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Joint Identification of Stepper Motor Parameters and of Initial Encoder Offset [★]

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Abstract: The paper presents a new procedure to identify at the same time the electrical parameters of a permanent magnet stepper motor (PMSM) and the initial offset of an incremental encoder. The model considers effects due to the permanent magnet and to variable reluctance, and the resulting theory is applicable to cases where both or only one of these terms is present. The standard DQ model of PMSM's assumes that the permanent magnet is lined up with a winding when the position is zero. When an incremental encoder is used, an initialization procedure is required to zero the initial offset. In contrast, this paper computes a transformed model that accounts for the initial offset. then develops a least-squares identification algorithm that estimates the machine's electrical parameters together with the offset angle. Experiments show that the estimation procedure and a closed-control method using the estimated offset perform similarly compared to when the offset is reset to zero using an initialization procedure.

Keywords: Permanent magnet stepper motor, synchronous motors, parameter identification, offset calibration, sliding modes.

1. INTRODUCTION

Permanent Magnet Stepper Motors (PMSM's) are widely used in industry for position control, especially in manufacturing applications. PMSM's are more robust than brush DC motors and produce a high torque per volume. They are often controlled in open-loop, although the potential loss of synchronism limits operation away from resonances and from high acceleration profiles. These problems can be resolved by using closed-loop control methods with position sensors of sufficient precision. The typical position sensor in industrial applications is the incremental encoder. With such a sensor, the zero position is the motor position when the system is powered-up. However, precise control methods using the *DQ* transformation require that the zero position be aligned with the permanent magnet. An initialization procedure must then be implemented to zero the initial position offset. Typically, this is achieved by applying a large current to one phase of the motor. However, this technique assumes that the load and friction torques are sufficiently small so that the position converges to the desired value. In this paper, we propose an identification procedure that eliminates the need for initialization of the position sensor. It combines the identification of the

machine's electrical parameters with the estimation of the offset angle.

Modelling of PMSM's is discussed in Goedel [1984] and Sinha et al. [1974], while the estimation of PMSM parameters was studied in Blauch et al. [1993], Kim and Lorenz [2002], and Nahid Mobarakeh et al. [2001]. Methods to calibrate the position sensor include Konghirun [2005], where an automatic offset calibration is proposed for Quadrature Encoder Pulse (QEP), Segarich et al. [2009] where a method based on the induced currents through the stator windings is developed, and Jung and Ha [1998] where a solution is proposed using the same transformation as in this article, but machine parameters are not estimated.



Fig. 1. Test Bench available at the LAGIS

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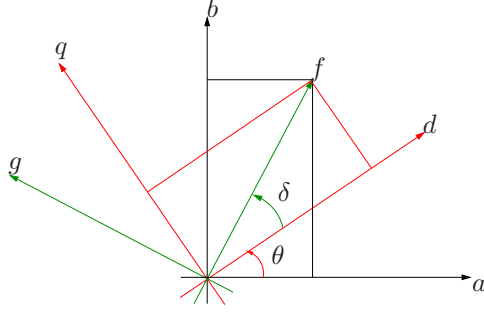


Fig. 2. Transformation of variables in the different frames

The contribution of this paper is to show that joint estimation of the motor parameters and of the offset is possible with a relatively simple algorithm. A model for a hybrid stepper motor is considered, which includes pure PM stepper motors and synchronous reluctance motors as special cases. Experiments were performed using the test bench shown on figure 1, available at the LAGIS laboratory, École Centrale de Lille in France. The results show that the method is as effective at obtaining the motor parameters as a method based on DQ identification and encoder initialization. Closed-loop control results are also comparable.

The article is divided into four parts. Section 2 presents the model of the PMSM in three different reference frames. In Section 3, an identification procedure is developed for systems including an offset angle. Section 4 presents the experimental results of the identification and compares the results to those obtained when the sensor is initialized. The last section is devoted to evaluating the closed-loop performance.

2. MODEL OF THE PMSM

In this section, the model of a hybrid PMSM is presented in three different frames, including the frame that will be used for the joint identification of the motor parameters and of the position offset. The axes of the different frames are shown in Fig. 2.

2.1 Model in the winding frame $a - b$:

The electrical equations for the two windings a and b of the PMSM are given by

$$\begin{cases} \frac{d\Psi_a}{dt} = v_a - Ri_a \\ \frac{d\Psi_b}{dt} = v_b - Ri_b \end{cases} \quad (1)$$

where Ψ_a and Ψ_b are the total flux linkages in windings a and b , v_a and v_b are the voltages applied to the windings, i_a and i_b are the winding currents, and R is the resistance of a winding. Considering a PMSM with n_p rotor teeth, the total flux linkages are assumed to be of the form

$$\begin{pmatrix} \Psi_a \\ \Psi_b \end{pmatrix} = L(\theta) \begin{pmatrix} i_a \\ i_b \end{pmatrix} + \Psi_0 D(\theta) \quad (2)$$

where

$$L(\theta) = \begin{pmatrix} L_0 + L_2 \cos(2n_p\theta) & L_2 \sin(2n_p\theta) \\ L_2 \sin(2n_p\theta) & L_0 - L_2 \cos(2n_p\theta) \end{pmatrix} \quad (3)$$

$$D(\theta) = \begin{pmatrix} \cos(n_p\theta) \\ \sin(n_p\theta) \end{pmatrix} \quad (4)$$

θ is the angular position of the rotor, L_0 is the average inductance of a winding as the motor rotates, L_2 is the mean-to-peak variation of the inductance, and Ψ_0 is the contribution of the permanent magnet to the flux Ψ_a when $\theta = 0$.

Using the expressions for the fluxes, the electrical equations become

$$L(\theta) \frac{d}{dt} \begin{pmatrix} i_a \\ i_b \end{pmatrix} = \begin{pmatrix} v_a - Ri_a \\ v_b - Ri_b \end{pmatrix} - \frac{\partial L(\theta)}{\partial \theta} \omega \begin{pmatrix} i_a \\ i_b \end{pmatrix} - \Psi_0 \omega \frac{\partial D(\theta)}{\partial \theta} \quad (4)$$

where $\omega = d\theta/dt$ is the angular velocity of the rotor and

$$\begin{aligned} \frac{\partial L(\theta)}{\partial \theta} &= 2n_p L_2 \begin{pmatrix} -\sin(2n_p\theta) & \cos(2n_p\theta) \\ \cos(2n_p\theta) & \sin(2n_p\theta) \end{pmatrix} \\ \frac{\partial D(\theta)}{\partial \theta} &= n_p \begin{pmatrix} -\sin(n_p\theta) \\ \cos(n_p\theta) \end{pmatrix} \end{aligned} \quad (5)$$

The mechanical equation is

$$J \frac{d\omega}{dt} = -f_v \omega - C_r \text{sgn}(\omega) + \tau_e \quad (6)$$

where J is the moment of inertia of the rotor (including the load), f_v is the coefficient of viscous friction, C_r is the coefficient of Coulomb friction and τ_e is the torque. By conservation of energy, the torque is given by

$$\tau_e = \Psi_0 \begin{pmatrix} i_a & i_b \end{pmatrix} \frac{\partial D(\theta)}{\partial \theta} + \frac{1}{2} \begin{pmatrix} i_a & i_b \end{pmatrix} \frac{\partial L(\theta)}{\partial \theta} \begin{pmatrix} i_a \\ i_b \end{pmatrix} \quad (7)$$

which yields

$$\begin{aligned} \tau_e &= -Ki_a \sin(n_p\theta) + Ki_b \cos(n_p\theta) \\ &\quad + n_p L_2 ((-i_a^2 + i_b^2) \sin(2n_p\theta) + 2i_a i_b \cos(2n_p\theta)) \end{aligned} \quad (8)$$

where $K = n_p \Psi_0$ is the torque constant (and also the back-EMF constant).

2.2 Model in the rotating frame $d - q$:

The model can be transformed using Park's transformation Park [1929],

$$\begin{pmatrix} \Psi_d \\ \Psi_q \end{pmatrix} = U(\theta) \begin{pmatrix} \Psi_a \\ \Psi_b \end{pmatrix} \quad (9)$$

where

$$U(\theta) = \begin{pmatrix} \cos(n_p\theta) & \sin(n_p\theta) \\ -\sin(n_p\theta) & \cos(n_p\theta) \end{pmatrix} \quad (10)$$

The inverse transformation is

$$\begin{pmatrix} \Psi_a \\ \Psi_b \end{pmatrix} = U^T(\theta) \begin{pmatrix} \Psi_d \\ \Psi_q \end{pmatrix} \quad (11)$$

Differentiating (11)

$$\frac{d}{dt} \begin{pmatrix} \Psi_a \\ \Psi_b \end{pmatrix} = U^T(\theta) \frac{d}{dt} \begin{pmatrix} \Psi_d \\ \Psi_q \end{pmatrix} + \omega \frac{\partial U^T(\theta)}{\partial \theta} \begin{pmatrix} \Psi_d \\ \Psi_q \end{pmatrix} \quad (12)$$

where

$$\frac{\partial U(\theta)}{\partial \theta} = n_p \begin{pmatrix} -\sin(n_p\theta) & \cos(n_p\theta) \\ -\cos(n_p\theta) & -\sin(n_p\theta) \end{pmatrix} \quad (13)$$

Therefore

$$\begin{aligned}
\frac{d}{dt} \begin{pmatrix} \Psi_d \\ \Psi_q \end{pmatrix} &= U(\theta) \frac{d}{dt} \begin{pmatrix} \Psi_a \\ \Psi_b \end{pmatrix} - \omega U(\theta) \frac{\partial U^T(\theta)}{\partial \theta} \begin{pmatrix} \Psi_d \\ \Psi_q \end{pmatrix} \\
&= U(\theta) \begin{pmatrix} v_a - Ri_a \\ v_b - Ri_b \end{pmatrix} - n_p \omega \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} \Psi_d \\ \Psi_q \end{pmatrix} \\
&= \begin{pmatrix} v_d - Ri_d + n_p \omega \Psi_q \\ v_q - Ri_q - n_p \omega \Psi_d \end{pmatrix} \quad (14)
\end{aligned}$$

while

$$\begin{aligned}
\begin{pmatrix} \Psi_d \\ \Psi_q \end{pmatrix} &= U(\theta) L(\theta) U^T(\theta) \begin{pmatrix} i_d \\ i_q \end{pmatrix} + \Psi_0 U(\theta) D(\theta) \\
&= L(0) \begin{pmatrix} i_d \\ i_q \end{pmatrix} + \begin{pmatrix} \Psi_0 \\ 0 \end{pmatrix} \quad (15)
\end{aligned}$$

where

$$L(0) = \begin{pmatrix} L_0 + L_2 & 0 \\ 0 & L_0 - L_2 \end{pmatrix} \quad (16)$$

The DQ model of the hybrid PMSM becomes

$$\begin{aligned}
L_d \frac{di_d}{dt} &= v_d - Ri_d + n_p \omega L_q i_q \\
L_q \frac{di_q}{dt} &= v_q - Ri_q - n_p \omega L_d i_d - K\omega \quad (17)
\end{aligned}$$

where

$$L_d = L_0 + L_2, \quad L_q = L_0 - L_2 \quad (18)$$

The torque is

$$\begin{aligned}
\tau_e &= \Psi_0 (i_d \ i_q) U(\theta) \frac{\partial D(\theta)}{\partial \theta} \\
&\quad + \frac{1}{2} (i_d \ i_q) U(\theta) \frac{\partial L(\theta)}{\partial \theta} U^T(\theta) \begin{pmatrix} i_d \\ i_q \end{pmatrix} \quad (19)
\end{aligned}$$

After simplifications

$$\tau_e = K i_q + n_p (L_d - L_q) i_d i_q \quad (20)$$

The second term in the torque equation is the reluctance torque. In some permanent magnet motors, the torque is small enough that one can assume $L_d = L_q$. Conversely, a synchronous reluctance motor corresponds to $K = 0$. The motor model considered here encompasses all these cases.

The $d - q$ transformation is advantageous because it results in constant voltages and currents at constant speed (instead of the high-frequency phase variables). However, the $d - q$ transformation requires a position measurement that is aligned with the d axis. For systems using an incremental encoder, this means that the system must be initialized so that the back-emf term $K\omega$ only shows up in the q axis, *i.e.*, so that the axis of the PM is aligned with phase a when $\theta = 0$.

2.3 Model in the rotating frame with position offset $f - g$:

Consider now the effect of a position offset, so that the actual position is δ when the measured value is 0. The dq transformation is applied to the variables using the measured angle, and the transformed variables are labelled fg instead of dq . This means that the variables are transformed into an $f - g$ frame of reference rotating at the same speed as the $d - q$ frame, but with some offset angle δ , and

$$\begin{aligned}
\begin{pmatrix} \Psi_f \\ \Psi_g \end{pmatrix} &= U(\theta + \delta) \begin{pmatrix} \Psi_a \\ \Psi_b \end{pmatrix} \\
&= U(\delta) \begin{pmatrix} \Psi_d \\ \Psi_q \end{pmatrix} \quad (21)
\end{aligned}$$

Using the same derivations as for the $d - q$ transformation

$$\frac{d}{dt} \begin{pmatrix} \Psi_f \\ \Psi_g \end{pmatrix} = \begin{pmatrix} v_f - Ri_f + n_p \omega \Psi_g \\ v_g - Ri_g - n_p \omega \Psi_f \end{pmatrix} \quad (22)$$

while

$$\begin{aligned}
\begin{pmatrix} \Psi_f \\ \Psi_g \end{pmatrix} &= U(\delta) \begin{pmatrix} L_d i_d + \Psi_0 \\ L_q i_q \end{pmatrix} \\
&= U(\delta) \begin{pmatrix} L_d & 0 \\ 0 & L_q \end{pmatrix} U^T(\delta) \begin{pmatrix} i_f \\ i_g \end{pmatrix} + \Psi_0 \begin{pmatrix} \cos(n_p \delta) \\ -\sin(n_p \delta) \end{pmatrix} \\
&= L(-\delta) \begin{pmatrix} i_f \\ i_g \end{pmatrix} + \Psi_0 D(-\delta) \quad (23)
\end{aligned}$$

It follows that the electrical equations of the $f - g$ model of the motor are

$$\frac{d}{dt} \begin{pmatrix} i_f \\ i_g \end{pmatrix} = L^{-1}(-\delta) \begin{pmatrix} v_f - Ri_f + n_p \omega \Psi_g \\ v_g - Ri_g - n_p \omega \Psi_f \end{pmatrix} \quad (24)$$

and the torque is

$$\begin{aligned}
\tau_e &= K (i_f \sin(n_p \delta) + i_g \cos(n_p \delta)) \\
&\quad + n_p (L_d - L_q) \left(\frac{1}{2} \sin(2n_p \delta) (i_f^2 - i_g^2) + \cos(2n_p \delta) i_f i_g \right) \quad (25)
\end{aligned}$$

3. IDENTIFICATION OF THE PARAMETERS

In this section, a method is proposed for the identification of the machine parameters, including the offset angle. The least-squares algorithm is at the heart of the identification procedure (Blanch et al. [1993]). Consider the equation

$$y[n] = W^T[n] P_{nom} \quad (26)$$

where y is the output vector, W is the regressor matrix, and P_{nom} is the nominal (unknown) parameter vector. Given measurements of y and W , the objective is to determine P , an estimate of the nominal parameter vector P_{nom} . The error equation is formed by subtracting the output from the estimated output. By definition, the residual error R_e is equal to the sum of the norm squared error over an interval $[N_0, N_1]$, and the least-squares estimate minimizes the residual error.

3.1 Identification algorithm without offset

At steady-state, the $d - q$ variables are constant. With $\delta = 0$, it follows that

$$\begin{pmatrix} v_d \\ v_q \end{pmatrix} = \begin{pmatrix} i_d & 0 & -n_p \omega i_q & 0 \\ i_q & n_p \omega i_d & 0 & K\omega \end{pmatrix} \begin{pmatrix} R \\ L_q \\ L_d \\ K \end{pmatrix} \quad (27)$$

Equation (26) is applicable with

$$y[n] = \begin{pmatrix} v_d[n] \\ v_q[n] \end{pmatrix}$$

$$W[n] = \begin{pmatrix} i_d[n] & i_q[n] \\ -n_p\omega[n]i_q[n] & 0 \\ 0 & n_p\omega i_d[n] \\ 0 & \omega[n] \end{pmatrix}$$

$$P_{nom} = (R \ L_d \ L_q \ K)^T$$

Then, $L_0 = (L_d + L_q)/2$ and $L_2 = (L_d - L_q)/2$.

3.2 Identification algorithm with offset

In the same manner, the variables in the $f-g$ frame (24) are related by

$$\begin{pmatrix} v_f \\ v_g \end{pmatrix} = R \begin{pmatrix} i_f \\ i_g \end{pmatrix} + n_p\omega \begin{pmatrix} -\Psi_f \\ \Psi_g \end{pmatrix} \quad (28)$$

where

$$\begin{pmatrix} \Psi_f \\ \Psi_g \end{pmatrix} = \begin{pmatrix} L_0 + L_2 \cos(2n_p\delta) & -L_2 \sin(2n_p\delta) \\ -L_2 \sin(2n_p\delta) & L_0 - L_2 \cos(2n_p\delta) \end{pmatrix} \begin{pmatrix} i_f \\ i_g \end{pmatrix} + K\omega \begin{pmatrix} \sin(n_p\delta) \\ \cos(n_p\delta) \end{pmatrix} \quad (29)$$

Equation (26) is applicable with

$$y[n] = \begin{pmatrix} v_f[n] \\ v_g[n] \end{pmatrix}$$

$$W[n] = \begin{pmatrix} i_f[n] & i_g[n] \\ n_p\omega[n]i_f[n] & -n_p\omega[n]i_g[n] \\ -n_p\omega[n]i_g[n] & 0 \\ 0 & n_p\omega i_f[n] \\ \omega[n] & 0 \\ 0 & \omega[n] \end{pmatrix}$$

$$P_{nom} = (R \ L_1 \sin(2n_p\delta) \ L_0 - L_1 \cos(2n_p\delta) \ \dots \ L_0 + L_1 \cos(2n_p\delta) \ K \sin(n_p\delta) \ K \cos(n_p\delta))^T$$

From the estimated vector P , estimates of the original parameters can be deduced using $R = p_1$, $L_0 = (p_3 + p_4)/2$, $K = \sqrt{p_5^2 + p_6^2}$, $L_2 = (p_5^2 + p_6^2)p_2/(2p_5p_6)$, and

$$\delta = \begin{cases} \arctan\left(\frac{p_5}{p_6}\right)/n_p & \text{if } \hat{c} > 0 \\ \pi/2n_p & \text{if } \hat{s} = 1 \\ -\pi/2n_p & \text{if } \hat{s} = -1 \\ \left(\arctan\left(\frac{p_5}{p_6}\right) - \pi\right)/n_p & \text{if } \hat{c} < 0 \text{ and } \hat{s} > 0 \\ \left(\arctan\left(\frac{p_5}{p_6}\right) + \pi\right)/n_p & \text{if } \hat{c} < 0 \text{ and } \hat{s} < 0 \end{cases}$$

where $\hat{c} = p_6/\sqrt{p_5^2 + p_6^2}$, $\hat{s} = p_5/\sqrt{p_5^2 + p_6^2}$ are estimates of $\cos(n_p\delta)$ and $\sin(n_p\delta)$, respectively.

4. EXPERIMENTAL RESULTS

Experiments were performed by applying various voltages v_f and v_g . Due to the open-loop stability of the motor, the speed converged even with a position offset. Once the velocity was (approximately) constant, the average values

of the currents and of the velocity were computed over a small time interval, yielding one data point for the least-squares algorithm. Various values of v_f and v_g were applied to the motor to obtain velocities covering a large range. Multiple data points were thereby obtained for the least-squares algorithm, from which estimates of the parameters were computed.

To evaluate the results, two cases are discussed. In the first subsection, $f-g$ identification is performed using the encoder with an offset δ . In the second subsection, the encoder is initialized by applying a DC current to winding a and $d-q$ identification is performed.

4.1 Identification with position offset

To show the performance of the offset estimator, identification was performed with and without the parameter δ . Fig. 3 shows the output vector from (26) as a function of ω , which is the same in both cases. The components of the output vector are the voltages v_f and v_g , whose jagged appearance is due to the fact that multiple values of the voltages can yield the same velocity, and multiple values were deliberately applied to increase the richness of the data. The green curve shows the fit from the least-squares algorithm (*i.e.*, $W^T[n]P$, where P is the least-squares estimate of the parameters) when the offset is not estimated. The red curve shows the least-squares fit when the offset is estimated. The match of the least-squares fit with the data on the figure is found to be very good when the offset is included, but not otherwise.

The estimated values are given in Table 1. Case 1 is when the offset is not included, and case 2 when it is. The electrical parameters and the back-emf will be compared to the parameters identified in the next section using the $d-q$ procedure. The angle estimated in the experiment is $\delta = \frac{-1.08}{50} \text{rad} = -1.24^\circ$, or 62 electrical degrees.

4.2 Identification with encoder initialization

When the encoder is initially calibrated using a DC current, the least-squares algorithm is applied in the $d-q$ frame using equations (27). The results are shown Fig. 4. Similarly to the previous section, the output vector from

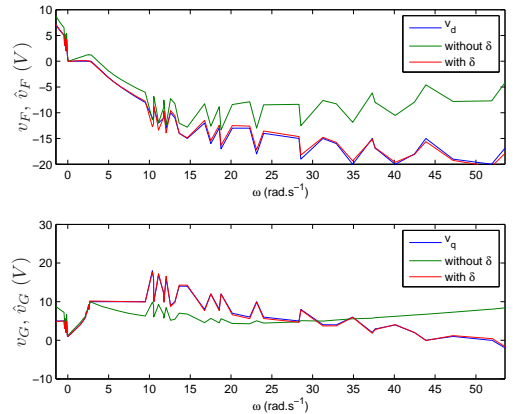


Fig. 3. Representation of the identification of the electrical parameters and the calibrage offset in the $f-g$ frame

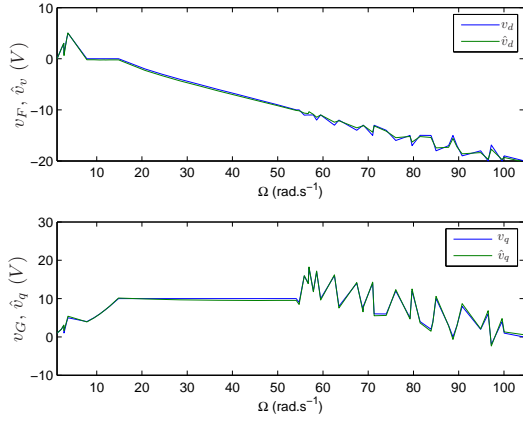


Fig. 4. Representation of the identification of the electrical parameters in the $d - q$ frame

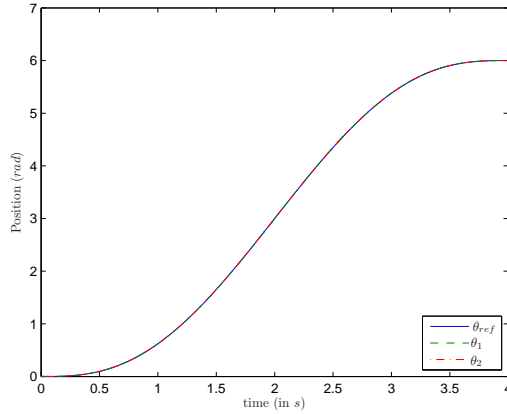


Fig. 5. Trajectory tracking (Slow experimentation)

(26) is shown as a function of ω , as well as the fit from the least-squares algorithm. The least-squares fit is very good. The results are shown in Table 1 as case 3. Compared to case 2, the estimates are very close. The small variation between the parameters may originate from the fact that the experiments are different. Indeed, Fig 4 shows that the velocity reached by the motor for the same input voltage is bigger when the position is initialized.

5. CLOSED LOOP PERFORMANCES

The estimated parameters were also used in closed-loop control experiments. The control law used in this section relied on the flatness of the model and high-order sliding modes (see Nollet et al. [2008]). The control law and the trajectory to be tracked are the same as in Nollet et al. [2008], but with the inductance L replaced by L_d and L_q

Parameters	Case 1	Case 2	Case 3
$R(\Omega)$	3.69	2.80	2.83
$L_0(mH)$	10.2	9.8	10.7
$L_2(mH)$	-0.36	-0.59	-0.33
$K(Nm.A^{-1})$	0.088	0.29	0.27
$\delta(rad.s^{-1})$	X	$-21.7.10^{-3}$	X

Table 1. Results of the parameter estimation in the $d - q$ frame.

where applicable. We present the results of experiments at two different speeds. For both cases, the tracking is shown for the angle calibrated using the estimated angle δ , and using an initialization with a DC current i_a .

The desired position in the "slow" experiment goes from 0 to $6rad$ in 4 seconds, following a trajectory based on a Bernstein polynomial interpolation equation of degree 5. On Fig 5, the following variables are plotted: the desired position θ_{ref} is shown in blue, the position in the case where the estimated δ is used (case 1) is shown in green, and the position in the case where the position is initialized using i_a (case 2) is shown in red. Fig 6 shows the respective errors. One finds that there is no major difference between the two solutions.

For the second experiment, the position moves from 0 to $60rad$ in 4 seconds. The results are plotted Fig. 7 and 8 and show that, at higher speed, both solutions gives comparable results.

6. CONCLUSIONS

In this paper, a method was proposed to estimate jointly the PMSM parameters and the initial offset angle of an incremental encoder. Special cases of the hybrid PMSM model include pure PM motors and synchronous reluctance motors. Although initialization of an encoder can be easily performed by applying a current to one phase of the motor, the method assumes that the load and friction torques are sufficiently small so that the position reaches the desired position. The proposed method does not make such an assumption and has the additional benefit of estimating not only the offset angle but also the machine's electrical parameters. Such results could be used for the tuning of the control law, or for failure detection. The use of online estimation methods using the algorithms presented in Delpoux and Floquet [2011] is also being investigated. As parameters may vary over time, such methods would make it possible to update the model parameters during real-time operation.

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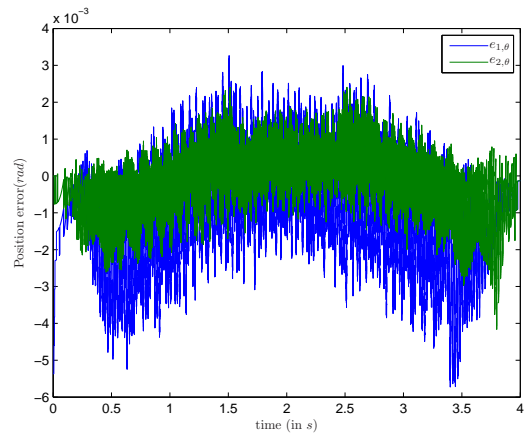


Fig. 6. Tracking error (Slow experimentation)

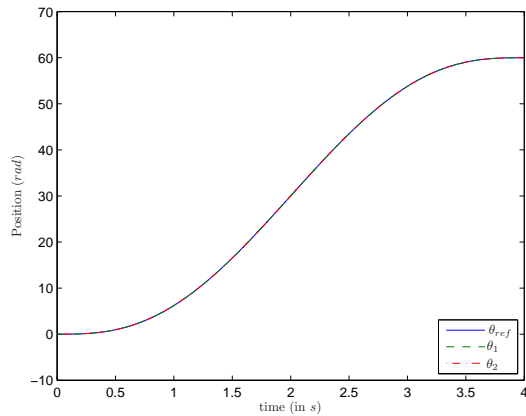


Fig. 7. Trajectory tracking (Fast experimentation)

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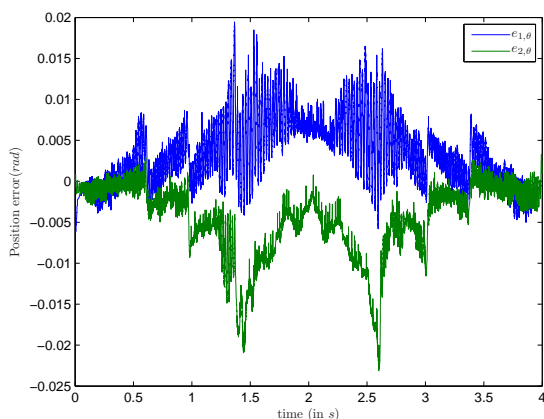


Fig. 8. Tracking error (Fast experimentation)