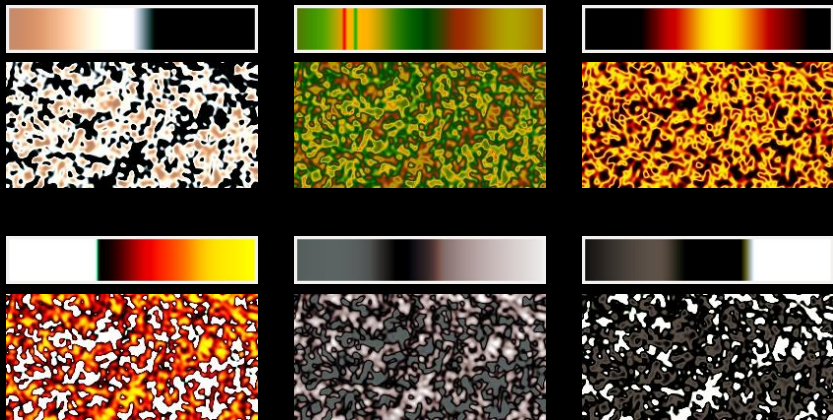
## I.1 Definition

Nonlinear operations summarized in color maps



## I.1 Definition

Nonlinear operations summarized in color maps

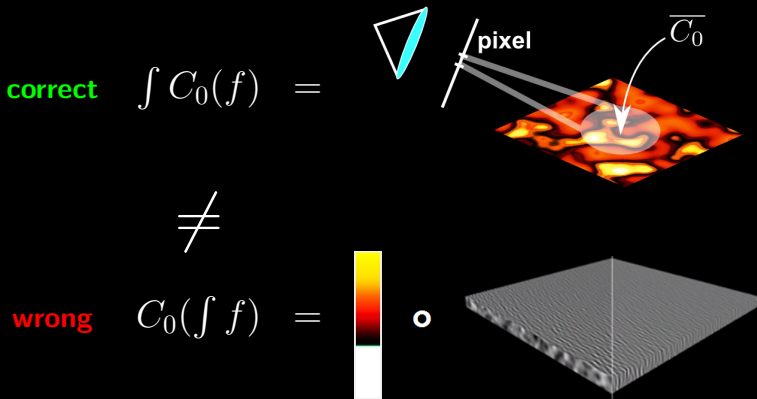


## I.2 Problem

### Important properties of procedural textures

- ▶ efficient on-the-fly evaluation
- ▶ intuitive control parameters

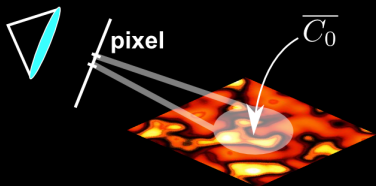
### Filtering does not work



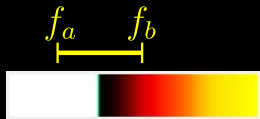
## I.3 Previous Work

[RTBS92, HCKT99, LLDD09]

$$\bar{C}_0 = \int C_0(f(x)) dx \approx \int_{f_a}^{f_b} C_0(f) df$$



texture filtering



color map

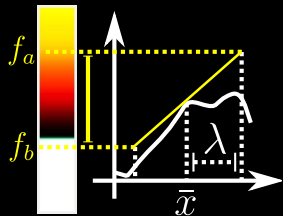


## I.3 Previous Work

### Box Filtering

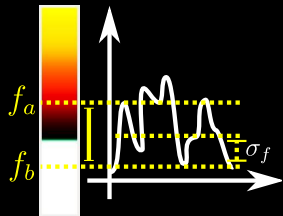
[Hart99]

- ▶ works only locally (first-order expansion)
- ▶ gradient ill-defined

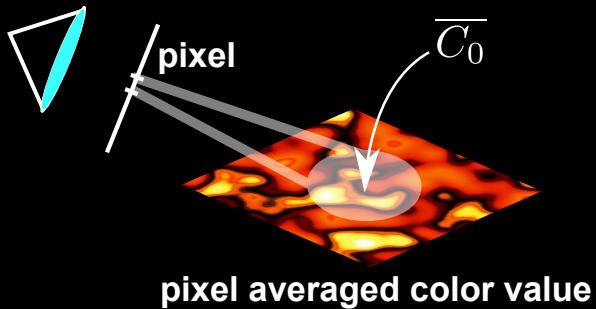


[Lagae09]

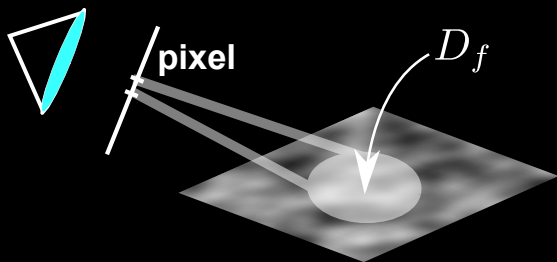
- ▶ better but Box Filter is still not ideal



## I.4 Our Method



## I.4 Our Method

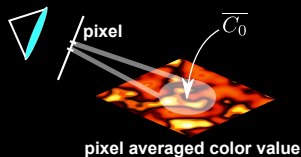


grayscale value distribution  
within pixel footprint





## I.4 Our Method



is exactly the inner product

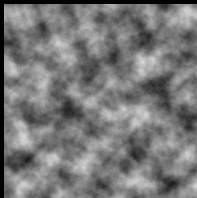
$$\bar{C}_0 = \left\langle \begin{array}{c} v \\ \left| \begin{array}{c} \text{bell curve} \\ \text{bell curve} \end{array} \right. \\ D_f \end{array} \right\rangle, \left\langle \begin{array}{c} \text{color bar} \end{array} \right\rangle$$

1. How to represent grayscale distributions?
2. How to compute the inner product?

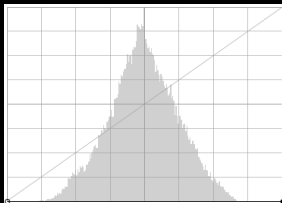
## I.4 Our Method

We choose Gaussian distributions

- ▶ noise = Gaussian process
- ▶ lightweight, analytical



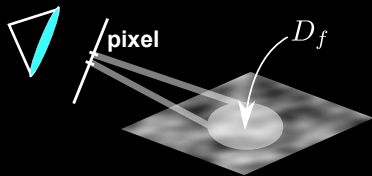
noise



noise histogram

## I.4 Our Method

1. fetch / compute  
noise Gaussian distribution

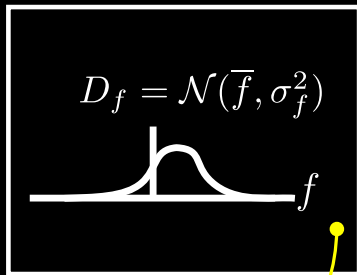
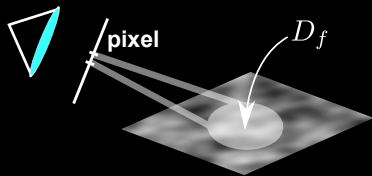


$$D_f = \mathcal{N}(\bar{f}, \sigma_f^2)$$

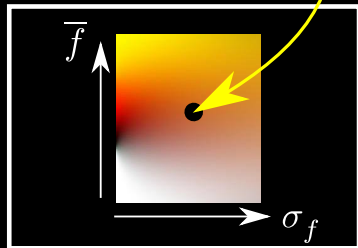
A graph showing a Gaussian distribution curve. The horizontal axis is labeled  $f$ . The curve is centered at a point marked with a vertical line, representing the mean  $\bar{f}$ . The area under the curve is shaded gray.

## I.4 Our Method

1. fetch / compute noise Gaussian distribution

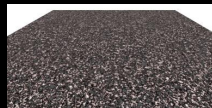
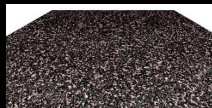
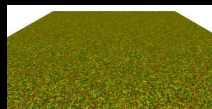
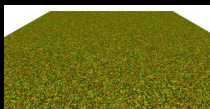
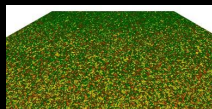
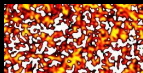
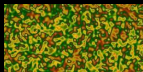


2. fetch pre-convoluted color map





# I.5 Results



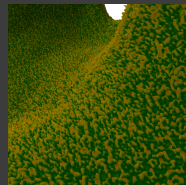
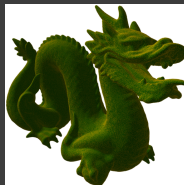
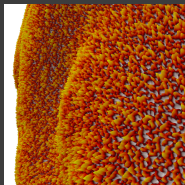
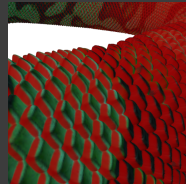
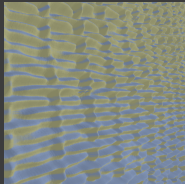
**Color map &  
close view**

**Naïve filtering**

**Ground Truth**

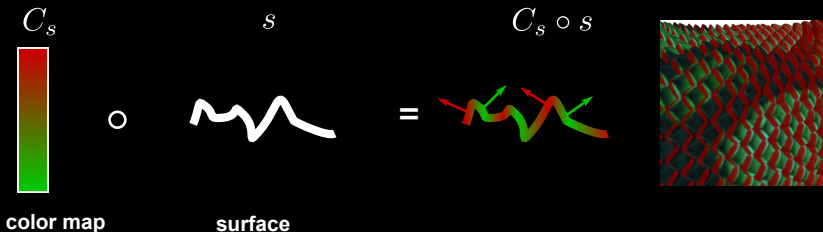
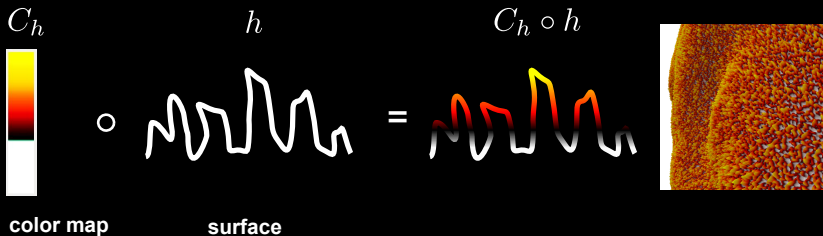
**Our model**

## II. Filtering Procedural Surfaces



## II.1 Color Mapping Surfaces

### Correlations with height and slope

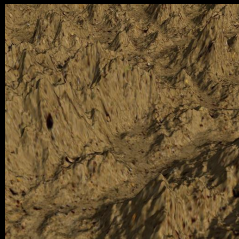


## II.1 Color Mapping Surfaces



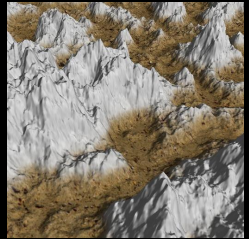
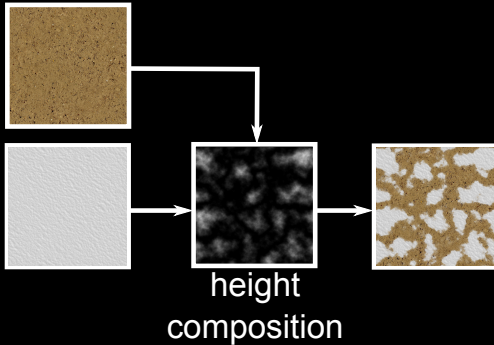
## II.1 Color Mapping Surfaces

ground textures



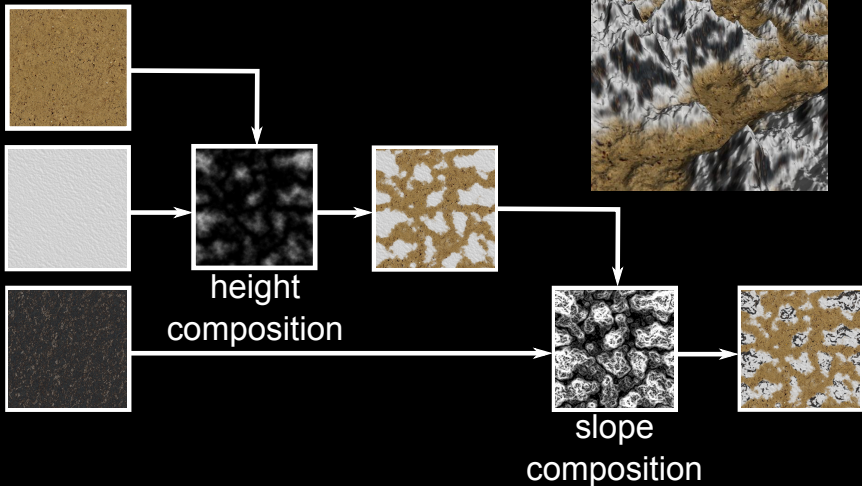
## II.1 Color Mapping Surfaces

ground textures



## II.1 Color Mapping Surfaces

ground textures



## II.1 Color Mapping Surfaces

### Correlations with height and slope

$C_h$



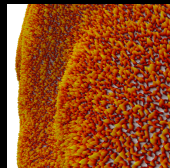
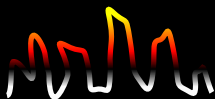
color map

$h$



surface

$C_h \circ h$



$C_s$



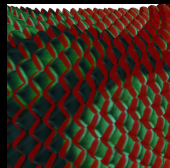
color map

$s$



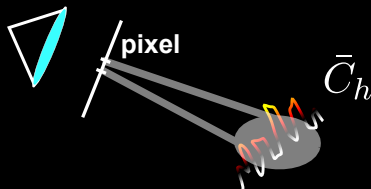
surface

$C_s \circ s$





## 11.2 Problem

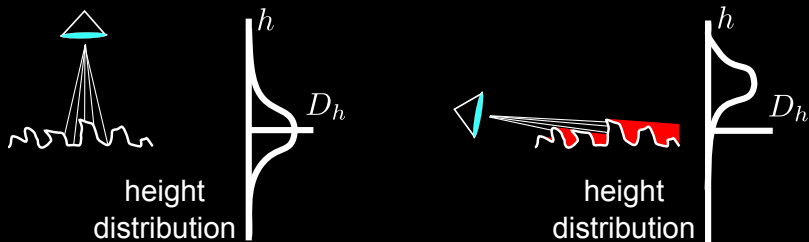


is exactly the inner product

$$\bar{C}_h = \left\langle \begin{array}{c} h \\ \text{height} \\ \text{distribution} \end{array} \right. D_h, \begin{array}{c} \text{color} \\ \text{bar} \end{array} \right\rangle$$

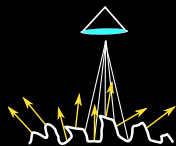
The equation shows the average height  $\bar{C}_h$  as the inner product of a height distribution and a color bar. The height distribution is represented by a bell-shaped curve with a peak at height  $h$ . The color bar is a vertical bar with a gradient from white at the bottom to yellow at the top, representing the color of the ground plane.

## II.2 Problem

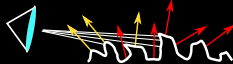


Height distribution  $D_h$  is view- and light-dependent because of **masking** and **shadowing**

## 11.2 Problem



slope (normal)  
distribution

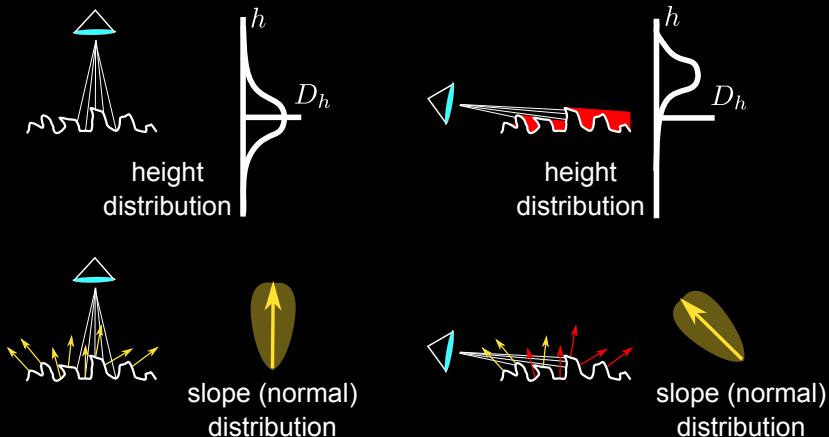


slope (normal)  
distribution



Slope distribution  $D_s$  is view-dependent  
because of **back-face culling** and **area weighting**

## II.2 Problem



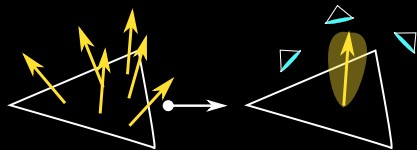
**These schemes are qualitative.  
How to model quantitatively view-dependency?**

## 11.2 Problem

View-dependency is usually NOT taken in account

e.g.

- ▶ [Smooth Transitions between Bump Rendering Algorithms], SIGGRAPH 93
- ▶ [Multiresolution Reflectance Filtering], EGSR05
- ▶ [Frequency Domain Normal Map Filtering], SIGGRAPH 07
- ▶ [LEAN Mapping], I3D 10



normal filtering on flat surface

## 11.2 Problem

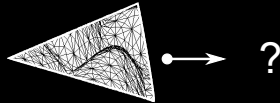
View-dependency is usually **NOT** taken in account

e.g.

- ▶ [Smooth Transitions between Bump Rendering Algorithms], SIGGRAPH 93
- ▶ [Multiresolution Reflectance Filtering], EGSR05
- ▶ [Frequency Domain Normal Map Filtering], SIGGRAPH 07
- ▶ [LEAN Mapping], I3D 10



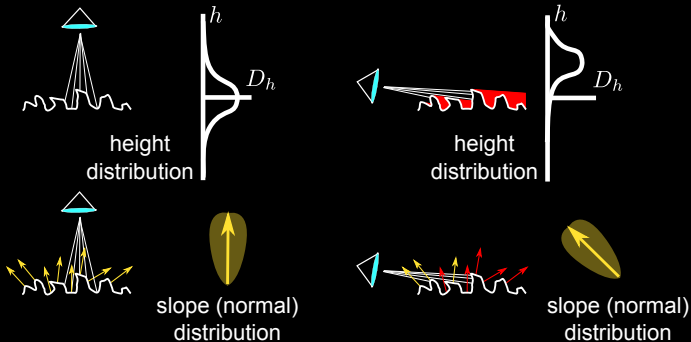
normal filtering on flat surface



normal filtering on detailed surface

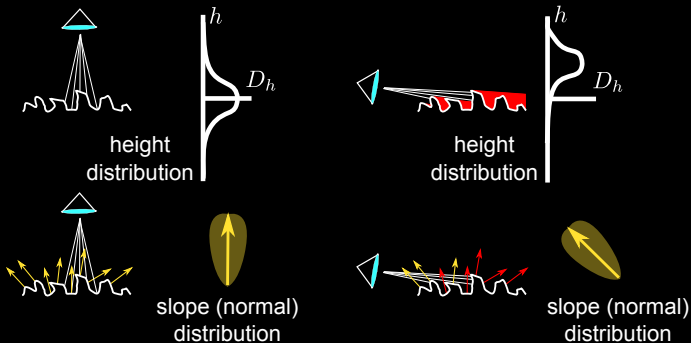
## II.3 Our Method

How to model and compute view-dependency?



## II.3 Our Method

How to model and compute view-dependency?



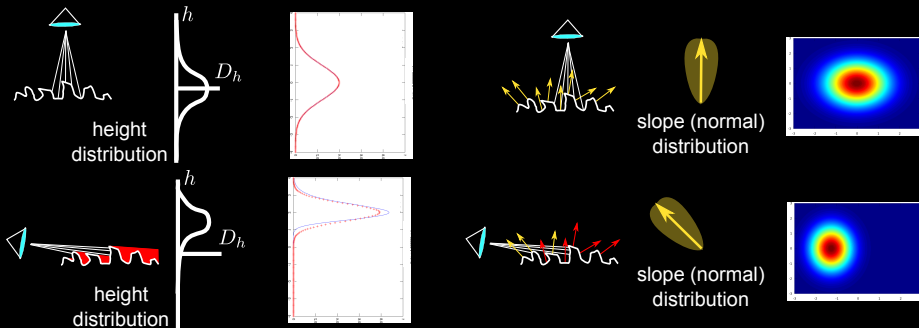
→ **micro-facet theory is the appropriate paradigm**

- ▶ physically sound formulation
- ▶ accurate analytical approximations



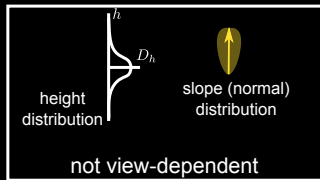
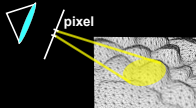
## II.3 Our Method

We derive accurate analytical approximations



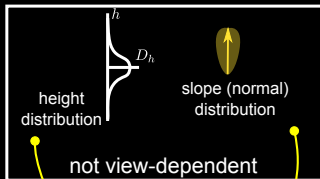
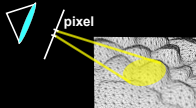
## II.3 Our Method

1. fetch / compute surface parameters

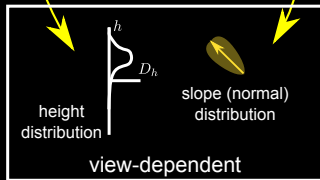


## II.3 Our Method

1. fetch / compute surface parameters

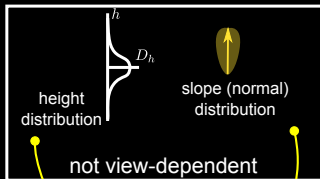
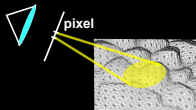


2. compute view-dependent surface parameters

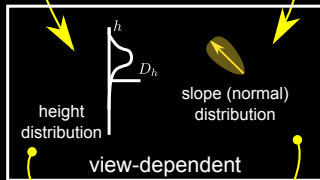


## II.3 Our Method

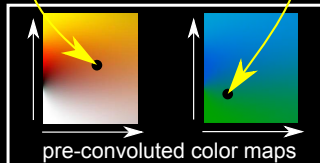
1. fetch / compute surface parameters



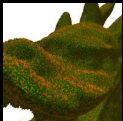
2. compute view-dependent surface parameters



3. fetch pre-convoluted color maps



## II.4 Results

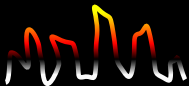


Color map &  
close view

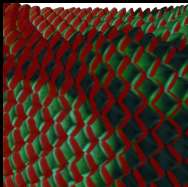
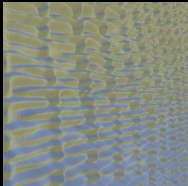
Texture filtering

Ground Truth

Surface filtering



## II.4 Results

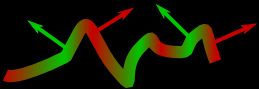


**Close view**

**Texture filtering**

**Ground Truth**

**Surface filtering**



## II.4 Results



**Texture filtering**



**Ground Truth**



**Surface Filtering**

**Tessellation  
ON**

**130Hz**

**<1Hz  
256 samples/pixel**

**130Hz**

**Tessellation  
OFF**

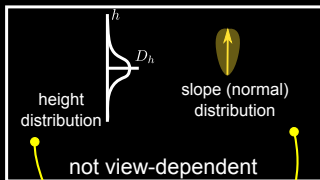
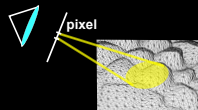
**869Hz**

**3Hz  
256 samples/pixel**

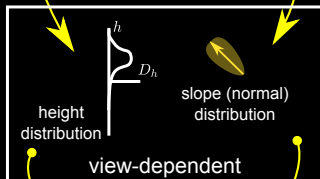
**800Hz**

## II.5 Implementation

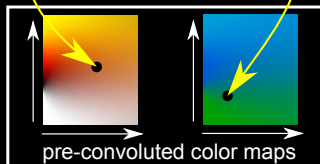
1. fetch / compute surface parameters



2. compute view-dependent surface parameters



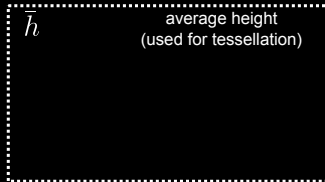
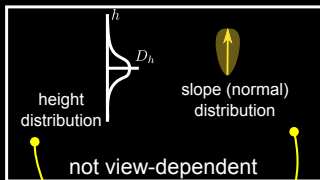
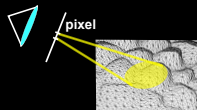
3. fetch pre-convoluted color maps



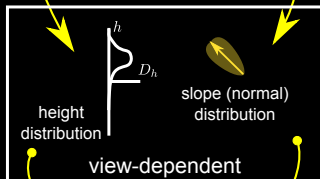


## II.5 Implementation

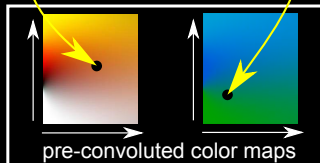
1. fetch / compute surface parameters



2. compute view-dependent surface parameters

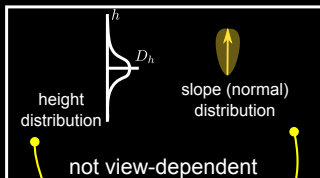
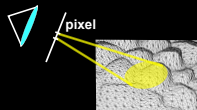


3. fetch pre-convoluted color maps



## II.5 Implementation

1. fetch / compute surface parameters

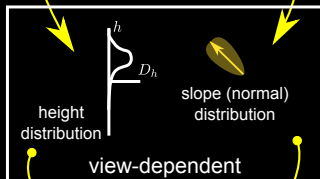


$$\bar{h}$$
$$\bar{h}^2$$

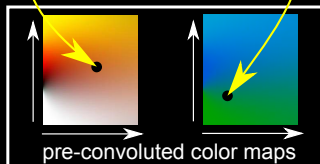
average height  
(used for tessellation)

height second momentum

2. compute view-dependent surface parameters

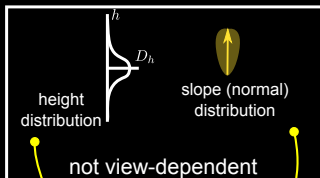
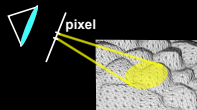


3. fetch pre-convoluted color maps



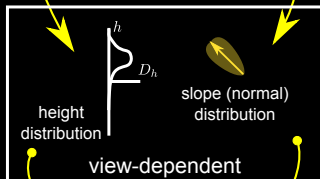
## II.5 Implementation

1. fetch / compute surface parameters

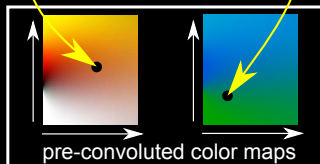


$$\begin{array}{l} \bar{h} \\ \bar{h}^2 \\ \bar{s}_x \quad \bar{s}_y \end{array} \quad \begin{array}{l} \text{average height} \\ \text{(used for tessellation)} \\ \text{height second momentum} \\ \text{average slope/normal} \\ \text{(used for shading)} \end{array}$$

2. compute view-dependent surface parameters



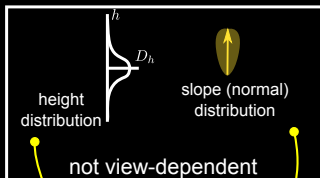
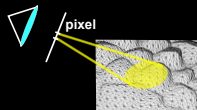
3. fetch pre-convoluted color maps



## II.5 Implementation

1.

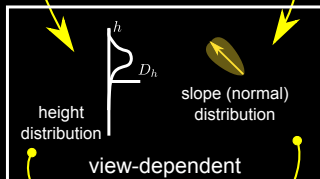
fetch / compute  
surface parameters



$\bar{h}$	average height (used for tessellation)
$\bar{h}^2$	height second momentum
$\bar{S}_x$ $\bar{S}_y$	average slope/normal (used for shading)
$\begin{bmatrix} \sigma_{s_x}^2 & c_{xy} \\ c_{xy} & \sigma_{s_y}^2 \end{bmatrix}$	slope covariance matrix (used in LEAN Mapping)

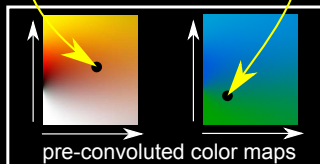
2.

compute view-dependent  
surface parameters



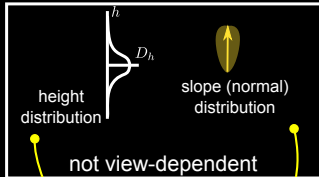
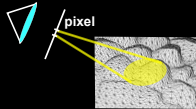
3.

fetch pre-convoluted  
color maps



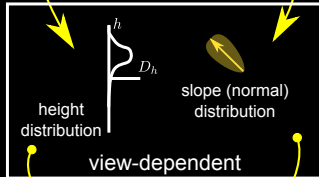
# II.5 Implementation

1. fetch / compute surface parameters



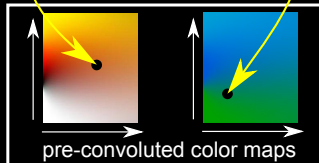
$\bar{h}$	average height (used for tessellation)
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$\begin{bmatrix} \sigma_{s_x}^2 & c_{xy} \\ c_{xy} & \sigma_{s_y}^2 \end{bmatrix}$	slope covariance matrix (used in LEAN Mapping)

2. compute view-dependent surface parameters

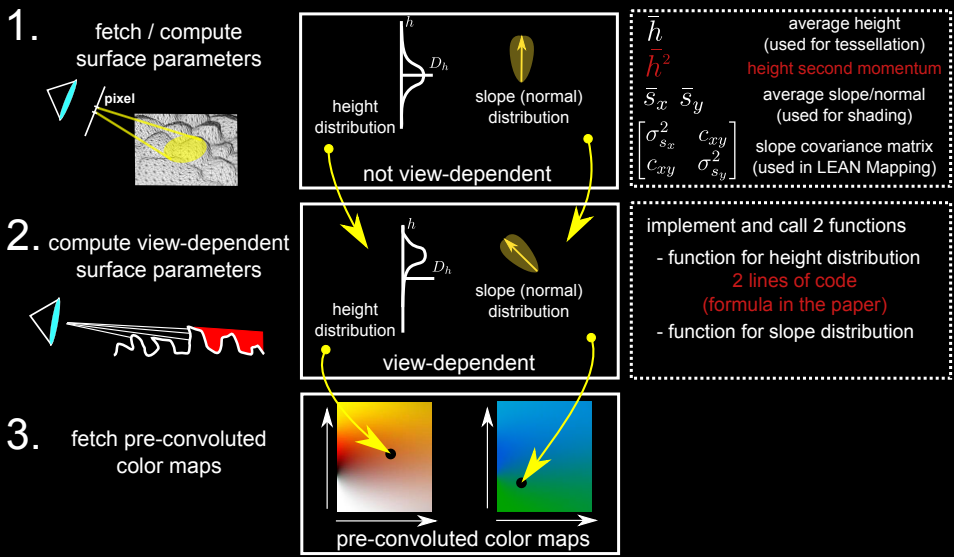


implement and call 2 functions	
-	function for height distribution
-	function for slope distribution

3. fetch pre-convoluted color maps



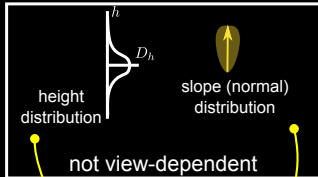
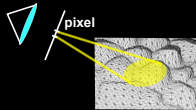
# II.5 Implementation



## II.5 Implementation

1.

fetch / compute  
surface parameters



$\bar{h}$  average height  
(used for tessellation)

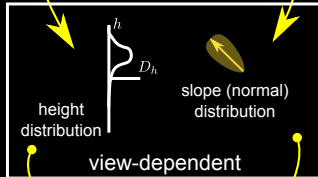
$\bar{h}^2$  height second momentum

$\bar{S}_x$   $\bar{S}_y$  average slope/normal  
(used for shading)

$\begin{bmatrix} \sigma_{s_x}^2 & c_{xy} \\ c_{xy} & \sigma_{s_y}^2 \end{bmatrix}$  slope covariance matrix  
(used in LEAN Mapping)

2.

compute view-dependent  
surface parameters

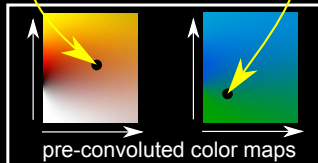


implement and call 2 functions

- function for height distribution  
2 lines of code  
(formula in the paper)
- function for slope distribution  
given in supplemental material

3.

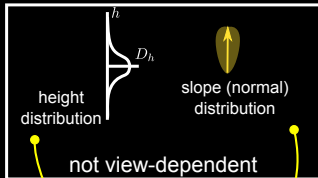
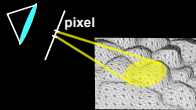
fetch pre-convoluted  
color maps



## II.5 Implementation

1.

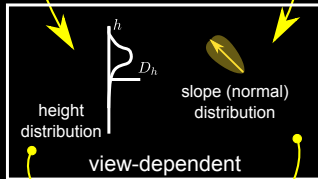
fetch / compute  
surface parameters



$\bar{h}$  average height  
(used for tessellation)  
 $\bar{h}^2$  height second momentum  
 $\bar{S}_x$   $\bar{S}_y$  average slope/normal  
(used for shading)  
 $\begin{bmatrix} \sigma_{s_x}^2 & c_{xy} \\ c_{xy} & \sigma_{s_y}^2 \end{bmatrix}$  slope covariance matrix  
(used in LEAN Mapping)

2.

compute view-dependent  
surface parameters

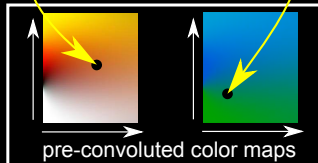


implement and call 2 functions

- function for height distribution  
2 lines of code  
(formula in the paper)
- function for slope distribution  
given in supplemental material

3.

fetch pre-convoluted  
color maps



pre-convoluted color maps

in practice we use  $256^2$  textures  
with 4 color components  
= 256KB per pre-convoluted



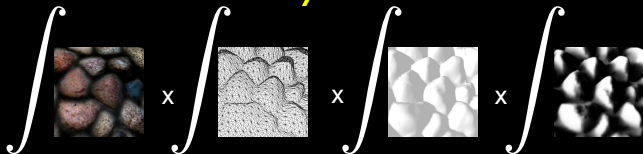
## Conclusion and Future Work

# Introduction

physically correct



$\neq$



physically wrong

energy conservation violated  
popping, aliasing, and inconsistent appearance

## Conclusion and Future Work

### Our LoD framework

- colors/material
- small-scale geometry
- visibility
- no BRDF

## Conclusion and Future Work

### Our LoD framework

- colors/material
- small-scale geometry
- visibility
- no BRDF

### Existing

#### physically-based rendering

- physically-based BRDFs
- physically incorrect LoD

## Conclusion and Future Work

### Our LoD framework

- colors/material
- small-scale geometry
- visibility
- **no BRDF**



### Existing physically-based rendering

- physically-based BRDFs
- **physically incorrect LoD**



micro-facet theory

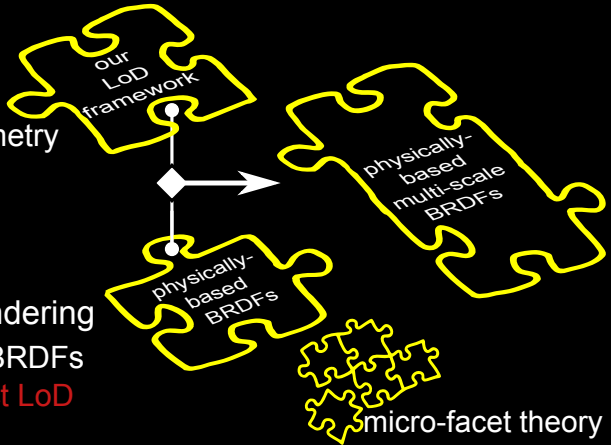
## Conclusion and Future Work

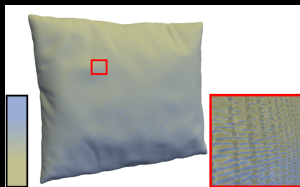
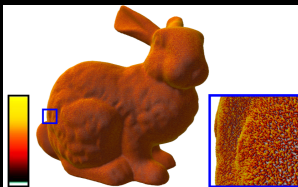
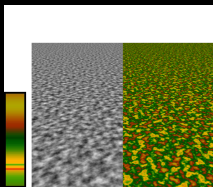
### Our LoD framework

- colors/material
- small-scale geometry
- visibility
- **no BRDF**

### Existing physically-based rendering

- physically-based BRDFs
- **physically incorrect LoD**





Thank you!

