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Boosted Human Re-identification using Riemannian Manifolds

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Abstract

This paper presents an appearance-based model to address the human re-identification problem. Human re-identification is an important and still unsolved task in computer vision. In many systems there is a requirement to identify individuals or determine whether a given individual has already appeared over a network of cameras. The human appearance obtained in one camera is usually different from the ones obtained in another camera. In order to re-identify people a human signature should handle difference in illumination, pose and camera parameters. The paper focuses on a new appearance model based on Mean Riemannian Covariance (MRC) patches extracted from tracks of a particular individual. A new similarity measure using Riemannian manifold theory is also proposed to distinguish sets of patches belonging to a specific individual. We investigate the significance of MRC patches based on their reliability extracted during tracking and their discriminative power obtained by a boosting scheme. Our method is evaluated and compared with the state of the art using benchmark video sequences from the ETHZ and the i-LIDS datasets. Re-identification performance is presented using a cumulative matching characteristic (CMC) curve. We demonstrate that the proposed approach outperforms state of the art methods. Finally, the results of our approach are shown on two further and more pertinent datasets.

Keywords: Re-identification, Covariance Matrix, Riemannian Manifold, Human Detection, Appearance Matching, Boosting

1. Introduction

Recently, cameras spread out across various domains that range from personal computers, video games, home surveillance applications, to large camera networks. These camera networks facility access to sports venue, monitored environments, such as airports, metro stations or car parks. A natural consequence of such situation is a need for an automated extraction of high-level semantic information from extremely large volumes of recorded video data. In many surveillance systems, the most desirable information is a knowledge about an *identity* of a detected object.

Human re-identification can be defined as a determination whether a given person of interest has already been observed over a network of cameras. This issue is also known as *the person re-identification* problem. Person re-identification can be considered on different levels depending on information cues which are currently available in the system. Biometrics such as iris [2], face [3], gait [4] or their combinations [5] can be used to recognize identities. Nevertheless, in most video surveillance scenarios such detailed information is not available due to video low-resolution or difficult segmentation (crowded environments).

In small video surveillance systems, this problem can be approached using temporal and visual information. One of the earliest works on associating appearances from disjoint cameras is [1]. A Bayesian framework has been proposed to fuse cues including inter-camera time intervals, location of exit/entrances, velocities of objects and a simple color histogram representation to perform re-identification. Nevertheless, in order to recognize people in large systems (*e.g.* metro stations, airports) where temporal transition time between cameras may differ greatly, matching of individuals has to rely on visual features alone. Therefore a robust modelling of a global appearance of an individual is necessary to re-identify a given person of interest. In these identification techniques, clothing is the most reliable information on an identity of an individual (we assume that individuals wear the same clothes between different sightings). These approaches are referred to as *appearance-based person re-identification*¹ which is the main topic of this paper.

¹The reader should be aware that in these approaches *the re-identification* term stands for matching similar appearances over a network of camera. These techniques can not be so accurate as iris recognition or face recognition, because the clothing is not enough distinctive.

An appearance-based approach relies on modelling a human signature using tracking and detection results. Re-identification techniques which exploit appearance information using only one image are referred to as *single-shot* approaches and until now they were the most popular methods. Currently, identification accuracy is improved by integrating information over many images. The methods, which employ multiple images of the same person as a training data, are called *multiple-shot* approaches.

As re-identification concerns a large sets of individuals acquired from different cameras, we need to provide a *distinctive* and *invariant* signature. This signature has to be based on *discriminative* features to allow browsing the most similar signatures over a network of cameras. It can be achieved by signature matching which has to handle differences in illumination, pose and camera parameters. Note that, inter-camera variations in lighting conditions, differences in illumination, different camera parameters, changes in object orientation and object pose make this task extremely difficult. Besides, occlusions (caused by other people or objects of the scene) and self-occlusions (caused by body parts) make the re-identification problem one of the hardest tasks in the video surveillance domain.

The main topic of this paper is a novel *multiple-shot* approach, which builds a specific human signature model to re-identify a given individual. In our approach, a human detection algorithm is used to find out people in video sequence (section 4.1). Then, the detected individual is tracked to gather as many frames as possible. The appearances obtained from the tracking results are used to extract discriminative signature. This paper makes the following contributions:

- We offer a new set of Mean Riemannian Covariance (MRC) patches extracted using Riemannian manifold theory. This mean covariance matrix not only keeps information about feature distribution but also carries out essential information on temporal changes of an appearance (section 5.3).
- We propose two methods to select and to enhance discriminative MRC patches, which can represent the human signature. We investigate the significance of these MRC patches in the two following ways (section 5.4): (1) we take advantage of patch reliability obtained during tracking; (2) a boosting scheme is developed to select the most discriminative patches reducing the amount of ambiguity among the human class.

- We introduce a new similarity measure between signatures, which enables to hold discriminative power coming from the relative position of MRC patches (section 5.5).
- We extract new sets of individuals from i-LIDS data to investigate more carefully advantages of using tracking results in building the *multiple-shot* signature. These publicly available datasets finally satisfy all requirements of the *multiple-shot* person re-identification (section 6).

2. Related Work

Recently, the person re-identification problem became one of the most important tasks in video surveillance. There is a natural consequence of an invention of robust human detection algorithms to extend approaches for recognition purposes. The *appearance based* methods are divided into two main groups, *single-shot* approaches and *multiple-shot* approaches.

As to *single-shot* approaches, in [6] the clothing color histograms taken over the head, shirt and pants regions together with the approximated height of a person is used as the discriminative feature. Similarly, clothing segmentation together with facial features [7] are employed to recognize individuals. In [8] an image of pedestrian is segmented into ten equally spaced horizontal strips. The median HSL color of the foreground pixels extracted from each of these ten strips is used as the set of features defining signature. This method detects loitering people by identification of the same person being present for a long time. The human signature represented by color patches along edges extracted from an appearance is proposed in [9]. The similarity of patches together with their geometric constraints is encoded in matching function.

In [10], a generative and discriminative models are combined together with online learning strategy to perform re-identification. The human appearance is represented by histograms computed over upper body, lower body and full body segment. The histograms are composed of color features, autocorrelograms and a bag of features based on SIFT [11] descriptor.

In [12] a human body parts detector is applied to establish the correspondence between appearances. First, specialized HOG-based detectors [13] identify body parts. Then, covariance descriptor [14] is used to represent appearance of detected body parts. Finally, a spatial pyramid scheme [15] is adopted to improve discriminative matching of two collections of body features.

Shape and appearance context model is proposed in [16]. A pedestrian image is segmented into regions and their color spatial information is registered into a co-occurrence matrix. This method works well if the system considers only a frontal viewpoint.

For more challenging cases, where viewpoint invariance is necessary, the ensemble of localized features (*ELF*) [17] has been proposed. Instead of designing a specific feature for characterizing people appearance, a machine learning algorithm constructs a model that provides maximum discriminability by filtering a set of simple features. Enhancement of discriminative power of each individual signature with respect to the others is also the main issue in [18]. Pairwise dissimilarity profiles between individuals have been learned and adapted into nearest neighbour classification. Similarly, in [19], a rich set of feature descriptors based on color, textures and edges have been used to reduce the amount of ambiguity among human class. The high-dimensional signature is transformed into a low-dimensional discriminant latent space using a statistical tool called Partial Least Squares (PLS) in one-against-all scheme. Nevertheless in both methods, an extensive learning phase based on the pedestrians to re-identify is necessary to extract discriminative profiles what makes the approaches non-scalable.

The person re-identification problem has been reformulated as a ranking problem in [20]. The authors present extensive evaluation of learning approaches and show that a ranking relevance based model can improve the reliability and accuracy.

Furthermore, a context information can be used to improve recognition accuracy. Visual information coming from surrounding people have been used in [21] to reduce ambiguity in person identification. This method shows that group association between two or more people can give valuable information about identity of an individual. Similarly, in [22] group context information handled by covariance descriptor [14] improves the performance of person re-identification.

Concerning *multiple-shot* approaches, in [23] the spatiotemporal graph is generated using ten consecutive frames for grouping spatiotemporally similar regions. Then, a clustering method is applied to capture the local descriptions over time and improve matching accuracy. Bag of features based on SIFT [11] descriptor together with online learning are proposed in [24] to improve matching accuracy. In [25] re-identification is performed using SURF [26] interest points collected during short video sequences. The interest points are stored in KD-tree to speed-up the query processing time.



Figure 1: The results of the query. The first image on the left is the query image. The true match is on the first position in the list.

In [27], AdaBoost scheme is applied to extract the most discriminative and invariant haar-like features. Here, again one-against-all learning scheme is used to catch human dissimilarities.

In [28], the authors propose to combine three features: 1) chromatic content (HSV histogram); 2) maximal stable colour regions (MSCR [29]) and 3) recurrent highly structured patches (RHSP). The extracted features are weighted by the distance with respect to the vertical axis to minimize effects of pose variations. Recurrent patches are also proposed in [30]. Epitome analysis is used to extract highly informative patches from the set of images.

Finally, in [31] re-identification is performed in aerial images. Here, the PageRank algorithm is applied to extract the most informative regions to distinguish individuals. First, the multiple images are integrated using undirected graph and then PageRank assign higher weights to prominent regions and degrade noisy regions by assigning them lower weights.

3. Problem Definition

We lay the problem as the following. We generate human signature for each person detected and tracked in our video surveillance system. Let us denote a signature as \mathfrak{s}_i^c , where i encodes the person's identity and c denotes the camera. By querying the database of signatures $\mathfrak{s}_j^{c'}$, where $c \neq c'$ with signature of interest \mathfrak{s}_i^c , we search for each signature its corresponding signature in another camera. The results of the query is the list of the most similar signatures ordered by increasing dissimilarity (see figure 1). The position in the list of the true match is called the rank score.

The underlying challenge of the problem arises from significant differences in illumination, pose and camera parameters. The same object acquired under different cameras shows color dissimilarities. Even identical cameras

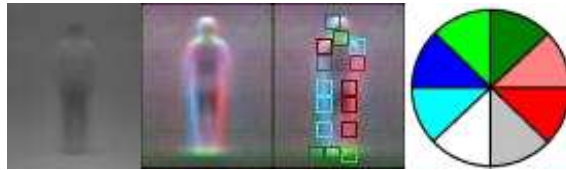


Figure 2: Mean human image with corresponding edge magnitudes and the 15 most dominant cells. From the left: the first image shows the mean human image calculated over all positive samples in the database; the second image shows the corresponding mean edge magnitude response; the third image shows this later image superposed with the 15 most dominant cells of size 8×8 pixels. The cell bounding boxes are drawn with a color set by their most dominant edge orientation with the scheme defined in the last image.

which have the same optical properties and are working under the same lighting conditions may not match in their color responses. Moreover, the pose variations due to camera and view point change as well as the articulation of a human body lead to significant differences in appearances of the same individual observed from different cameras.

4. Overview of the approach

A typical way of extracting appearance models in automatic surveillance systems is by first detection of objects in an image, and then by tracking them using different strategies. In this work, we focus only on human appearances. We detect and track humans using HOG-based detector, which philosophy is similar to [13]. Afterwards, we handle color dissimilarities caused by camera illumination differences by applying *histogram equalization* (section 4.2).

4.1. Human detection and tracking

We use a *Histogram of Oriented Gradient* (HOG) based technique to automatically detect humans in different scenes before their visual signatures are extracted for re-identification purposes. Our HOG technique is adapted from the face detection method [32] to detect human silhouette. The detection algorithm extracts histograms of gradient orientation, using a Sobel convolution kernel, in a multi-resolution framework. The technique was originally designed to detect faces using the assumption that facial features remain approximatively at the same location. However, locations of human silhouette features do not remain constant in templates with varying poses (*e.g.* knees are constantly changing position when walking; a shoulder

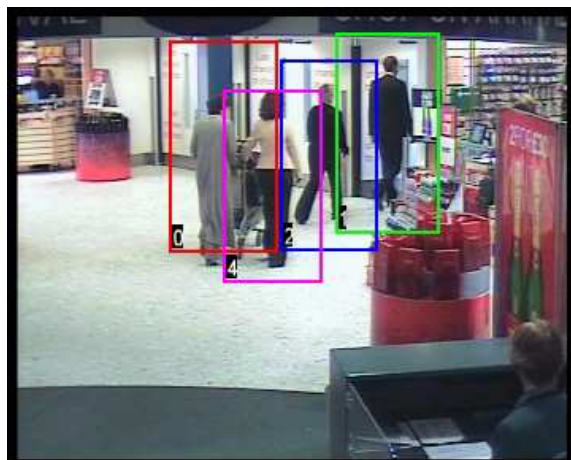


Figure 3: Examples of detected people.

changes position from walking to slightly bending when pushing a trolley). Hence, we modified algorithm to detect humans using cells located at specific locations around the human silhouette as shown in figure 2. The most dominant cells used to characterize human shapes are the 15 most dominant cells selected among 252 cells covering the human sample area. These most dominant cells are the cells having the closest HOG vector to the mean HOG vector calculated over the vectors (of the corresponding cell) from a human database. The system was trained using 10,000 positive and 20,000 negative image samples from the NICTA database [33]. Figure 3 shows an example of several detected persons in dynamically occluded scenario. Once a human has been detected and tracked, the next step is to handle color dissimilarities caused by camera illumination differences. Thus, we use color normalization technique called *histogram equalization*.

4.2. Color normalization

One of the most challenging problem using the color as a feature is that images of the same object acquired under different cameras show color dissimilarities. We use *histogram equalization* [34] to increase the overall contrast by brightening dark areas of the image, emphasizing details in those regions. Histogram equalisation stretches a range of histogram to be as close as possible to an uniform histogram. The approach is based on the idea that amongst all possible histograms, an uniformly distributed histogram has maximum entropy [35]. Maximizing the entropy of a distribution, we maximize its in-

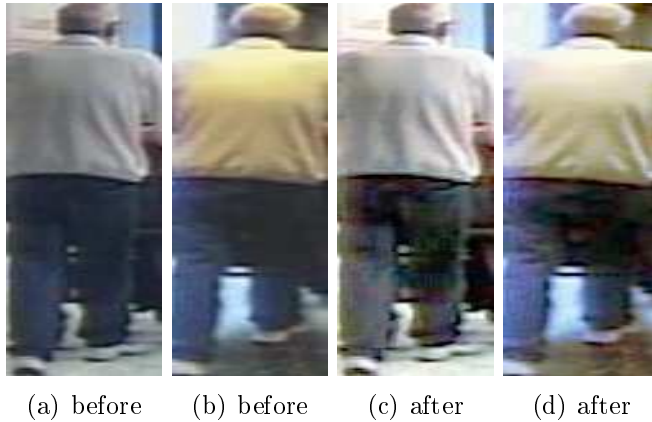


Figure 4: The first two columns show original images of the same person captured from different cameras in different environments. The last two columns show these images after histogram equalization.

formation and thus histogram equalization maximizes the information content of the output image. We apply the histogram equalization to each of the color channels (RGB) to maximize the entropy in each of those channels and obtain the invariant image. Figure 4 illustrates the effect of applying the histogram equalization technique to images of the same individual captured by different cameras. These images highlight the fact that a change in illumination leads to a significant change in the colors captured by the camera. The last two columns show result images after applying histogram equalization procedure. It is clear that the resulting images are much more similar than the two original images.

5. Human appearance

In this section we define our appearance model based on the novel MRC patches extracted from tracks of a specific individual. The input of our approach is a set of cropped images corresponding to human detection and tracking results, normalized by the histogram equalization applied to each of the color channels (RGB). From such normalized images we extract MRC patches (section 5.3). Nevertheless, before explaining details of the proposed MRC patches, we present a brief overview of the covariance descriptor and a short introduction to Riemannian geometry.

5.1. Covariance Descriptor

Here, we present an overview of the covariance descriptor [14] and its specialization in our approach. Covariance matrix can be computed from any type of image such as a one dimensional intensity image, three channel color image or even other types of images, *e.g.* infrared. Let I be an image and F be a d -dimensional feature image extracted from I

$$F(x, y) = \phi(I, x, y), \quad (1)$$

where the function ϕ can be any mapping such as color, intensity, gradients, filter responses, *etc.* For a given rectangular region $Reg \subset F$, let $\{f_k\}_{k=1\dots n}$ be the d -dimensional feature points inside Reg . The region Reg is represented with the $d \times d$ covariance matrix of the feature points

$$C_{Reg} = \frac{1}{n-1} \sum_{k=1}^n (f_k - \bar{f})(f_k - \bar{f})^T, \quad (2)$$

where \bar{f} is the mean of the points. Such defined covariance matrix can be computed in an efficient way for each subregion of an image using integral images [14].

In our approach we define the mapping $\phi(I, x, y)$ as

$$\left[x, y, R_{xy}, G_{xy}, B_{xy}, \nabla_{xy}^R, \theta_{xy}^R, \nabla_{xy}^G, \theta_{xy}^G, \nabla_{xy}^B, \theta_{xy}^B \right], \quad (3)$$

where x and y are pixel location, R_{xy}, G_{xy}, B_{xy} are RGB channel values and ∇ and θ corresponds to gradient magnitude and orientation in each channel, respectively.

The input image region is mapped to $d = 11$ dimensional feature image. Thus, the covariance region descriptor is represented by an 11×11 matrix. The descriptor encodes information of the variances of the defined features inside the region, their correlations with each other and spatial layout.

We show that the performance of the covariance features is superior to other methods as rotation and illumination changes are absorbed by covariance matrix. Moreover, we enhance robustness to local illumination variations in an image by using *the Pearson Product-Moment Correlation Coefficients* (PMCC) as elements of covariance matrices (such matrix is also often called *correlation matrix*). In a correlation matrix every element (i, j)

is normalized by the product of their standard deviations

$$\hat{C}_{Reg}(i, j) = \frac{C_{Reg}(i, j)}{\sigma_i \sigma_j}. \quad (4)$$

Since now, every matrix in this paper is assumed to be such normalized covariance matrix.

5.2. Riemannian Geometry

Covariance matrix as a positive definite and symmetric matrix can be seen as a tensor. The main problem is that such defined tensor space is a manifold that is not a vector space with the usual additive structure. A manifold is a topological space which is locally similar to an Euclidean space. A neighbourhood homomorphic to an open subset \mathfrak{R}^m can be defined for every point on the manifold. As symmetric positive definite matrices constitute a convex half-cone in the vector space of matrices, many usual operations, such as mean and distance, are stable in this space. Nevertheless problems arise when tensors are extracted from real data (estimated symmetric matrix could have negative eigenvalues). Therefore manifold is specified as Riemannian to determine a powerful framework using tools from differential geometry [36]. A Riemannian manifold \mathcal{M} is a differentiable manifold in which each tangent space has an inner product which varies smoothly from point to point. Since covariance matrices can be represented as a connected Riemannian manifold we apply operations such as the distance and the mean computation using this differential geometry.

5.2.1. Covariance Matrix Distance

The space of positive definite and symmetric covariance matrices can be formulated as a connected Riemannian manifold. Hence, we use the distance definition proposed by [37] to compute the dissimilarity between two covariance matrices

$$\rho(C_i, C_j) = \sqrt{\sum_{k=1}^d \ln^2 \lambda_k(C_i, C_j)}, \quad (5)$$

where $\lambda_k(C_i, C_j)_{k=1\dots d}$ are the generalized eigenvalues of C_i and C_j , determined by

$$\lambda_k C_i x_k - C_j x_k = 0, \quad k = 1 \dots d, \quad (6)$$

and $x_k \neq 0$ are the generalized eigenvectors.

5.2.2. Mean Covariance

Let C_1, \dots, C_N be a set of covariance matrices. The Karcher or Fréchet mean is the set of tensors minimizing the sum of squared distances. In the case of tensors, the manifold has a non-positive curvature, so there is a unique mean value μ

$$\mu = \arg \min_{C \in \mathcal{M}} \sum_{i=1}^N \rho^2(C, C_i), \quad (7)$$

where ρ is the covariance matrix distance (Eq. 5).

Since covariance matrices lay in a Riemannian manifold we use the intrinsic Newton gradient descent algorithm to compute the approximation mean covariance at step $t + 1$

$$\mu_{t+1} = \exp_{\mu_t} \left[\frac{1}{N} \sum_{i=1}^N \log_{\mu_t}(C_i) \right], \quad (8)$$

where \exp_{μ_t} and \log_{μ_t} are specific operators uniquely defined on the Riemannian manifold. This iterative gradient descent algorithm usually converges very fast (in experiments 5 iterations were enough, which is similar to [36]).

5.3. MRC Patches

In this section we define *the Mean Riemannian Covariance* (MRC) patches and explain their merits. Once a human has been detected and color has been normalized, we scale every cropped image into a fixed size $W \times H$. MRC patch corresponds to a square region (of size $\frac{W}{4} \times \frac{W}{4}$ and $\frac{W}{2} \times \frac{W}{2}$). We assume that such MRC patches can form patch combinations (see figure 5). In our approach we only consider patch combinations built using maximally two MRC patches. The patch combination may consist of two patches with the same size as well as with different size. Different patterns of a human appearance are captured from a window $W \times H$. We extract patches of size $\frac{W}{4} \times \frac{W}{4}$ shifted horizontally and vertically by $\frac{W}{8}$ and patches of size $\frac{W}{2} \times \frac{W}{2}$ shifted horizontally and vertically by $\frac{W}{4}$. The position of MRC patch on the fixed size window and the spatial correlation between patches is essential to carry out discriminative power.

There have already been proposed some statistics on covariance functions which take into account spatial and temporal changes [38, 39]. Nevertheless, these approaches assume that covariance function is a stationary (or weakly stationary) process in space and time. Unfortunately in our case we can

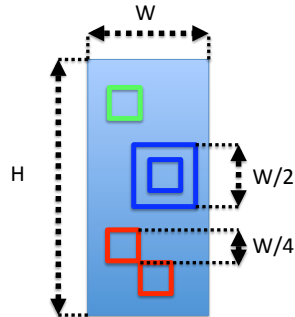


Figure 5: MRC Patches. Green patch corresponds to the single square region (the top). Blue patch is an example of combination (small - big) of two patches with the different size (the middle). Red patch illustrates combination (small - small) of patches with the same size (the bottom).

not make such strong assumptions as visual features mostly do not meet this requirement in a video sequence. Moreover, noisy human detections and gaps in tracking prevent the covariance functions to be separable in space and time. As it is hard to apply these statistic methods to our covariance matrices we have decided to use the mean covariance computed on a Riemannian manifold as a descriptor of a region in a video sequence.

Let C_1^p, \dots, C_N^p be a set of covariance matrices extracted during tracking of N frames corresponding to image square regions at position of patch p . We define MRC patch as the mean covariance of these covariance matrices (see section 5.2.2) computed using a Riemannian space (see figure 6). The mean covariance matrix as an intrinsic average blends all extracted matrices. This mean covariance matrix not only keeps information on features distribution but also carries ou ion about temporal changes of the appearance related to the position of patch p . Moreover, as we normalize covariance matrix, rotation and illumination changes are absorbed. MRC patch (the mean covariance matrix together with its position) is fundamental in our approach. Further, patch combinations are able to catch different patterns and spatial correlations of MRC patches. We claim that the combination of MRC patches is extremely efficient for re-identification purposes, which is confirmed in experimental results. Now we introduce a new reliability measure, which describes an invariance of a patch.

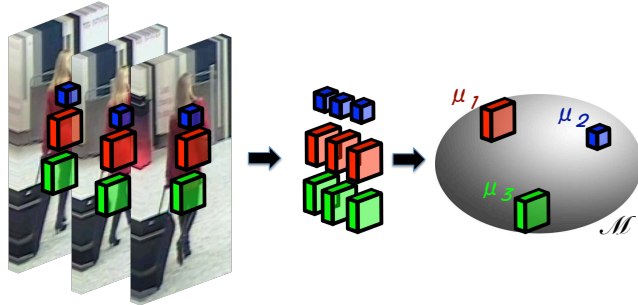


Figure 6: Computation of three MRC patches. Covariances gathered from tracking results are used to compute the mean covariance using Riemannian manifold space (depicted with the surface of the sphere). The mean covariance forms MRC patch.

5.3.1. Patch Reliability

Let R_1^p, \dots, R_N^p be a set of image square regions extracted during tracking of N frames at position of patch p . As we already know, for each such region we extract covariance C_i^p which encodes information of the variances of defined features f inside the region and their correlations.

Together with the mean covariance matrix we define the reliability measure \mathfrak{R} which describes invariance of the tracked image region

$$\mathfrak{R} = 1 - \frac{\sigma}{\max \sigma}, \quad \sigma = \frac{1}{N-1} \sum_{k=1}^N (\bar{f}_k - \bar{\Gamma})^2, \quad (9)$$

where $\bar{\Gamma}$ is the mean feature vector along N tracking regions and \bar{f}_k is the mean feature vector corresponding to region k , $\max \sigma$ corresponds to the maximal value of σ for the specific individual. As we assume that only partial occlusions may occur, the reliability works similarly to background subtraction. Here, our idea is to remove most variable features because we assume that these features are the noisiest (containing background). See figure 8 (b), the most unreliable features correspond to legs and background.

5.4. MRC Patch Selection

We represent a human signature by a set of MRC patches. The human signature should be built on patches which are discriminative and reliable. As already mentioned patches can form combinations. In this case we call it

a patch combination. These combinations together with a single MRC patch represent the MRC patch space. From this MRC patch space we select the most significant MRC patches. We propose two ways for the MRC patch selection to show how a learning phase can improve performance.

The first method is based on the patch reliability measure. We select the most reliable patches with the highest reliability among others. If the patch combination is considered, the reliability is an average of reliabilities of both patches. This selection method allows us to create the human signature without any learning phase.

In the second method, we extract discriminative features using boosting where we follow one-against all scheme. We lay the re-identification problem as classification where we separate the specific individual class from the rest of humans. Here, we assume that discriminative features of an individual extracted from one camera correspond to discriminative features of the same individual extracted from another camera. Let us assume that we want to *learn* the signature \mathfrak{s}_j^c . Each signature has an associated set of relevant observations (tracking results of human j in N frames from camera c) represented by a set of images $\mathfrak{J}_j^{+c} = \{I_{j,1}^c, \dots, I_{j,N}^c\}$. This set is used as positive samples in a learning phase. Negative samples are obtained from images extracted from the same camera during tracking the rest of humans: $\mathfrak{J}_j^{-c} = \{I_{i,k}^c\}_{i \neq j}$.

Here we take advantage of improved boosting algorithm using confidence-rated predictions [40]. An essential advantage of this approach is that a weak hypothesis not only generates a predicted classification but also a self-rated confidence score which estimates the confidence of its prediction. Later, we use this confidence value to define the similarity measure between two signatures.

In our approach weak hypotheses are searched on Riemannian manifold space where a weak classifier is represented by MRC patch extracted from positive samples. The manifold is a rather complicated space compared with euclidean. As an example, let us consider a linear classifier on $2D$ euclidean space. Having two points in this space, we can easily define a line which separates these points dividing the space into two. When we take a manifold as a space (let us imagine a torus) there is no way to separate a space into two. The first thought would be to map the manifold space to a higher dimensional Euclidean space, which can be considered as flattening the manifold. Nevertheless, in general case, such mapping into flattened space preserving distances between points on the manifold, does not exist. The global structure of the points will be disturbed.

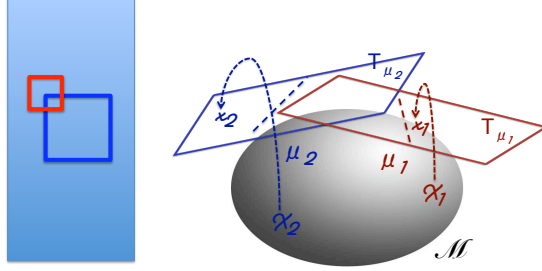


Figure 7: MRC Classifier. The manifold is depicted with the surface of the sphere, and the planes are the tangent spaces of the mean covariances. The samples \mathfrak{X}_i are projected to tangent space T_{μ_i} at means via \log_{μ} operation.

Therefore the evaluated samples are projected to the tangent spaces at the computed means, where weak classifiers are learned. At each iteration, weights of samples are adjusted through boosting. Next, we map the points to the tangent space at the mean and learn a weak classifier on this vector space. We do not go into details concerning learning on the manifold space as it is not the main topic of this paper. The interested reader is pointed to [41].

5.4.1. MRC Patch as a Weak Classifier

We define a weak classifier as function h based on distance computation on Riemannian manifold space (see figure 7). Image I is classified by a weak classifier built on patch p using a threshold function defined as

$$h(p, I) = \begin{cases} \alpha = \frac{1}{2} \ln\left(\frac{W_+^+}{W_-^+}\right) & \text{if } \sum_j w_j \rho(\mu_j, C_j) \leq T_p \\ \beta = \frac{1}{2} \ln\left(\frac{W_+^-}{W_-^-}\right), & \text{otherwise} \end{cases} \quad (10)$$

where W_+^+ , W_-^+ , W_+^- , W_-^- correspond to weighted sum of true positive, false positive, false negative and true negative samples, respectively. Threshold T_p and weights w_j are obtained by minimizing error of weak classifier during learning; μ_j is the mean covariance of MRC patch classifier and covariance C_j corresponds to the image region of I .

Each MRC patch and MRC patch combination extracted during tracking forms a weak classifier. From the set of weak classifiers, boosting algorithm selects the ones which together form a strong classifier. Details of boosting algorithm using confidence-rated predictions can be found in [40].

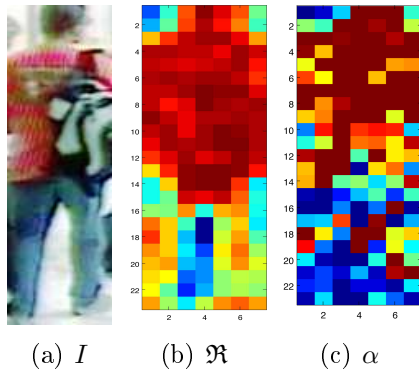


Figure 8: Illustration of patch significance: (a) one of many frames obtained during tracking; (b) reliability map obtained by the first method; (c) confidence map obtained by boosting. Colours correspond to significance of patches (for clarity only $\frac{W}{4} \times \frac{W}{4}$ patches, shifted by $\frac{W}{8}$ pixels are illustrated, red indicates the highest significance, blue the lowest).

We use the selected weak classifiers in MRC patch matching. In figure 8 we present reliability and confidence maps, based on reliability \mathfrak{R} and confidence α , respectively.

5.5. MRC Patch Matching

Given extracted human signatures, we introduce a way to effectively distinguish individuals. The human signature is represented by a set of relevant MRC patches, extracted using one of the aforementioned selection methods. MRC patch consists of the mean covariances with its positions. The position of the patch is essential to keep discriminative power of the human signature. In general, the matching of two signatures \mathfrak{s}_A and \mathfrak{s}_B is carried out by maximizing the similarity measure. We shift one signature over another to reduce body alignment issues. When we shift signature (see figure 9) we preserve relative position between patches to avoid wasting of discriminative property of the patch position. In our experiments the signature is shifted over another not more than $\frac{W}{4}$ pixels to maximize similarity. The similarity between two human signatures \mathfrak{s}_A and \mathfrak{s}_B is defined as

$$S(\mathfrak{s}_A, \mathfrak{s}_B) = \frac{1}{|K|} \sum_{i \in K} \frac{\beta_{A_i} + \beta_{B_i}}{\rho(\mu_{A_i}, \mu_{B_i})}, \quad (11)$$

where K stands for the set of corresponding patches in signature \mathfrak{s}_A and signature \mathfrak{s}_B ; ρ is the covariance matrix distance; β is a reliability (\mathfrak{R}) or

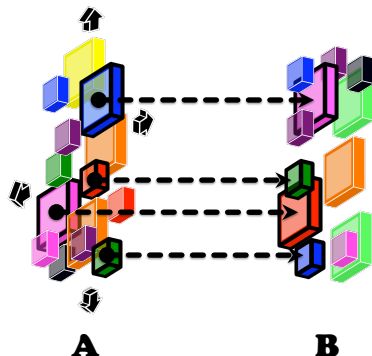


Figure 9: The similarity between two human signatures. Every signature is a set of MRC patches. Signature A is shifted left/right/up and down to find out the best corresponding patches in signature B (position of a patch determines matching). Connections in the figure represent corresponding patches. Some connections are suppressed for clarity.

a confidence (α) value of the corresponding patches depending on selection method. Here, we take advantages of the patch selection method which is able to choose the most informative patch combinations. The efficiency of patch combination is handled indirectly by β coefficients.

6. Experimental results

We evaluate our methods on the ETHZ and the i-LIDS dataset. Moreover, we extracted new sets of individuals from i-LIDS data to create more pertinent sets of individuals. The performance is shown using a cumulative matching characteristic (CMC) curve suggested in [42] as the validation method for the re-identification problem. The CMC curve represents the expectation of finding the correct match in the top n matches.

Experimental setup

Every human image is scaled into a fixed size of 64×192 pixels. We generate MRC patches of 16×16 pixels with 8 pixels step (it gives 161 patches). We generate MRC patches of 32×32 pixels with 16 pixels step (it gives 33 patches). Then, we generate combinations of MRC patches (small - small, small - big, big - big, we limit space of patches to those which are situated with the 16 pixels step). Finally, in total we have 3.401 MRC weak classifiers. In the evaluation the proposed selection method based only on reliability of patches is referred to as *Reliable Covariance Patches (RCP)* method and the method based on a boosting scheme is denoted as *Learned Covariance Patches (LCP)* method.

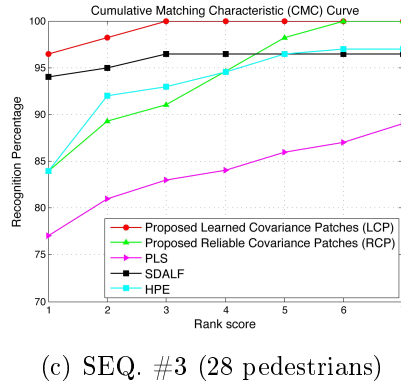
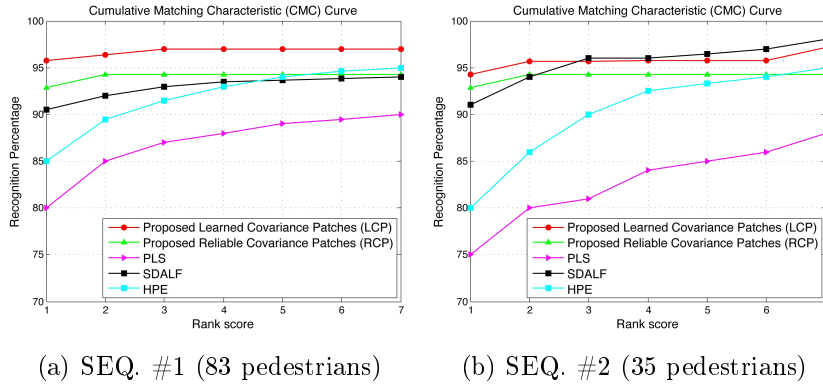


Figure 10: CMC curves obtained on ETHZ dataset. Our descriptors are noted as LCP and RCP respectively. We compare our methods with the results of HPE [30], SDALF [28] and PLS [19].

6.1. ETHZ dataset

ETHZ dataset was originally used for human detection [43]. In [19] this data has been adjusted for re-identification purposes². The modified dataset consists of three sequences: SEQ. #1 contains 83 pedestrians, SEQ. #2 contains 35 pedestrians and SEQ. #3 contains 28 pedestrians. The main drawback of this dataset is that re-identification is performed with the same camera. Since the human images are very similar, we randomly pick up a set of 10 consecutive frames from the beginning and from the end of each sequence to maximize challenging aspects and to be comparable with multi-

²ETHZ Dataset for Appearance-Based Modelling: <http://www.umiacs.umd.edu/schwartz/datasets.html>

image signatures from [28]. We compare our methods with HPE [30], PLS [19] and SDALF [28] (see figure 10). In SEQ. #1 our approaches outperform state of the art methods. SEQ. # 2 seems to be more challenging despite the fact that it has less number of individuals. Unfortunately, it is difficult to say which method performs the best in this sequence. Our proposed approaches perform better for the top rank, nevertheless after a few ranks curves are crossing. In SEQ. #3 LCP significantly outperforms all descriptors. LCP matching rate for the top rank is 96.42%. LCP method always outperforms RCP. The results show that discriminative learning improves performance.

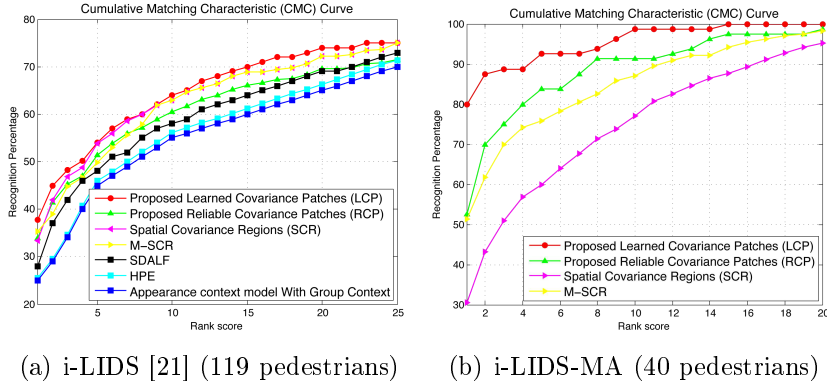
In our belief, despite such challenging aspects as illumination changes and occlusions the ETHZ dataset is not challenging enough to evaluate re-identification approaches. One of the most challenging issues in the re-identification problem is due to different camera settings, different color responses, different camera view points and different environments, which is not the case here. Hence, we have also evaluated our approach on images from more challenging i-LIDS (MCTS) dataset.

6.2. *i-LIDS dataset*

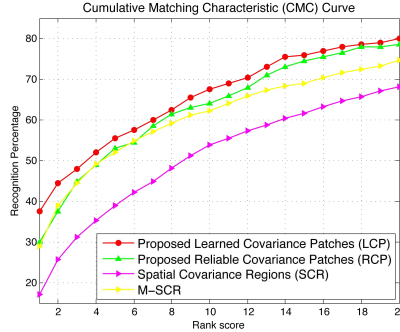
The experiments are performed on images from the 2008 i-LIDS Multiple-Camera Tracking Scenario (MCTS) dataset with multiple camera views. The evaluation dataset contains 476 images with 119 individuals automatically extracted by [21]. This dataset is very challenging since there are many occlusions and often only the top part of the person is visible. Unfortunately, this dataset does not fit very well for *multiple-shot* signature because the number of images per individual is very low. Hence, we applied simple affine transformation on the image to obtain multiple images (coordination of transformation matrix were changed by 5% and rotation angle was in range of $[-6^\circ; 6^\circ]$). As every transformation of an original image is allowed we claim that this solution is fair with the state of the art. On such generated data we follow the scheme of evaluation presented in [21].

We compared our approach with methods which obtained the best performance on this dataset: SCR [12], Appearance Context [21], HPE [30] and SDALF [28]³. As SCR belongs to *single-shot* approaches, we extended SCR

³For *multiple-image* signature, the authors in [28] assume that for each individual 4 images in average are given and test their approach using 3 images to build signature. Nevertheless, for 55 individuals (from 119) there is only maximum 3 images given. Thus, on 46% of the database, the method can not be evaluated. As the experimental setup is



(a) i-LIDS [21] (119 pedestrians) (b) i-LIDS-MA (40 pedestrians)



(c) i-LIDS-AA (100 pedestrians)

Figure 11: CMC curves obtained on i-LIDS datasets; (a) We compare our methods with the results of SCR [12] and M-SCR, HPE [30], SDALF [28] and Appearance context model with Group Context [21]; (b) and (c) We compare our methods with the results of SCR [12] and M-SCR.

to *multiple-shot* approach by applying "*set matching*" (the minimal distance between pair of images). This makes our evaluation fairer to SCR method. The extended SCR method is noted as M-SCR.

Our evaluation results together with state of the art approaches are presented in figure 11 (a). It is worth noting that performance is not very high because person images from the i-LIDS data are very challenging since they were captured from non-overlapping multiple camera views subject to significant occlusions and large variations in both view angle and illumination. Our LCP outperforms all descriptors. Nevertheless the difference between

not clear enough, we can not follow this evaluation scheme.

SCR [12] and M-SCR is not significant. We think that this is a consequence of scarce amount of images per pedestrian in this database. Therefore we have extracted two new sets of individuals from i-LIDS data to investigate more carefully advantage of using tracking results in building human signatures. These datasets finally satisfy all requirements of *multiple-shot* person re-identification.

i-LIDS-MA

First dataset contains 40 individuals extracted from two cameras. For each individual 46 frames are annotated manually from both cameras. Therefore we have $40 \times 2 \times 46 = 3680$ annotated images. We denote this dataset as i-LIDS-MA. For each pedestrian we create human signature using $N = 1$ (for SCR [12]) or $N = 10$ (for M-SCR, RCP, LCP) randomly selected images. Then, every signature is used as a query to the gallery set of signatures from different camera. The procedure has been repeated 10 times and average CMC curves together with our results are displayed in figure 11 (b). As we can notice our LCP outperforms significantly SCR. LCP matching rate for the top rank is 80% in comparison with SCR which obtained 30%. Curves of RCP and M-SCR are between others. Also our RCP is a little bit better than M-SCR. We outperform SCR because our human signature is based on MRC patches which take advantage of tracking results and keep information on temporal changes of an appearance. Moreover, the results show that the discriminative learning phase improves performance. Nevertheless, this manually annotated dataset does not reflect real video surveillance scenario where humans are detected and tracked automatically. Consequently, we applied HOG-based human detector and tracker to obtain 100 individuals seen from both cameras. In this case, detection and tracking results are noisy which makes the dataset more challenging. We name this dataset as i-LIDS-AA.

i-LIDS-AA

This dataset contains 100 individuals. For each individual we extracted a different number of frames depending on the tracking difficulties. In total, the dataset contains 10754 images. The performance on this dataset is shown in figure 11 (c). The evaluation scheme was the same as for i-LIDS-MA dataset. The results show again that our descriptors outperform significantly SCR, and also are better than M-SCR. Nevertheless, performance is not very high in comparison with the results obtained on i-LIDS-MA. It shows one of the main limitations that our approach performance directly depends on hu-

man detection results (*e.g.* detected bounding boxes not accurately centred around the people, only part of the people are detected due to occlusion). We have also evaluated the proposed technique using hierarchical matching (we extracted human signatures on different resolutions, then during feature matching we maximized similarity through all extracted resolutions). Nevertheless, performance did not change significantly (at most, we obtained 1% - 2% improvement in accuracy) with a great increase of time consumption. Moreover, using hierarchical matching (giving more flexibility to the appearance) we lose discriminative properties of the spatial correlation (*e.g.* we can match noise). However, the results show that despite this limitation our descriptors perform better than state of the art approaches.

7. Discussion

The results definitively show that the boosting scheme improves performance. Nevertheless, discriminative approaches are often accused of non-scalability (like [18, 19]). It is true that in these approaches (in our as well) an extensive learning phase is necessary to extract discriminative signatures. These approaches are difficult to apply to real scenarios where new people appear continuously. First, the learning phase prevents to generate signatures in real-time. Second, every time when a new signature is created we have to update all signatures in the database (one-against-all scheme). For example, in PLS [19] there is a requirement to have all the gallery signatures beforehand, in order to estimate weights on the appearance model. When one pedestrian is added, weights must be recomputed which makes the approach not-suitable for video surveillance systems.

As a solution to scalability issues we can propose to extract a *reference dataset* which can be used as negative samples for learning a discriminative signature. This *reference dataset* can be chosen offline to be the most representative. Nevertheless, in this case, a time consumption issue still remains. As in the system, there is no constraints for a *real-time* signature generation, there already exist learning approaches which can operate in reasonable time. Moreover, recently, driven by the insatiable market demand for real-time, the programmable *Graphic Processor Unit* (GPU) has evolved into a highly parallel, multithreaded, manycore processor with tremendous computational power and very high memory bandwidth. These new hardware architectures such as NVIDIA [44] are investigated to speed up the computation of pattern recognition problems. Currently, step by step, well known learning algo-

rithms [45] or time consuming descriptors [46] are ported to such specialized architectures. As image and media processing demand a lot of computation power, this direction seems to fit perfectly for more sophisticated approaches. We claim that the usage of high-performance computing can be a solution to make a discriminative learning more suitable for video-surveillance systems.

8. Conclusions

We have proposed a new approach for the human re-identification problem. An extensive evaluation has been performed on the ETHZ and the i-LIDS datasets. We have shown that the proposed MRC patches computed using a Riemannian manifold theory can extract essential information on an appearance of a human and its variability. The experiments show that a joint combination of these distinctive patches constructs a robust invariant human signature, which can handle differences in camera parameters. Finally, we have proposed to evaluate re-identification approaches on two more pertinent sets of individuals.

In the future work we will consider how to minimize the influence of noisy human detection and tracking on matching human signatures. Also we are planing to consider 2D/3D body parts modelling to improve matching of different poses of individuals. Finally, we are going to investigate performance of GPU-based discriminative learning to make the approach suitable for real-time video surveillance systems.

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