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Mmg3d : User Guide

Cécile Dobrzynski

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Mmg3d : User Guide

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Project-Team Bacchus

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Abstract: *Mmg3d* is a tetrahedral fully automatic remesher. Starting from a tetrahedral mesh, it produces quasi-uniform meshes with respect to a metric tensor field. This tensor prescribes a length and a direction for the edges, so that the resulting meshes will be anisotropic. The software is based on local mesh modifications and an anisotropic version of Delaunay kernel is implemented to insert vertices in the mesh. Moreover, *Mmg3d* allows one to deal with rigid body motion and moving meshes. When a displacement is prescribed on a part of the boundary, a final mesh is generated such that the surface points will be moved according this displacement. More details can be found on <http://www.math.u-bordeaux1.fr/~doobj/logiciels/mmg3d.php>.

Key-words: tetrahedral mesh, mesh adaptation, anisotropic mesh, moving mesh.

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Manuel utilisateur pour le remaillieur Mmg3d

Résumé : Mmg3d est un remaillieur tétraédrique entièrement automatique. Partant d'un maillage composé de tétraèdres, il produit un maillage quasi uniforme respectant un tenseur de métrique. Ce tenseur prescrit une taille et une direction pour les arêtes du maillage ce qui implique que le maillage résultant peut être anisotrope. Le code est basé sur des modifications locales et une version anisotrope du noyau de Delaunay est implémentée pour insérer les points dans le maillage. De plus, Mmg3d permet de traiter des problèmes de déplacement de corps : quand un déplacement est prescrit sur une partie de la frontière, le maillage final généré sera tel que les points de la surface auront bougé en accord avec ce déplacement. Le code est téléchargeable sur le site suivant : <http://www.math.u-bordeaux1.fr/~dobj/logiciels/mmg3d.php>.

Mots-clés : maillage tétraédrique, maillage anisotrope, maillage mobile, adaptation de maillage.

1 Mesh generation by local modifications

1.1 Context

Anisotropic mesh adaptation methods are revealed very efficient for CFD simulations (see for example [1, 5, 9, 10]) : these methods allow to control the accuracy of numerical solution while simultaneously reducing the number of mesh vertices to a minimum. An interesting potentiality of local anisotropic mesh adaptation is also related to the accurate tracking and approximation of a dynamically evolving interface [4].

In those contexts, the creation of 3D anisotropic meshes is essential. In our approach, we rely on local mesh modifications. Vertex insertion is handled using the anisotropic extension of the Delaunay kernel [3]. The description of the other operators that are involved can be found in the book [6]. Their extension to the anisotropic case is straightforward. Let us simply mention here that we use a combination of edge flips, edge collapsing, node relocation and vertex insertion operations, all driven by the anisotropic metric specifications.

1.2 Overview

Generalities: Mmg3d is an anisotropic fully tetrahedral automatic remesher. Beginning with a tetrahedral mesh, it modifies it iteratively to be in agreement with prescribed sizes (and directions) and/or to move all or a part of the domain boundary (rigid bodies displacement).

The software reads a mesh and it is possible to prescribe a map for edges sizes/directions and/or a displacement vector for the mesh nodes.

The mesh is then modified by using local mesh modifications of which an insertion procedure based on anisotropic Delaunay kernel.

NB : For the moment, only volumic mesh (i.e. the tetrahedra) is treated. No modification of the surface triangulation made (except for the rigid bodies movements and global splitting).

Mesh adaptation/optimization: Starting from a mesh and a size/direction map, the mesh is modified to fit with the prescription. The algorithm is decomposed in two parts. First, the edges lengths are analysed: the long edges are cutted and the short ones are deleted. Then, when the point density is in agreement with the prescribed size, there is a phase of quality optimization (edges swaps and point relocation).

NB : In the case where there is no prescribed size, we create one with the initial mesh (in analyzing the edges lengths).

Bodies movement: When a displacement is prescribed on the initial mesh, the final mesh will be such that the surface vertex will be at a new position corresponding with the prescribed displacement. This movement can be made by keeping constant the number of nodes (but it is not an obligation). The final mesh will always be valid (in conform meaning).

NB : The surface vertex are moved without geometric checks. All quality criterion are based on volumic mesh.

2 Installation

2.1 Distribution and authors

Mmg3d is written by two authors:

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INRIA Bordeaux - Sud-Ouest, EPI Bacchus	Université Pierre et Marie Curie
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Version 4.0 of Mmg3d is distributed as free/libre software, under the terms of the GNU GENERAL PUBLIC LICENSE. The term of this license is detailed here:
<http://www.math.u-bordeaux1.fr/~dobj/logiciels/download/LICENCE.txt>

You can download the source code of Mmg3d as well as precompiled versions on the following website:

<http://www.math.u-bordeaux1.fr/~dobj/logiciels/download/>

2.2 Langages and platforms

Mmg3d is entirely written in C (C89 ANSI norm). The current version counts about 55000 lines of source code. The code is optionnaly coupled with SCOTCH library [8] and has been tested on all major computer architectures and operating systems.

2.3 Compilation and installation

2.3.1 Compilation

To easily compile Mmg3d , please use `cmake` tools [7] and refer to the file `INSTALL.txt`.

Remark: By default, Mmg3d use the library SCOTCH to renumber the nodes and the elements of the initial mesh. You can download this library on the following website:

<http://www.labri.fr/perso/pelegrin/scotch/>

If you don't want to use SCOTCH, you can specify on `cmake` that you would compile without this library. In this case, Mmg3d could run more slowly.

2.3.2 Installation

If you download a precompiled version of Mmg3d , you just have to unzip it:

```
gzip -d mmg3d4.0-linux.gz
```

3 Mesh generation using binary

3.1 Input

- The input mesh will be to mesh format. This format is just composed by one file (binary or ASCII), named for example `toto.mesh` ou `toto.meshb`.

This file is organised in series of fields identified by key words. Besides vertex coordinates and tetrahedra list, you can specify other information like faces list, corners, edges, etc.

Example 1:

#MESH file with triangles and tetrahedra
MeshVersionFormatted 2

Dimension 3

Vertices

8
0 0 0 1
0 1 0 1
1 1 0 1
1 0 0 1
0 0 1 1
0 1 1 1
1 1 1 1
1 0 1 1

Triangles

12
1 4 8 15
1 2 4 10
3 2 7 14
8 3 7 12
5 8 6 11
2 5 6 13
5 2 1 13
8 5 1 15
7 6 8 11
2 6 7 14
4 3 8 12
2 3 4 10

Tetrahedra

6
1 2 8 4 2
8 3 2 7 2
2 5 8 6 2
8 5 2 1 2
2 7 6 8 2
2 4 3 8 2

End

Example 2:

#MESH file with quadrilaterals and hexahedra

MeshVersionFormatted 2

Dimension 3

Vertices

8
0 0 0 1
0 1 0 1
1 1 0 1
1 0 0 1
0 0 1 1
0 1 1 1
0 1 1 1
1 1 1 1
1 0 1 1

Quadrilaterals

6
1 2 3 4 10
5 6 7 8 11
4 3 7 8 12
1 2 6 5 13
3 2 6 7 14
4 1 5 8 15

Hexahedra

1
1 2 3 4 5 6 7 8 2

End

The detailed description of this format is made in appendix A.

- An isotropic/anisotropic metric can be specified on each input mesh vertices. This metric is given in an other file with SOL format (binary or ASCII). This file must have the same name as the MESH file with the extension `.sol(b)` (for example `toto.sol` or `toto.solb`).

This file is organised in series of fields identified by key words.

Example 1:

```
#Example SOL file for isotropic metric
MeshVersionFormatted 2
```

```
Dimension 3
```

```
SolAtVertices
```

```
8
```

```
1 1
```

```
0.1
```

```
0.1
```

```
0.1
```

```
0.1
```

```
0.1
```

```
0.1
```

```
0.1
```

```
0.1
```

```
End
```

Example 2:

```
#Example SOL file for anisotropic metric
MeshVersionFormatted 2
```

```
Dimension 3
```

```
SolAtVertices
```

```
8
```

```
1 3
```

```
100 0 100 0 0 100
```

```
100 0 100 0 0 100
```

```
100 0 100 0 0 100
```

```
100 0 100 0 0 100
```

```
100 0 100 0 0 100
```

```
100 0 100 0 0 100
```

```
100 0 100 0 0 100
```

```
100 0 100 0 0 100
```

```
End
```

The detailed description of this format is made in appendix A.

3.2 Options

All options are given in command line:

- `-0 n` with n an integer:
 - `-0 0` : mesh optimization.
 - `-0 1` : mesh generation in agreement with a prescribed metric, including points insertion/suppression and mesh optimization.
 - `-0 4` : option 1 + global splitting, warning global splitting involves splitting of boundaries (triangles)
 - `-0 9` : rigid bodies displacement and optimization (see 5).
 - `-0 10` : transformation of an hexahedral/prism mesh into tetrahedral one (see 6).
 - `-0 -1` : same as described previously without the optimization phase.
- `-d` : debug mode.
- `-h` : command summary, the following message will be written in your xterm:

```
-- MMG3d, Release 4.0 c (March 6, 2012)
Copyright (c) LJLL/IMB, 2010
usage: mmg3d4.0 [-v[n]] [-h] [-m n] [opts...] filein[.mesh] [-out fileout]

** Generic options :
-d      Turn on debug mode
-h      Print this message
-v [n]  Tune level of verbosity
-m [n]  Set memory size to n Mbytes

-0 [n]  Optimization level
1      adaptation
```

```

 4      use global splitting (warning modify boundary mesh)
 9      moving mesh
10      transform an hexahedral/prism mesh in a tetrahedral mesh
-n      turn off optimisation

** Misc. options
-bucket [n]   Specify the size of bucket per dimension
-noswap       no edge or face flipping
-nomove       no point relocation
-noinsert     no new point
-out fileout  Specify output file name
-rn n num     Specify the number of vertices by box to renumber nodes and the renumberings
-dt dt       to compute the node speed

```

- `-v n`
`n` defines the verbosity level (default 3).
- `-m n`
the integer `n` defines the allocated memory in Megabytes.
By default, the software allows to generate a mesh with maximum 500 000 points or 3 000 000 tetrahedra.
- `-mov name` : gives the displacement filename (option 9, see 5).
- `-dt t` : to compute the node speed (option 9, see 5).
- `-in name` : gives the input filename.
- `-out nom` : gives the output filename.
- `-bucket` : specifies the bucket size (default 64).
- `-noswap` : generates the mesh without applied edge swaps.
- `-noinsert` : generates the mesh in keeping constant the number of nodes (no points insertion or edge deletion).
- `-nomove` : generates the mesh without point relocation in optimization stage.
- `-rn n num` : this option concerns renumbering stage. The integer `n` is the number of vertices by box (by default 500) and `num` allows to tell when the renumbering stage appears: 0: no renumbering stage ; 1: renumbering at beginning ; 2: renumbering after insertion stage ; 3 (default): renumbering at the beginning and after insertion stage.

3.3 Running

In this paragraph, we suppose that you have a MESH file named `c1.mesh`¹ that you would remesh and optionnaly an associated metric named `c1.sol`². To launch the software, it is enough to type one of the following commands in terminal window:

```
mmg3d4.0 -O 1 c1
mmg3d -O 1 -in c1
```

You will obtain a new mesh named `c1.o.meshb` and the associated metric named `c1.o.solb`.

If you would modify the output name: `mmg3d4.0 -O 1 c1 myoutname.mesh` or `mmg3d -O 1 -in cube -out myoutname.mesh`

In this case, you will obtain the two following files : `myoutname.mesh` and `myoutname.sol`

To visualize this mesh, you could use the software `Medit` downloadable at the following url: <http://www.ann.jussieu.fr/~frey/logiciels/>

Remark : in the case where there is no metric file, the software builds one starting from the initial mesh.

NB : if you do not give the file extension (`.mesh(b)`), `Mmg3d` first finds the binary file then if there is no `meshb` file, it tries to open ASCII file. In other words, if you have in the same directory the files `toto.mesh` and `toto.meshb` and that you type `mmg3d -O 1 toto`, the infile will be `toto.meshb`.

4 Mesh generation with library using

4.1 File arguments

To use `Mmg3d` as a library, you must include the file `libmmg3d.h` and call the following C-function:

```
int MMG_mmg3dlib(int opt[9],MMG_pMesh mesh,MMG_pSol sol)
```

This function takes three arguments:

1. a tabular containing nine integers. This tabular allows to specify code option, see 4.2,
2. a pointer on a `MMG_Mesh` object which contains initial mesh informations, see 4.3,
3. a pointer on a `MMG_sol` object which contains metric specification , see 4.4.

This function returns an integer which is strictly positive if the mesh procedure anormally ended. At the end, the pointers of `MMG_Mesh` and `MMG_Sol` types contain the new mesh and the associated metric.

¹you can download it at this address : <http://www.math.u-bordeaux1.fr/~dobj/logiciels/data/c1.mesh>

²<http://www.math.u-bordeaux1.fr/~dobj/logiciels/data/c1.sol>

4.2 Options

As on the binary using, the `Mmg3d` call is done with options. This one must be specified on the tabular `int opt[9]`. This tabular contains:

0. an integer defining the remeshing mode:
 - 0 : mesh optimization.
 - 1 : mesh generation in agreement with a prescribed metric, including points insertion/suppression and mesh optimization.
 - 4 : option 1 + global splitting, warning global splitting involves splitting of boundaries (triangles)
 - 9 : rigid bodies displacement and optimization (see 5).
 - 10 : transformation of an hexahedral/prism mesh into tetrahedral one (see 6).
 - 1 or -4 or -9 : same as described previously without the optimization phase.
1. debugging mode: 1 for debugging mode, 0 if not,
2. bucket size: default 64,
3. the possibility to generate the mesh with applied or not edge swaps: 1 not authorizing edge swaps.
4. the possibility to generate the mesh in keeping constant the number of nodes (no points insertion or edges suppression): 1 to keep constant the number of nodes, 0 if not,
5. the possibility to generate the mesh with or without point relocation in optimization stage: 1 to avoid point relocation, 0 if not,
6. verbosity level: default 3,
7. this integer concerns renumbering stage, it allows to tell when renumbering stage appears: 0: no renumbering stage ; 1: renumbering at beginning ; 2: renumbering after insertion stage ; 3 (default): renumbering at the beginning and after insertion stage.
8. this integer concerns renumbering stage, it is the number of vertices by box (default 500),

4.3 Mesh format

To use `Mmg3d` as a library, you must define the informations describing the mesh. This informations are specified in a particular structure named `Mesh` (the prototype is in `libm3d.h`).

Details for the structure `MMG_Mesh` : this structure can be decomposed on five parts :

1. the general mesh informations:
 number of nodes (`np`) and maximal number of nodes which will be generated (`npmax`)
 number of surface triangles (`nt`) and maximal number of triangles which could be generated (`npmax`)
 number of tetrahedra (`ne`) and maximal number of tetrahedra which could be generated (`nemax`)
2. the vertex (`MMG_pPoint point`):
 This part contains for all the vertex, their coordonnates and their logic (reference)
3. the surface triangles (`MMG_pTria tria`):
 This part contains for all the surface triangles, the points number of their three vertex and their logic (reference),
4. the tetrahedra (`MMG_pTetra tetra`):
 This part contains for all the tetrahedra, the points number of their four vertex and their logic (reference, number of subdomain),
5. the displacement prescribed on each vertex (in rigid movement case, see 5)(`MMG_pDispl disp`):
 This part contains a displacement vector for all vertex mesh.

Definition/initialisation of `MMG_Mesh` structure: to define the `MMG_Mesh` structure, you need to allocate and initialize all the elements described on the previous paragraph. The next steps explains how to do that and give the C-code corresponding:

1. Define a pointer on a `MMG_Mesh` structure:

```
MMG_pMesh mymmgmesh
```

2. Allocate this pointer:

```
mymmginet = (MMG_pMesh) calloc(1, sizeof(MMG_Mesh));
```

3. Give the nodes, triangles and tetrahedra numbers of your mesh:

```
mymmginet->np = nbpoint;  
mymmginet->nt = nbtri;  
mymmginet->ne = nbtetra;
```

4. Give the nodes, triangles, tetrahedra maximum numbers:

```
mymmgmesh->npmax = nbpointmax;
mymmgmesh->ntmax = nbtrimax;
mymmgmesh->nemax = nbtetramax;
```

5. Allocate the structure `Point`, `Tetra`, `Tria`, `Disp` et `adja`

```
mymmgmesh->point = (MMG_pPoint) calloc(mymmgmesh->npmax+1, sizeof(MMG_Point));
mymmgmesh->tetra = (MMG_pTetra) calloc(mymmgmesh->nemax+1, sizeof(MMG_Tetra));
mymmgmesh->tria = (MMG_pTria) calloc(mymmgmesh->ntmax+1, sizeof(MMG_Tria));
mymmgmesh->adja = (int*) calloc(4*mymmgmesh->nemax+5, sizeof(int));
mymmgmesh->disp = (MMG_pDispl) calloc(mymmgmesh->npmax+1, sizeof(MMG_Displ));
mymmgmesh->disp->mv = (double*) calloc(3*(mymmgmesh->npmax+1), sizeof(double));
mymmgmesh->disp->alpha = (short*) calloc(mymmgmesh->npmax+1, sizeof(short));
```

6. Initialize the `Point` structure, that means for all the nodes, give the coordinates and the reference:

```
MMG_pMesh mymmgmesh;
MMG_pPoint ppt;

for (k=1; k<=mymmgmesh->np; k++) {
    ppt = &mymmgmesh->point[k];
    ppt->c[0] = coorx;
    ppt->c[1] = coory;
    ppt->c[2] = coorz;
    ppt->ref = logic;
}
```

NB : The node are numbered from 1 to `mymmgmesh->np` in a contiguous way.

7. Initialize the `Tetra` structure, that means for all tetrahedra, give the number nodes of the four vertex and the reference:

```
MMG_pMesh mymmgmesh;
MMG_pTetra ptetra;

for (k=1; k<=mymmgmesh->ne; k++) {
    ptetra = &mymmgmesh->tetra[k];
    ptetra->v[0] = num1;
    ptetra->v[1] = num2;
    ptetra->v[2] = num3;
    RT n° 422 ptetra->v[3] = num4;
    ptetra->ref = logic;
}
```

NB : The tetrahedra are numbered from 1 to `mymmgmesh->ne` in a contiguous way.

- (optional) Initialize the `Tria` structure, that means for all surface triangles, give the node number of the three vertex and the reference.

```
MMG_pMesh mymmgmesh;
MMG_pTria ptriangle;

for (k=1; k<=mymmgmesh->nt; k++) {
    ptriangle = &mymmgmesh->tria[k];
    ptriangle->v[0] = num1;
    ptriangle->v[1] = num2;
    ptriangle->v[2] = num3;
    ptriangle->ref = logic;
}
```

NB : The node are numbered from 1 to `mymmgmesh->nt` in a contiguous way

- (optional) If you treat bodies movements, initialize the `Disp` structure:

```
MMG_pMesh mymmgmesh;
MMG_pDispl pd;

for (k=1; k<mymmgmesh->np; k++) {
    pd = &mesh->mymmgdisp[k];
    pd->mv[0] = depx;
    pd->mv[1] = depy;
    pd->mv[2] = depz;
}
```

4.4 Metric definition/initialization

To adapt the mesh according to a metric, you must define it in a `MMG_Sol` structure, like that:

- Define a pointer on a `Sol` structure:

```
MMG_pSol sol;
```

- Allocate this pointer:

```
sol = (MMG_pSol)calloc(1,sizeof(MMG_Sol));
```

- Give the points number:

```
sol->np = nbpoint; (this number is equal to mesh->np)
sol->npmax = nbpointmax; (this number is equal to mesh->npmax)
```

4. Give the metric type, *i.e.* isotropic or anisotropic:

```
sol->offset = 6 for an anisotropic metric
sol->offset = 1 for an isotropic metric
```

5. Allocate the tabular containing the metric field:

```
sol->met = (double*)calloc(sol->npmax+1,sol->offset*sizeof(double));
sol->metold = (double*)calloc(sol->npmax+1,sol->offset*sizeof(double));
```

6. Initialize the `met` structure, that means, give on each point the metric values:

```
for (k=1; k<=mesh->np; k++) {
    isol = (k-1) * sol->offset + 1;
    for (i=0; i<sol->offset; i++)
        sol->met[isol + i] = metrique[ pointindice_k + i ];
}
```

4.5 Output

The `MMG_pMesh` and the `MMG_pSol` returned by the function are respectively the final mesh and the final metric.

5 Bodies movement

5.1 Data input

Same as the standard case 3.1, the software reads a mesh format file containing the initial mesh and possibly a sol file containing the metric field.

To do the mesh movement, the software reads a second sol file containing a displacement vector defining on each mesh vertex.

NB : At the end of the run, only boundary will be displaced according to the input displacement.

5.2 Options

All options are specified on command line. See 3.2.

5.3 Running

In this paragraph, we suppose that you have a mesh file named `testoption9.mesh`³ that you would remesh, a sol file containing the displacement on each mesh vertex `depooption9.sol`⁴ and optionally an associated metric named `testoption9.sol`.

To launch the software, it is enough to type the following command in terminal window:

³ <http://www.math.u-bordeaux1.fr/~doj/logiciels/data/testoption9.mesh>

⁴ <http://www.math.u-bordeaux1.fr/~doj/logiciels/data/depooption9.mesh>

```
mng3d -0 9 testoption9 -mov depoption9
```

You will obtain a new mesh which name will be `testoption9.o.meshb`.

Remark : to obtain an ASCII file, you have to specify the output name:

```
mng3d -0 9 testoption9 testoption9.o.mesh -mov depoption9
```

To visualize this mesh, you could use the software `Medit` downloadable at the following url: <http://www.ann.jussieu.fr/~frey/logiciels/>

Remark : in the case where there is no metric file, the software builds one starting from the initial mesh.

NB : if you do not give the file extension (`.mesh(b)`), `Mng3d` first finds the binary file then if there is no `mesh(b)` file, it tries to open ASCII file. In other words, if you have in the same directory the files `toto.mesh` and `toto.meshb` and that you type `mng3d -0 [n] toto`, the infile will be `toto.meshb`. To use the file `toto.mesh`, you have to type `Mng3d -0 [n] toto.mesh`

5.4 Data output

After running, you will obtain two files : a mesh file containing the new mesh and a sol file. The mesh file will be such as the boundary will be at the place prescribed by input displacement.

6 Hexahedra/Prisms cutting

6.1 Data input/output

The software reads a mesh format file (see A) containing the initial mesh. This mesh can be composed by hexahedra, prims and tetrahedra and boundary elements can be composed by triangles and/or quadrilaterals. After running, you will obtain a mesh file containing tetrahedra and triangles.

6.2 Cutting

Hexahedra cutting A majority of hexahedra are cut into six tetrahedra. The others are subdivided into twelve tetrahedra by adding a vertex at the barycenter of the hexadron.

Prims cutting A majority of prism are cutted into three tetrahedra. The others are subdivided into eight tetrahedra with adding a vertex at the barycenter of the prims.

7 Results evaluation

7.1 Elements quality

Definition: The quality measurement for a tetrahedron K in isotropic case is the following:

$$Q_K = \frac{h_s^3}{V_K},$$

where $h_s = \sqrt{\sum_{i=1}^6 h_i^2}$, h_i being the length of the edge i of the tetrahedron K and V_K its volume.

When an anisotropic metric is defined on each mesh point, the quality is more difficult to define. In `Mmg3d`, we choose to calculate the tetrahedron quality as its quality measured on the euclidian space relative to an average metric defined on the tetrahedron. Lets P_1, P_2, P_3, P_4 the vertex of K . The average quality on K is given by the following formula:

$$\mathcal{M}_{moy} = \frac{1}{4} \left(\sum_{i=1}^4 \mathcal{M}_i^{-1} \right)^{-1},$$

where \mathcal{M}_i is the metric at P_i .

The following expression gives the quality of K on the metric \mathcal{M}_{moy} :

$$Q_K = \frac{\left(\sum_{1 \leq i < j \leq 6} {}^t \overrightarrow{P_i P_j} \mathcal{M}_{moy} \overrightarrow{P_i P_j} \right)^{\frac{3}{2}}}{\sqrt{\text{Det}(\mathcal{M}_{moy})} V_K}$$

NB : Such a criterion allows to decide if a simplex is a good element. You can notice that the quality Q_K varies in $[1, +\infty[$ and that the smaller the volume of the tetrahedra is and the higher Q_K is.

Histogram: At the end of the execution, `Mmg3d` prints quality histogram. For instance:

```
-- MESH QUALITY    1136
AVERAGE QUALITY      1.4413
BEST ELEMENT QUALITY  1.0767
WORST ELEMENT QUALITY 2.2574
WORST ELEMENT    1183 (1125)  277 165 114 224

HISTOGRAMM
  1 < Q <    2      1130    99.47 %
  2 < Q <    3        6     0.53 %
```

In the previous histogram:

`1136` number of tetrahedra
`WORST ELEMENT 1183 (1125)` 1125 is the number of the tetrahedra with the worst quality

7.2 Edges lengths and efficiency index

Definition: We define an index allowing to quickly judge if the mesh is in agreement with the metric field. Let us note l_i the length of the edge e_i in the metric. The *efficiency index* of a mesh is defined as the exponential of the mean between the difference with 1 of all the lengths l_i normalized by the number of mesh edges. Let us call τ this index:

$$\tau = \exp \left(\frac{1}{ne} \sum_{i=1}^{ne} e_i \right)$$

with $e_i = l_i - 1$ si $l_i < 1$ and $e_i = \frac{1}{l_i} - 1$ if $l_i > 1$ and ne the number of mesh edges.

Histogram: At the end of the execution, the software prints the efficiency index and a length histogram. For example:

```
-- RESULTING EDGE LENGTHS 1115
AVERAGE LENGTH           0.9428
SMALLEST EDGE LENGTH     0.5975      172      252
LARGEST  EDGE LENGTH     1.5942      215      254
EFFICIENCY INDEX         0.8630
0.71 < L < 1.41         1088  97.58 %

HISTOGRAMM
0.50 < L < 0.71          18    1.61 %
0.71 < L < 0.90          554  49.69 %
0.90 < L < 1.11          330  29.60 %
1.11 < L < 1.41          204  18.30 %
1.41 < L < 2.00           9    0.81 %
```

In the previous histogram:
1115 number of edges
172 252 vertex of the smallest edges
215 254 vertex of the largest edges

8 Mesh visualization

To visualize this mesh, you could use the software `Medit` downloadable at the following url:
<http://www.ann.jussieu.fr/~frey/logiciels/>

9 Error and warning

The principal errors are the following:

- `NOT FOUND.` ou `UNABLE TO OPEN`: you have a problem with the input files.
- `INVALID METRIC`: the specified metric on several points is not a metric: the matrix determinant or the eigenvalues are not strictly positive.
- `WARNING: WRONG SOLUTION NUMBER. IGNORED`: the specified metric is ignored, the file does not contain the same number of points than the mesh file.
- `WARNING: INCOMPLETE MESH`: the software did not have enough memory to generate the mesh, thus the final mesh is probably not saturated in term of number of nodes. However, the final mesh is valid so you can rerun `Mmg3d` beginning with this final mesh by increasing

the memory (`-m 500` for instance).

NB : In this case, the final mesh is correct (in sense of conformity) even if it is not well adapted to the prescribed metric.

10 Examples

10.1 Mesh adaptation

10.1.1 Uniform metric aligned with axes

The metric tensor is diagonal and defined on each vertex P in the following way:

$$\mathcal{M}(P) = \begin{pmatrix} \frac{1}{\alpha^2 h^2} & 0 & 0 \\ 0 & \frac{1}{\beta^2 h^2} & 0 \\ 0 & 0 & \frac{1}{\gamma^2 h^2} \end{pmatrix}$$

The edges length in the direction x (resp. y et z) is αh (resp. βh et δh)

The initial mesh can be one of those represented on the Figure 1. The Figure 2 shows some volumic cuts on adapted meshes for several α, β, δ values.

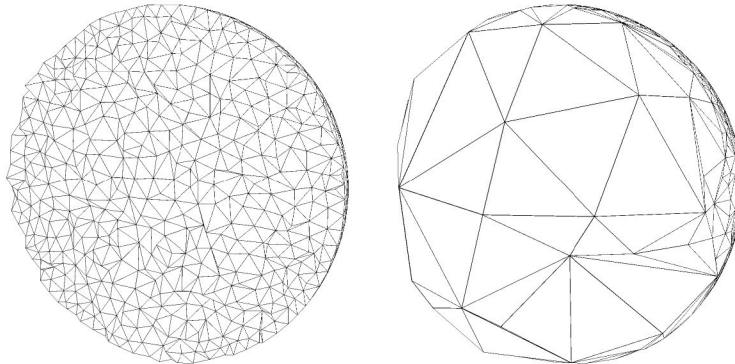


Figure 1: Volumic cuts in initial meshes.

10.1.2 Examples of anisotropic adaptation

The Figure 3 shows an example of mesh adaptation where the metric is analytically defined (for more details, see [2]) An example of anisotropic adaptation on CFD simulation is represented on the Figure 4. Figure 5 shows an example of analytical surface captured with anisotropic mesh adaptation (see [3]).

10.2 Rigid bodies moving

As mentioned previously, our local anisotropic mesh adaptation approach allows to handle rigid-body displacement problems without difficulty. For all the following examples, the displacement of a part of the mesh boundary is given analytically or by the result from a fluid calculation,

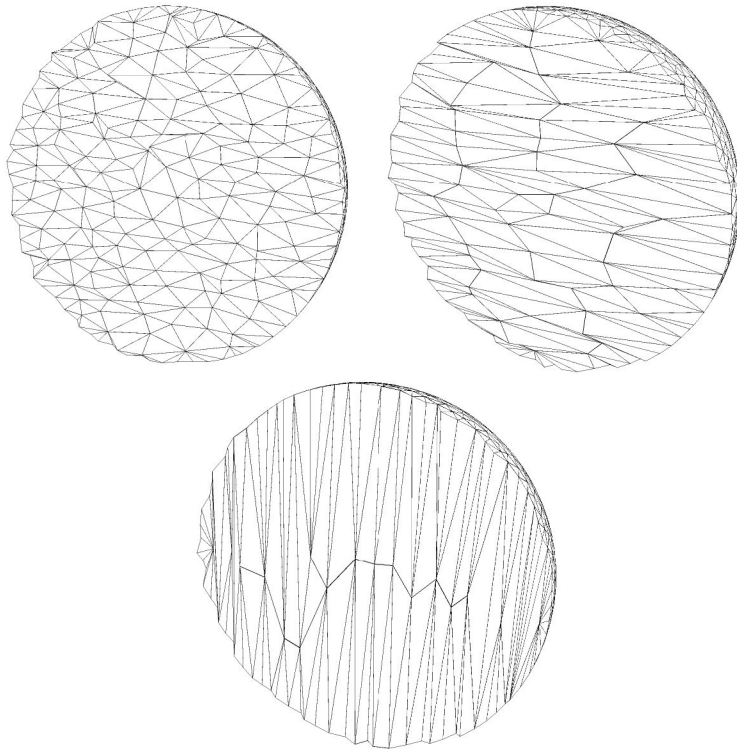


Figure 2: Volumic cut in adapted meshes: in the left top $\alpha = 2$, $\beta = 1$ et $\gamma = 1$; in the right top $\alpha = 1$, $\beta = 5$ et $\gamma = 1$; on the bottom $\alpha = 1$, $\beta = 1$ et $\gamma = 10$.

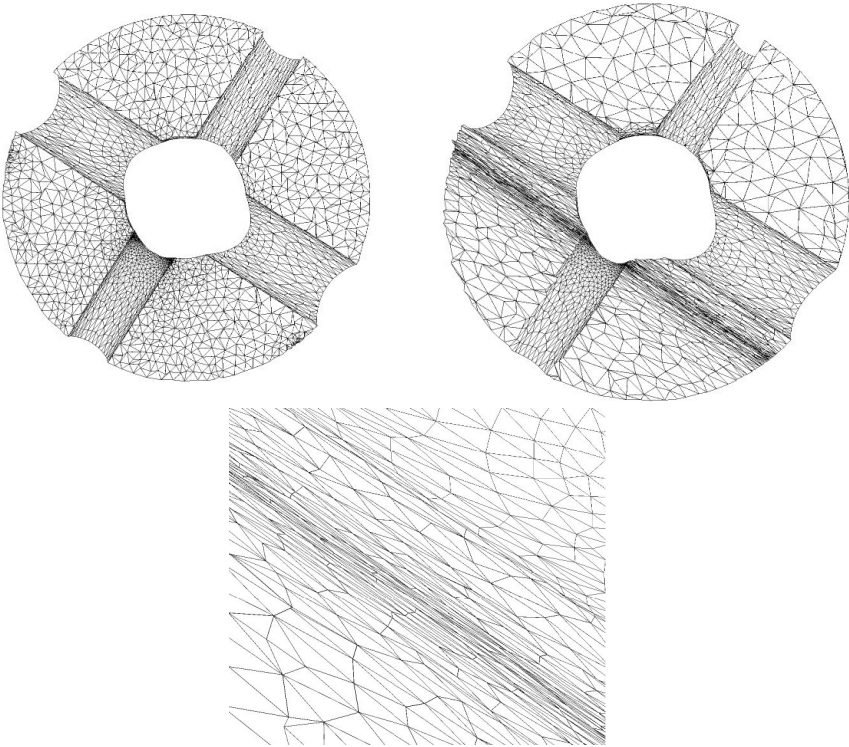


Figure 3: Volumic cuts on initial mesh and adapted mesh. Zoom on anisotropic meshes.

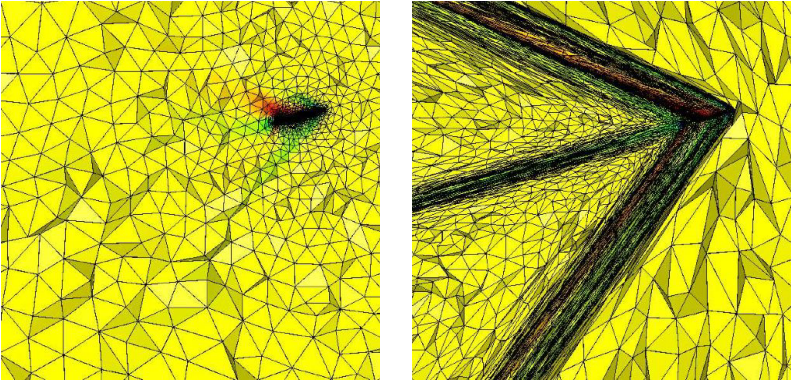


Figure 4: Supersonic flow around an airplane (mach 1.6, angle attack 3 degree, diameter of the box 1km): volumic cut on initial and adapted meshes.

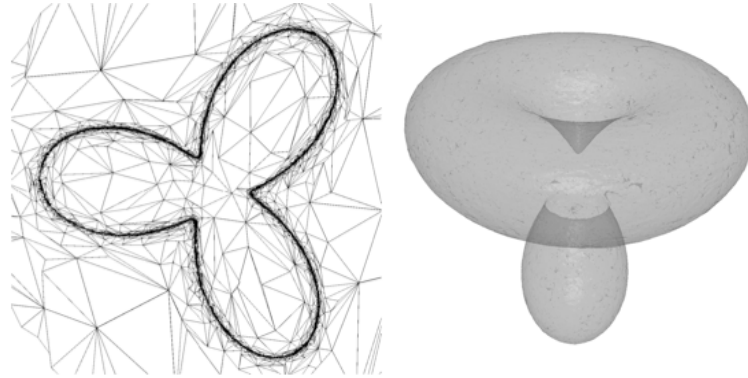


Figure 5: Example of mesh adaptation to capture an implicitly defined surface: cutting plane through tetrahedral element (left) and isosurface reconstruction (right)

then we apply the linear elasticity equation to define a discrete displacement field at all mesh vertices and at least, we run `Mmg3d` to move the mesh.

Moving object on an uniform mesh. The aim of this example is to move horizontally a car profile on a domain while keeping constant the number of nodes. The Figure 6 shows some volumic cuts on the tetrahedral mesh after several displacements.

Moving an object on an anisotropic mesh. In this example, the initial mesh is adapted to an anisotropic metric field. The aim is to move two spheres in the domain while keeping the anisotropy. On the Figure 7, some volumic cuts are represented.

Airflow around a rotating helicopter propeller. In this example, we perform an airflow simulation around an helicopter propeller. The flow is governed by the classical compressible Euler equations of the fluid dynamics. We consider that the propeller turns with a constant angular velocity $\theta = 2\pi/10 \text{ rad.s}^{-1}$, i.e. thus making 10 full rotations per second. In this simulation, one mesh is generated at each time step $dt = 1e - 4$ seconds, thus 1000 meshes are needed to achieve a complete revolution.

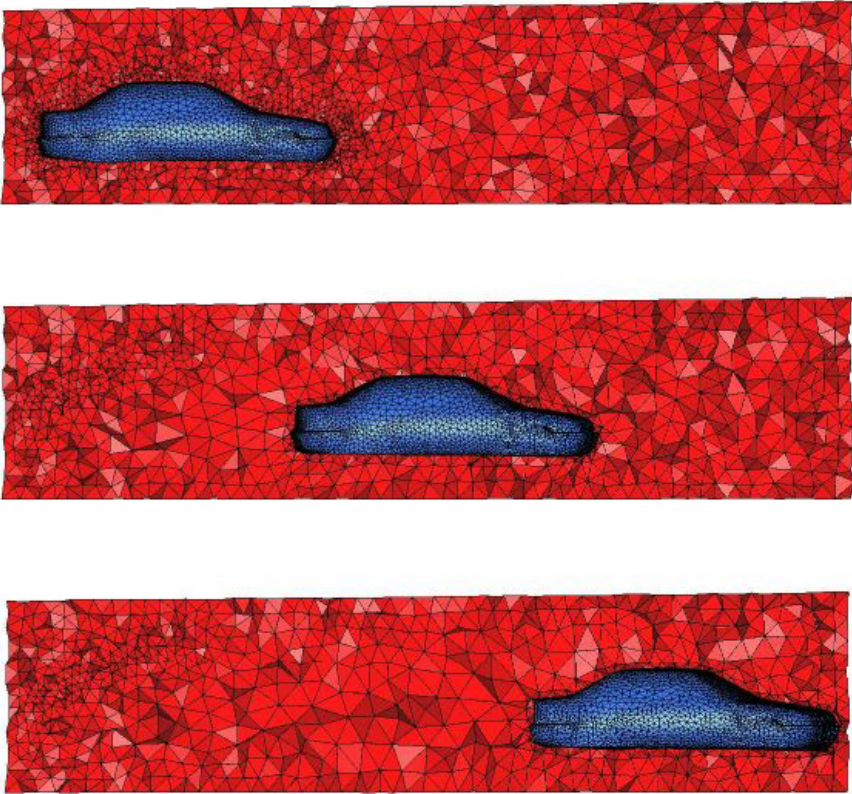


Figure 6: Volumic cuts after one, 75 and 150 boundary moves.

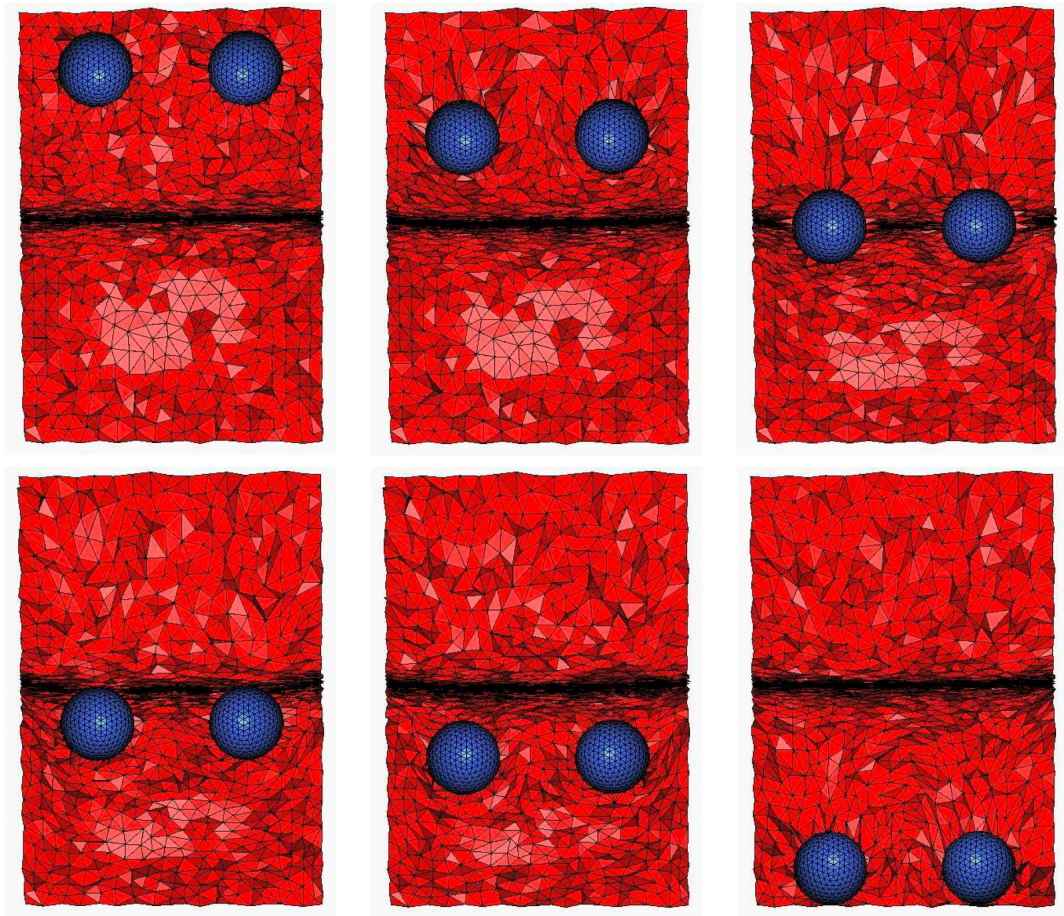


Figure 7: Displacement of 2 particles with respect of an anisotropic metric field.

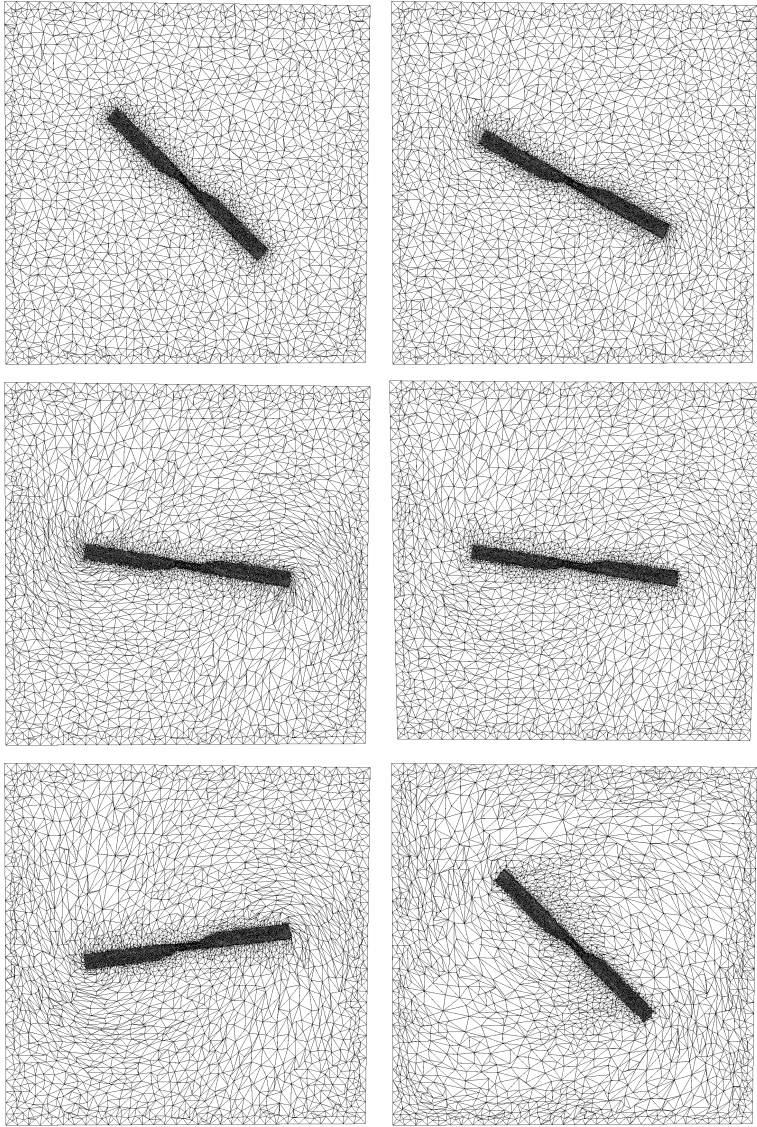


Figure 8: Propeller in rotation: cut through the tetrahedra after 1, 45, 99, 100, 145 and 500 rotations.

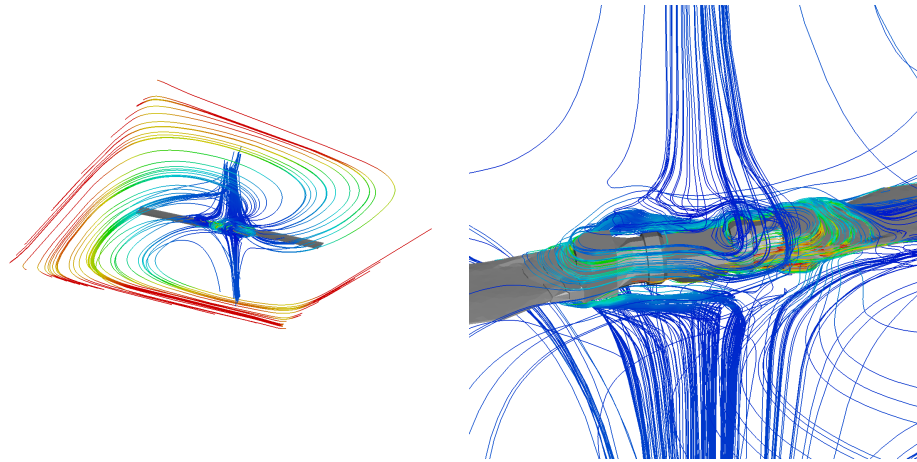


Figure 9: Propeller in rotation: streamlines.

11 FAQ

- How can I specify Boundary Conditions that remain untouched by Mmg3d ?

The boundary faces are the Triangles. To locate a boundary condition, you can put the same reference on a set of triangles. This reference will be unchanged by Mmg3d .

- What must I put like the reference number?

You can put every integer. However the new vertex created by Mmg3d will have a reference number equal to zero. Be careful, if there are several reference numbers for tetrahedra, Mmg3d will consider several subdomains.

- In a mesh with only tetrahedra, is it mandatory to specify Edges and Triangles to Mmg3d ?

No, you can give only the tetrahedra.

A Appendix 1 : Files format (MESH and SOL)

Mmg3d reads and writes mesh files with **MESH** format and solutions (metric or displacement) with **SOL** format.

These files formats allows to read/write binary and ASCII files. They are composed by one file (`xx.mesh` or `xx.meshb` or `xx.sol` or `xx.solb`) which contains all needed information for mesh (or solution) description.

On the following paragraph, we will describe first the ASCII format then the binary one.

ASCII file The file is organised with key words. The comments line must begin with the character `#`. The "blank", the line return (or `<CR>`) and the "tabs" are considered as separators.

1. The file must begin with the keyword `MeshVersionFormatted` followed by the version number. This number indicates if the file contains single or double precision reals.

`MeshVersionFormatted 1` : file writing with simple precision

`MeshVersionFormatted 2` : file writing with double precision

2. The next keyword is about the space dimension:

`Dimension 3`

NB : the dimension could be equal to 2 but it is not relevant for Mmg3d .

3. The file must end by the keyword `End`.

File MESH Before the keyword `End`, you have to define all the mesh characteristics: vertex, elements (triangles, quadrilaterals, tetrahedra, hexahedra...), etc. Those entities are defined as follows:

NB : The entities number begins to 1 (and not 0 like in C langage)

Vertices

np

$x_1 y_1 z_1 ref_1$

...

$x_{np} y_{np} z_{np} ref_{np}$

with np the number of mesh nodes, $x_i y_i z_i$ the coordinates of vertex i and ref_i its reference (an integer).

NB : In dimension 2, it is just $x_i y_i ref_i$

Triangles

nt

$v_1^1 v_1^2 v_1^3 ref_1$

...

$v_{nt}^1 v_{nt}^2 v_{nt}^3 ref_{nt}$

with nt the number of mesh triangles, v_i^j the number of vertex j of triangle i and ref_i its reference.

Quadrilaterals

nq

$v_1^1 v_1^2 v_1^3 v_1^4 ref_1$

...

$v_{nq}^1 v_{nq}^2 v_{nq}^3 v_{nq}^4 ref_{nq}$

with nq the number of quadrilaterals, v_i^j the number of vertex j of quadrilaterals i and ref_i its reference.

Tetrahedra*ntet* $v_1^1 v_1^2 v_1^3 v_1^4 ref_1$

...

 $v_{ntet}^1 v_{ntet}^2 v_{ntet}^3 v_{ntet}^4 ref_{ntet}$

with *ntet* the number of tetrahedra, v_i^j the number of vertex *j* of tetrahedron *i* and *ref_i* its reference.

Hexahedra*nh* $v_1^1 v_1^2 v_1^3 v_1^4 v_1^5 v_1^6 v_1^7 v_1^8 ref_1$

...

 $v_{nh}^1 v_{nh}^2 v_{nh}^3 v_{nh}^4 v_{nh}^5 v_{nh}^6 v_{nh}^7 v_{nh}^8 ref_{nh}$

with *nh* the number of hexahedra, v_i^j the number of vertex *j* of hexahedron *i* and *ref_i* its reference.

Edges*ne* $e_1^1 e_1^2 ref_1$

...

 $e_{ne}^1 e_{ne}^2 ref_{ne}$

with *ne* the number of (boundary) edges, $e_i^1 e_i^2$ the numbers of the two vertex which compose the edge *i* and *ref_i* its reference.

SOL file Like **MESH** format, **SOL** format is composed by keywords describing if the solution is defined on the vertices, triangles, tetrahedra, etc..

NB : On Mmg3d , only datas on vertices are taken into account.

The keywords are the following:

SolAtVertices**SolAtEdges,****SolAtTriangles,****SolAtQuadrilaterals,****SolAtTetrahedra,****SolAtPentahedra,****SolAtHexahedra,****SolAtVertices,****SolAtVertices,**

```
SolAtEdges,  
SolAtTriangles,  
SolAtQuadrilaterals,  
SolAtTetrahedra,  
SolAtPentahedra,  
SolAtHexahedra,
```

Next you have to give the number of entities:

```
number of vertex for SolAtVertices,  
number of triangles for SolAtTriangles,  
number of tetrahedra SolAtTetrahedra,  
etc...
```

Then you have to indicate the number of solutions and the type of each of them:

```
1 for scalar solution  
2 for vectorial solution  
3 for tensor (only symmetrical tensor are treated)
```

Example 1: scalar solution specified on mesh vertices.

```
MeshVersionFormatted
```

```
1
```

```
Dimension
```

```
3
```

```
SolAtVertices
```

```
10
```

```
1 1
```

```
0.396303
```

```
0.364391
```

```
0.422417
```

```
0.456066
```

```
0.5
```

```
0.5
```

```
0.5
```

```
0.5
```

```
0.10942
```

```
0.257269
```

```
End
```

Example 2: three solutions specified on mesh tetrahedra. In this example, the first solution is a scalar one (one value per tetrahedron), the second is a vectorial one (two values) and the third is a tensorial one (three values).

```
MeshVersionFormatted
1

Dimension
2

SolAtTetrahedra
5
3 1 2 3
0.396303 0.2 0.3 0.4 0.5 0.7
0.364391 0.2 0.3 0.4 0.5 0.7
0.422417 0.2 0.3 0.4 0.5 0.7
0.456066 0.2 0.3 0.4 0.5 0.7
0.5 0.2 0.3 0.4 0.5 0.7

End
```

Example 3: vectorial solution specified on mesh vertices.

```
MeshVersionFormatted
1

Dimension
3

SolAtVertices
5
1 2
0.396303 0.2 0.3
0.364391 0.2 0.3
0.422417 0.2 0.3
0.456066 0.2 0.3
0.5 0.2 0.3

End
```

Binary format The **MESH** and **SOL** can be written in binary. It is also based on keywords but those last are given with numbers. The correspondance table between numbers and keywords are given as follows:

MeshVersionFormatted	1
Dimension	3
Vertices	4
Edges	5
Triangles	6
Quadrilatéraux	7
Tetrahedra	8
Pentahedra	9
Corners	13
Ridges	14
RequiredVertices	15
RequiredEdges	16
RequiredTriangles	17
RequiredQuadrilaterals	18
TangentAtEdgesVertices	19
NormalAtVertices	20
NormalAtTriangleVertices	21
NormalAtQuadrilateral	22
AngleOfCorner	23
BoundingBox	50
Tangent	59
Normal	60
TangentAtVertices	61
SolAtVertices	62

Thus the file must begin with the integer 1 which has been followed by the version number (1 for simple précision, 2 for double précision).

Next, there is the integer 3 (**Dimension**) then an integer corresponding to the file position at the end of the information concerning the dimension, *i.e.* after the integer indicating the dimension (so it is the number 20: an integer is stored on 4 bits and including this one, we will write five integers) then the space dimension (2 or 3).

The continuation of the file is composed by other keywords with the following convention: just after the keyword number, you have to indicate the file position at the end of the information concerning this keyword then you give this information.

Example : To write in binary the following mesh:

```
MeshVersionFormatted 2
```

```
Dimension 3
```

```
Vertices
```

```
4
0 0 0 1
1 0 1 1
0 1 1 1
1 1 1 1
```

```
Tetrahedra
1
1 2 3 4 52
```

```
End
```

you have to write in binary file the following number:

```
1 2 3 20 3 4 132 0. 0. 0. 1 1 0. 1. 1 0. 1. 1. 1 1. 1. 1 8 1 2 3 4 52 54
```

Explanation :

1 : `MeshVersionFormatted`

2 : version number

3 : `Dimension`

20 : file position at the end of the information concerning the keyword `Dimension`

4 : `Vertices`

140 : file position at the end of the information concerning the keyword `Vertices`: each vertex is composed by three double precision real and an integer (reference), and a double precision real is stored on 8 bits thus each vertex information is composed by $8*3+4=28$ bits. There are 4 vertex so 112 bits. Then we add the integers for the keyword and the number of vertices ($2*4$ bits) and 20 bits for the previous fields. The result is well 140.

8 : `Tetrahedra`

168 : file position at the end of the information concerning the keyword `Tetrahedra`: each tetrahedron information is composed by 5 integers.

54 : `End`

References

- [1] T.J. Baker. Mesh adaptation strategies for problems in fluid dynamics. *Finite Elements in Analysis and Design*, 25(3-4):243–273, 1997.
- [2] C. Dobrzynski. *Adaptation de maillage anisotrope 3D et application a l'aero-thermique des batiments*. PhD thesis, Université Pierre et Marie Curie – Paris VI, November 2005.
- [3] C. Dobrzynski and P. Frey. Anisotropic delaunay mesh adaptation for unsteady simulations. Proc.of 17th Int. Meshing Roundtable, Pittsburgh, USA, 2008.
- [4] Vincent Ducrot and Pascal Frey. Geometric approximation control of interfaces using an anisotropic metric. (contrôle de l'approximation géométrique d'une interface par une métrique anisotrope.). *Comptes Rendus. Mathématique. Académie des Sciences, Paris*, 345(9):537–542, 2007.
- [5] P.J. Frey and F. Alauzet. Anisotropic mesh adaptation for cfd simulations. *Comput. Methods Appl. Mech. Engrg.*, 194(48-49):5068–5082, 2005.
- [6] P.J. Frey and P.-L. George. *Mesh generation. Application to finite elements*. Wiley, Paris, 2nd edition, 2008.
- [7] Ken Martin and Bill Hoffman. An Open Source Approach to Developing Software in a Small Organization. *IEEE Software*, 24(1):46–53, 2007.
- [8] François Pellegrini. Distilling knowledge about Scotch. In Uwe Naumann, Olaf Schenk, Horst D. Simon, and Sivan Toledo, editors, *Dagstuhl Seminar - Combinatorial Scientific Computing*, Dagstuhl Seminar Proceedings, page <http://drops.dagstuhl.de/opus/volltexte/2009/2091/>, Dagstuhl, Germany, July 2009. Schloss Dagstuhl - Leibniz-Zentrum fuer Informatik, Germany. 12 pages.
- [9] J. Peraire, J. Peiro, and K. Morgan. Adaptive remeshing for three-dimensional compressible flow computations. *J. Comp. Phys.*, 103:269–285, 1992.
- [10] J. F. Remacle, X. Li, M. S. Shephard, and J. E. Flaherty. Anisotropic Adaptive Simulation of Transient Flows using Discontinuous Galerkin Methods. *Int. J. Numer. Meth. Engng*, 62:899–923, 2004.

Contents

1	Mesh generation by local modifications	3
1.1	Context	3
1.2	Overview	3
2	Installation	4
2.1	Distribution and authors	4
2.2	Langages and platforms	4
2.3	Compilation and installation	4
2.3.1	Compilation	4
2.3.2	Installation	4
3	Mesh generation using binary	5
3.1	Input	5
3.2	Options	6
3.3	Running	8
4	Mesh generation with library using	8
4.1	File arguments	8
4.2	Options	9
4.3	Mesh format	9
4.4	Metric definition/initialization	12
4.5	Output	13
5	Bodies movement	13
5.1	Data input	13
5.2	Options	13
5.3	Running	13
5.4	Data output	14
6	Hexahedra/Prisms cutting	14
6.1	Data input/output	14
6.2	Cutting	14
7	Results evaluation	14
7.1	Elements quality	14
7.2	Edges lengths and efficiency index	15
8	Mesh visualization	16
9	Error and warning	16
10	Examples	17
10.1	Mesh adaptation	17
10.1.1	Uniform metric aligned with axes	17
10.1.2	Examples of anisotropic adaptation	17
10.2	Rigid bodies moving	17
11	FAQ	24

A Appendix 1 : Files format (MESH and SOL)

24



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