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Black-box optimization benchmarking of IPOP-saACM-ES and BIPOP-saACM-ES on the BBOB-2012 noiseless testbed

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ABSTRACT
In this paper, we study the performance of IPOP-saACM-ES and BIPOP-saACM-ES, recently proposed self-adaptive surrogate-assisted Covariance Matrix Adaptation Evolution Strategies. Both algorithms were tested using restarts till a total number of function evaluations of 10^6D was reached, where D is the dimension of the function search space. We compared surrogate-assisted algorithms with their surrogate-less versions IPOP-aCMA-ES and BIPOP-CMA-ES, two algorithms with one of the best overall performance observed during the BBOB-2009 and BBOB-2010. The comparison shows that the surrogate-assisted versions outperform the original CMA-ES algorithms by a factor from 2 to 4 on 8 out of 24 noiseless benchmark problems, showing the best results among all algorithms of the BBOB-2009 and BBOB-2010.

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The active version of the CMA-ES proposed in [8, 11] in- terpreted as a filter (to select λₚᵥₑ promising pre-children) and/or to estimate the fitness of some individuals in the current population. An example of surrogate-assisted CMA-ES with filtering strategy can be found in [14].

A well-known drawback of surrogate-assisted optimization is a strong dependence of the results on hyper-parameters used to build the surrogate model. Some optimal settings of hyper-parameters for a specific set of problems can be found by offline tuning, however for a new problem they are unknown in the black-box scenario. Moreover, the optimal hyper-parameters may dynamically change during the optimization of the function.

Motivated by this open issues, new self-adapted surrogate-assisted aACM-ES algorithm have been proposed combining surrogate-assisted optimization of the expensive function and online optimization of the surrogate model hyper-parameters [15].

Categories and Subject Descriptors
G.1.6 [Numerical Analysis]: Optimization—global optimization, unconstrained optimization; F.2.1 [Analysis of Algorithms and Problem Complexity]: Numerical Algorithms and Problems

General Terms
Algorithms

Keywords
Benchmarking, black-box optimization, evolution strategy, CMA-ES, self-adaptation, surrogate models, ranking support vector machine, surrogate-assisted optimization

1. INTRODUCTION

When dealing with expensive optimization objectives, the surrogate-assisted approaches proceed by learning a surro-
it can be numerically controlled [8]. Since in our study we do not observe any negative effects of this issue, we will use aCMA-ES, the active version of the CMA-ES, for comparison with the surrogate-assisted algorithms.

2.2 The ** ACM-ES

The ** ACM-ES [15] is the surrogate-assisted version of the (μ/μw, λ)-CMA-ES, where the surrogate model is used, periodically instead of, the expensive function for direct optimization. The use of Ranking SVM allows to preserve the property of CMA-ES of invariance with respect to rank-preserving transformation of the fitness function. The property of invariance with respect to the orthogonal transformation of the search space is preserved thanks to the definition of the kernel function by the covariance matrix, adapted during the search.

In ** ACM-ES we perform the following surrogate-assisted optimization loop: we optimize the surrogate model \( f \) for \( n \) generations by the CMA-ES, then we continue and optimize the expensive function \( f(x) \) for one generation. To adjust the number of generations \( n \) for the next time, the model error can be computed as a fraction of incorrectly predicted comparison relations that we observe, when we compare the ranking of the last \( \lambda \) evaluated points according to \( f(x) \) and \( \hat{f} \). The ** ACM-ES uses the generation of the CMA-ES as a black-box procedure, and it has been shown in [15], that the improvement of the CMA-ES from passive to active version (aCMA-ES) leads to a comparable improvement of its surrogate-assisted versions (** ACM-ES and ** ACM-ES).

The main novelty of the ** ACM-ES is the online optimization of the surrogate model hyper-parameters during the optimization of the fitness function. The algorithm performs the search in the space of model hyper-parameters, generating \( \lambda_{hyp} \) surrogate models in each iteration. The fitness of the model can be measured as a prediction error of the ranking on the last \( \lambda \) evaluated points. This allows the user to define only the range of hyper-parameters and let algorithm to find the most suitable values for the current iteration \( t \).

The detailed description of ** ACM-ES is given in [15].

2.3 The Benchmarked Algorithms

For benchmarking we consider four CMA-ES algorithms in restart scenario: IPOP-aCMA-ES [8], BIPOP-CMA-ES [4], IPOP-** ACM-ES and BIPOP-** ACM-ES [15]. For IPOP-** ACM-ES and BIPOP-** ACM-ES we use the same parameters of the CMA-ES and termination criteria in IPOP and BIPOP scenario as in the original papers. The default parameters for ** ACM-ES algorithms are given in [15].

3. RESULTS

Results from experiments according to [5] on the benchmark functions given in [2, 6] are presented in Figures 2, 3 and 4 and in Tables 1 and 2. The expected running time (ERT), used in the figures and table, depends on a given target function value, \( f_t = \text{f}_{\text{opt}} + \Delta f \), and is computed over all relevant trials (on the first 15 instances) as the number of function evaluations executed during each trial while the best function value did not reach \( f_t \), summed over all trials and divided by the number of trials that actually reached \( f_t \) [5, 16]. Statistical significance is tested with the rank-sum test for a given target \( \Delta f_t \left(10^{-8}\right) \) as in Figure 2 using, for each trial, either the number of needed function evaluations to reach \( \Delta f_t \) (inverted and multiplied by \(-1\)), or, if the target was not reached, the best \( \Delta f \)-value achieved, measured only up to the smallest number of overall function evaluations for any unsuccessful trial under consideration.

The IPOP-** ACM-ES and BIPOP-** ACM-ES represent the same algorithm (** ACM-ES) before the first restart occurs, therefore, the results are very similar for the uni-modal functions, where the optimum usually can be found without restarts. The ** ACM-ES outperforms aCMA-ES usually by a factor from 2 to 4 on \( f_1, f_2, f_3, f_6, f_{10}, f_{11}, f_{12}, f_{13} \) and \( f_{14} \) for dimensions between 5 and 20. The speedup in dimension 2 is less pronounced for problems, where the running time is too short to improve the search. This is the case for \( f_2 \) Linear Slope function, where the speedup can be observed only for dimension 20, because the optimum can be found after about 200 function evaluations. To improve the search on functions with small budgets it would make sense to use the surrogate model right after the first \( g_{\text{start}} = 1 \) generation of the CMA-ES, while in this study this parameter \( g_{\text{start}} \) was set to 10 generations.

The good results on uni-modal functions can be explained by the fact, that while using the same amount of information (all previously evaluated points), ** ACM-ES processes this information in a more efficient way by constructing the approximation model of the function. Similar effect of more efficient exploitation of the available information can be observed for aCMA-ES in comparison to CMA-ES.

The speedup on multi-modal functions is less pronounced, because they are more difficult to approximate and the final surrogate model often has a bad precision. In this case the adaptation of the number of generations leads to an oscillation of \( n \) close to 0, such that the surrogate model is not used for optimization or used for small number of generations.

The BIPOP versions of CMA-ES usually perform better than IPOP on \( f_{23} \) and \( f_{24} \), where the optimum is more likely to be found if use small initial step-size. This leads to overall better performance of the BIPOP versions and BIPOP-** aCMA-ES in particular. The better performance of the latter in comparison with BIPOP-CMA-ES can be partially explained by the fact of using the active covariance matrix update. However, this is not the case for \( f_{20} \) functions in 5-D and \( f_{15\ldots19} \) in 20-D (see Fig. 3 and Fig. 4).

The ** ACM-ES algorithms improve the records in dimension 10 and 20 on \( f_7, f_{10}, f_{13}, f_{12}, f_{13}, f_{14}, f_{15}, f_{16}, f_{20} \).
The results presented here do not take into account the model hyper-parameters optimization, where $\lambda_{hyp}$ surrogate models should be built at each iteration, which leads to an increase of CPU time per function evaluation by a factor of $\lambda_{hyp}$. For BIPOP-*aACM-ES and IPOP-*aACM-ES $\lambda_{hyp}$ was set to 20.

5. CONCLUSION

In this paper, we have compared the recently proposed self-adaptive surrogate-assisted BIPOP-*aACM-ES and IPOP-*aACM-ES with the BIPOP-CMA-ES and IPOP-CMA-ES. The surrogate-assisted *aACM-ES algorithms outperform the original ones by a factor from 2 to 4 on uni-modal functions, and usually perform not worse on multi-modal functions. The *aACM-ES algorithms improve the records on 8 out of 24 functions in dimension 10 and 20.

6. ACKNOWLEDGMENTS

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7. REFERENCES

Figure 2: Expected running time (ERT in number of \( f \)-evaluations) divided by dimension for target function value \( 10^{-8} \) as \( \log_{10} \) values versus dimension. Different symbols correspond to different algorithms given in the legend of \( f_1 \) and \( f_{24} \). Light symbols give the maximum number of function evaluations from the longest trial divided by dimension. Horizontal lines give linear scaling, slanted dotted lines give quadratic scaling. Black stars indicate statistically better result compared to all other algorithms with \( p < 0.01 \) and Bonferroni correction number of dimensions (six). Legend: ◊ BIPOP-CMA, ▽ BIPOP-saACM, ★ IPOP-aCMA, □ IPOP-saACM.
Figure 3: Bootstrapped empirical cumulative distribution of the number of objective function evaluations divided by dimension (FEvals/D) for 50 targets in $10^{[-8..2]}$ for all functions and subgroups in 5-D. The “best 2009” line corresponds to the best ERT observed during BBOB 2009 for each single target.
Figure 4: Bootstrapped empirical cumulative distribution of the number of objective function evaluations divided by dimension (FEvals/D) for 50 targets in $10^{1-8.2}$ for all functions and subgroups in 20-D. The “best 2009” line corresponds to the best ERT observed during BBOB 2009 for each single target.
<table>
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<th>#succ</th>
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<th>1e1 1e0 1e-1 1e-3 1e-5 1e-7</th>
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<td>2.8(2) 2.7(2) 2.6(2) 2.5(2) 2.4(2)</td>
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Table 1: Expected running time (ERT in number of function evaluations) divided by the respective best ERT measured during BBOP-2009 (given in the respective first row) for different ∆f values in dimension 5. The central 80% range divided by two is given in braces. The median number of conducted function evaluations is additionally given in italics, if ERT(10⁻⁷) = ∞. #succ is the number of trials that reached the final target f_{opt} + 10⁻⁸. Best results are printed in bold.
Table 2: Expected running time (ERT in number of function evaluations) divided by the respective best ERT measured during BBOB-2009 (given in the respective first row) for different $\Delta f$ values in dimension 20. The central 80% range divided by two is given in braces. The median number of conducted function evaluations is additionally given in italics. # succ is the number of trials that reached the final target $f_{\min} + 10^{-5}$. Best results are printed in bold.