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Ask the locals: multi-way local pooling for image recognition

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Abstract

Invariant representations in object recognition systems are generally obtained by pooling feature vectors over spatially local neighborhoods. But pooling is not local in the feature vector space, so that widely dissimilar features may be pooled together if they are in nearby locations. Recent approaches rely on sophisticated encoding methods and more specialized codebooks (or dictionaries), e.g., learned on subsets of descriptors which are close in feature space, to circumvent this problem. In this work, we argue that a common trait found in much recent work in image recognition or retrieval is that it leverages locality in feature space on top of purely spatial locality. We propose to apply this idea in its simplest form to an object recognition system based on the spatial pyramid framework, to increase the performance of small dictionaries with very little added engineering. State-of-the-art results on several object recognition benchmarks show the promise of this approach.

1. Introduction

Much recent work in image recognition has underscored the importance of locality constraints for extracting good image representations. Methods that incorporate some way of taking locality into account define the state of the art on many challenging image classification benchmarks such as Pascal VOC, Caltech-101, Caltech-256, and 15-Scenes [11, 39, 42, 43, 45].

The spatial pyramid [25] has emerged as a popular framework to encapsulate more and more sophisticated feature extraction techniques [4, 11, 39, 41, 42, 45]. The global representation of an image is obtained by extracting image descriptors such as SIFT [28] or HOG [9] on a dense grid, encoding them over some learned codebook or dictionary (coding step), and then summarizing the distribution of the codes in the cells of a spatial pyramid by some well-chosen aggregation statistic (pooling step).

Several recent papers have focused on refining the coding step, one purpose of which is to produce representations that can be aggregated (pooled) without losing too much information in the process. Pooling, which has long been part of popular recognition architectures such as convolutional networks [26], gives robustness to small transformations of the image. It is related to Koenderink's concept of locally orderless images [24], and can be traced back to Hubel and Wiesel's seminal work on complex cells in the visual cortex [18]. The simplest pooling operation consists in averaging the feature vectors within a spatial neighborhood. One fact that makes the coding step necessary is that descriptors such as SIFT or HOG cannot be averaged with their neighbors without losing a considerable amount of information: the average of several widely different SIFT features doesn't tell us much about the content of the underlying image. Hence, coding is generally designed to produce representations that can be added with each other without diluting the signal. The original spatial pyramid proposal used vector quantization (K-means), which can be seen as a way of turning SIFT vectors into very sparse, 1-of-K codes. When obtained by averaging over spatial neighborhoods, the pooled codes can be interpreted as local histograms of visual words. Recent work has proposed to replace this hard quantization step of individual SIFT descriptors by soft vector quantization [36], or sparse coding [41], including sparse coding of local groups of SIFT descriptors (macrofeatures) instead of single ones, in our previous work [4].

While the pooling operations are often performed over local spatial neighborhoods, the neighborhoods may contain feature vectors that are very heterogeneous, possibly leading to the loss of a large amount of information about the distribution of features, as illustrated in Fig. (1). Restricting the pooling to feature vectors that are similar in the multidimensional input space (or nearby) [21, 45] remedies this problem. The usefulness of considering similar inputs for smoothing noisy data over a homogeneous sample to reduce noise without throwing out the signal has long been recognized in the image processing and denoising communities [6, 8], and has been successfully incorporated to denoising methods using sparse coding [30]. It is interesting to note that considerations of locality often pull cod-
The contributions of this work are threefold. First, we show how several recent feature extracting methods can be viewed in a unified perspective as preventing pooling from losing too much relevant information. Second, we demonstrate empirically that restricting pools to codes that preserve as much information as possible about the distribution of features, then the pooling step itself should become more selective.

The paper is organized as follows. Sec. 2 introduces the general classification pipeline that is used in this paper and much previous work and motivates our approach. Sec. 3 presents related work. Experiments are presented in Sec. 4.

2. General image recognition architecture and proposed approach

As argued in our previous work [4], many modern methods for image classification, such as convolutional and deep belief networks [17, 20, 26, 32], bags of features [34], histograms of gradients for pedestrian detection [9], or the spatial pyramid [25], implement an alternating series of coding and spatial pooling steps. Classification is then performed with some standard classifier such as a kernel or linear support vector machine (SVM), or logistic regression.

2.1. Feature extraction

Our setting for feature extraction is the following. Let \( I \) denote an input image. First, low-level descriptors \( x_i \) (e.g., SIFT or HOG) are extracted densely at \( N \) locations identified with their indices \( i = 1, \ldots, N \). Coding is performed at each location by applying some operator that is chosen to ensure that the resulting codes \( \alpha_i \) retain useful information (e.g., input data can be predicted from them), while having some desirable properties (e.g., compactness). Here, we focus on hard vector quantization and sparse coding, that both minimize some regularized error between inputs and the reconstructions that can be obtained from the codes.

Hard vector quantization is the simplest coding step, used in the bag-of-features framework [34]. It models the data with \( K \) clusters, representing each \( x_i \) by a one-of-\( K \) encoding of its cluster assignment:

\[
\alpha_i \in \{0,1\}^K, \quad \alpha_{i,j} = 1 \iff j = \arg\min_{k \leq K} \|x_i - d_k\|_2^2, \quad (1)
\]

where \( d_k \) denotes the \( k \)-th codeword of a codebook that is usually learned by an unsupervised algorithm such as K-means. The extreme sparseness of the codes produced (only...
Sparse coding \cite{31} reconstructs the input as a linear combination of few codewords:

\[
\alpha_i = \arg \min_{\alpha} L_i(\alpha, \mathbf{D}) = \| \mathbf{x}_i - \mathbf{D}\alpha \|^2 + \lambda \| \alpha \|_1, \quad (2)
\]

where \( \| \alpha \|_1 \) denotes the \( \ell_1 \) norm of \( \alpha \), \( \lambda \) is a parameter that controls the sparsity of \( \alpha \), and \( \mathbf{D} \) is some dictionary, which can be obtained by K-means, or for better performance, trained by minimizing the average of \( L_i(\alpha_i, \mathbf{D}) \) over all samples, alternatively over \( \mathbf{D} \) and the \( \alpha_i \). It is well known that the \( \ell_1 \) penalty induces sparsity and makes the problem tractable \( \text{e.g.,} \ [27, 29] \).

A pooling operator then takes the varying number of codes that are located within \( M \) possibly overlapping regions of interest \( \text{e.g.,} \), the cells of a spatial pyramid), and summarizes them as a single vector of fixed length. The representation for the global image is obtained by concatenating the representations of each region of interest, possibly overlapping im-

\[
\mathbf{h} = \arg \max_{\mathcal{Y}_{\mathbf{m}}} \langle \mathbf{x}, \mathbf{y} \rangle, \quad \text{where} \quad \mathbf{y} \in \mathbb{R}^2 \text{ denotes a pixel location, and } \mathbf{x} \in \mathbb{R}^d \text{ is a vector, or configuration, encoding the local image structure at } \mathbf{y} \quad \text{e.g., a SIFT descriptor, with } d = 128 . \text{ A feature set } \mathcal{Z} \text{ is associated with each image, its size potentially varying from one picture to the next.}
\]

Spatial pooling considers a fixed – that is, predetermined and image-independent – set of \( M \) possibly overlapping image regions \( \mathcal{Y}_i \) to \( \mathcal{Y}_M \). To these, we add a fixed set of \( P \) (multi-dimensional) bins \( \mathcal{X}_i \) to \( \mathcal{X}_P \) in the configuration space. In this work, the spatial bins are the cells in a spatial pyramid, and the configuration space bins are the Voronoi cells of clusters obtained using K-means.

Denoting by \( g \) the pooling operator \( \text{average or max in the previous section), the pooled feature is obtained as:} \]

\[
h_{(m,p)} = g_{(i \in \mathcal{Y}_m, j \in \mathcal{X}_p)}(\alpha_{(i,j)}). \quad (5)
\]

Bags of features can be viewed as a special case of this in two ways: either by considering the 1-of-\( K \) encoding presented above, followed by global pooling in the configuration space \( (P = 1) \), or with a simplistic encoding that maps all inputs to 1, but does fine configuration space binning \( (P = K) \). Accordingly, the feature extraction in this paper can be viewed either as extending the sparse coding spatial pyramid by making configuration space pooling local, or as extending the hard-vector-quantized spatial pyramid by replacing the simplistic code by sparse coding: descriptors are first decomposed by sparse coding over a dictionary of size \( K \); the same descriptors are also clustered over a K-means dictionary of size \( P \); finally, pooling of the sparse codes is then performed separately for each cluster \( \text{as in aggregated coding} \ [21] \) – see Sec. 3 --, but with sparse codes, yielding a feature of size \( K \times P \times S \) if there are \( S \) spatial bins.

While this does not apply to max pooling, local pooling can be viewed as implementing local bilinear classification when using average pooling and linear classification: the pooling operator and the classifier may be swapped, and classification of local features then involves computing \( \beta_{xy}^T \mathbf{W} \alpha \), where \( \beta_{xy} \) is a \( (S \times P) \)-dimensional binary vector that selects a subset of classifiers corresponding to the configuration space and spatial bins, and \( \mathbf{W} \) is a \( (S \times P) \times K \) matrix containing one \( K \)-dimensional local classifier per row.
3. Related work about locality in feature space

We start our review of previous work with a caveat about word choice. There exists an unfortunate divergence in the vocabulary used by different communities when it comes to naming methods leveraging neighborhood relationships in feature space: what is called "non-local" in work in the vein of signal processing [6, 30] bears a close relationship to "local" fitting and density estimation [11, 33, 39, 43]. Thus, non-local means [6] and locally-linear embedding [33] actually perform the same type of initial grouping of input data by minimal Euclidean distance. This discrepancy stems from the implicit understanding of "local" as either "spatially local", or "local in translation-invariant configuration space".

3.1. Preserving neighborhood relationships during coding

Previous work has shown the effectiveness of preserving configuration space locality during coding, so that similar inputs lead to similar codes. This can be done by explicitly penalizing codes that differ for neighbors. The DrLIM system of siamese networks in [16], and neighborhood component analysis [13], learn a mapping that varies smoothly with some property of the input by minimizing a cost which encourages similar inputs to have similar codes (similarity can be defined arbitrarily, as locality in input space, or sharing the same illumination, orientation, etc.) Exploiting image self-similarities has also been used successfully for denoising [6, 8, 30].

Locality constraints imposed on the coding step have been adapted to classification tasks with good results. Laplacian sparse coding [11] uses a modified sparse coding step in the spatial pyramid framework. A similarity matrix of input SIFT descriptors is obtained by computing their intersection kernel, and used in an added term to the sparse coding cost. The penalty to pay for the discrepancy between a pair of codes is proportional to the similarity of the corresponding inputs. This method obtains state-of-the-art results on several object recognition benchmarks. Locality-constrained linear coding [39] (LLC) projects each descriptor on the space formed by its k nearest neighbors (k is small, e.g., k = 5). This procedure corresponds to performing the first two steps of the locally linear embedding algorithm [33] (LLE), except that the neighbors are selected among the atoms of a dictionary rather than actual descriptors, and the weights are used as features instead of being mere tools to learn an embedding.

Sparse coding methods incorporating a locality constraint share the property of indirectly limiting activation of a given component of the vectors representing descriptors to a certain region of the configuration space. This may play a role in their good performance. For example, in LLC coding, the component corresponding to a given dictionary atom will be non-zero only if that atom is one of the k nearest neighbors of the descriptor being encoded; the non-zero values aggregated during pooling then only come from these similar descriptors. Several approaches have implemented this strategy directly during the pooling step, and are presented in the next section.

3.2. Letting only neighbors vote during pooling

Pooling involves extracting an ensemble statistic from a potentially large group of inputs. However, pooling too drastically can damage performance, as shown in the spatial domain by the better performance of spatial pyramid pooling [25] compared to whole-image pooling.

Different groups have converged to a procedure involving preclustering of the input to create independent bins over which to pool the data. In fact, dividing the feature space into bins to compute correspondences has been proposed earlier by the pyramid match kernel approach [14]. However, newer work does not tile the feature space evenly, relying instead on unsupervised clustering techniques to adaptively produce the bins.

The methods described here all perform an initial (hard or soft) clustering to partition the training data according to appearance, as in the usual bag-of-words framework, but then assigning a vector to each cluster instead of a scalar. The representation is then a "super-vector" that concatenates these vectors instead of being a vector that concatenates scalars.

Aggregated coding [21] and super-vector coding [45] both compute, for each cluster, the average difference between the inputs in the cluster, and its centroid: (1) SIFT descriptors $x_i$ are extracted at regions of interest, (2) visual words $c_k$ are learned over the whole data by $K$-means, (3) descriptors of each image are clustered, (4) for each cluster $C_k$, the sum $\sum_{x \in C_k}(x - c_k)$ is computed, (5) the image descriptor is obtained by concatenating the representations for each cluster.

If the centroids were computed using only the descriptors in a query image, the representation would be all zeros, because the centroids in K-means are also obtained by averaging the descriptors in each cluster. Instead, the centroids are computed using descriptors from the whole data, implicitly representing a "baseline image" against which each query image is compared. Thus, encoding relatively to the cluster centroid removes potentially complex but non-discriminative information. This representation performs very well on retrieval [21] and image classification [45] (Pascal VOC2009) benchmarks.

Another related method [42] that obtains high accuracy on the Pascal datasets combines the preclustering step of aggregated and super-vector coding, with sparse decomposition over individual local dictionaries learned inside each cluster. Both approaches using preclustering for image classification [42, 45] have only reported results using gigantic global descriptors for each image. Indeed, the high results obtained in [42] are attributed to the possibility of learning
a very large overcomplete dictionary (more than 250,000 atoms) which would be computationally infeasible without preclustering, but can be done by assembling a thousand or more smaller local dictionaries. The experiments presented in the next section seek to isolate the effect of local pooling that is inherent in this scheme.

4. Experiments

We perform experiments on three image recognition datasets: 15-Scenes [25], Caltech-101 [10] and Caltech-256 [15]. All features are extracted from grayscale images. Large images are resized to fit inside a 300 × 300 box. SIFT descriptors are extracted densely over the image, and encoded into sparse vectors using the SPAMS toolbox [1]. We adopt the denser 2 × 2 macrofeatures of our previous work [4], extracted every 4 pixels, for the Caltech-256 and Caltech-101 databases, and every 8 pixels for the Scenes, except for some experiments on Caltech-256 where standard features extracted every 8 pixels are used for faster processing. The sparse codes are pooled inside the cells of a three-level pyramid (4 × 4, 2 × 2 and 1 × 1 grids); max pooling is used for all experiments except those in Sec. 4.2.3, which compare it to other pooling schemes. We apply an \( \ell_{1,5} \) normalization to each vector, since it has shown slightly better performance than no normalization in our experiments (by contrast, normalizing by \( \ell_1 \) or \( \ell_2 \) norms worsens performance). One-versus-all classification is performed by training one linear SVM for each class using LIBSVM [7], or after (Post) the encoding, \( K \): dictionary size, and \( P \): number of configuration space bins.

### 4.1. Pooling locally in configuration space yields state-of-the-art performance

Experiments presented in Table 1 and 2 compare the performance of sparse coding with a variety of configuration space pooling schemes, with a list of published results of methods using grayscale images and a single type of descriptor. Local pooling always improves results, except on the Scenes for a dictionary of size \( K = 256 \). When local pooling in the configuration space is used (\( P \geq 1 \), clustering is performed using the \( K \)-means algorithm to obtain cluster centers. Following the usual practice [15, 25, 39], we use 30 training images on the Caltech-101 and Caltech-256 datasets, 100 training images on the Scenes dataset; the remaining images are used for testing, with a maximum of 50 and 20 test images for Caltech-101 and Caltech-256, respectively. Experiments are run ten times on ten random splits of training and testing data, and the reported result is the mean accuracy and standard deviation of these runs. Hyperparameters of the model (such as the regularization parameter of the SVM or the \( \lambda \) parameter of sparse coding) are selected by cross-validation within the training set. Patterns of results are very similar for all three datasets, so results are shown only on Caltech-101 for some of the experiments; more complete numerical results on all three datasets can be found in the supplemental material.

<table>
<thead>
<tr>
<th>Method</th>
<th>Caltech 30 tr.</th>
<th>Scenes</th>
</tr>
</thead>
<tbody>
<tr>
<td>Boiman et al. [3]</td>
<td>70.4</td>
<td>-</td>
</tr>
<tr>
<td>Boureau et al. [4]</td>
<td><strong>75.7 ± 1.1</strong></td>
<td>85.6 ± 0.2</td>
</tr>
<tr>
<td>Gao et al. [11]</td>
<td>-</td>
<td><strong>89.8 ± 0.5</strong></td>
</tr>
<tr>
<td>Jain et al. [19]</td>
<td>69.6</td>
<td>-</td>
</tr>
<tr>
<td>Lazebnik et al. [25]</td>
<td>64.4 ± 0.8</td>
<td>81.4 ± 0.5</td>
</tr>
<tr>
<td>van Gemert et al. [36]</td>
<td>64.1 ± 1.2</td>
<td>76.7 ± 0.4</td>
</tr>
<tr>
<td>Wang et al. [39]</td>
<td>73.44</td>
<td>-</td>
</tr>
<tr>
<td>Yang et al. [41]</td>
<td>73.2 ± 0.5</td>
<td>80.3 ± 0.9</td>
</tr>
<tr>
<td>Zhang et al. [44]</td>
<td>66.2 ± 0.5</td>
<td>-</td>
</tr>
<tr>
<td>Zhou et al. [46]</td>
<td>-</td>
<td>84.1 ± 0.5</td>
</tr>
</tbody>
</table>

| K = 256, Pre, \( P = 1 \)    | 70.5 ± 0.8    | 78.8 ± 0.6   |
|                              | 74.0 ± 1.0    | 81.5 ± 0.8   |
|                              | 75.0 ± 0.8    | 81.1 ± 0.5   |
|                              | 75.5 ± 0.8    | 81.0 ± 0.3   |
|                              | 74.2 ± 1.1    | 81.5 ± 0.8   |
|                              | 75.6 ± 0.6    | 81.9 ± 0.7   |
| K = 256, Post, \( P = 16 \)  | 75.1 ± 0.8    | 80.9 ± 0.6   |
|                              | 76.4 ± 0.8    | 81.1 ± 0.6   |
|                              | 76.7 ± 0.8    | 81.1 ± 0.5   |
| K = 1024, Pre, \( P = 1 \)   | 75.6 ± 0.9    | 82.7 ± 0.7   |
|                              | 76.3 ± 1.1    | 82.7 ± 0.9   |
|                              | 76.2 ± 0.8    | 81.4 ± 0.7   |
|                              | **76.9 ± 1.0**| 83.3 ± 1.0   |
|                              | **77.3 ± 0.6**| 83.1 ± 0.7   |
| K = 1024, Post, \( P = 16 \) | **77.0 ± 0.8**| 82.9 ± 0.6   |
|                              | **77.1 ± 0.7**| 82.4 ± 0.7   |

Table 1. Results on Caltech-101 (30 training samples per class) and 15-scenes for various methods. Results for our method are given as a function of whether clustering is performed before (Pre) or after (Post) the encoding, \( K \): dictionary size, and \( P \): number of configuration space bins.

4.1.1 Using pyramids in configuration space

We examine whether it is advantageous to combine fine and coarse clustering, in a way reminiscent of the levels of the spatial pyramid. With large dictionaries, local pooling in the configuration space does not always perform better than standard global pooling (see Tables 1 and 2). However, combining levels of different coarseness gives performance better than or similar to that of the best individual level, as has been observed with the spatial pyramid [25].

This significantly improves performance on the Caltech-101 dataset. To the best of our knowledge, our performance of 77.3% on the Caltech-101 benchmark, is above all previously published results for a single descriptor type.

Using grayscale images — although better performance has been reported with color images (e.g., 78.5% ± 0.4 with a saliency-based approach [22]), multiple descriptor types (e.g., methods using multiple kernel learning have achieved 77.7% ± 0.3 [12], 78.0% ± 0.3 [2, 37] and 84.3% [40] on Caltech-101 with 30 training examples), or subcategory learning (83% on Caltech-101 [35]). On the Scenes benchmark, preclustering does improve results for small dictionaries (K ≤ 256, see supplemental material), but not for larger ones (K = 1024). While our method outperforms the Laplacian sparse coding approach [11] on the Caltech 256 dataset, our performance is much below that of Laplacian sparse coding on the Scenes database.

### 4.1.2 Pre- vs. Post-Clustering

One advantage of using the same dictionary for all features is that the clustering can be performed after the encoding. The instability of sparse coding could cause features similar in descriptor space to be mapped to dissimilar codes, which would then be pooled together. This does not happen if clustering is performed on the codes themselves. While pre-clustering may perform better for few clusters, post-clustering yields better results when enough clusters are used (P ≥ 64); a dictionary of size K = 1024 reaches 77.1 ± 0.7 accuracy on Caltech-101 with P = 64 bins (to be compared to 76.2 ± 0.8 when clustering before coding), while a dictionary of size K = 256 yields 76.7 ± 0.8 with P = 128 bins (to be compared to 75.5 ± 0.8 with preclustering). Fig. 2 also shows that performance drops for larger P, irrespective of whether the clustering is performed before or after the encoding.

<table>
<thead>
<tr>
<th>Dictionary</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Boiman et al. [3] (K = 1024)</td>
<td>37.0</td>
</tr>
<tr>
<td>Gao et al. [11] (K = 1024)</td>
<td>35.7 ± 0.1</td>
</tr>
<tr>
<td>Kim et al. [23]</td>
<td>36.3</td>
</tr>
<tr>
<td>van Gemert et al. [36] (K = 128)</td>
<td>27.2 ± 0.5</td>
</tr>
<tr>
<td>Wang et al. [39] (K = 4096)</td>
<td>41.2</td>
</tr>
<tr>
<td>Yang et al. [41] (K = 1024)</td>
<td>34.0 ± 0.4</td>
</tr>
</tbody>
</table>

Table 2. Recognition accuracy on Caltech 256, 30 training examples, for several methods using a single descriptor over grayscale. For our method, results are shown as a function of whether clustering is performed before (Pre) or after (Post) the encoding, K: dictionary size, and P: number of configuration space bins.

4.2 Gaining a finer understanding of local configuration space pooling

In this section, we investigate how much local configuration space pooling can enhance the performance of small dictionaries, how it compares to learning one local dictionary per configuration bins, and what pooling and weighting schemes work best in our pipeline.

#### 4.2.1 Local pooling boosts small dictionaries

Fig. 3(a) shows results for various assignments of components between atoms (K) and centroids (P). Pooling more locally in configuration space (P > 1) can considerably boost the performance of small dictionaries.

Unsurprisingly, larger dictionaries consistently beat smaller ones combined with preclustering-driven pooling, at same total number of components; this can be seen from the downwards slope of the grey dashed lines in Fig. 3(a) linking data points at constant K * P. However, if P is allowed to grow more, small dictionaries can outperform larger ones. This leads to good performance with a small dictionary; e.g., a dictionary of just K = 64 atoms coupled with a preclustering along P = 64 centroids achieves 73.0 ± 0.6% on Caltech-101.

#### 4.2.2 Comparison with cluster-specific dictionaries

In addition to learning richer, more local dictionaries, learning one dictionary per cluster as done in [39, 42] inherently leads to more local pooling. Experiments in this section seek to disentangle these effects. As shown in Fig. 3(b), more than half of the improvement compared to no preclustering is usually due to the separate clustering rather than more specific dictionaries. The smaller the dictionary, the...
4.2.3 Pooling operator and cluster weighting

When concatenating the vectors corresponding to each pool, it is not clear whether they should be weighted according to the prominence of the cluster, measured as the ratio $N_i/N$ of the number $N_i$ of inputs falling into cluster $i$, over the total number $N$ of inputs. Denoting by $w_i$ the weight for cluster $i$, we compare three weighting schemes: identical weight ($w_i = 1$), a weight proportional to the square root of the ratio ($w_i = \sqrt{N_i/N}$) as proposed by Zhou et al. [45], or the ratio itself ($w_i = N_i/N$).

As shown in Fig. 3(c), the weighting scheme assigning the same weight to each cluster performs better when max pooling is used, except for very small dictionaries. When average pooling is used, the best weighting scheme is the square root weighting, which empirically validates the choice in [45], but performance is below that of max pooling. Based on these results, max pooling with identical weighting for all clusters has been used for all other experiments in the paper.

5. Conclusion

While there is no question that making coding more stable and more specific is advantageous, the simple procedure of clustering the data in order to make pooling local in configuration space is a powerful tool for image recognition. The main conclusions of this work are that (1) more local configuration space pooling in itself boosts performance, dramatically so with smaller dictionaries; (2) it is advantageous to use pyramids rather than grids, analogously to spatial pooling; (3) with enough configuration space bins, better performance may be obtained when the clustering is performed just before the pooling step, rather than before the coding step; (4) performance drops if too many bins are added.

Our ongoing efforts are focused on adapting the same ideas to pooling across features when there is a topology on the feature extractors, instead of simply pooling each component separately. We hope that considering locality in all dimensions simultaneously (feature space, between feature extractors, and space itself) will lead to even more robust invariant recognition.

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